

Meson production in the ISR reactions at BaBar

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Motivation of ISR study at BaBar

- Low energy e^+e^- cross section dominates in hadronic contribution to $a_\mu = (g-2)/2$ of muon (R measurement).
- Direct e^+e^- data in 1.4 - 2.5 GeV region have (**had!**) very low statistics
- New inputs for hadron spectroscopy at low masses and charmonium region

- ISR at BaBar gives competitive (**even dominates!**) statistics
- BaBar has excellent capability for ISR study
- All major hadronic processes are studied (green == published)

$$e^+e^- \rightarrow 2\mu\gamma, 2\pi\gamma, 2K\gamma, 2p\gamma, 2\Lambda\gamma, 2\Sigma\gamma, \Lambda\Sigma\gamma, \Lambda_c\Lambda_c\gamma$$

$$e^+e^- \rightarrow 3\pi\gamma$$

$$e^+e^- \rightarrow 2(\pi^+\pi^-)\gamma, K^+K^-\pi^+\pi^-\gamma, K^+K^-\pi^0\pi^0\gamma, 2(K^+K^-)\gamma$$

$$e^+e^- \rightarrow 2(\pi^+\pi^-\pi^0\pi^0)\gamma, 3(\pi^+\pi^-)\gamma, K^+K^-2(\pi^+\pi^-)\gamma$$

$$e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0\gamma \text{ (preliminary)}, \pi^+\pi^-\pi^0\pi^0\pi^0\gamma, \pi^+\pi^-\pi^0\eta\gamma \dots$$

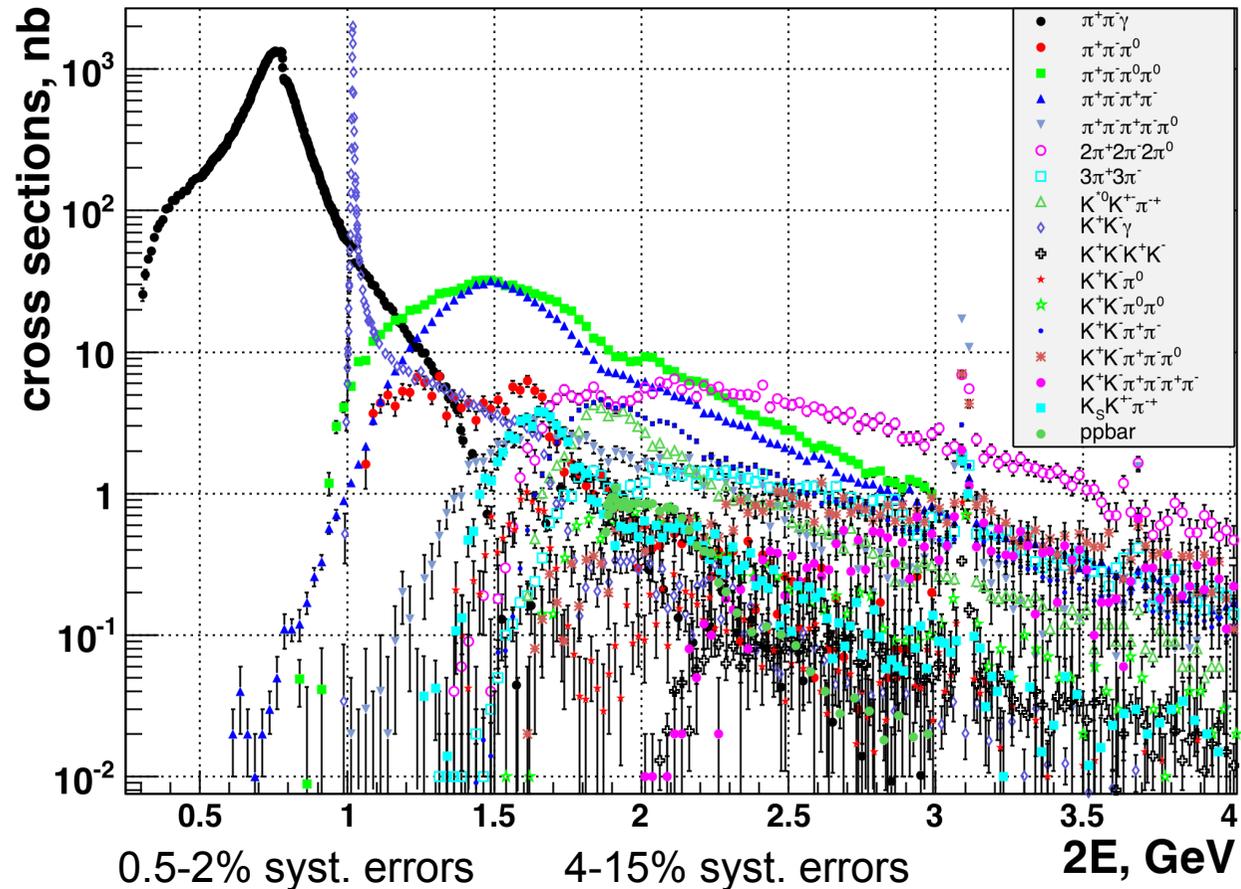
$$e^+e^- \rightarrow K^+K^-\pi^0\gamma, K^+K^-\eta\gamma \text{ (} KK^*\gamma, \phi\pi^0\gamma, \phi\eta\gamma \dots)$$

$$e^+e^- \rightarrow \pi^+\pi^-\pi^+\pi^-\pi^0/\eta\gamma, K^+K^-\pi^+\pi^-\pi^0/\eta\gamma$$

$$e^+e^- \rightarrow KK_S\pi\pi^0/\eta\gamma, K_S K_L, K_S K_L \pi^+\pi^-, K_S K_S \pi^+\pi^-(K^+K^-)$$

Some reactions are being updated to the full BaBar data with $\sim 500 \text{ fb}^{-1}$

BaBar measurements summary

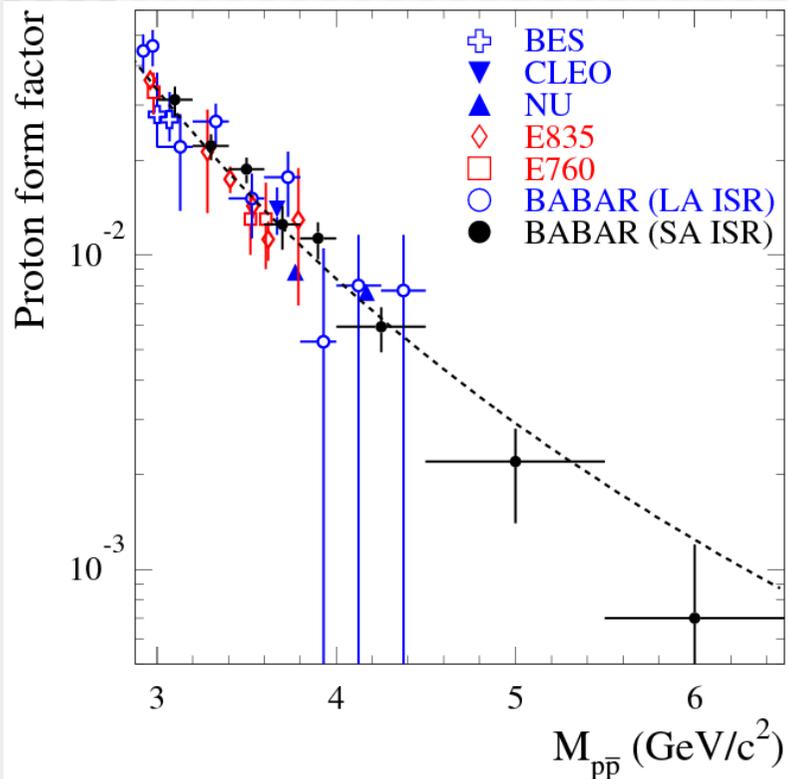


To calculate R in the energy range 1-2 GeV the processes $\pi^+\pi^-3\pi^0$, $\pi^+\pi^-4\pi^0$, $K_S K_L$, $K_S K_L \pi\pi$, $K_S K^+ \pi^-\pi^0$ are under study: $\pi^+\pi^-2\pi^0$ is still preliminary. Work is in progress.

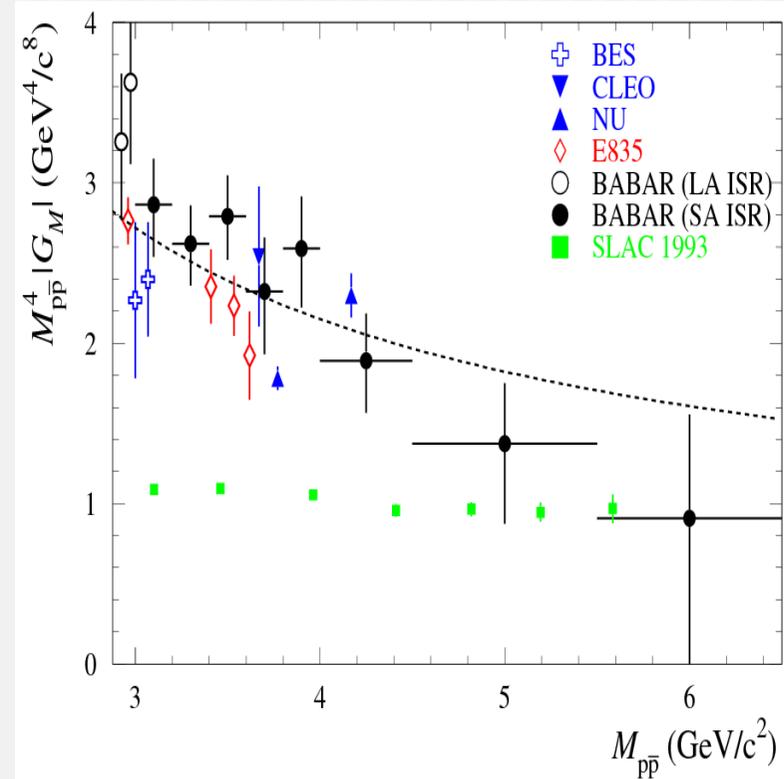
BaBar measured: $e^+e^- \rightarrow \bar{p}p$

Published **Phys. Rev. D 88, 072009 (2013)**

Non-tagged (Small Angle) ISR study allows to extend proton FF study to 6.5 GeV



Fit is in agreement with QCD prediction



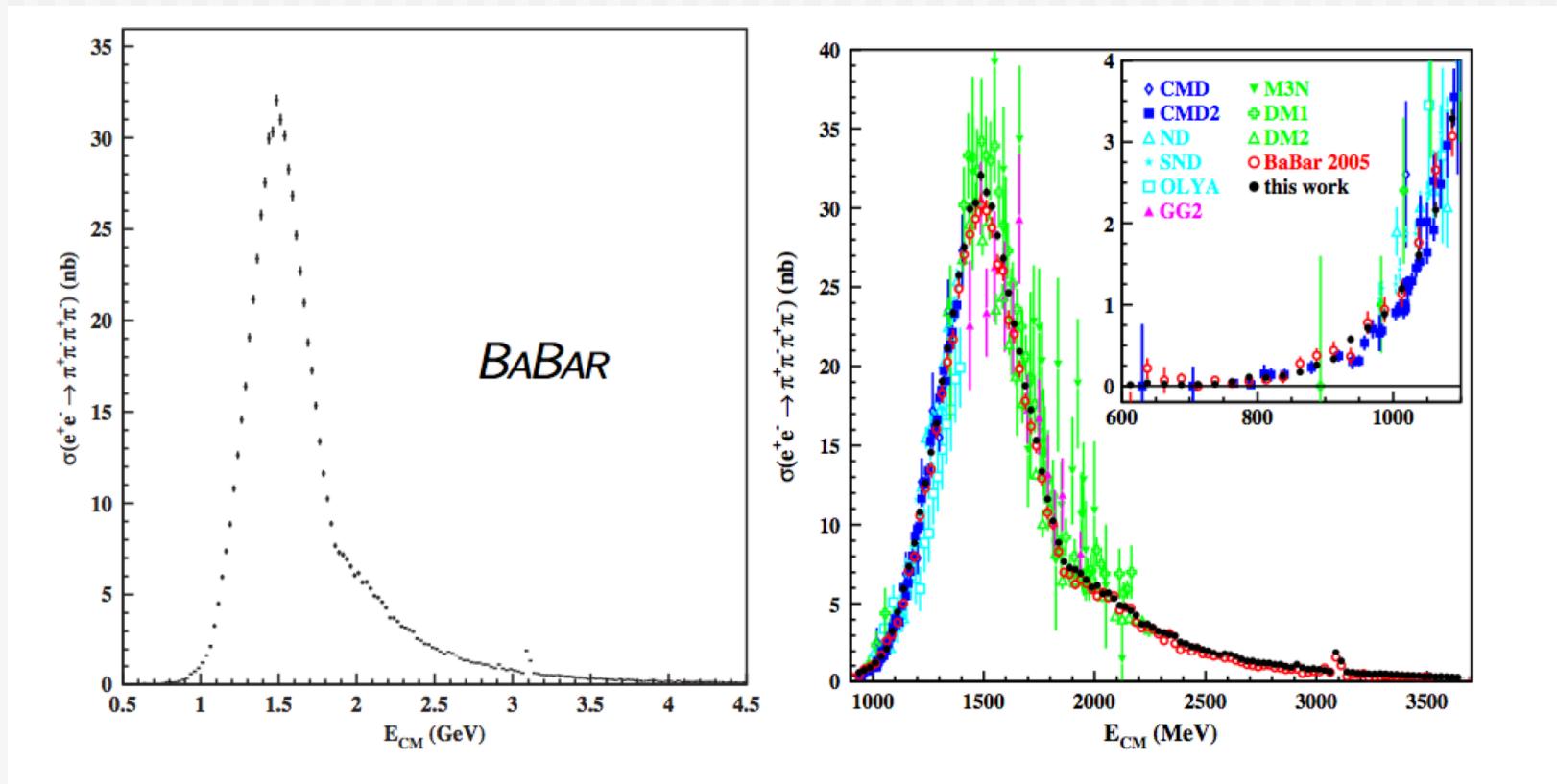
The asymptotic values of the space- and time-like form factors are expected to be the same. The new BABAR SA ISR measurement gives an indication that the difference between the time- and space-like form factors decreases with mass increase.

BaBar updated: $e^+e^- \rightarrow \pi^+\pi^-\pi^+\pi^-$

Published PRD 85 112009 (2012)

Based on 454 fb⁻¹ dataset (statistical uncertainties are shown)

Our result is more precise than the current world average (<3% systematic error)

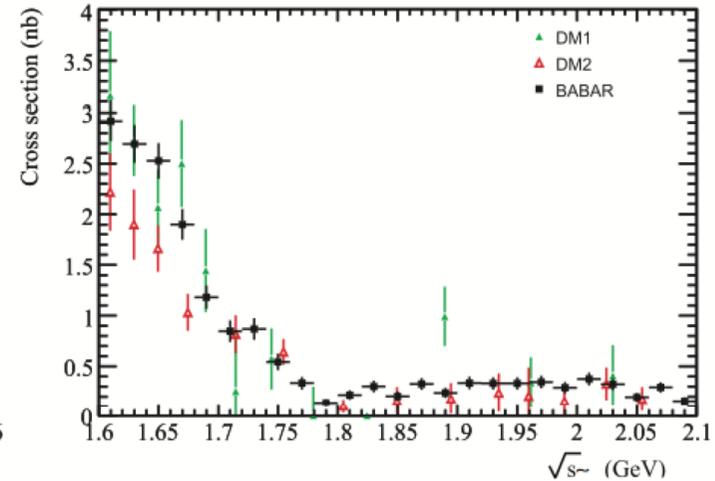
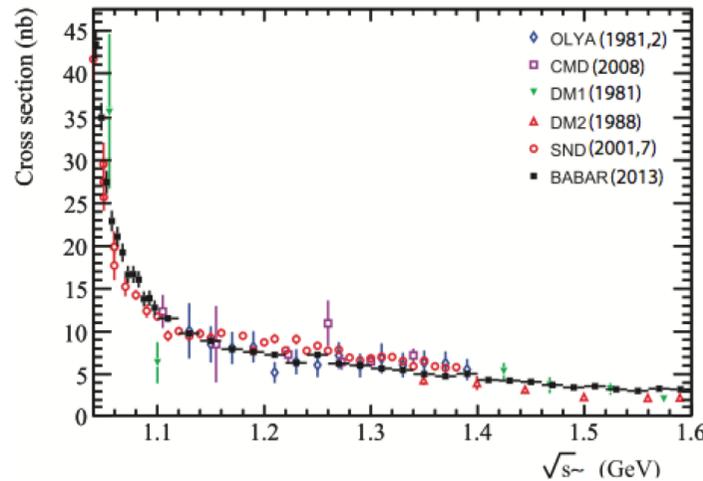
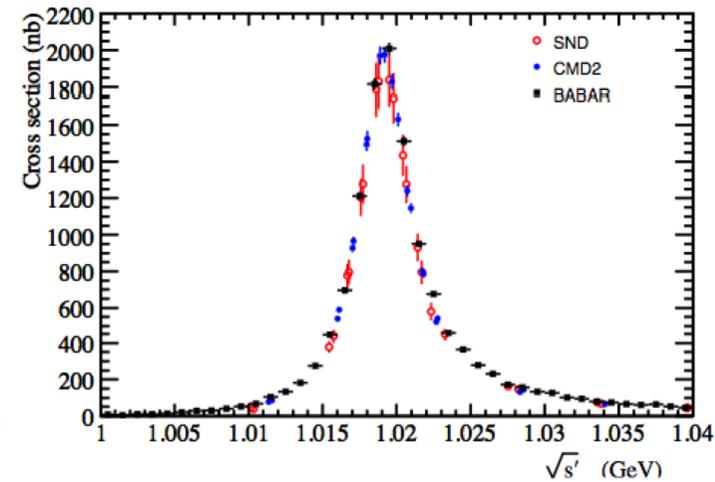
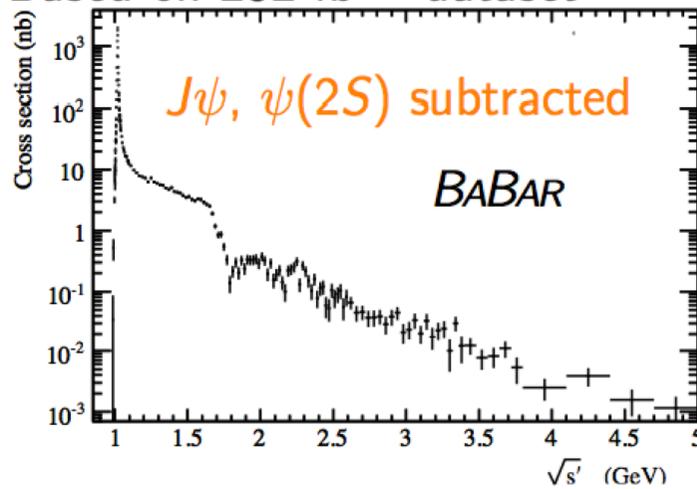


BaBar measured: $e^+e^- \rightarrow K^+K^-$

Published **Phys. Rev. D 88, 032013 (2013)**

Our result is more precise than the current world average

Based on 232 fb^{-1} dataset



Contribution of missing channels to a_μ

SM-to-experiment comparison [in units 10^{-10}]

QED	116 584 71.81	± 0.02
Leading hadronic vacuum polarization (VP)	690.30	± 5.26
Sub-leading hadronic vacuum polarization	-10.03	± 0.11
Hadronic light-by-light	11.60	± 3.90
Weak (incl. 2-loops)	15.32	± 0.18
<hr/>		
Theory	11659179.00	± 6.46
Experiment	11659208.00	± 6.30
<hr/>		
Exp – theory	29.00	± 9.03

a_μ ($\sqrt{s} < 1.8$ GeV)	K^+K^-	$2(\pi^+ \pi^-)$	$3(\pi^+ \pi^-)$	$2(\pi^+ \pi^- \pi^0)$
without BABAR	21.63 ± 0.70	14.20 ± 0.90	0.10 ± 0.10	1.42 ± 0.30
with BABAR	22.93 ± 0.30	13.35 ± 0.45	0.11 ± 0.02	0.89 ± 0.09

Missing channels contribute 5.98 ± 0.42 or 12.46 ± 0.76 if $\sqrt{s} < 2.0$ GeV

Contribution from $KK\pi$, $KK2\pi$, $2\pi3\pi^0$, $2\pi4\pi^0$, 7π , 8π ... added using iso-spin relations

$$e^+e^- \rightarrow K_S K_L, K_S K_L \pi^+ \pi^-, K_S K_S \pi^+ \pi^- (K^+ K^-)$$

We present (with more details) new results on the study of the processes:

$$e^+e^- \rightarrow K_S K_L$$

$$e^+e^- \rightarrow K_S K_L \pi^+ \pi^-$$

$$e^+e^- \rightarrow K_S K_S \pi^+ \pi^-$$

$$e^+e^- \rightarrow K_S K_S K^+ K^-$$

Based on 469 fb⁻¹ integrated luminosity.

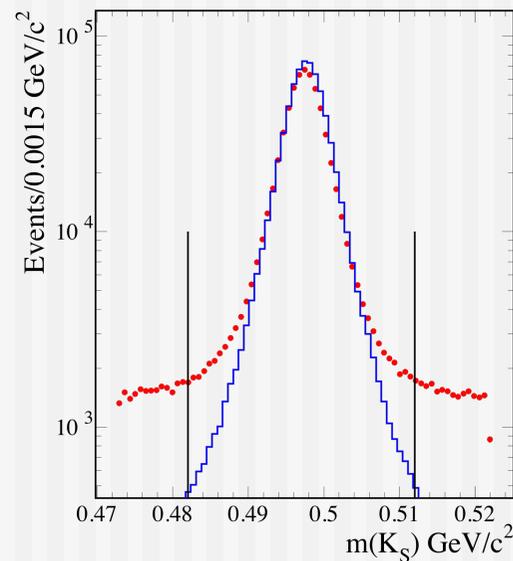
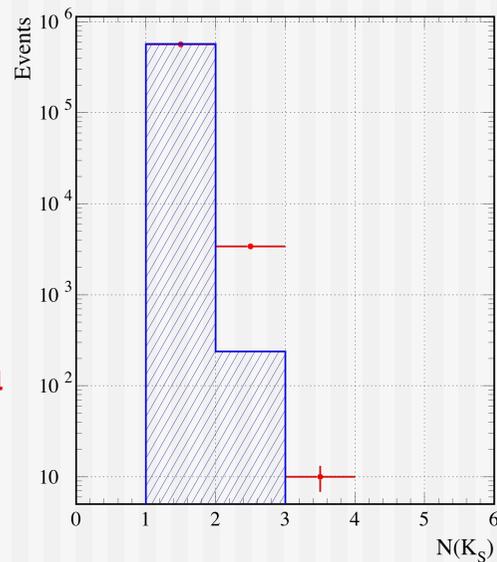
Recently (May 6) published [Phys. Rev. D 89, 092002 \(2014\)](#)

K_S selection (in $\pi^+\pi^-$ decay)

Loop over all K_S candidates with ISR photon with $E_\gamma > 3$ GeV, and select events with:

- Good quality K_S coming from IP
- No electron ID for either charged track

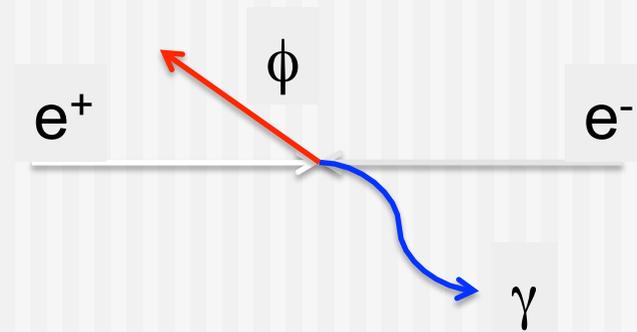
Simulation
of $\phi\gamma \rightarrow K_S K_L \gamma$
compare to data



Dominated by $\phi\gamma \rightarrow K_S K_L \gamma$ process if require **NO** additional tracks from IP

$e^+e^- \rightarrow \phi \gamma \rightarrow K_S K_L \gamma$ (without K_L detection)

$$\begin{aligned} E_0 &= E^+ + E^- \\ \vec{p}_0 &= \vec{p}^+ + \vec{p}^- \\ \vec{p}_\gamma &= n E_\gamma \end{aligned}$$



Assuming $e^+e^- \rightarrow \phi\gamma$ reaction
Use ϕ mass to get $E_{\gamma\text{ISR}}$

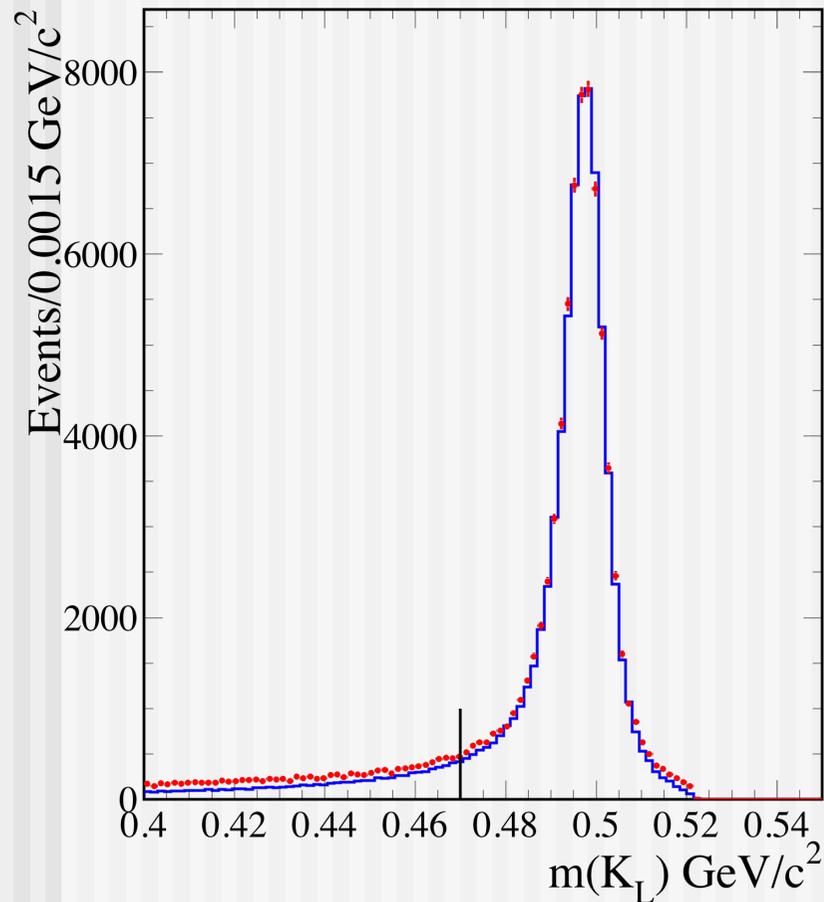
$$E_\gamma^c = \frac{E_0^2 - p_0^2 - m_\phi^2}{2(E_0 - \vec{p}_0 \cdot \vec{n}_\gamma)}$$

Using energy-momentum conservation and detected K_S
we determine K_L mass and direction:

$$m^2(K_L) = \left(E^+ + E^- - E_\gamma^c - E_{K_S}\right)^2 - \left(p^+ + p^- - p_\gamma^c - p_{K_S}\right)^2$$

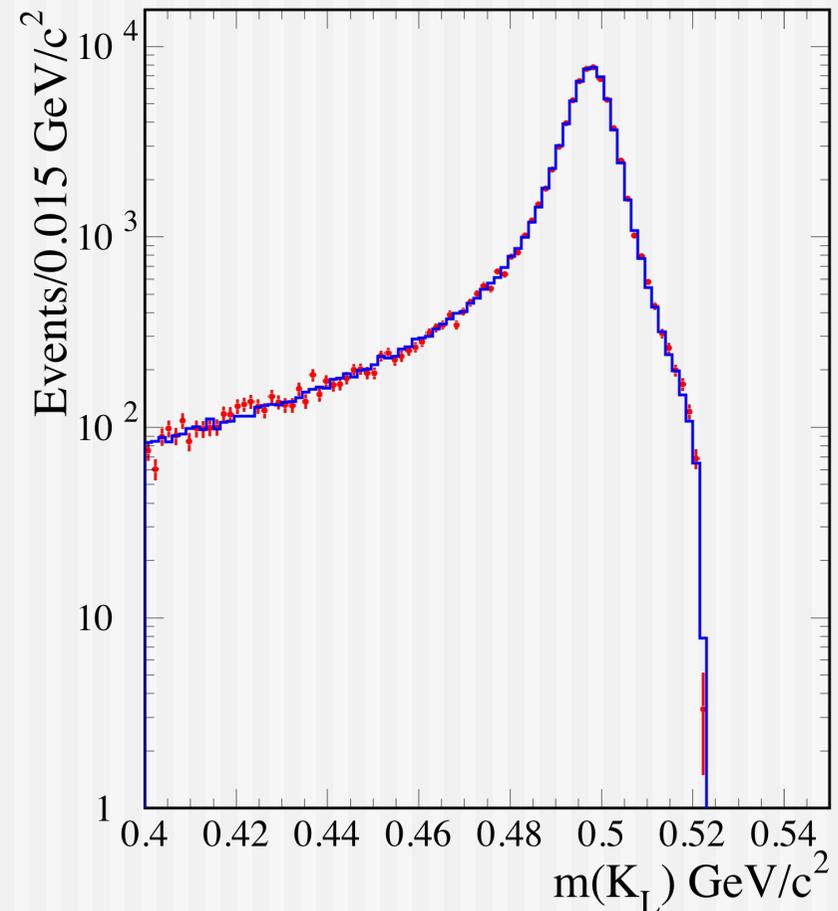
Using this events we can study K_L detection.

K_L mass using ϕ mass constraint



MC normalized to two bins at peak

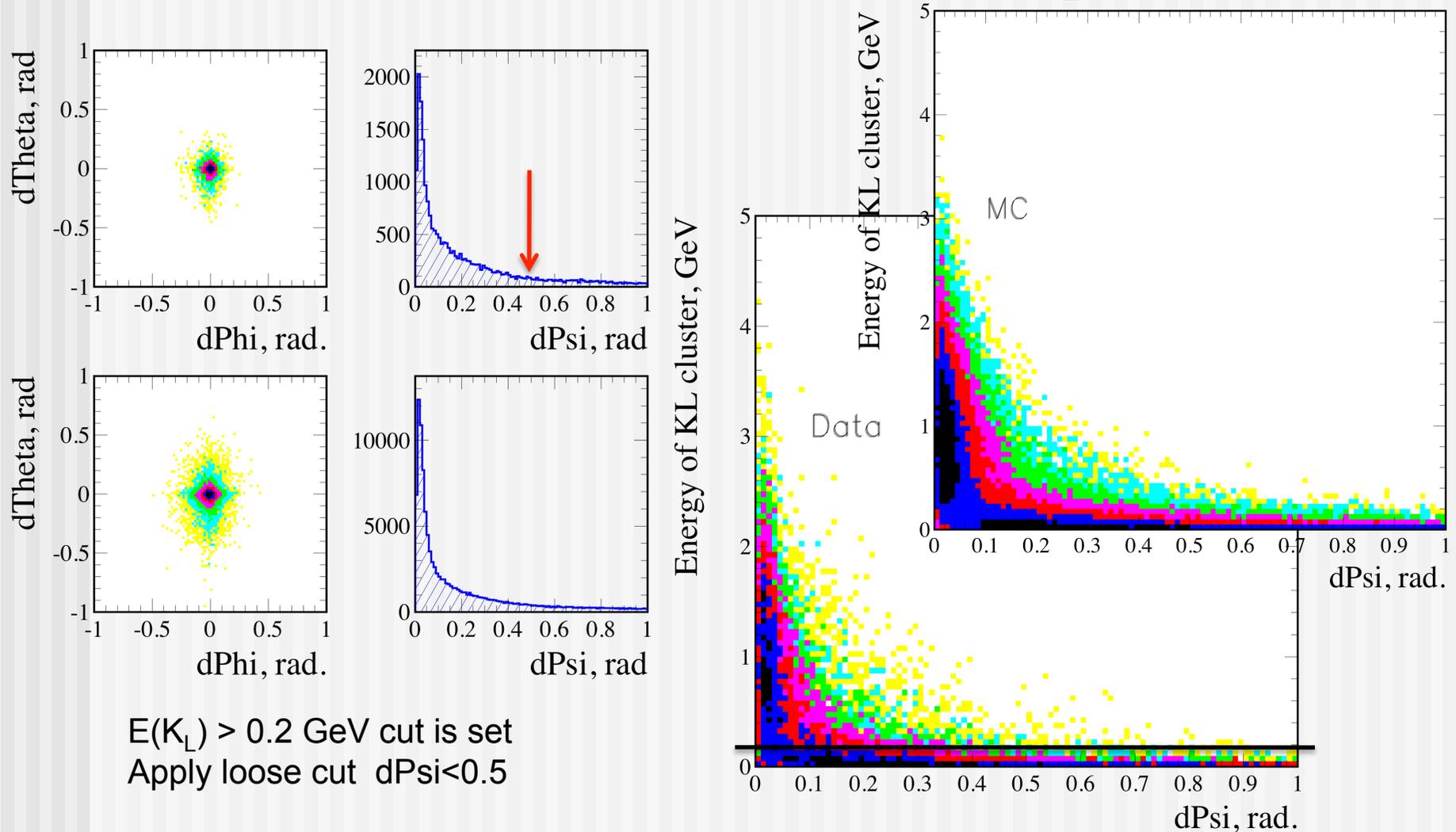
Very low background!



After background subtraction (5.6%) we have **81012±285** events (**447434±669** MC). We estimate ~0.5% systematic error for background subtraction uncertainty.

How K_L cluster in Calorimeter looks like?

1. Search for EMC cluster closest to K_L direction:

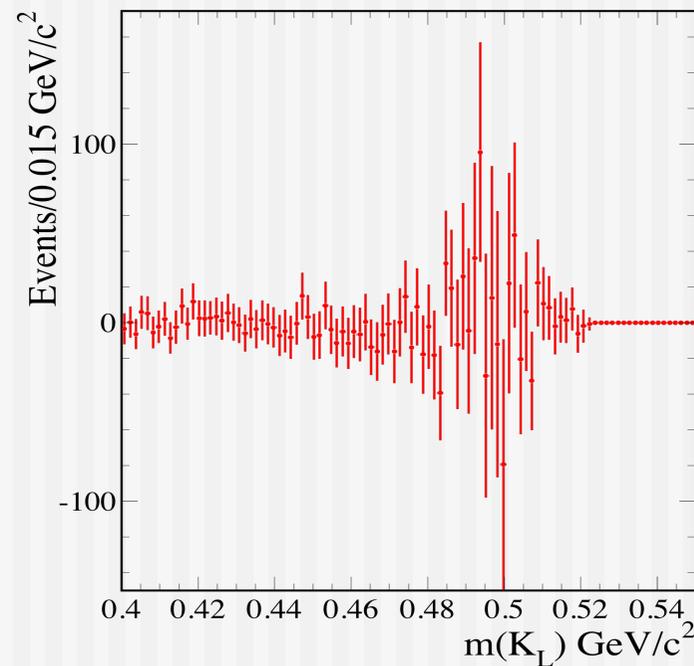
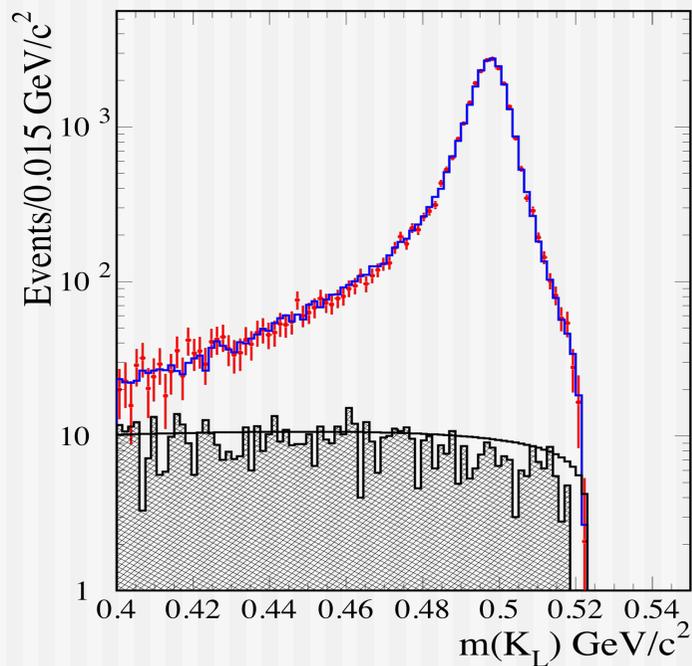


$E(K_L) > 0.2$ GeV cut is set
Apply loose cut $d\Psi < 0.5$

K_L detection probability in EMC $\sim 48\%$ ($\sim 6\%$ data-MC difference)

K_L EMC detection probability

Taking coordinates of EMC cluster we perform 3C kinematic fit (K_L momentum is float) and for events, selected by $\chi^2 < 15$ we calculate $m(K_L)$

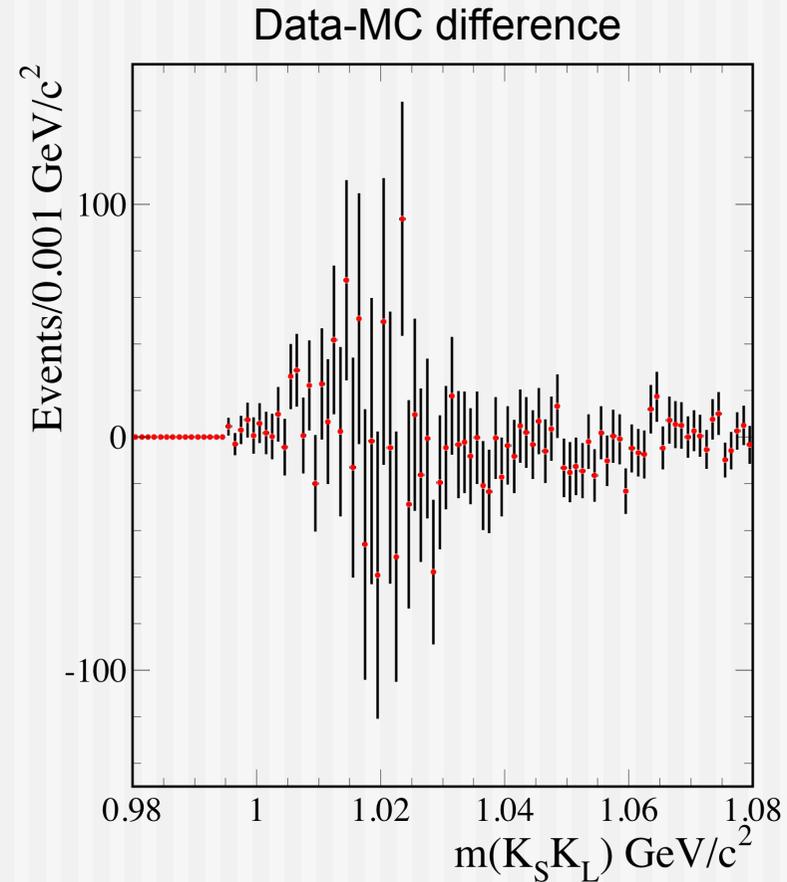
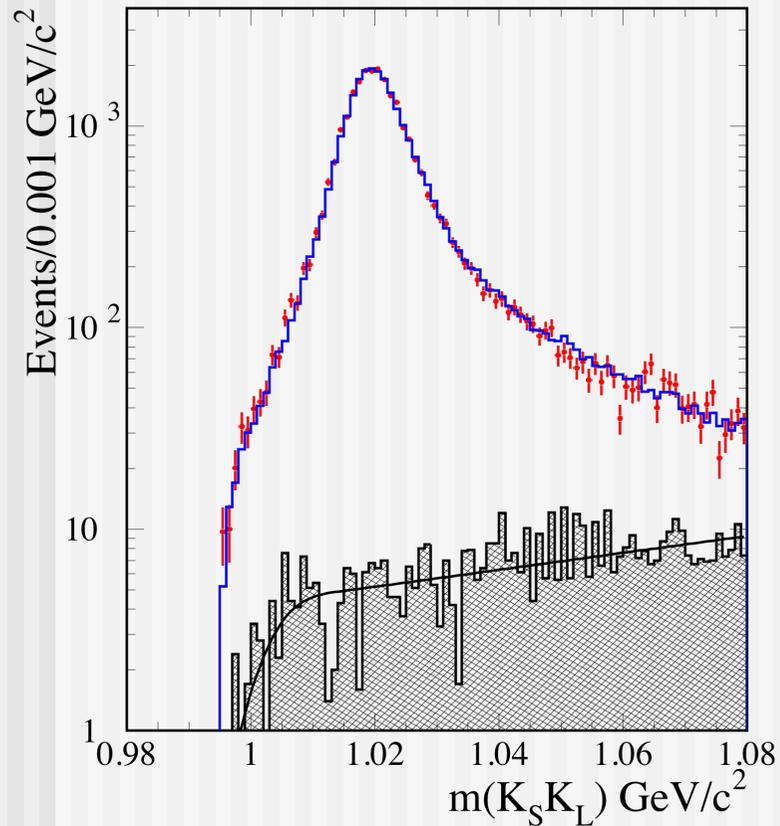


After 814 background events subtraction we obtain 27925 ± 176 events for data and 164179 ± 405 events for MC. By comparing with numbers without K_L detection:

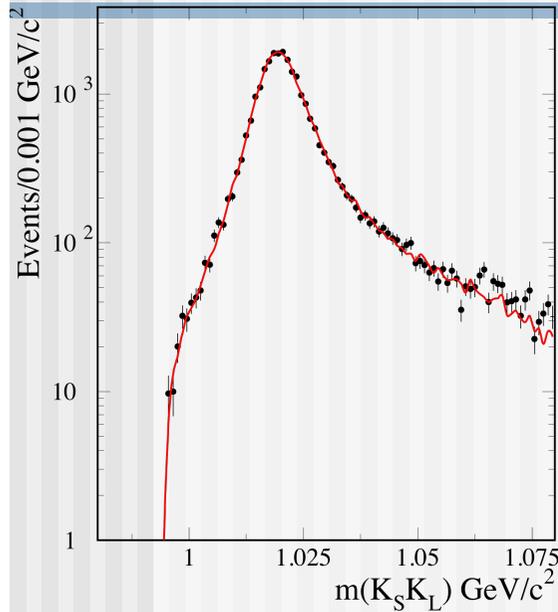
Data/MC = 0.9394 ± 0.0052 (0.6%) (includes also χ^2 cut efficiency)
Used in all other analyses.

ϕ signal in $e^+e^- \rightarrow K_S K_L$ reaction

Use events with $\chi^2 < 15$ and reconstructed parameters of K_S and K_L to calculate $m(K_S K_L)$

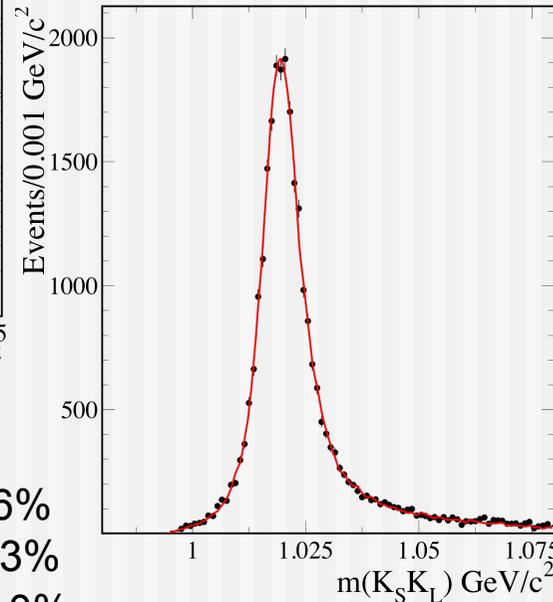


Fit to ϕ parameters



Fit:

$$\begin{aligned}\sigma_0 &= 1409 \pm 33 \pm 42 \pm 15 \text{ nb} \\ m &= 1019.462 \pm 0.042 \pm 0.050 \pm 0.025 \text{ MeV}/c^2 \\ \Gamma_0 &= 4.205 \pm 0.103 \pm 0.050 \pm 0.045 \text{ MeV}\end{aligned}$$



CMD-2

$$\begin{aligned}\sigma_0 &= 1376 \pm 6 \pm 23 \text{ nb} \\ m &= 1019.483 \pm 0.011 \pm 0.025 \text{ MeV}/c^2 \\ \Gamma_0 &= 4.280 \pm 0.033 \pm 0.025 \text{ MeV} \\ \Gamma_{ee} &= 1.235 \pm 0.006 \pm 0.022 \text{ keV}\end{aligned}$$

PDG2010-2012

$$\begin{aligned}m &= 1019.455 \pm 0.020 \text{ MeV}/c^2 \\ \Gamma_0 &= 4.26 \pm 0.04 \text{ MeV} \\ \Gamma_{ee} &= 1.27 \pm 0.04 \text{ keV} \\ B_{KSKL} &= 0.342 \pm 0.004 \\ B_{ee} \cdot B_{KSKL} &= 1.006 \pm 0.016\end{aligned}$$

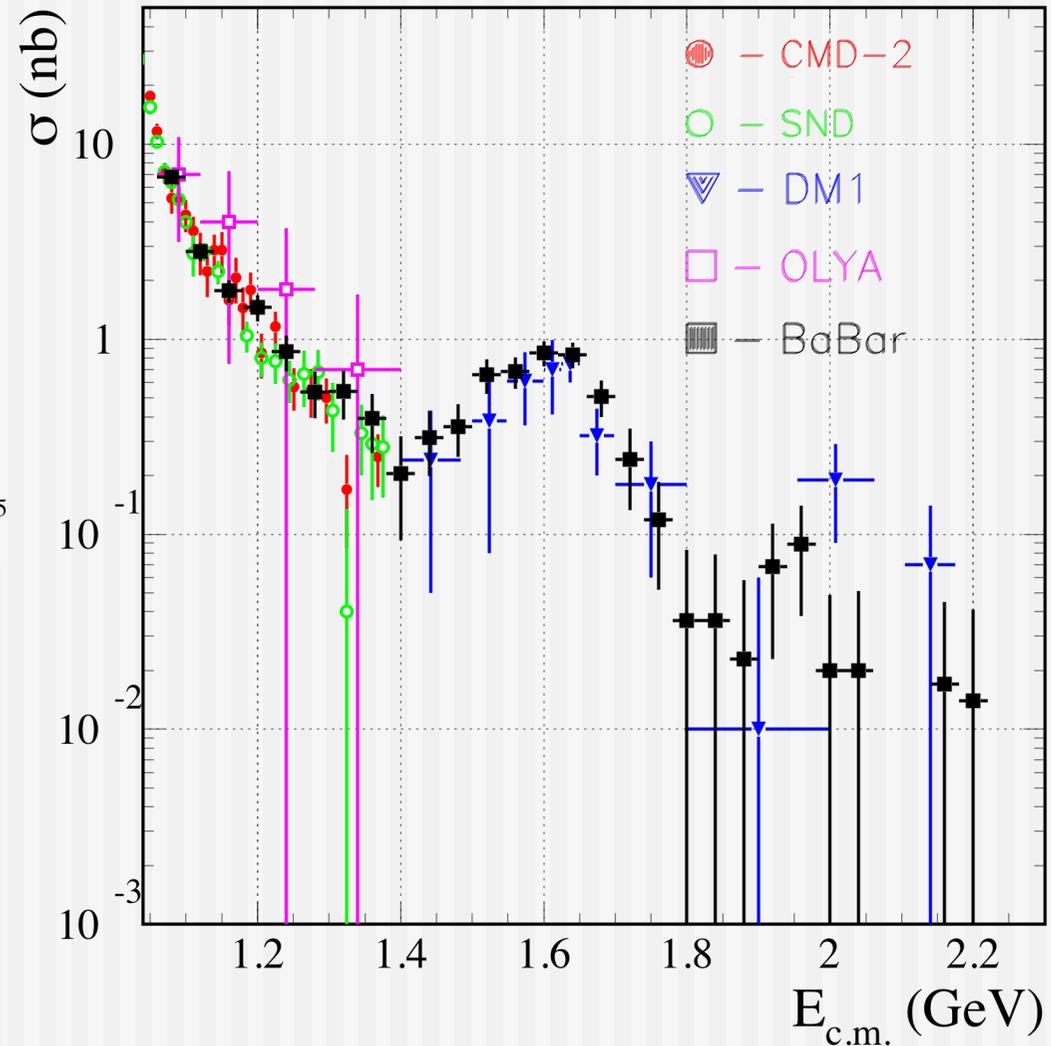
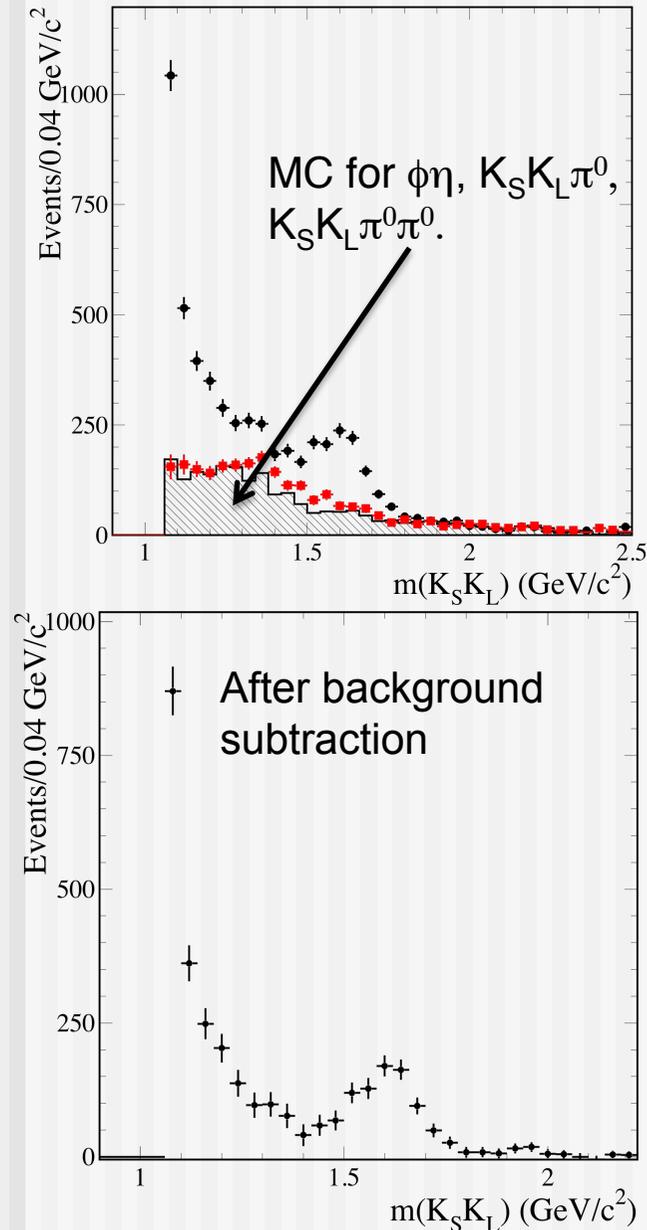
Systematic uncertainty:

K_L efficiency (+ χ^2)	0.6%
BGFilter efficiency	2.3%
K_S efficiency	1.0%
ISR photon	0.5%
Luminosity	0.5%
Rad.corr.	1.0%
Track overlap	0.6%
Background sub.	0.5%
	2.9%

BaBar

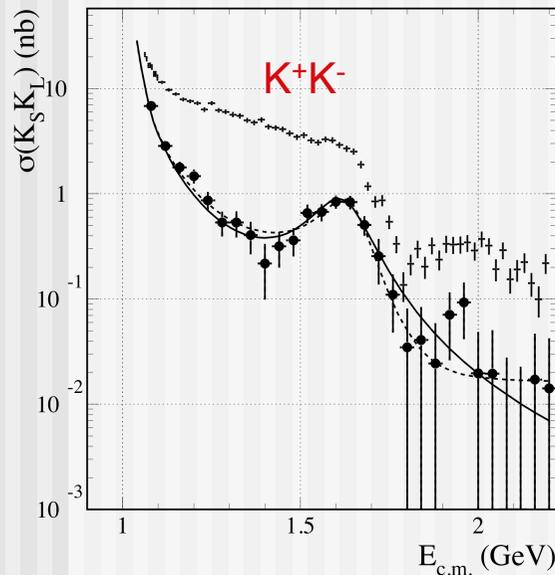
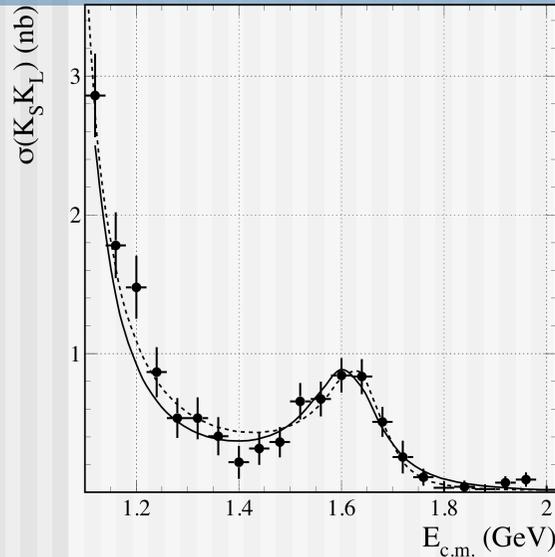
$$\begin{aligned}\Gamma_{ee} \cdot B_{KSKL} &= 0.4200 \pm 0.0033 \pm 0.0122 \pm 0.0019 \text{ keV} \\ \Gamma_{ee} &= 1.228 \pm 0.037 \pm 0.014_{(PDG \ B_{KSKL})} \text{ keV} \\ B_{ee} \cdot B_{KSKL} &= 0.986 \pm 0.030 \pm 0.009_{(PDG \ \Gamma_{KSKL})}\end{aligned}$$

$e^+e^- \rightarrow K_S K_L$ cross section for $m(K_S K_L) > 1.06$ GeV



Systematic error $\sim 10\%$ ($\sim 30\%$ for $\sigma < 0.3$ nb),
dominated by background subtraction procedure.

Is it $\phi(1680)$? Fit with single BW



$$\sigma(s) = \frac{P(s)}{s^{5/2}} \left| \frac{A_{\phi(1020)}}{\sqrt{P(m_\phi)}} + \frac{A_X}{\sqrt{P(m_X)}} \cdot e^{i\varphi} + A_{bkg} \right|^2$$

$$P(s) = \left((s/2)^2 - m_{K^0}^2 \right)^{3/2}$$

$$A(s) = \frac{\Gamma(m^2) \cdot m^3 \sqrt{\sigma_0 \cdot m}}{s - m^2 + i\sqrt{s}\Gamma(s)}$$

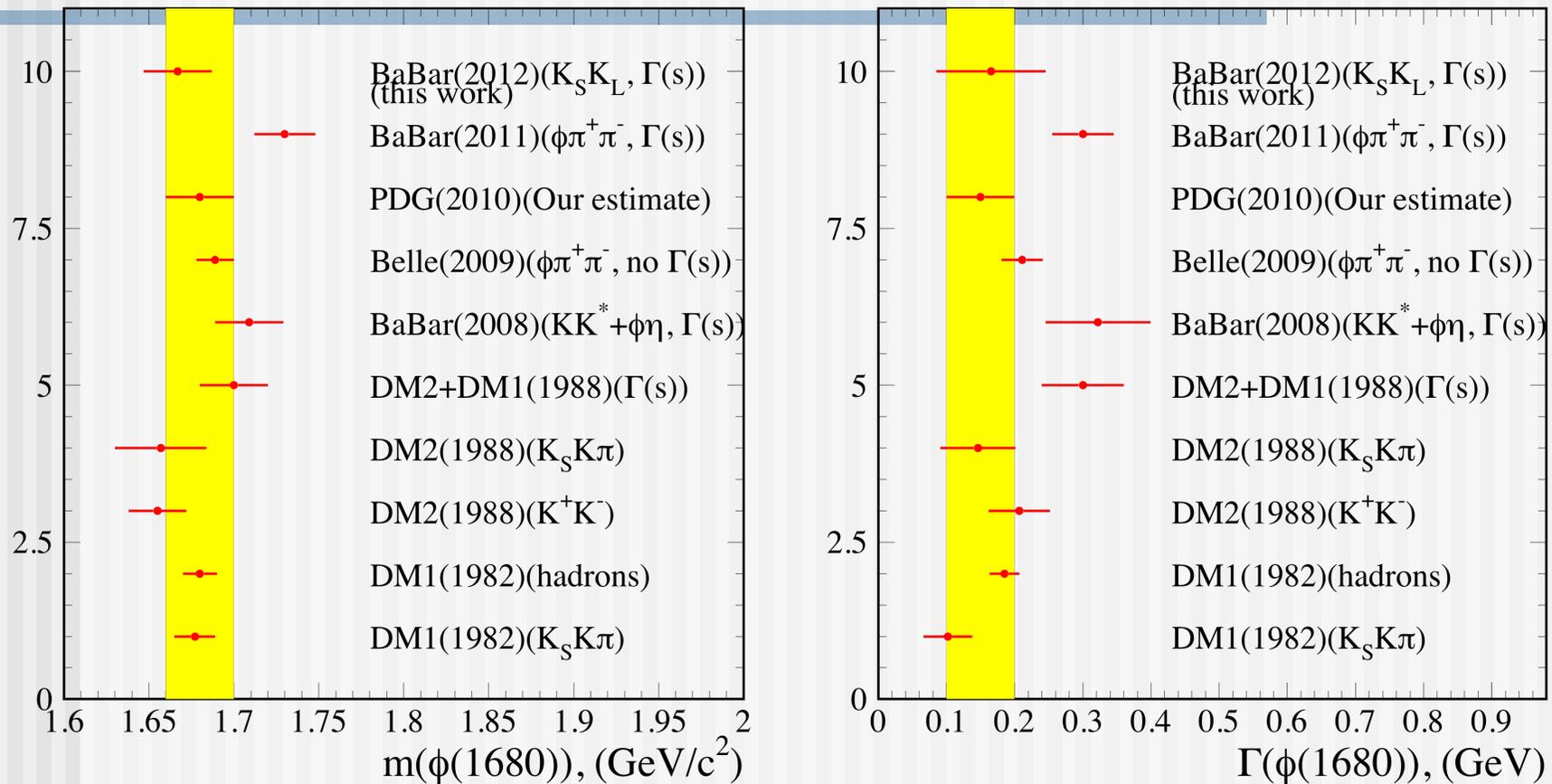
$$\Gamma(s) = \Gamma \cdot \sum_f B_f \cdot \frac{P_f(s)}{P_f(m_f^2)}$$

$$A_{\phi(1020)} = A_\phi + A_\omega - A_\rho, \quad f = K^* K, \phi\eta, \phi\pi\pi, K_S K_L$$

$$\begin{aligned} \sigma_0 &= 0.46 \pm 0.10 \pm 0.04 \text{ nb} \\ m &= 1674 \pm 12 \pm 6 \text{ MeV}/c^2 \\ \Gamma_0 &= 165 \pm 38 \pm 70 \text{ MeV} \\ \varphi &= 3.01 \pm 0.38 - \text{fixed to } \pi \\ \sigma_{bkg} &= 0.36 \pm 0.18 \text{ nb} \\ \Gamma_{ee} \cdot B_{K_S K_L} &= 14.3 \pm 2.4 \pm 1.5 \pm 6.0 \text{ eV} \end{aligned}$$

Simultaneous $K_S K_L$ and $K^+ K^-$ (and $\pi\pi$) fit is needed to separate $I=0,1$ states and $\omega(1420, 1650)$, $\rho(1450, 1700)$ contribution

What we know about $\phi(1680)$



Energy dependence significantly increase width.

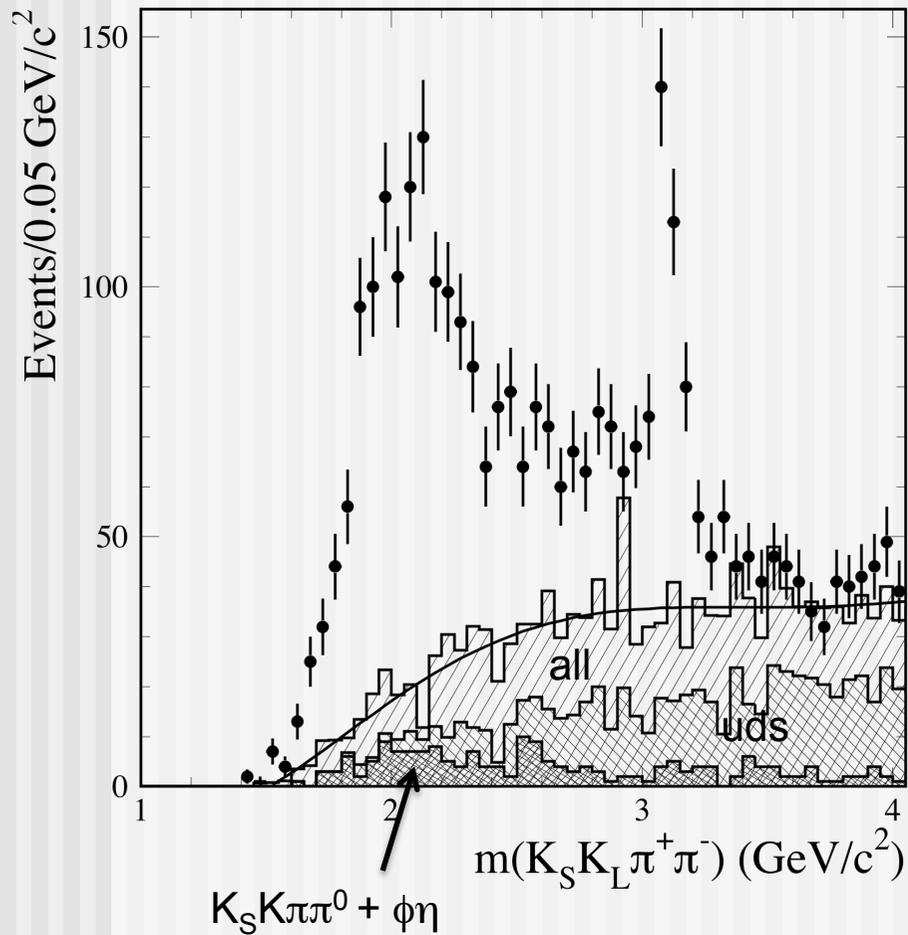
BaBar has measured $\phi(1680)$ parameters in major decay modes:

$\phi(1680) \rightarrow K_S K\pi, KK\pi^0 (K^*K), \phi\eta, \phi\pi\pi, K_S K_L$ - still no info in PDG

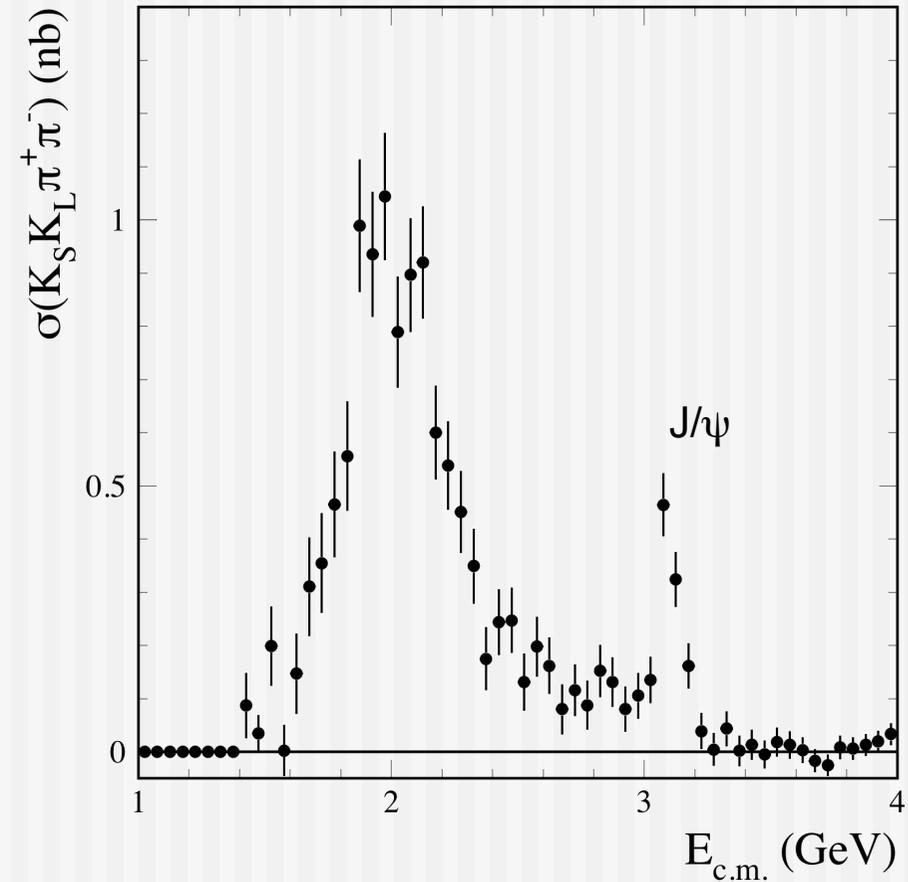
$K_S K_L \pi^+ \pi^- \gamma$ event selection

- Select (best) K_S
- Select ISR photon with $E > 3 \text{ GeV}$
- Two additional tracks from IP (no kaon ID)
- Cycle over remaining clusters with $E > 0.2 \text{ GeV}$ – K_L candidates
- Best χ^2 for 3C fit (K_L momentum float)
- $\chi^2 > 100$ and $|\text{Im}_{\gamma L} - 0.135| > 0.03$ for the $K_S K_L \pi^+ \pi^- \gamma$ hypothesis

$e^+e^- \rightarrow K_S K_L \pi^+ \pi^-$ cross section

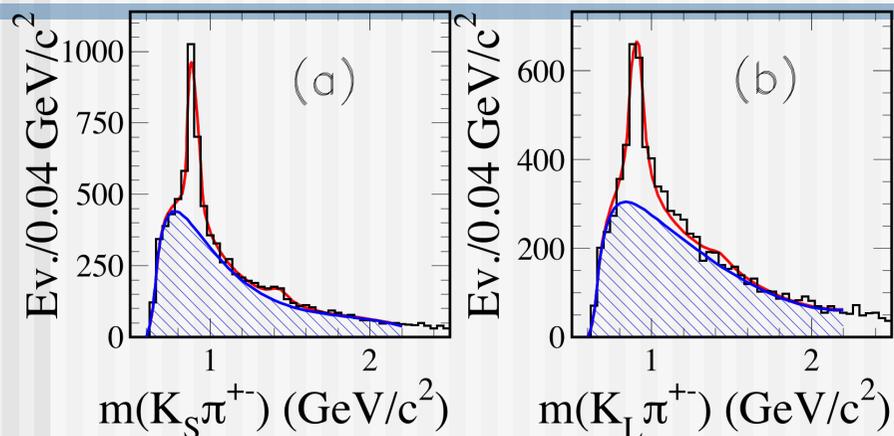


1580 events after background subtraction



No other measurements exist

Some mass distributions

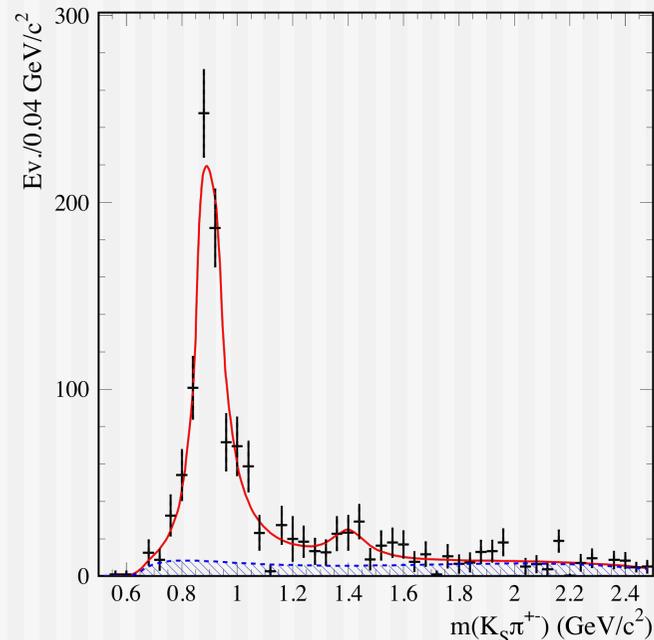
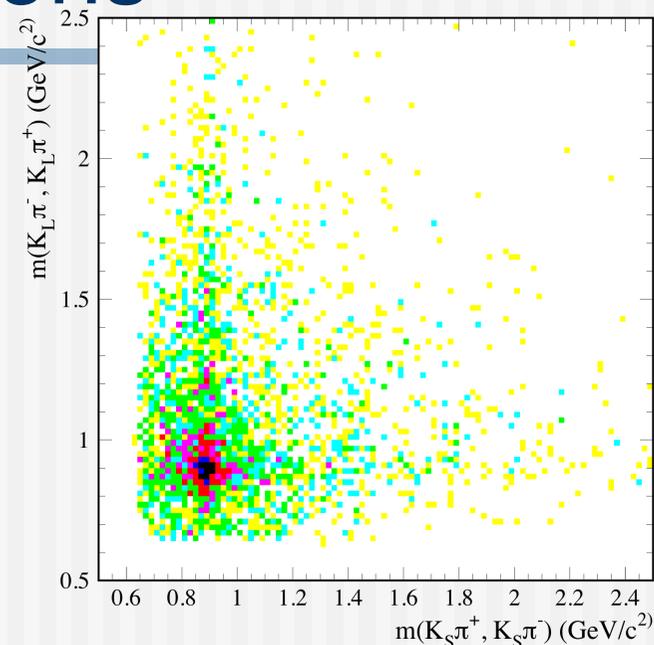


Very clear $K^*(892)^\pm$ signals with
 1322 ± 70 for $K^{*\pm}(K_S\pi)$ and 1362 ± 78 for $K^{*\pm}(K_L\pi)$
 Plus 183 ± 48 events for $K_2(1430)^\pm$

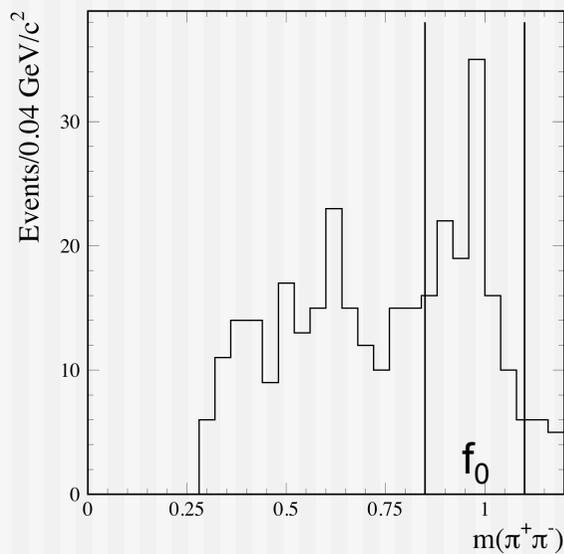
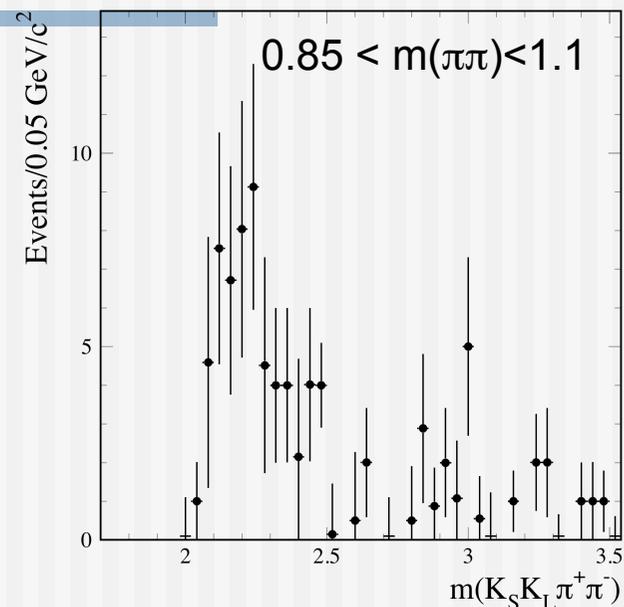
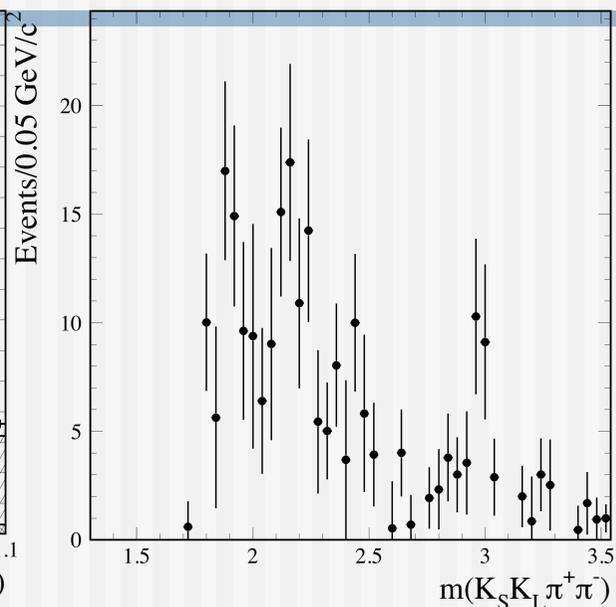
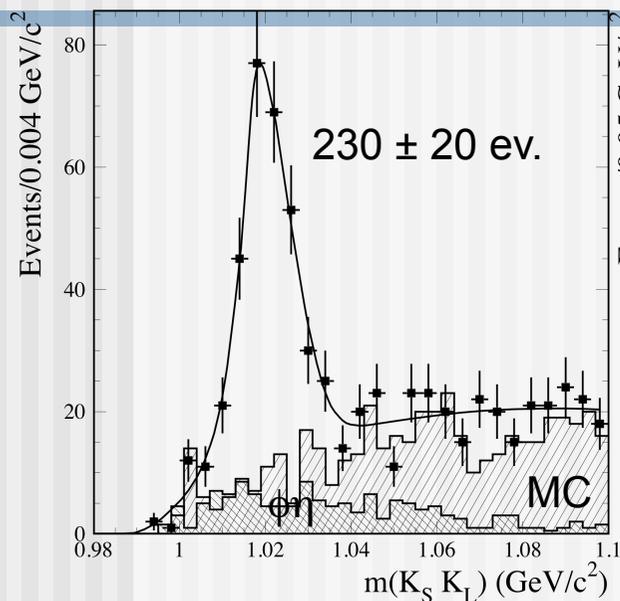
How large is $K^*(892)^+K^*(892)^-$?
 Fit slice in $m(K_L\pi^{+-})$ for number of $K_S\pi^{+-}$

Very clear signal with 913 ± 37 events (70%)
 of $K^*(892)^+K^*(892)^-$ correlated production!
 And 90 ± 16 for $K^*(892)^+K_2^*(1430)^+$.

We have negligible contribution from $K^*(892)^0\bar{K}^*(892)^0$
 from our $K^+K^-\pi^+\pi^-$ analysis! And relatively large for
 $K^*(892)^+K^*(892)^-$ from our $K^+K^-\pi^0\pi^0$ analysis.

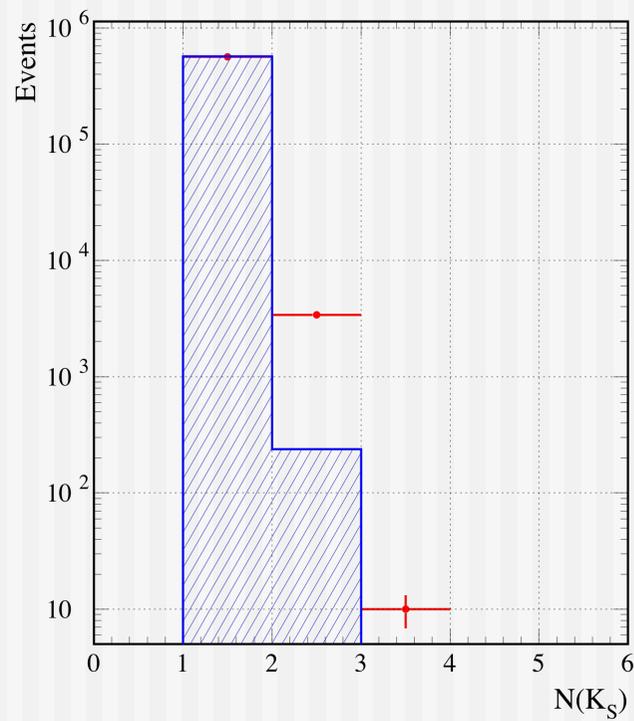


$\phi(1020)\pi^+\pi^-$ contribution



$\phi\pi^+\pi^-$ ($\phi f_0(980)$)
 seen as expected in
 agreement with our
 $K^+K^-\pi^+\pi^-$ study

$K_S K_S(2\pi, 2K)$ in ISR study



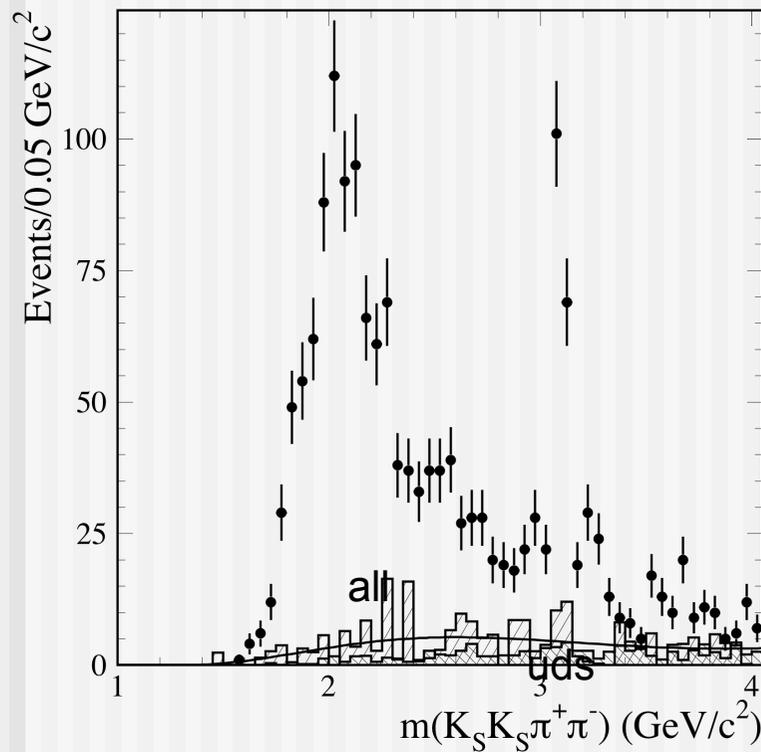
About 3000 ISR events with 2 good K_S

$K_S K_S \pi^+ \pi^- (K^+ K^-) \gamma$ event selection

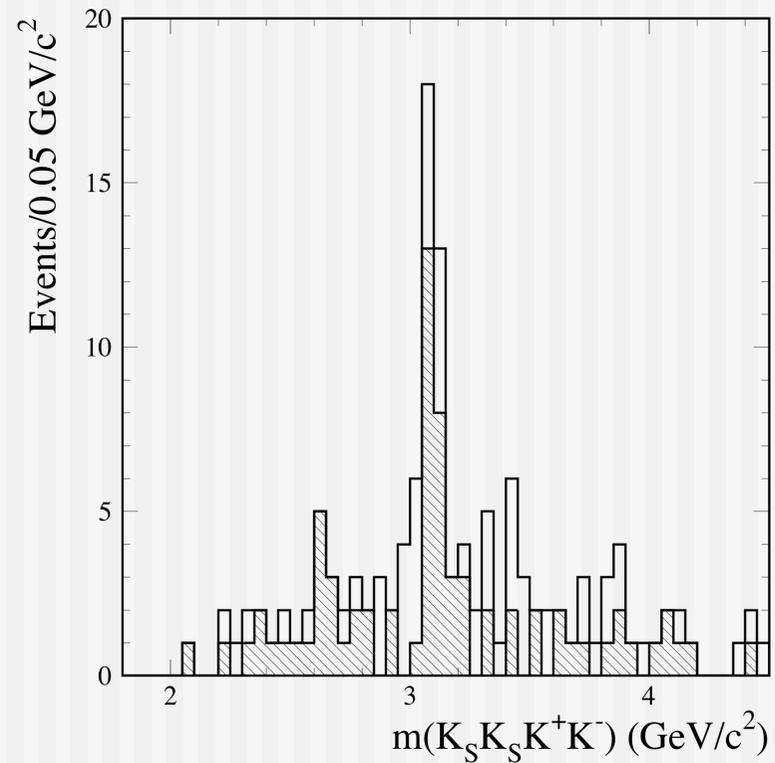
- Select 2 (best) K_S
- Select ISR photon with $E > 3$ GeV
- Two additional tracks from IP with pion or kaon ID
- Best χ^2 for 4C fit assuming $K_S K_S \pi^+ \pi^- (K^+ K^-) \gamma$ hypotheses

Six tracks with ISR photon – very low background!

$K_S K_S \pi^+ \pi^- (K^+ K^-)$ mass distribution



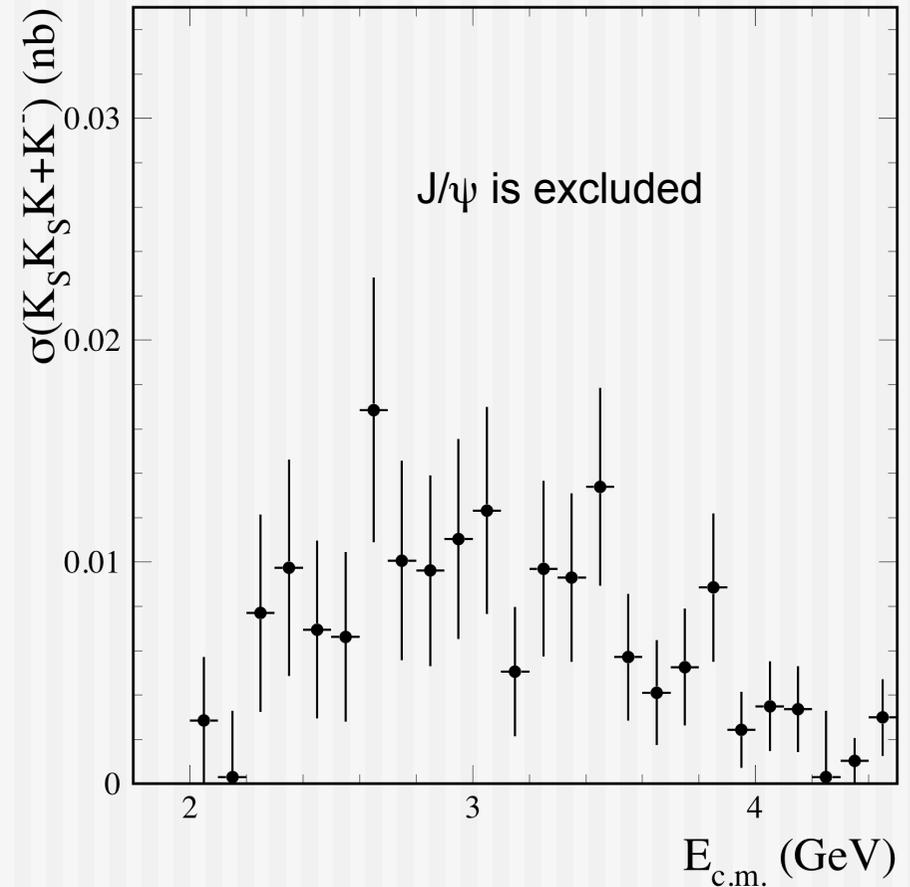
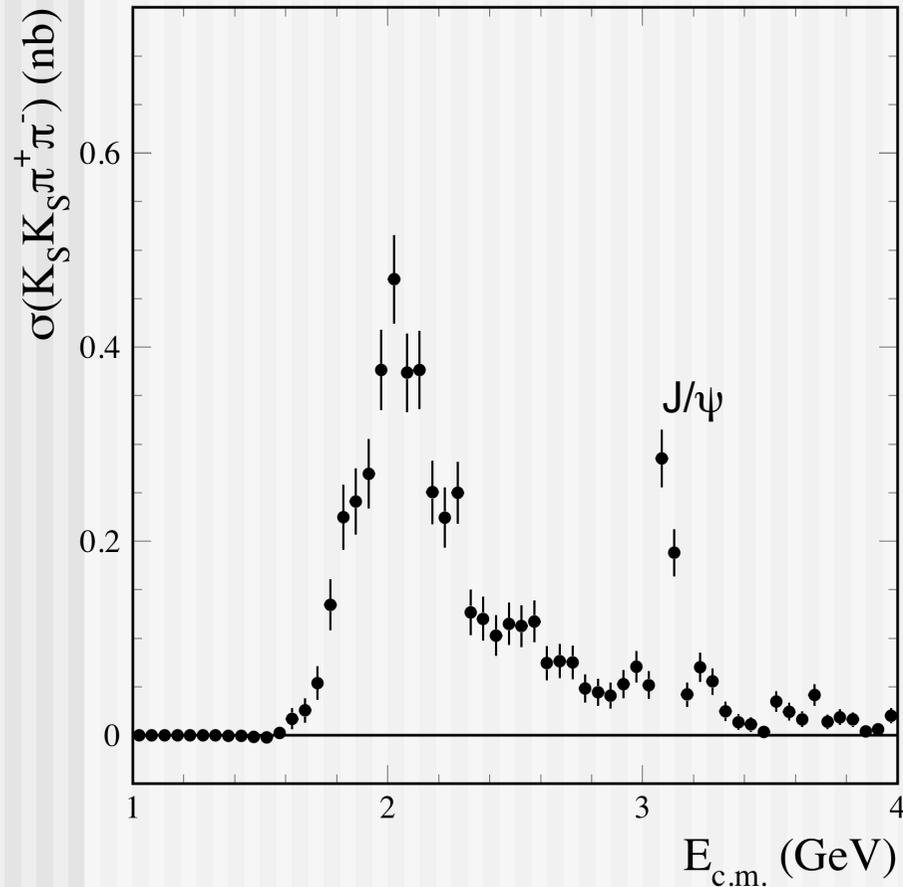
1479 events after background subtraction



129 events – assume no background
(shaded: $\phi(1020) K_S K_S$)

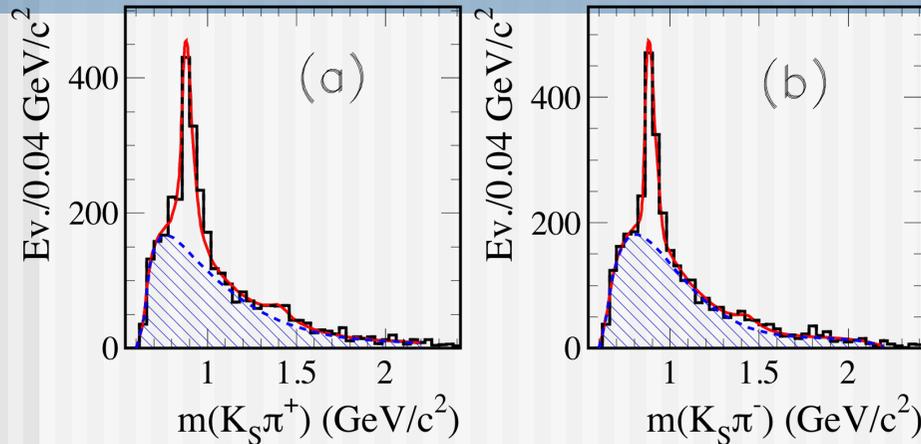
Detection efficiency from MC is about 4%

$e^+e^- \rightarrow K_S K_S \pi^+ \pi^- (K^+ K^-)$ cross sections



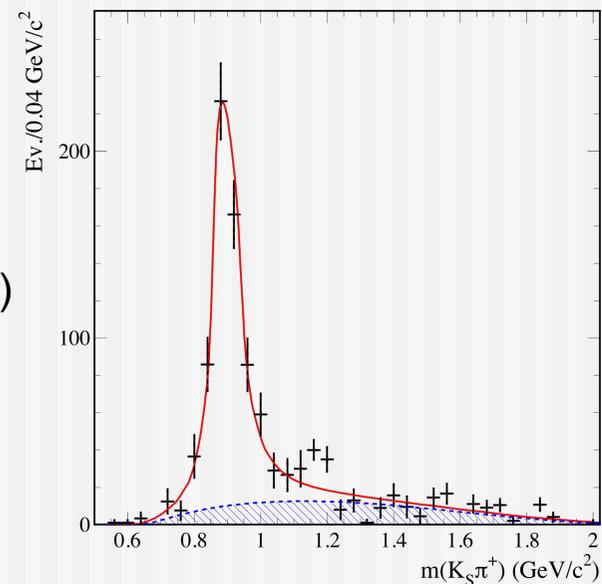
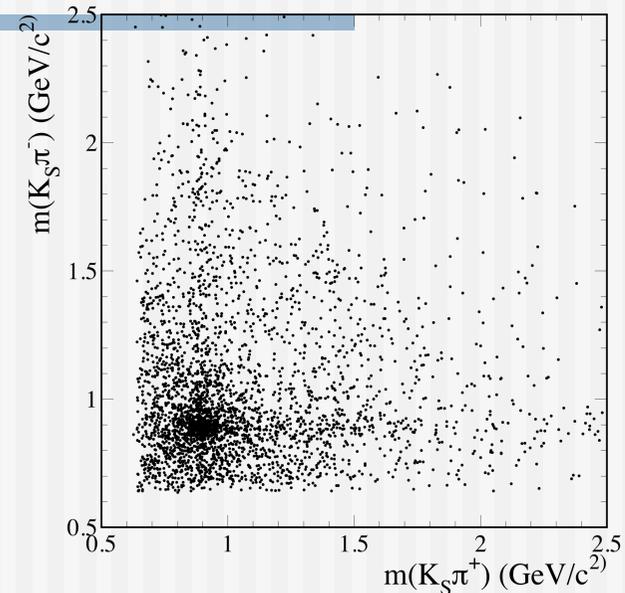
No other measurements exist

Some mass distributions (1)



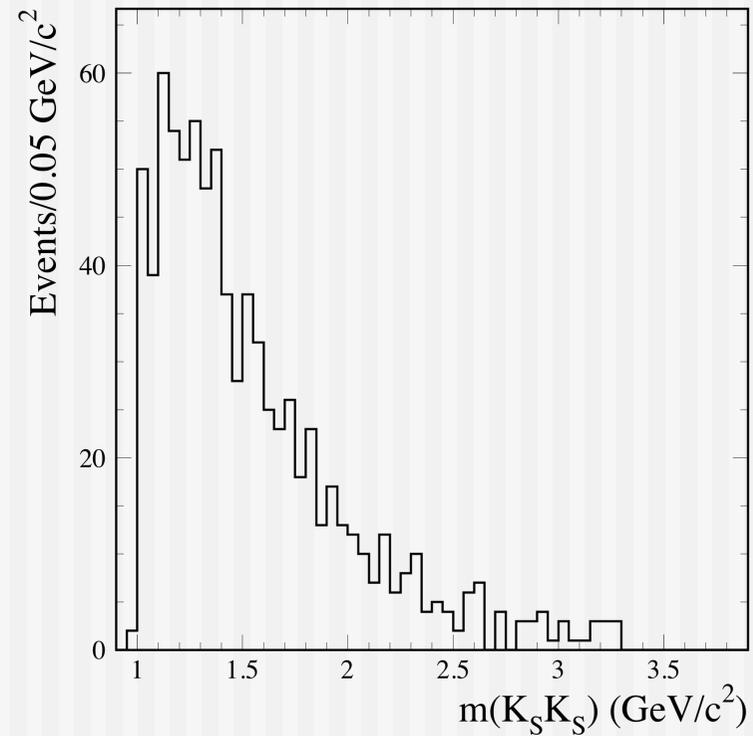
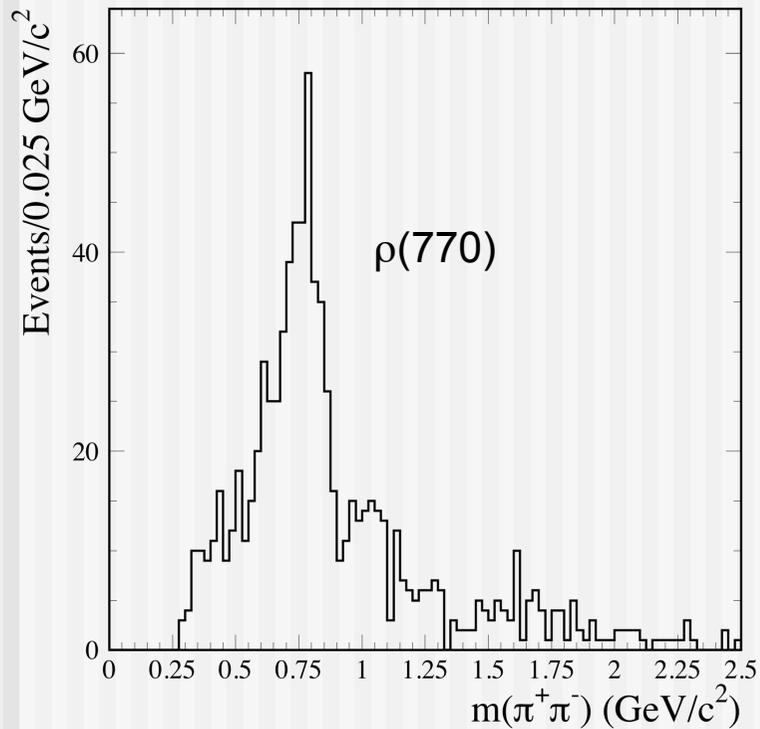
Very clear $K^*(892)^\pm$ signals with
 829 ± 49 for $K^{*+}(K_S\pi^+)$ and 856 ± 50 for $K^{*-}(K_S\pi^-)$
 Plus 116 ± 40 (70 ± 34) events for $K_2^*(1430)^\pm$

How large is $K^*(892)^+K^*(892)^-$?
 Fit slice in $m(K_S\pi^-)$ for number of $K_S\pi^+$
 Very clear signal with $742 \pm 30 \pm 100$ events (50%)
 of $K^*(892)^+K^*(892)^-$ correlated production!
 No $K^*(892)^+K_2^*(1430)^+$ seen.



Some mass distributions (2)

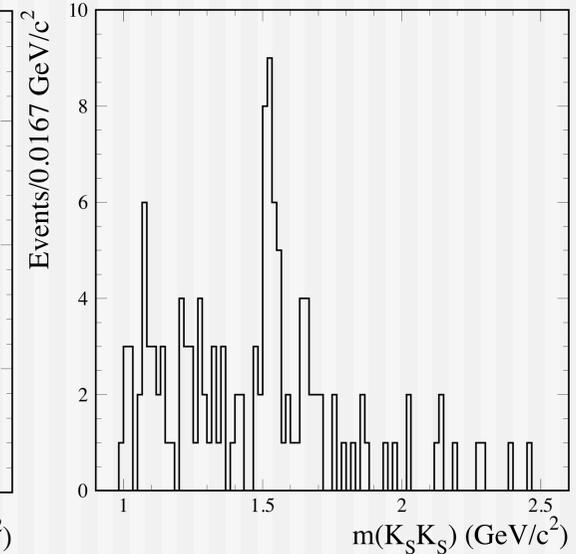
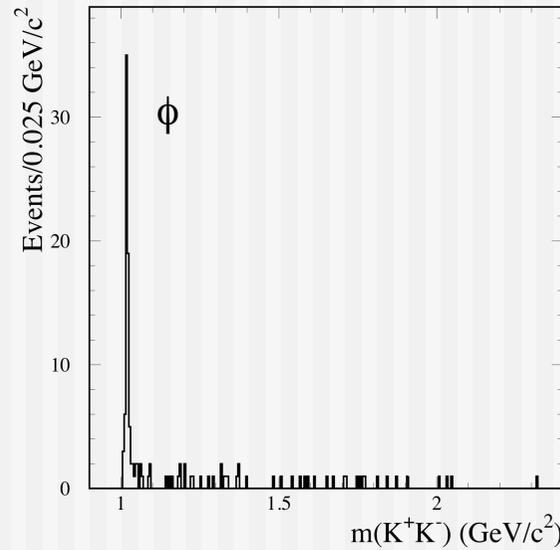
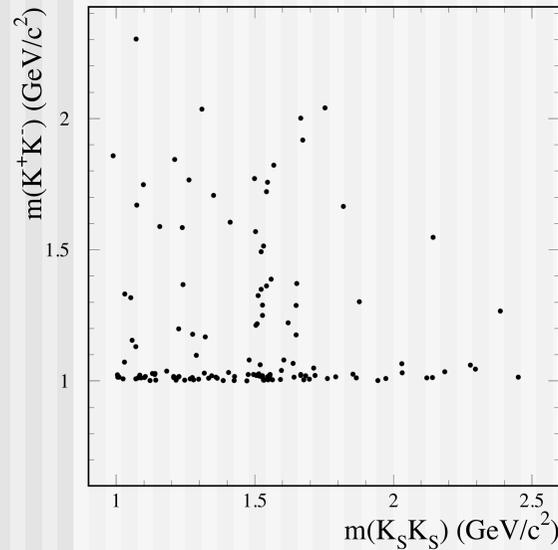
If we exclude $K^*(892)^+K^*(892)^-$ by $|m(K_S\pi) - m(K^*)| < 0.15 \text{ GeV}/c^2$ in both combinations:



Plus some number of $K^*(892)K_S\pi$ events

Some mass distributions (3)

For the $K_S K_S K^+ K^-$ channel:



$N(K^+K^- f_2') = 29 \pm 7$ events

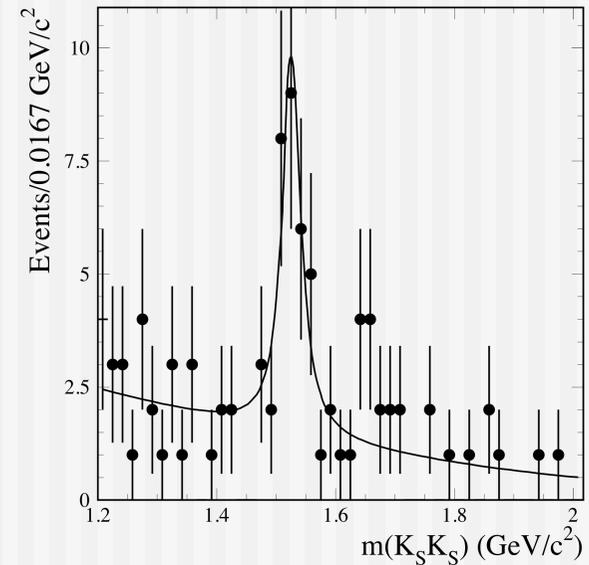
$m(K_S K_S) = 1.526 \pm 0.007$ GeV/c²

$\Gamma = 0.037 \pm 0.013$ GeV

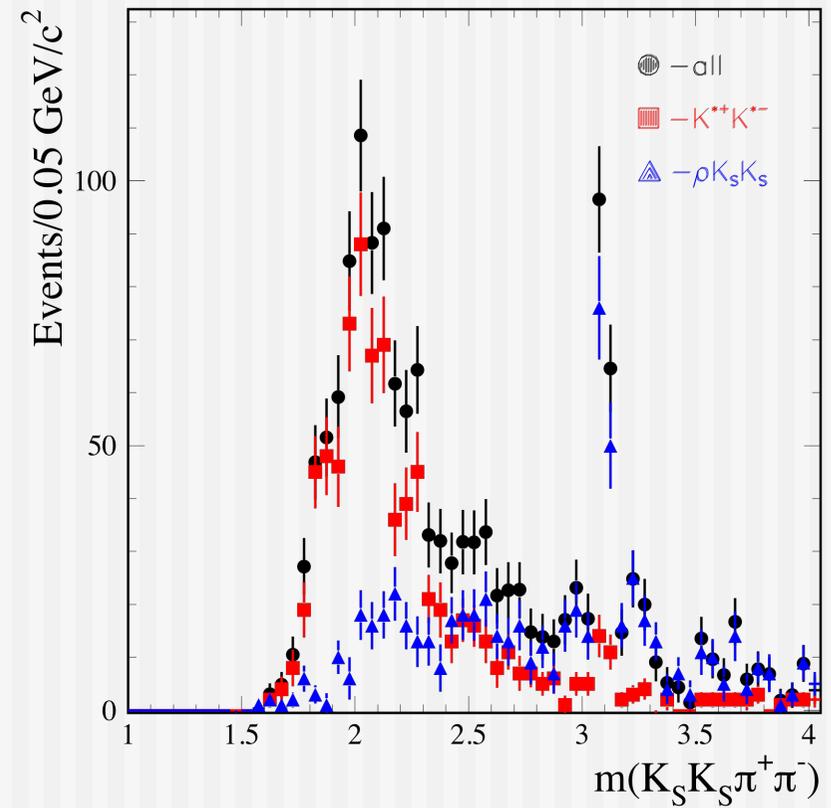
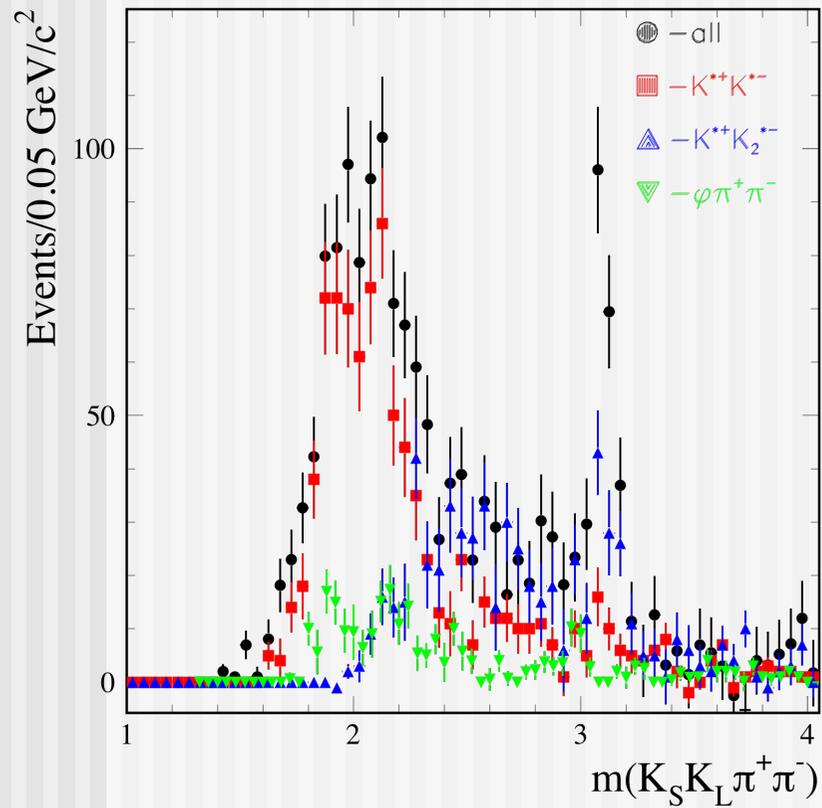
PDG:

$m(f_2') = 1.525 \pm 0.005$ GeV/c²

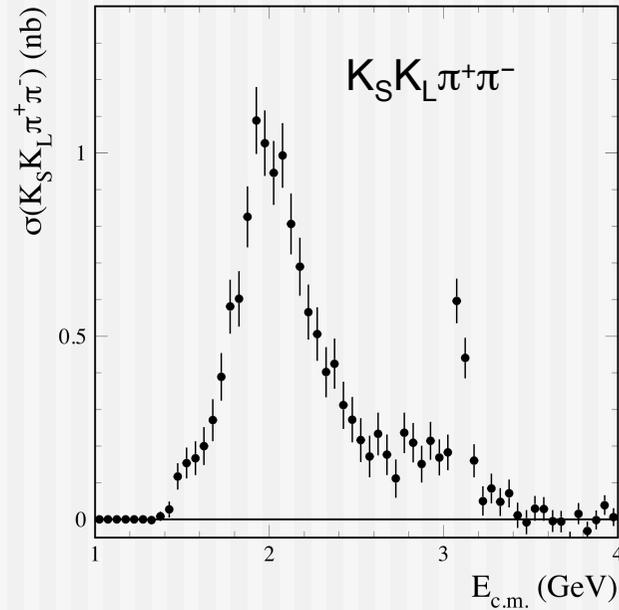
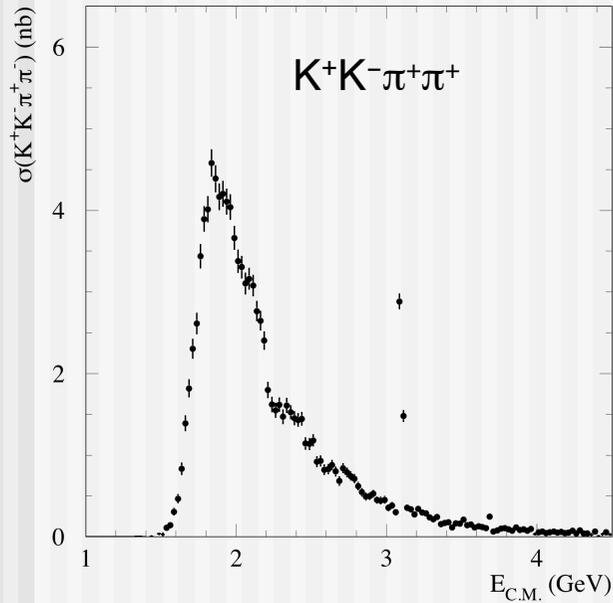
$\Gamma = 0.073 \pm 0.006$ GeV



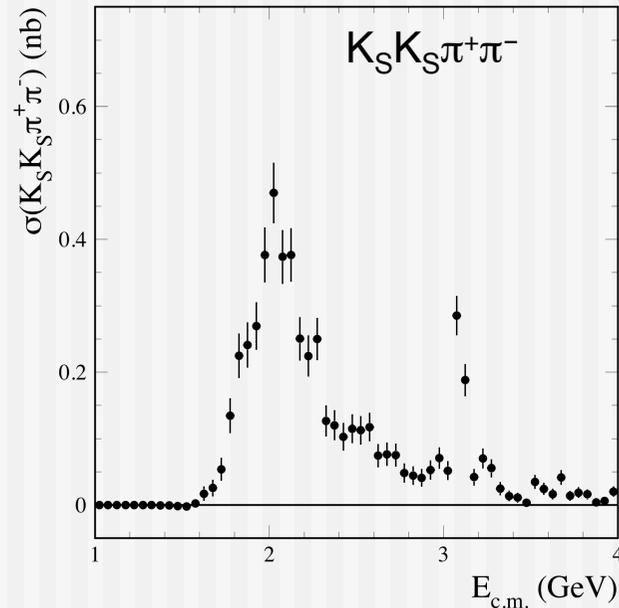
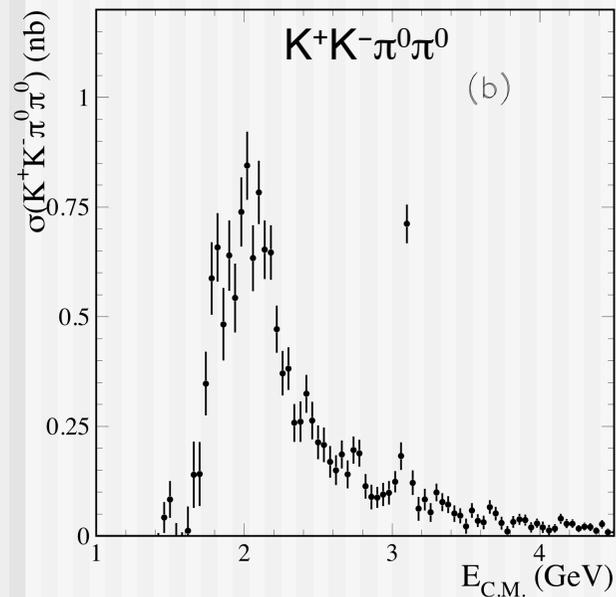
$K_S K_L \pi^+ \pi^-$, $K_S K_S \pi^+ \pi^-$ signal decomposition



The cross section comparison – BaBar data



we'd expect:
 $N(K_S K_S \pi^+ \pi^-) =$
 $1/2 N(K_S K_L \pi^+ \pi^-)$



Iso-spin relations for $K^+K^-\pi^+\pi^+$ vs. $K^+K^-\pi^0\pi^0$ vs. $K_S K_L \pi^+\pi^-$ vs. $K_S K_S \pi^+\pi^-$

Only $K^*(892)^+K^*(892)^-$ contribution can be compared using iso-spin relations, and we expect:

$$\begin{aligned} N(K^+K^-\pi^0\pi^0) &= \frac{1}{4} N(K^0\bar{K}^0 \pi^+\pi^-) \\ N(K_S K_L \pi^+\pi^-) &= \frac{1}{2} N(K^0\bar{K}^0 \pi^+\pi^-) \\ N(K_S K_S \pi^+\pi^-) &= N(K_L K_L \pi^+\pi^-) = \frac{1}{4} N(K^0\bar{K}^0 \pi^+\pi^-) \end{aligned}$$

We detected correlated pairs:

$$N(K^+K^-\pi^0\pi^0) = 1750 \pm 60 \quad \text{eff} = 8\%$$

$$N(K_S K_L \pi^+\pi^-) = 2098 \pm 209 \quad \text{eff} = 5\%$$

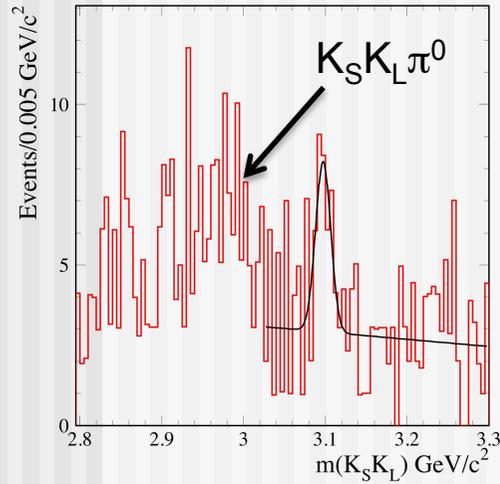
$$N(K_S K_S \pi^+\pi^-) = 742 \pm 104 \quad \text{eff} = 4.5\%$$

Should be equal numbers after efficiency normalized to 5% and iso-spin correction:

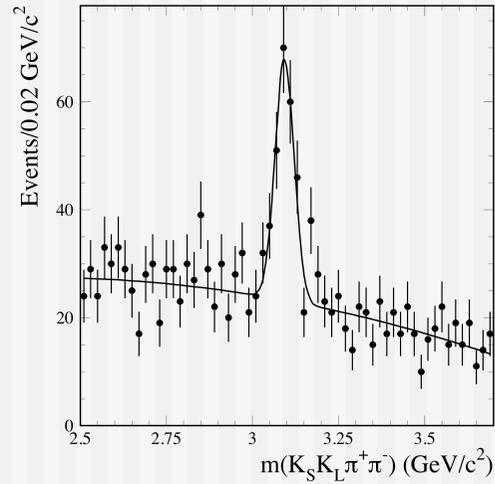
$$2188 \pm 76 \quad \sim \quad 2098 \pm 209 \quad \sim \quad 1648 \pm 232 \quad \text{Some tension } (\sim 2 \text{ sigma})$$

30% 63% 50% of all events – how the rest are related?
 to g-2 relation?

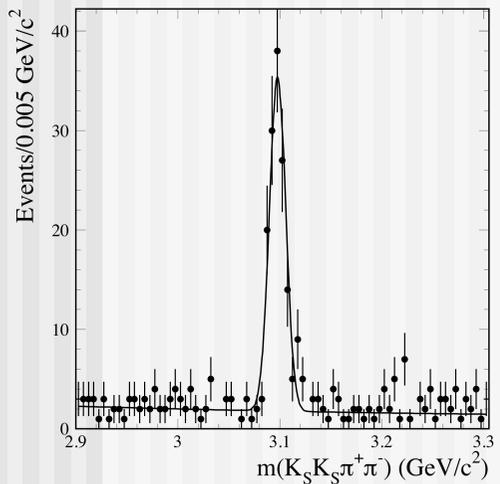
J/ψ region



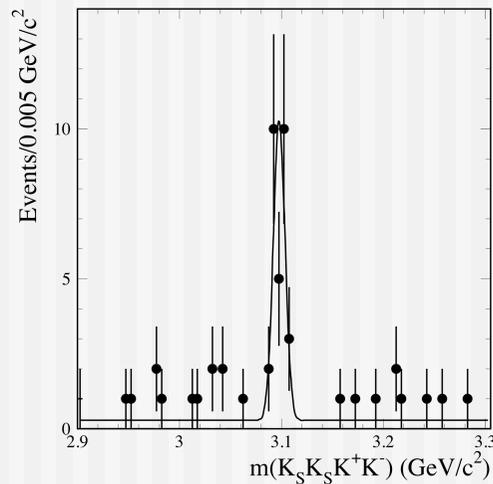
$N = 24.6 \pm 7.5$



$N = 154 \pm 19$



$N = 248 \pm 27$



$N = 28.5 \pm 5.1$

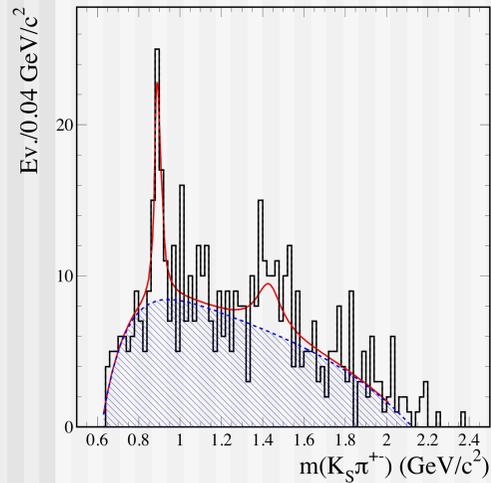
We observe a J/ψ signal in all studied channels

We measure:

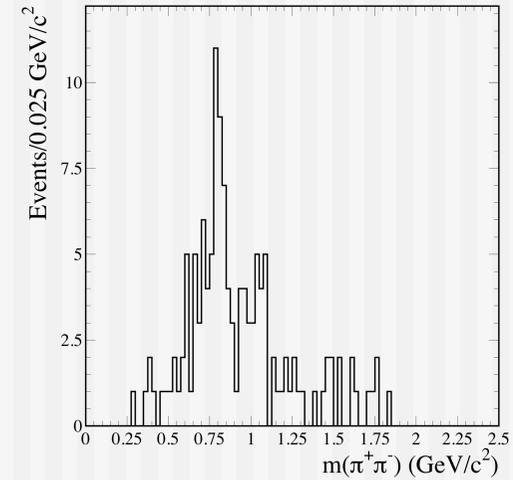
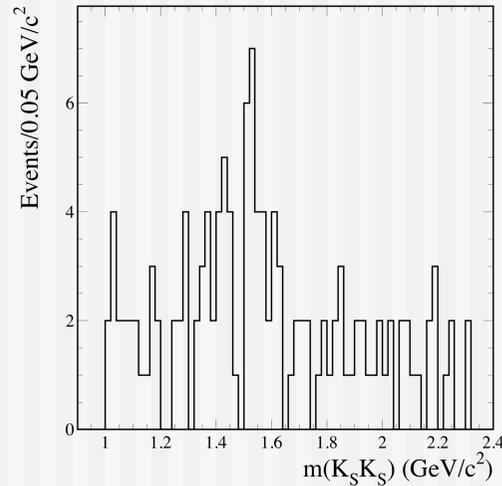
$$\mathcal{B}_{J/\psi \rightarrow f} \cdot \Gamma_{ee}^{J/\psi} = \frac{N_{J/\psi \rightarrow f} \cdot m_{J/\psi}^2}{6\pi^2 \cdot d\mathcal{L}/dE \cdot \epsilon_f(m_{J/\psi}) \cdot C}$$

J/ψ intermediate states

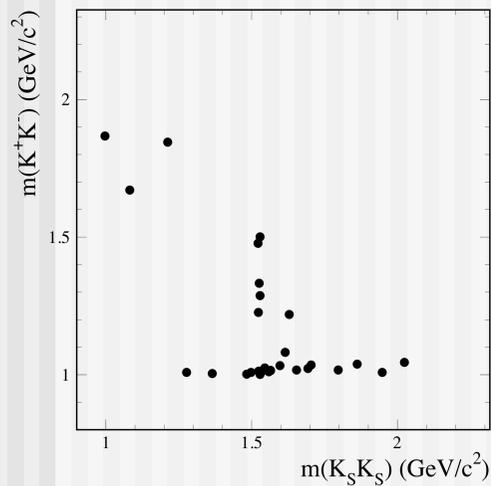
For $K_S K_S \pi^+ \pi^-$



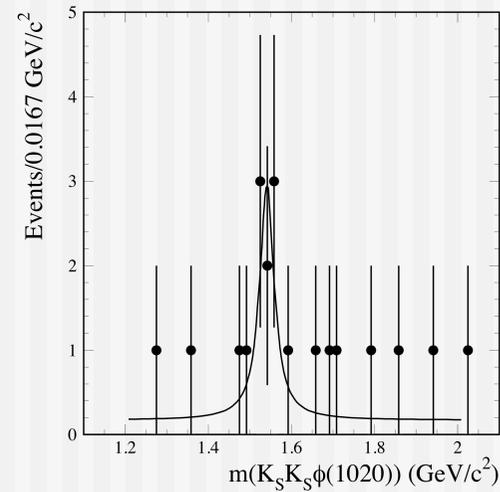
If $K^*(892)^+ K^*(892)^-$ are excluded:



For $K_S K_S K^+ K^-$



$N(\phi K_S K_S) = 20 \pm 5$



$N(\phi f_2') = 11 \pm 4$

J/ψ decay results (Preliminary)

Measured Quantity	Measured value (eV)	This work Br (10 ⁻³) Γ _{ee} = 5.55 ± 0.14 keV	PDG 2012
Γ _{ee} • Br(J/ψ → K _S K _L)	1.13±0.34±0.11	0.20 ± 0.06 ± 0.02	0.146 ± 0.026 S=2.7
Γ _{ee} • Br(J/ψ → K _S K _L π ⁺ π ⁻)	20.9±2.7±2.1	3.7 ± 0.6 ± 0.4	no entry
Γ _{ee} • Br(J/ψ → K _S K _S π ⁺ π ⁻)	9.3±0.9±0.5	1.68 ± 0.16 ± 0.08	no entry
Γ _{ee} • Br(J/ψ → K _S K _S K ⁺ K ⁻)	2.3±0.4±0.1	0.42 ± 0.08 ± 0.02	no entry
Γ _{ee} • Br(J/ψ → K _S K _S φ) • Br(φ → K ⁺ K ⁻)	1.6±0.4±0.1	0.58 ± 0.14 ± 0.03	no entry
Γ _{ee} • Br(J/ψ → f ₂ 'φ) • Br(φ → K ⁺ K ⁻) • B(f ₂ ' → K _S K _S)	0.88±0.34±0.04	0.45±0.17 ± 0.02	0.8 ± 0.4 S=2.7

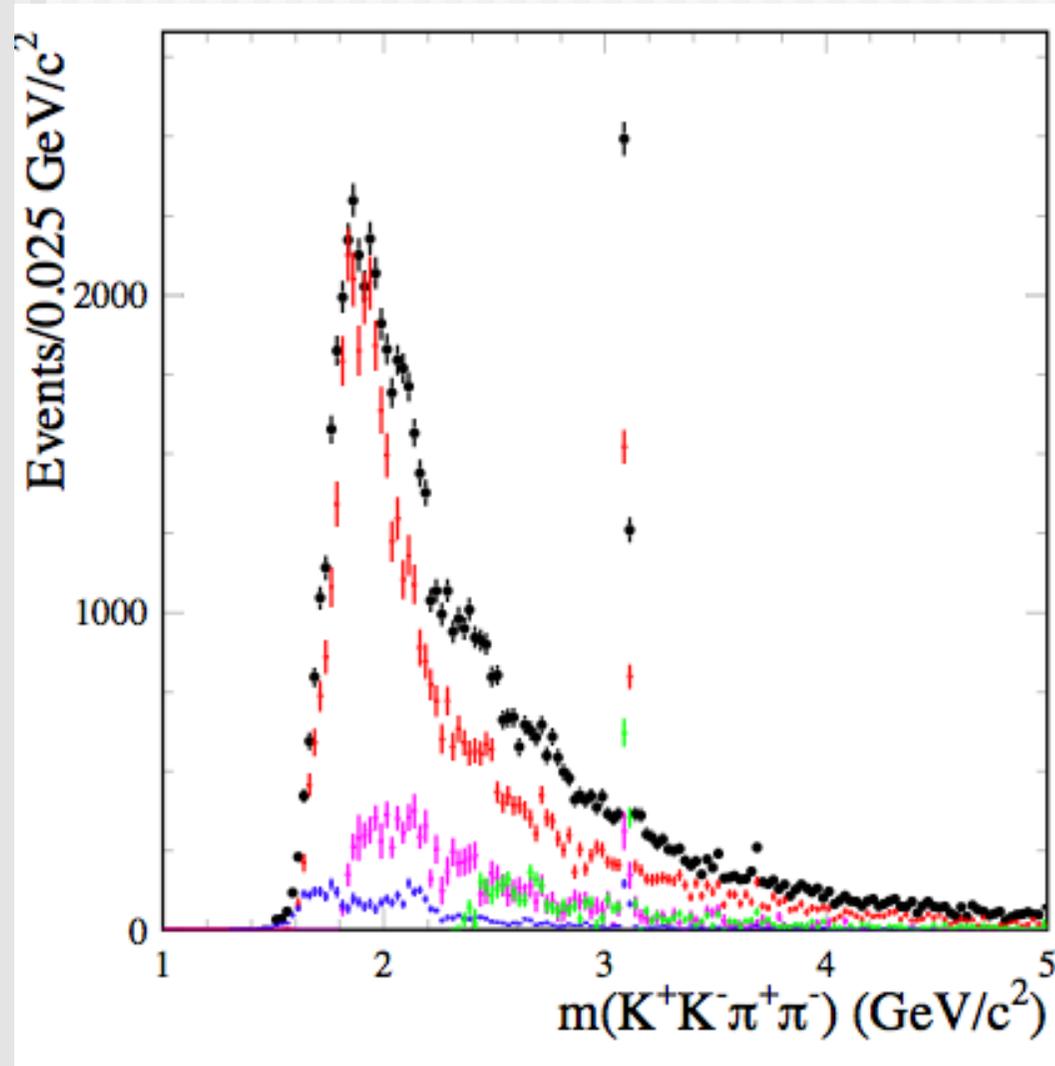
$$B(J/\psi \rightarrow \phi f_2') = (0.48 \pm 0.18) \cdot 10^{-3} \text{ (MarkII)}$$

$$B(J/\psi \rightarrow \phi f_2') = (1.23 \pm 0.026 \pm 0.20) \cdot 10^{-3} \text{ (DM2)}$$

Summary

- BaBar continues analysis of collected data and ISR studies in particular
- Recently published results for $e^+e^- \rightarrow \pi^+\pi^-\pi^+\pi^-$, K^+K^- reactions have the best to date accuracy.
- New analysis of $K_S K_L$, $K_S K_L \pi^+\pi^-$, $K_S K_S \pi^+\pi^-$, $K_S K_S K^+K^-$ has been performed
- The $e^+e^- \rightarrow K_S K_L \pi^+\pi^-$, $K_S K_S \pi^+\pi^-$, $K_S K_S K^+K^-$ cross sections were never studied before
- Using these cross sections we can reduce uncertainty in the muon g-2 calculation.
- J/ψ decays to $K_S K_L \pi^+\pi^-$, $K_S K_S \pi^+\pi^-$, $K_S K_S K^+K^-$ have been measured for the first time.
- Results for the $\pi^+\pi^-\pi^0\pi^0$ and $K_S K \pi \pi^0$ should come out soon

Decomposition of $K^+K^-\pi^+\pi^-$ mass spectrum



$K^+K^-\pi^+\pi^-$
 $K^{*0}(892)K\pi$
 $K^+K^-\rho(770)$
 $\phi\pi^+\pi^-$
 $K_2^{*0}(1430)K\pi$

Tables with cross sections
(corrected for BF) are provided

SM prediction for muon g-2

ArXiv:1010.4180, arXiv:1105.3149

$$a_{\mu}^{\text{experimental}} = (g-2)/2$$

11 659 208.9 \pm 6.3 $\times 10^{-10}$ world average

$$a_{\mu}^{\text{theory}} = a_{\mu}^{\text{QED}} + a_{\mu}^{\text{EW}} + a_{\mu}^{\text{hadron}}$$

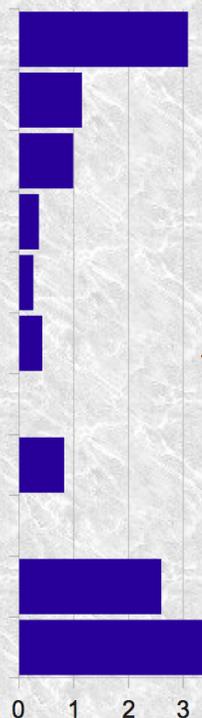
QED contribution	11 658 471.808 \pm 0.015	Kinoshita & Nio, Aoyama et al
EW contribution	15.4 \pm 0.2	Czarnecki et al
NLO hadronic	-9.8 \pm 0.1	HLMNT11

Hadronic contributions

LO hadronic 694.1 \pm 4.3 $\times 10^{-10}$ HLMNT 11

main channels contribution to precision at $\sqrt{s} < 1.8 \text{ GeV}$

From direct integration
Without model constraints
 δa_{μ}



$\pi^+\pi^-$	505.65 \pm 3.09	
$\pi^+\pi^-2\pi^0$	18.62 \pm 1.15	
$\pi^+\pi^-\pi^0$	47.38 \pm 0.99	(mostly from omega region)
$2\pi^+2\pi^-$	13.64 \pm 0.36	(BaBar)
K^+K^-	22.95 \pm 0.26	(BaBar)

from Isospin relations 5.98 ± 0.42 for not measured $KK\pi, KK2\pi, 2\pi4\pi^0, 2\pi3\pi^0$

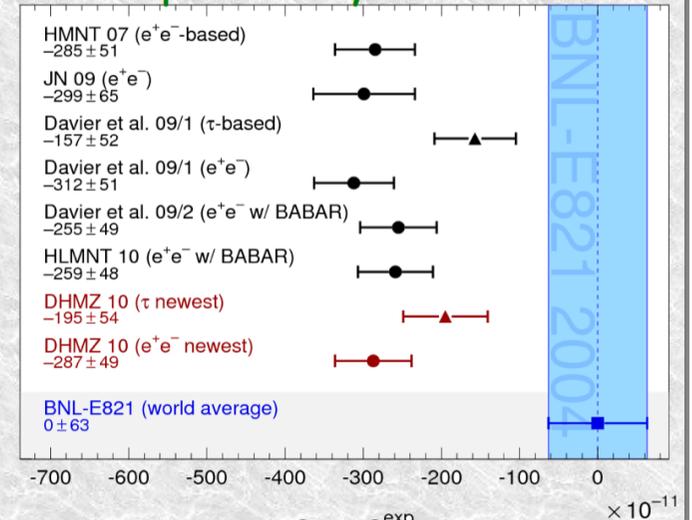
(or 12.46 ± 0.76 for $\sqrt{s} < 2 \text{ GeV}$) (1.5-3 σ of total error - crucial in case of isospin violation)

Rqcd_[2-11.09GeV] 41.19 \pm 0.82

Light-by-light 10.5 \pm 2.6 Prades, de Rafael & Vainshtein

Theory TOTAL \pm 4.9

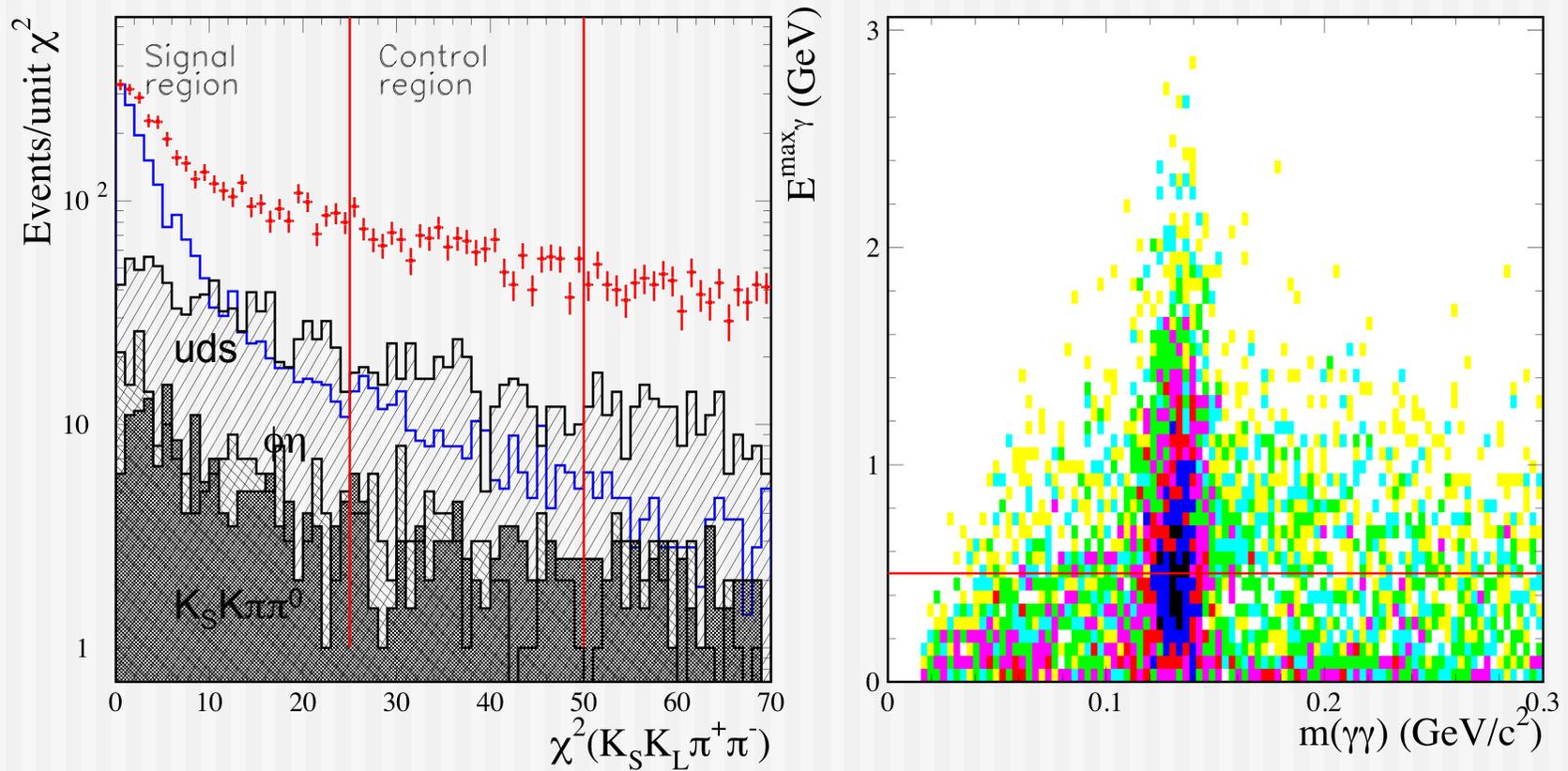
$\Delta \text{Exp} - \text{Theory} \sim 3.3 - 3.6\sigma$



$a_{\mu} - a_{\mu}^{\text{exp}}$
New g-2 experiments at FNAL and J-PARC have plans to reduce precision to 1.5×10^{-10}

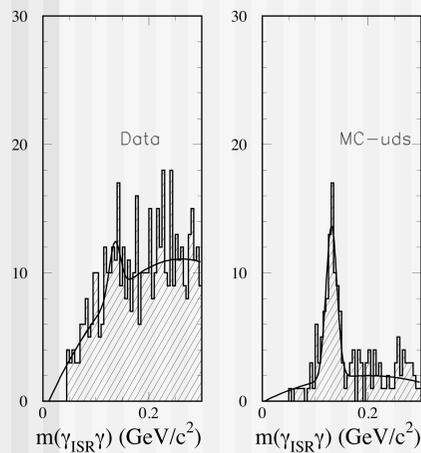
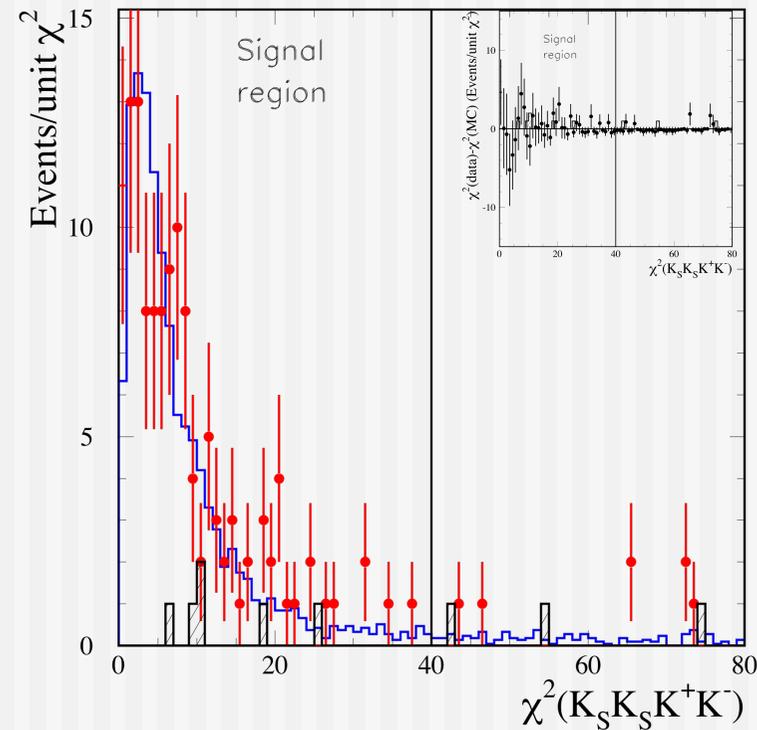
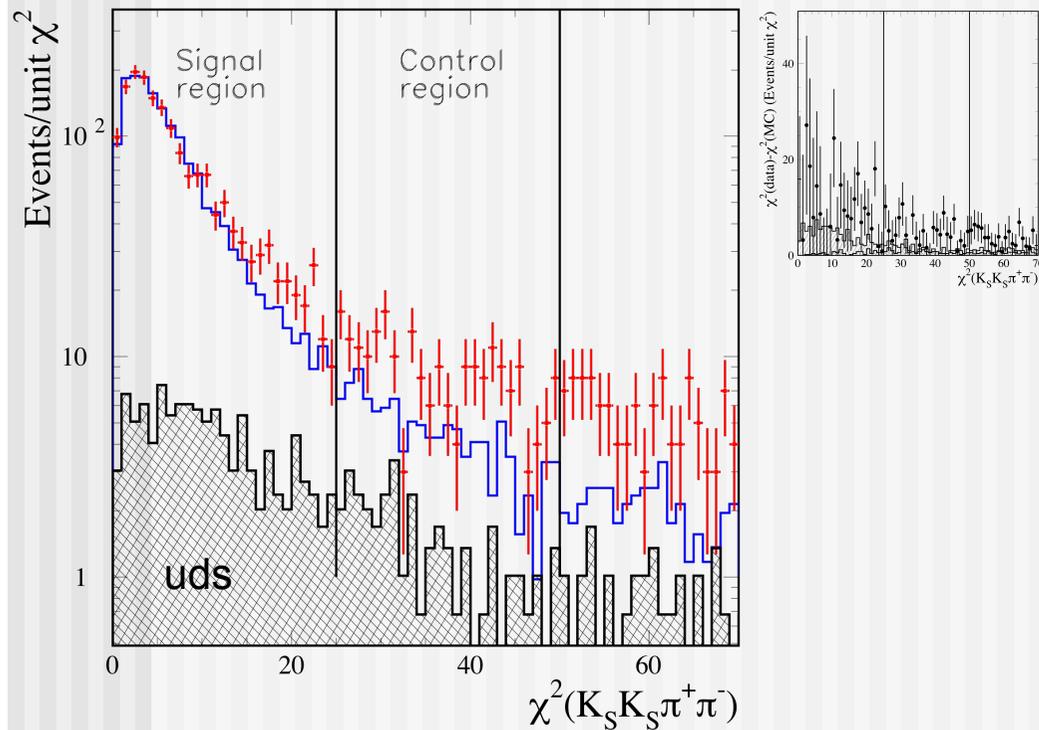
need more theory, probably with help of experimental Transition FormFactors

$K_S K_L \pi^+ \pi^- \gamma$ selection – K_L is cluster in EMC

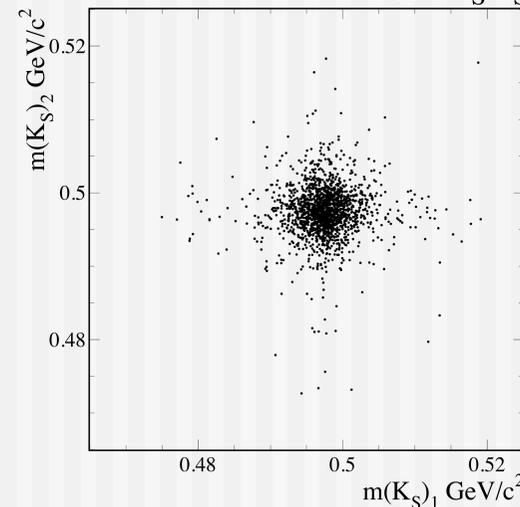


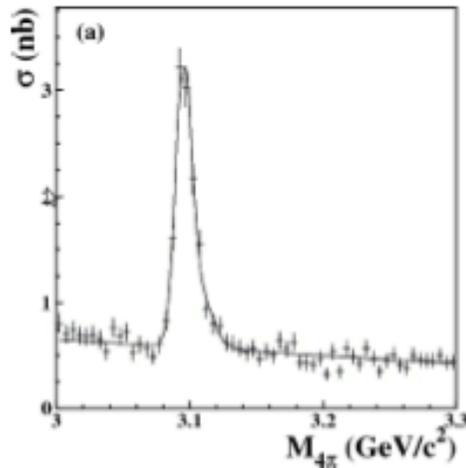
Huge background from events with π^0 . Cut $E_{\gamma}^{\max} < 0.5$ GeV does not help much. Known background does not explain what we see – use observed side band for the background estimate.

$K_S K_S \pi^+ \pi^- (K^+ K^-) \gamma$ selection



Very low background,
21/61 data-MC uds normalization



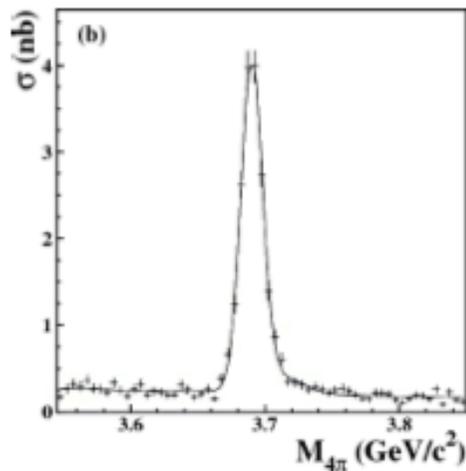


$$\mathcal{B}_{J/\psi \rightarrow 2(\pi^+ \pi^-)} \cdot \sigma_{int}^{J/\psi} = \frac{N(J/\psi \rightarrow 2(\pi^+ \pi^-))}{d\mathcal{L}/dE \cdot \epsilon_{MC}} = (48.9 \pm 2.1_{stat} \pm 1.0_{syst}) \text{ MeV}/c^2 \text{ nb}$$

$$\mathcal{B}_{J/\psi \rightarrow 2(\pi^+ \pi^-)} = (3.67 \pm 0.16_{stat} \pm 0.08_{syst} \pm 0.09_{ext}) \cdot 10^{-3}$$

$$\mathcal{B}_{J/\psi \rightarrow 2(\pi^+ \pi^-)}^{PDG} = (3.55 \pm 0.23) \cdot 10^{-3}$$

→ agrees with PDG, higher in precision



$$\mathcal{B}_{\psi(2S) \rightarrow J/\psi \pi^+ \pi^-} \cdot \mathcal{B}_{J/\psi \rightarrow \mu^+ \mu^-} \cdot \sigma_{int}^{\psi(2S)} = \frac{N(\psi(2S) \rightarrow \pi^+ \pi^- \mu^+ \mu^-)}{d\mathcal{L}/dE \cdot \epsilon_{MC}} = (84.7 \pm 2.2_{stat} \pm 1.8_{syst}) \text{ MeV}/c^2 \text{ nb}$$

$$\mathcal{B}_{\psi(2S) \rightarrow J/\psi \pi^+ \pi^-} = 0.354 \pm 0.009_{stat} \pm 0.007_{syst} \pm 0.007_{ext}$$

$$\mathcal{B}_{\psi(2S) \rightarrow J/\psi \pi^+ \pi^-}^{PDG} = 0.336 \pm 0.005$$

$$\mathcal{B}_{\psi(2S) \rightarrow J/\psi \pi^+ \pi^-}^{CLEO} = 0.3504 \pm 0.009_{stat} \pm 0.0007_{syst} \pm 0.0077_{ext}$$

→ agrees with recent CLEO result (PRD 78, 011102 (2008))

J/ψ region for $K^+K^-\pi^+\pi^-$, $K^+K^-\pi^0\pi^0$, $K^+K^-K^+K^-$

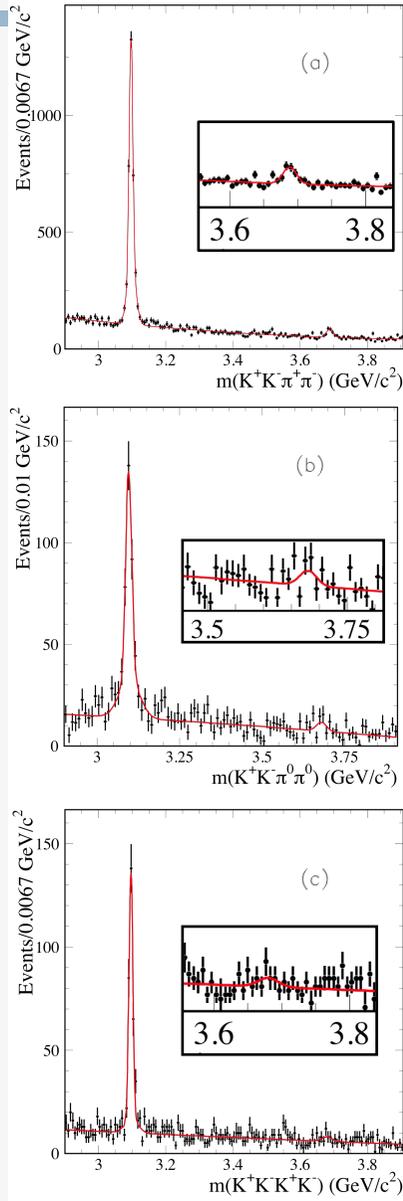


TABLE XIII: Summary of the J/ψ and $\psi(2S)$ branching fraction values obtained in this analysis.

Measured Quantity	Measured Value (eV)	J/ψ or $\psi(2S)$ Branching Fraction (10^{-3})	
		This work	PDG2010
$\Gamma_{ee}^{J/\psi} \cdot \mathcal{B}_{J/\psi \rightarrow K^+K^-\pi^+\pi^-}$	$37.94 \pm 0.81 \pm 1.10$	$6.84 \pm 0.15 \pm 0.27$	6.6 ± 0.5
$\Gamma_{ee}^{J/\psi} \cdot \mathcal{B}_{J/\psi \rightarrow K^+K^-\pi^0\pi^0}$	$11.75 \pm 0.81 \pm 0.90$	$2.12 \pm 0.15 \pm 0.18$	2.45 ± 0.31
$\Gamma_{ee}^{J/\psi} \cdot \mathcal{B}_{J/\psi \rightarrow K^+K^-K^+K^-}$	$4.00 \pm 0.33 \pm 0.29$	$0.72 \pm 0.06 \pm 0.05$	0.76 ± 0.09
$\Gamma_{ee}^{J/\psi} \cdot \mathcal{B}_{J/\psi \rightarrow K^{*0}\bar{K}_2^{*0} \cdot \mathcal{B}_{K^{*0} \rightarrow K^+\pi^-} \cdot \mathcal{B}_{\bar{K}_2^{*0} \rightarrow K^-\pi^+}$	$8.59 \pm 0.36 \pm 0.27$	$6.98 \pm 0.29 \pm 0.21$	6.0 ± 0.6
$\Gamma_{ee}^{J/\psi} \cdot \mathcal{B}_{J/\psi \rightarrow K^{*0}\bar{K}^{*0} \cdot \mathcal{B}_{K^{*0} \rightarrow K^+\pi^-} \cdot \mathcal{B}_{\bar{K}^{*0} \rightarrow K^-\pi^+}$	$0.57 \pm 0.15 \pm 0.03$	$0.23 \pm 0.06 \pm 0.01$	0.23 ± 0.07
$\Gamma_{ee}^{J/\psi} \cdot \mathcal{B}_{J/\psi \rightarrow \phi\pi^+\pi^-} \cdot \mathcal{B}_{\phi \rightarrow K^+K^-}$	$2.19 \pm 0.23 \pm 0.07$	$0.81 \pm 0.08 \pm 0.03$	0.94 ± 0.09
$\Gamma_{ee}^{J/\psi} \cdot \mathcal{B}_{J/\psi \rightarrow \phi\pi^0\pi^0} \cdot \mathcal{B}_{\phi \rightarrow K^+K^-}$	$1.36 \pm 0.27 \pm 0.07$	$0.50 \pm 0.10 \pm 0.03$	0.56 ± 0.16
$\Gamma_{ee}^{J/\psi} \cdot \mathcal{B}_{J/\psi \rightarrow \phi K^+K^-} \cdot \mathcal{B}_{\phi \rightarrow K^+K^-}$	$2.26 \pm 0.26 \pm 0.16$	$1.66 \pm 0.19 \pm 0.12$	1.83 ± 0.24^a
$\Gamma_{ee}^{J/\psi} \cdot \mathcal{B}_{J/\psi \rightarrow \phi f_0} \cdot \mathcal{B}_{\phi \rightarrow K^+K^-} \cdot \mathcal{B}_{f_0 \rightarrow \pi^+\pi^-}$	$0.69 \pm 0.11 \pm 0.05$	$0.25 \pm 0.04 \pm 0.02$	0.18 ± 0.04^b
$\Gamma_{ee}^{J/\psi} \cdot \mathcal{B}_{J/\psi \rightarrow \phi f_0} \cdot \mathcal{B}_{\phi \rightarrow K^+K^-} \cdot \mathcal{B}_{f_0 \rightarrow \pi^0\pi^0}$	$0.48 \pm 0.12 \pm 0.05$	$0.18 \pm 0.04 \pm 0.02$	0.17 ± 0.07^c
$\Gamma_{ee}^{J/\psi} \cdot \mathcal{B}_{J/\psi \rightarrow \phi f_x} \cdot \mathcal{B}_{\phi \rightarrow K^+K^-} \cdot \mathcal{B}_{f_x \rightarrow \pi^+\pi^-}$	$0.74 \pm 0.12 \pm 0.05$	$0.27 \pm 0.04 \pm 0.02$	0.72 ± 0.13^d
$\Gamma_{ee}^{\psi(2S)} \cdot \mathcal{B}_{\psi(2S) \rightarrow K^+K^-\pi^+\pi^-}$	$1.92 \pm 0.30 \pm 0.06$	$0.81 \pm 0.13 \pm 0.03$	0.75 ± 0.09
$\Gamma_{ee}^{\psi(2S)} \cdot \mathcal{B}_{\psi(2S) \rightarrow K^+K^-\pi^0\pi^0}$	$0.60 \pm 0.31 \pm 0.03$	$0.25 \pm 0.13 \pm 0.02$	no entry
$\Gamma_{ee}^{\psi(2S)} \cdot \mathcal{B}_{\psi(2S) \rightarrow K^+K^-K^+K^-}$	$0.22 \pm 0.10 \pm 0.02$	$0.09 \pm 0.04 \pm 0.01$	0.060 ± 0.014
$\Gamma_{ee}^{\psi(2S)} \cdot \mathcal{B}_{\psi(2S) \rightarrow \phi\pi^+\pi^-} \cdot \mathcal{B}_{\phi \rightarrow K^+K^-}$	$0.27 \pm 0.09 \pm 0.02$	$0.23 \pm 0.08 \pm 0.01$	0.117 ± 0.029
$\Gamma_{ee}^{\psi(2S)} \cdot \mathcal{B}_{\psi(2S) \rightarrow \phi f_0} \cdot \mathcal{B}_{\phi \rightarrow K^+K^-} \cdot \mathcal{B}_{f_0 \rightarrow \pi^+\pi^-}$	$0.17 \pm 0.06 \pm 0.02$	$0.15 \pm 0.05 \pm 0.01$	0.068 ± 0.024^e

^a $\mathcal{B}_{J/\psi \rightarrow \phi \bar{K}K}$ obtained as $2 \cdot \mathcal{B}_{J/\psi \rightarrow \phi K^+K^-}$.

^bNot corrected for the $f_0 \rightarrow \pi^0\pi^0$ mode.

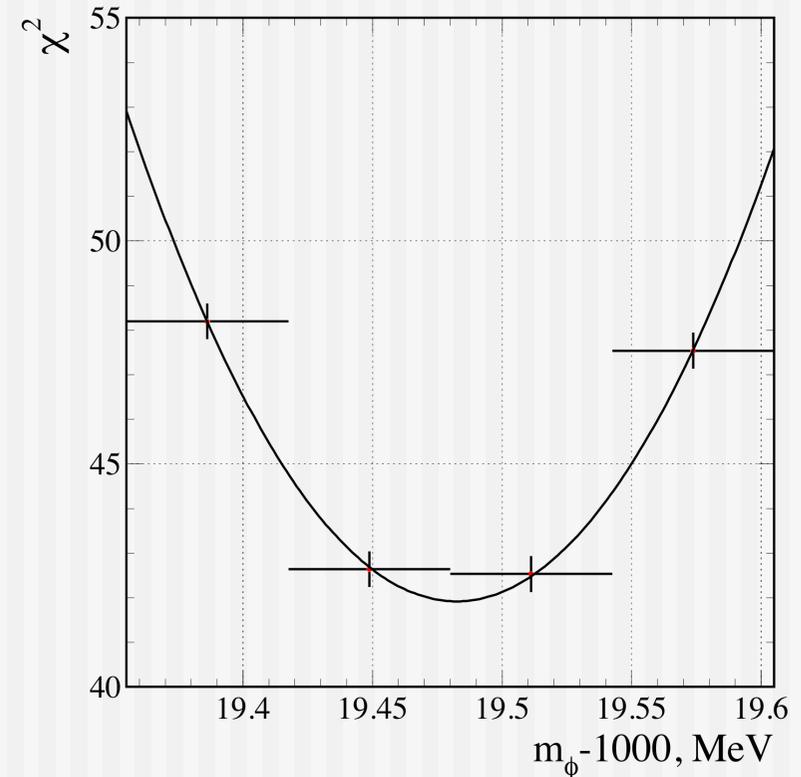
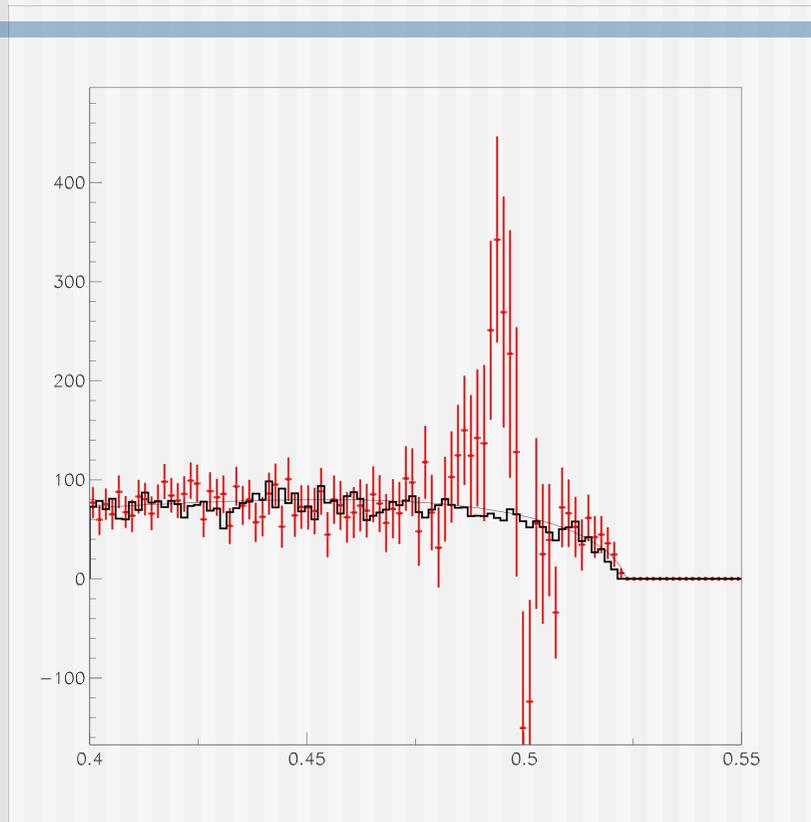
^cNot corrected for the $f_0 \rightarrow \pi^+\pi^-$ mode.

^dWe compare our $\phi f_x, f_x \rightarrow \pi^+\pi^-$ mode with $\phi f_2(1270)$.

^e $\mathcal{B}_{\psi(2S) \rightarrow \phi f_0}, f_0 \rightarrow \pi^+\pi^-$

Small systematic errors allow BaBar to improve BF for major decay modes.

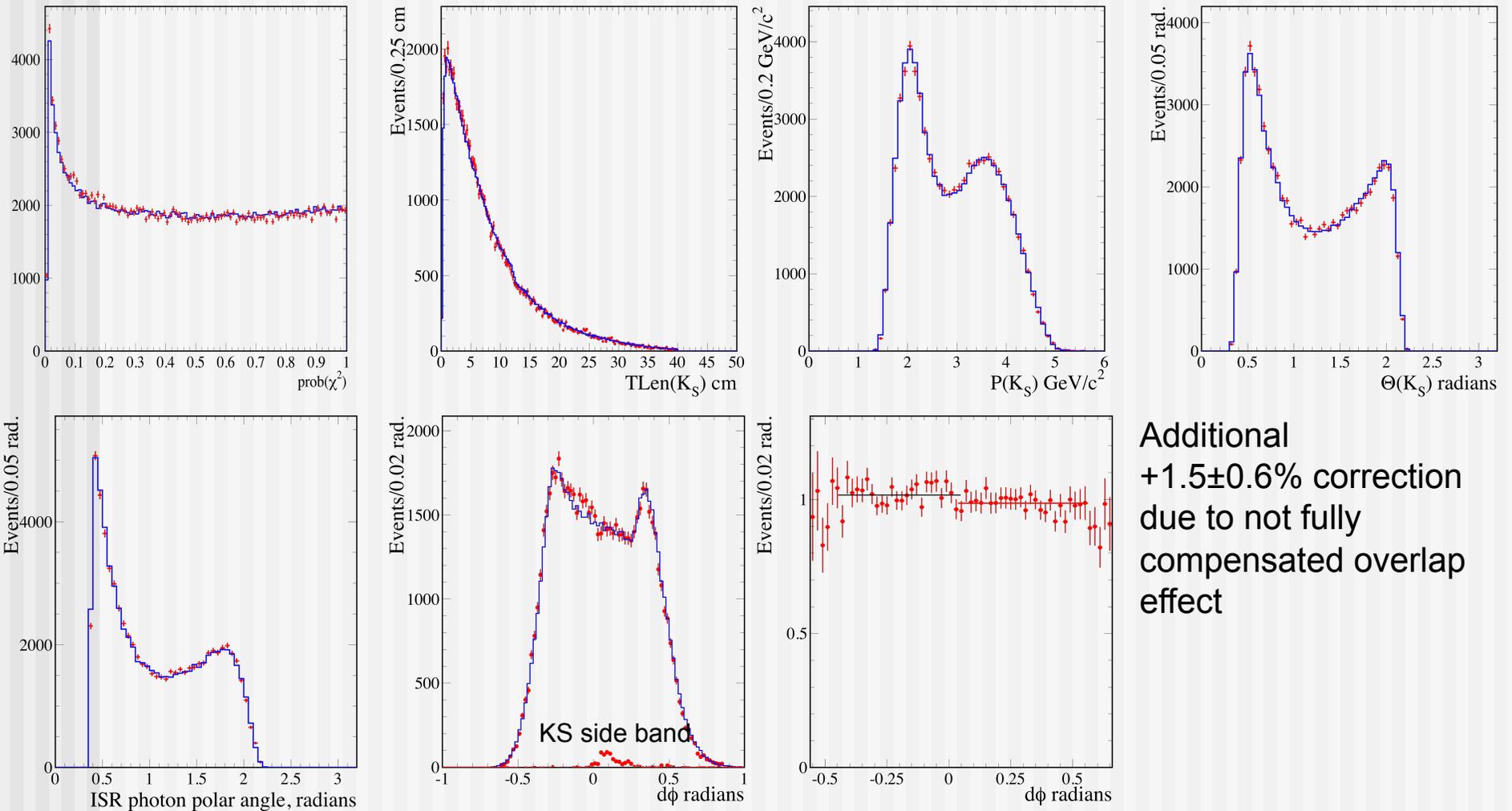
$\phi(1020)$ mass



In MC we know all inputs and can create a “test” $m(K_L)$ distribution and compare with data. And the only free parameter is $\phi(1020)$ mass. By varying ϕ mass we calculate χ^2 value by fitting data-MC difference with “ARGUS” function. We obtain:

$m_\phi = 1019.483 \pm 0.040 \pm 0.036 \text{ MeV}/c^2$: 24 keV – K^0 mass uncertainty, 20 keV – K_S momentum, 18 keV – DCH-EMC mis-alignment.

How other distributions look like

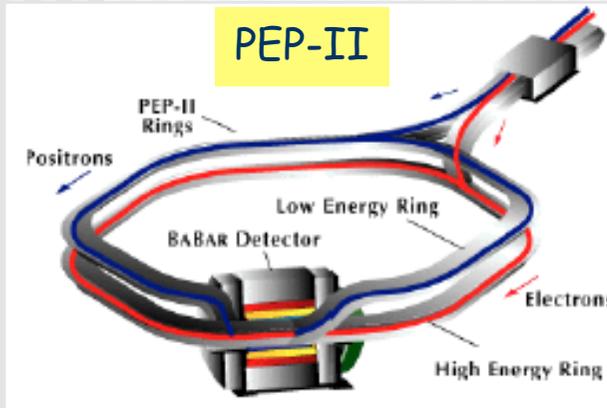


Additional
 $+1.5 \pm 0.6\%$ correction
 due to not fully
 compensated overlap
 effect

Clean events with small systematic errors - 1% from KS, 0.5% ISR photon, 0.5% background, 0.6% from overlap effect.

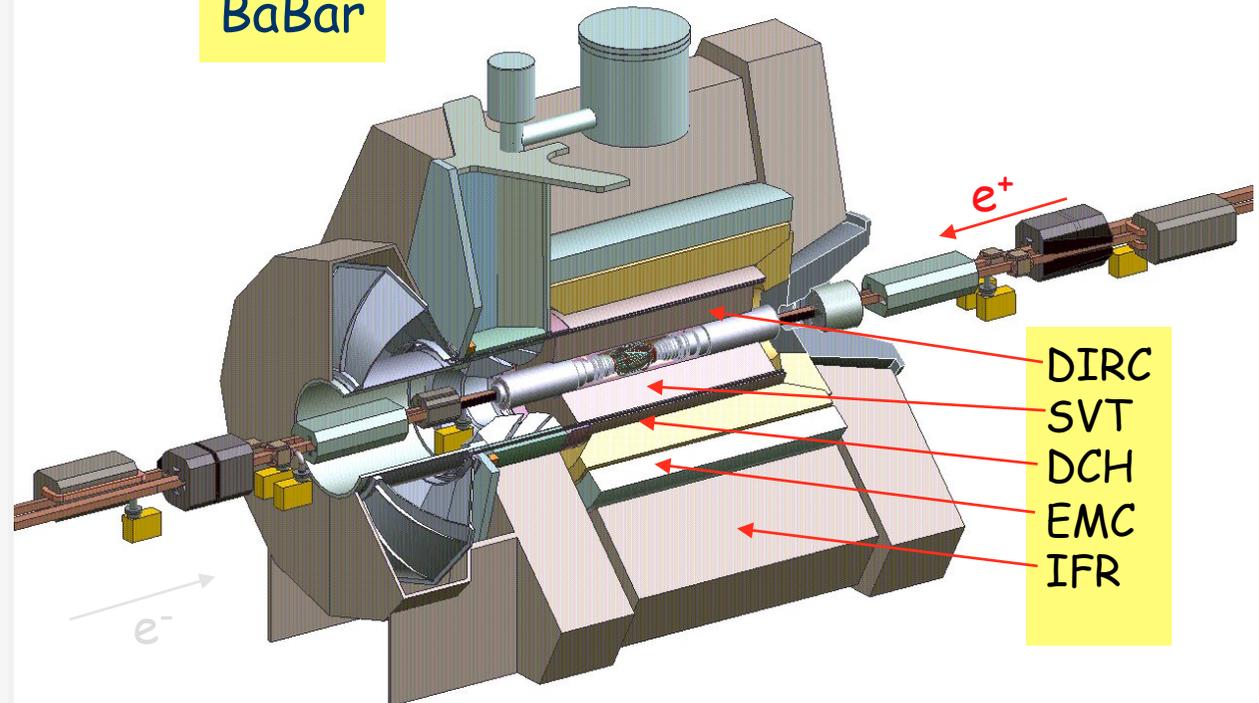
PEP-II e+e- collider, Babar detector

$E_+ = 3.1 \text{ GeV}, E_- = 9 \text{ GeV}$



$E_{CM} = M(Y(4S)) = 10.6 \text{ GeV}$
 2000 - 2008 yrs
 $\Delta L = 500 \text{ fb}^{-1}$
 $N(B) = 10^9$

BaBar



$$\frac{d\sigma(s, x)}{dx d(\cos\theta)} = W(s, x, \theta) \cdot \sigma_0(s(1-x)),$$

$$W(s, x, \theta) = \frac{\alpha}{\pi x} \left(\frac{2 - 2x + x^2}{\sin^2 \theta} - \frac{x^2}{2} \right), \quad x = \frac{2E_\gamma}{\sqrt{s}}$$

θ - photon polar angle in c.m.

