Exclusive photoproduction of J/Ψ and Ψ' mesons in proton-proton collisions

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Outline

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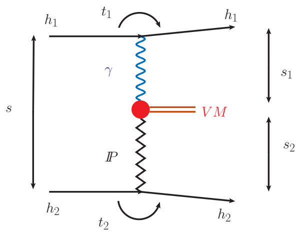
Introduction

1. Exclusive production of J/Ψ meson in photon-proton collisions has been studied in the energy range $W \sim 20 - 300\ GeV$ (recently at HERA, LHCb)
2. This energy range is relevant for the exclusive photoproduction in proton-antiproton collisions at Tevatron energies for not too large rapidities of the meson
3. For Tevatron we have only one experimental point for J/Ψ and Ψ' mesons at $y = 0$
4. New experimental data in proton-proton collisions for J/Ψ and Ψ' mesons in the rapidity range $y \sim 2.0 - 4.5$ (LHCb)

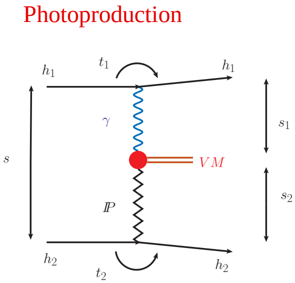
The possible mechanism to production of vector meson in hadronic collisions

Photoproduction



Khoze-Martin-Ryskin 2002
Klein-Nystrand 2004

The possible mechanism to production of vector meson in hadronic collisions



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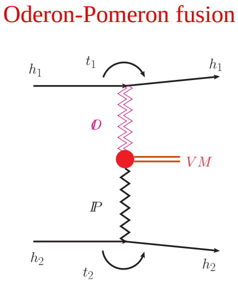

Schäfer, Mankiewicz, Nachtmann 1991
Bzdak, Motyka, Szymanowski, Cudell 2007

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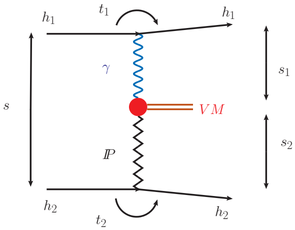
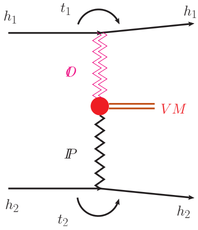


Khoze-Martin-Ryskin 2002
Klein-Nystrand 2004

Oderon-Pomeron fusion



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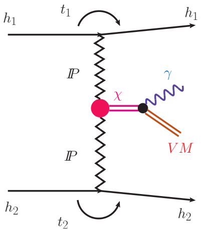
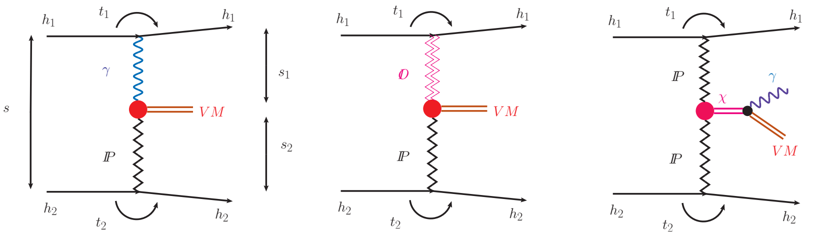
Radiative Decay of χ_c



Pasechnik, Szczurek, Teryaev 2008

The possible mechanism to production of vector meson in hadronic collisions

Photoproduction | Oderon-Pomeron fusion | Radiative Decay of χ_c



Khoze-Martin-Ryskin 2002
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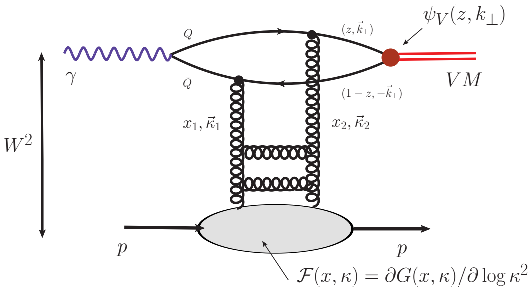
Bzdak, Motyka, Szymanowski, Cudell 2007

Pasechnik, Szczurek, Teryaev 2008

- In our analysis we restrict only to photon-Pomeron fusion mechanism

Diagram for exclusive photoproduction $\gamma p \to J/\Psi p$



- $\psi_v(z, k^2) \to$ wave function of the vector meson
- $\mathcal{F}(x, \kappa^2) \to$ unintegrated gluon distribution function
- $x \sim (Q^2 + M^2_{J/\Psi})/W^2$

The production amplitude for $\gamma p \to J/\Psi p$

The full amplitude:

$$\mathcal{M}_T(W,\Delta^2) = (i+\rho_T)\,\Im m\mathcal{M}_T(W,\Delta^2=0,Q^2=0)\ \exp(-\frac{B(W)\Delta^2}{2})$$

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The imaginary part of the amplitude can be written as:

$$\Im m\,\mathcal{M}_T(W,\Delta^2=0,Q^2=0) = W^2\frac{c_v\sqrt{4\pi\alpha_{em}}}{4\pi^2}\int_0^1\frac{dz}{z(1-z)}\int_0^\infty \pi dk^2\psi_V(z,k^2)$$
$$\int_0^\infty\frac{\pi d\kappa^2}{\kappa^4}\alpha_S(q^2)\mathcal{F}(x_{eff},\kappa^2)\Big(A_0(z,k^2)\,W_0(k^2,\kappa^2)+A_1(z,k^2)\,W_1(k^2,\kappa^2)\Big)$$

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Real part

$$\rho_T = \frac{\Re e\mathcal{M}_T}{\Im m\mathcal{M}_T} = \frac{\pi}{2}\,\Delta_{\mathbf{P}}$$

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Slope parameter

$$B(W) = B_0 + 2\alpha'_{eff}\log\left(\frac{W^2}{W_0^2}\right)$$

Total cross section for $\gamma p \to J/\Psi(\Psi')\ p$

Total cross section can be written as:

$$\sigma_T(\gamma p \to J/\Psi p) = \frac{1 + {\rho_T}^2}{16\pi B(W)} \left| \frac{\Im m \mathcal{M}_T(W, \Delta^2 = 0, Q^2 = 0)}{W^2} \right|^2$$

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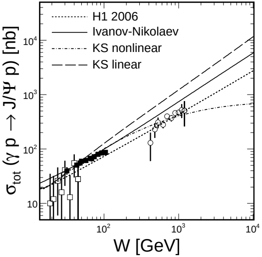

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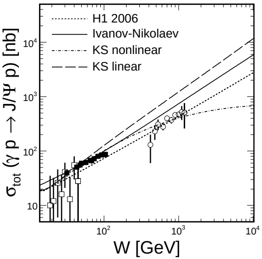

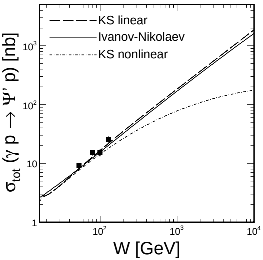

HERA data and extracted LHCb data

- H1 Collaboration, Phys. Lett. B541 (2002) 251
- H1 Collaboration, Eur. Phys. J. C46 (2006) 585
- H1 Collaboration, Eur. Phys. J. C73 (2013) 2466

Parameters of the vector meson wave functions

Decay electronic width

$$\Gamma(V \to e^+e^-) = \frac{4\pi\alpha_{em}^2 c_V^2}{3M_V^3} \cdot g_V^2 \cdot K_{NLO}$$

g_v -leptonic decay constant

$$g_V = \frac{8N_c}{3} \int \frac{d^3\vec{p}}{(2\pi)^3} (M + m_q)\, \psi_v(z,k)$$

How to choose parameters of the wave function

- $\Gamma(V \to e^+e^-) \Rightarrow g_V$
- $\psi_v(z,k) \Rightarrow g_V$
- normalization
- orthogonality

I.P.Ivanov, N.N.Nikolaev, A.A.Savin: Phys.Part.Nucl.37 (2006)

Radial excitations

Gauss wave function

$$\psi_{1S}(k^2) = C_1 \exp(-\frac{k^2 a_1^2}{2})$$

$$\psi_{2S}(k^2) = C_2(\xi_0 - p^2 a_2^2)\exp(-\frac{k^2 a_2^2}{2})$$

Coulomb wave function

$$\psi_{1S}(k^2) = \frac{C_1}{\sqrt{M}} \frac{1}{(1 + a_1^2 k^2)^2}$$

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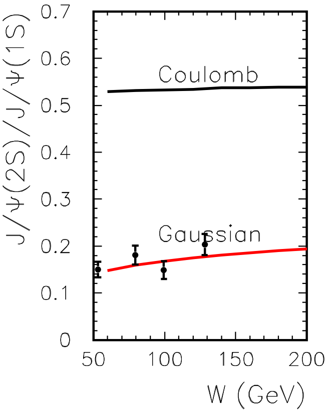
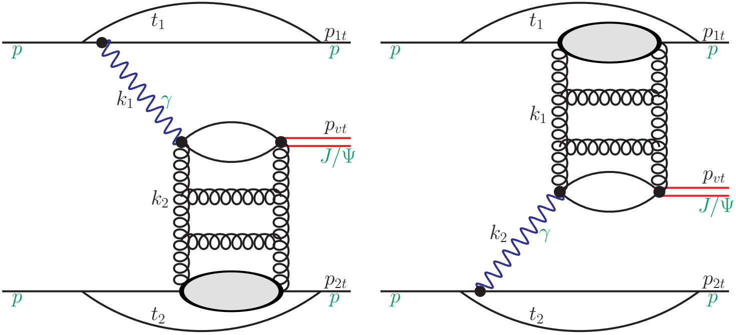


- strong dependence on the wave function
- H1 Collaboration, Phys. Lett. B541 (2002) 251

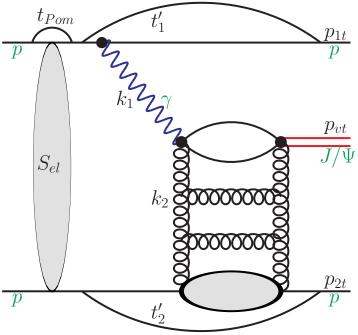
Diagram for exclusive production of $J/\Psi(\Psi')$ meson in proton-proton collisions



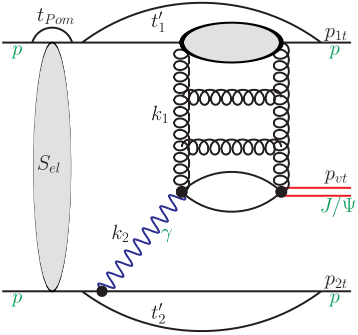
photon-Pomeron

Pomeron-photon

Diagram for $pp \to p\, J/\Psi(\Psi')\, p$ with absorptive corrections



photon-Pomeron



Pomeron-photon

Amplitude for process $pp \to p\, J/\Psi(\Psi')\, p$

Full apmlitude for $pp \longrightarrow pVp$

$$\begin{aligned} \boldsymbol{M}(\boldsymbol{p}_1, \boldsymbol{p}_2) &= \int \frac{d^2\boldsymbol{k}}{(2\pi)^2}\, S_{el}(\boldsymbol{k})\, \boldsymbol{M}^{(0)}(\boldsymbol{p}_1 - \boldsymbol{k}, \boldsymbol{p}_2 + \boldsymbol{k}) \\ &= \boldsymbol{M}^{(0)}(\boldsymbol{p}_1, \boldsymbol{p}_2) - \delta\boldsymbol{M}(\boldsymbol{p}_1, \boldsymbol{p}_2) \end{aligned}$$

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Amplitude without absorption

$$\begin{aligned} \boldsymbol{M}^{(0)}(\boldsymbol{p}_1,\boldsymbol{p}_2) &= e_1 \frac{2}{z_1}\frac{\boldsymbol{p}_1}{t_1}\mathcal{F}_{\lambda_1'\lambda_1}(\boldsymbol{p}_1,t_1)\mathcal{M}_{\gamma h_2\to V h_2}(s_2,t_2,Q_1^2) \\ &+ e_2 \frac{2}{z_2}\frac{\boldsymbol{p}_2}{t_2}\mathcal{F}_{\lambda_2'\lambda_2}(\boldsymbol{p}_2,t_2)\mathcal{M}_{\gamma h_1\to V h_1}(s_1,t_1,Q_2^2) \end{aligned}$$

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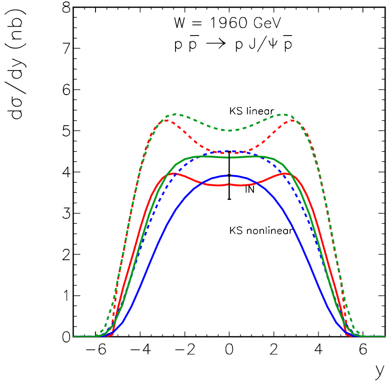
Absorptive corrections for the amplitude

$$\delta\boldsymbol{M}(\boldsymbol{p}_1,\boldsymbol{p}_2) = \int \frac{d^2\boldsymbol{k}}{2(2\pi)^2}\, T(\boldsymbol{k})\, \boldsymbol{M}^{(0)}(\boldsymbol{p}_1-\boldsymbol{k},\boldsymbol{p}_2+\boldsymbol{k})$$

Old results for Tevatron



- old results
- CDF Collaboration, T.Aaltonen et al. Phys. Rev. Lett. 102 (2009)
- A.Cisek PhD thesis (2012)
- different UGDFs
- Gauss wave function

Helicity conserving and helicity flip amplitudes

The full amplitude for the $pp \to pVp$ process can be written as

$$\mathcal{M}^{\lambda_1\lambda_2\to\lambda_1'\lambda_2'\lambda_V}_{h_1h_2\to h_1h_2V}(s,s_1,s_2,t_1,t_2) = \mathcal{M}_{\gamma\mathbf{P}} + \mathcal{M}_{\mathbf{P}\gamma}$$

$$= \langle p_1',\lambda_1'|J_\mu|p_1,\lambda_1\rangle\epsilon^*_\mu(q_1,\lambda_V)\frac{\sqrt{4\pi\alpha_{em}}}{t_1}\mathcal{M}^{\lambda_{\gamma^*}\lambda_2\to\lambda_V\lambda_2}_{\gamma^*h_2\to Vh_2}(s_2,t_2,Q_1^2)$$

$$+\langle p_2',\lambda_2'|J_\mu|p_2,\lambda_2\rangle\epsilon^*_\mu(q_2,\lambda_V)\frac{\sqrt{4\pi\alpha_{em}}}{t_2}\mathcal{M}^{\lambda_{\gamma^*}\lambda_1\to\lambda_V\lambda_1}_{\gamma^*h_1\to Vh_1}(s_1,t_1,Q_2^2)$$

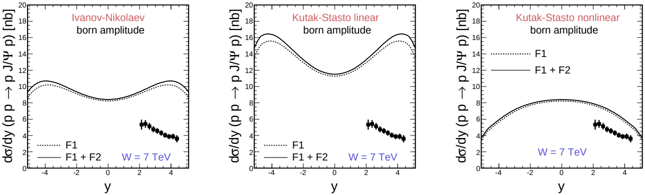
Simple structure:

$$\langle p_1',\lambda_1'|J_\mu|p_1,\lambda_1\rangle\epsilon^*_\mu(q_1,\lambda_V) = \frac{(\boldsymbol{e}^{*(\lambda_V)}\boldsymbol{q}_1)}{\sqrt{1-z_1}}\,\frac{2}{z_1}\,\cdot$$

$$\cdot\chi^\dagger_{\lambda'}\Big\{F_1(Q_1^2) - \frac{i\kappa_p F_2(Q_1^2)}{2m_p}(\boldsymbol{\sigma}_1\cdot[\boldsymbol{q}_1,\boldsymbol{n}])\Big\}\chi_\lambda$$

- The coupling with F_1 - proton helicity conserving, F_2 - proton helicity flip

Dirac vs Pauli form factors (Born)



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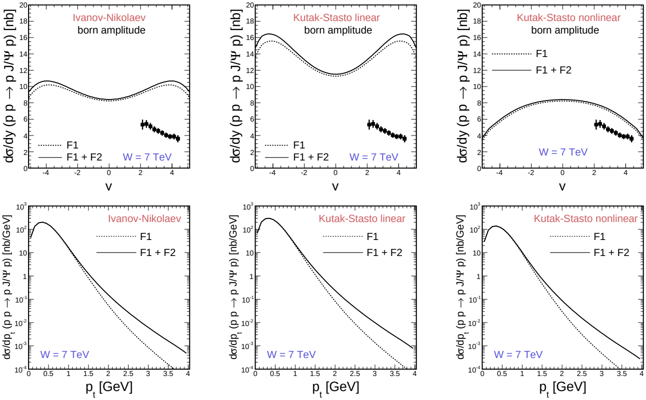
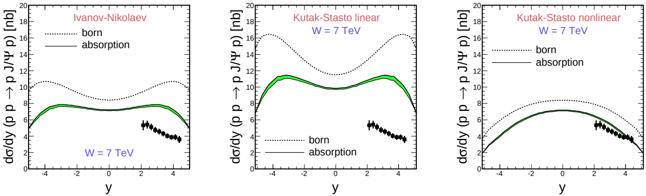


- R. Aaij et al. (LHCb collaboration), J. Phys. **G40** (2013) 045001
- R. Aaij et al. (LHCb collaboration), arXiv:1401.3288 [hep-ex]
- At large p_t we get an enhancement factor of the cross section of order of 10
- Absorption must be included

Absorption effect



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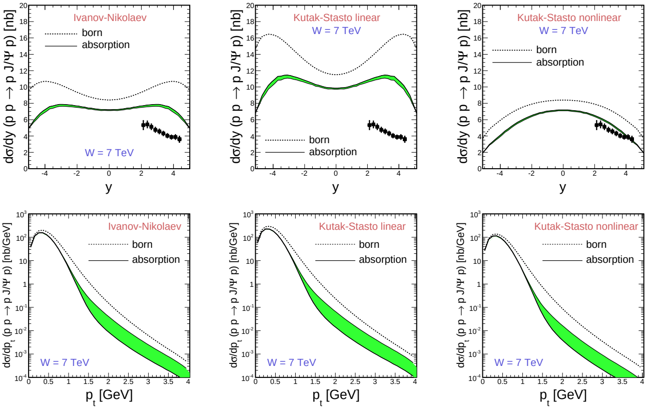
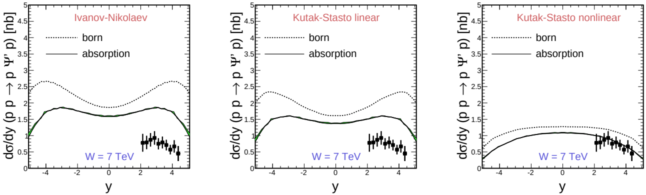


- R. Aaij et al. (LHCb collaboration), arXiv:1401.3288 [hep-ex]
- Absorption may be bigger

Excited state Ψ'



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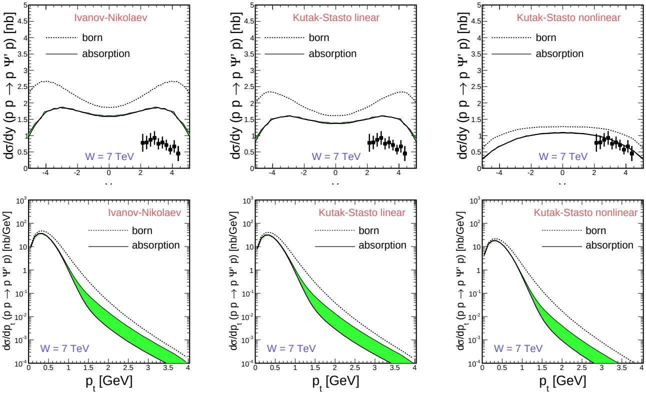
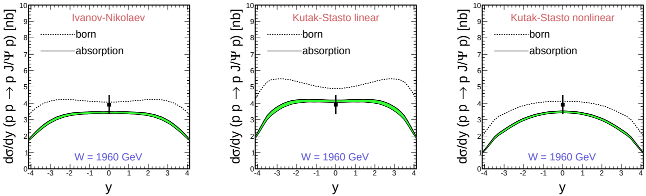


- R. Aaij et al. (LHCb collaboration), arXiv:1401.3288 [hep-ex]
- Absorption may be bigger
- The same shape for Ψ' and J/ψ

Absorption effect for J/Ψ and Ψ' at the Tevatron



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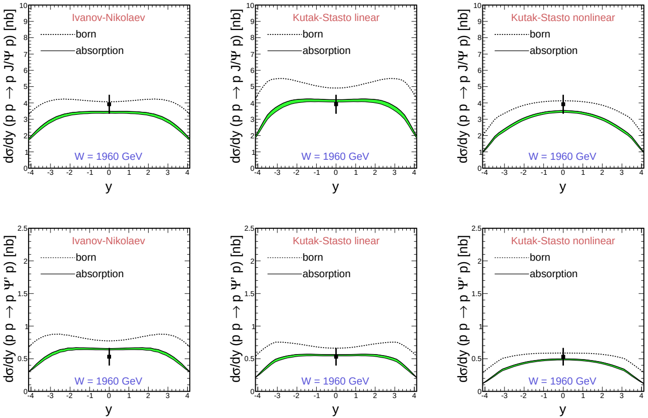
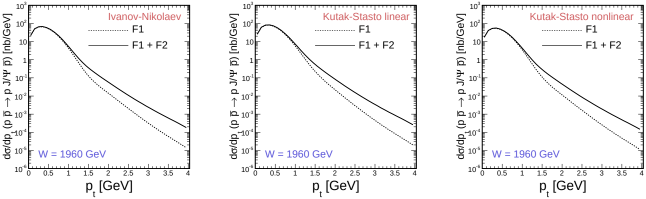


- CDF Collaboration, T.Aaltonen et al., Phys. Rev. Lett. 102 (2009)

Dirac and Pauli form factor (Born) for J/Ψ and Ψ' at the Tevatron



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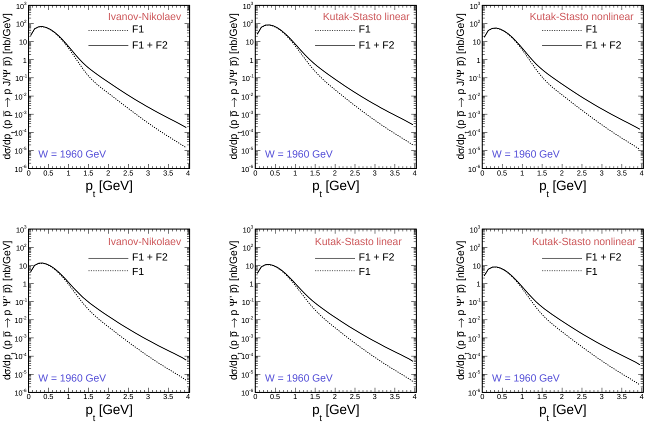

Conclusions

1. We have compared our results with recent HERA ($\gamma p \longrightarrow J/\Psi(\Psi')\ p$) and LHCb ($pp \longrightarrow p\ J/\Psi(\Psi')\ p$) data.
2. $d\sigma/dy = d\sigma^{\gamma\mathbb{P}}/dy + d\sigma^{\mathbb{P}\gamma}/dy$ only in the Born approximation.
3. Sensitivity to the quarkonium wave function and testing UGDF.
4. $d\sigma/dp_t$ is interesting (spin flip, Pomeron-Odderon fusion) but difficult to measure.
5. Absorptive corrections have been included. Their effect depends on p_t and y.