

# $\bar{K}N \rightarrow K\bar{E}$ reaction in chiral unitary models up to NLO

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# Outline

- Introduction
- State-of-the art of chiral unitary models for the meson-baryon interaction in the  $S=-1$  sector
- The  $\bar{K}N \rightarrow K\Xi$  reaction
- Production of  $\Xi$  in nuclei
- Conclusions

Describing the **dynamics of hadrons at low energies** from the **QCD** Lagrangian (*quark* and *gluon* d.o.f.) is a **highly non-perturbative problem**



One may address this problem through the modern perspective of **Chiral Perturbation Theory ( $\chi$ PT)**: effective theory with **hadron degrees of freedom** which respects the symmetries of QCD, in particular the (spontaneously broken) chiral symmetry.

In ordinary  $\chi$ PT:

→ convergence restricted to low energy physics

→ not adequate close to bound-states (pole in the T-matrix)



**Unitarized non-perturbative schemes** ( $U\chi$ PT) allow to extend the predictive power of the chiral theories.

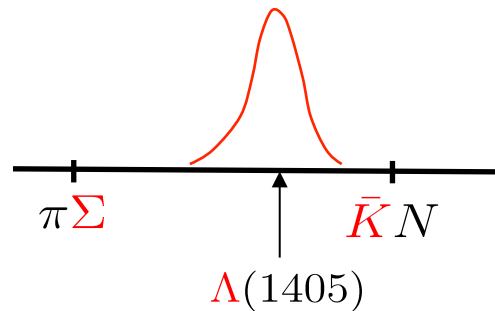


With these **non-perturbative** methods several known resonances have been generated as poles in the scattering amplitude (quasi-bound states) and many hadron reaction cross sections have been nicely reproduced.

## The case of the $\Lambda(1405)$

(a nice example of the success of non-perturbative chiral approaches)

Kbar-N scattering in the isospin  $I=0$  channel is dominated by the presence of the  $\Lambda(1405)$ , located only 27 MeV below the Kbar-N threshold



- Back in 1950, Dalitz and Tuan already proposed that the Kbar-N interaction is attractive enough to generate a **quasi-bound state**, the  $\Lambda(1405)$ , below the Kbar-N threshold and embedded in the  $\pi\Sigma$  continuum.
  - R. H. Dalitz and S. F. Tuan, *Phys. Rev. Lett.* **2** (1959) 425.
  - R. H. Dalitz and S. F. Tuan, *Annals of Phys.* **10** (1960) 307
- In 1995 Kaiser, Siegel and Weise reformulated the problem in terms of the effective **chiral unitary theory** in coupled channels.
  - N. Kaiser, P. B. Siegel, and W. Weise, *Nucl. Phys.* **A594** (1995) 325

- For the **next 10 years (up to 2006)** much work was devoted to this subject with various degrees of sophistication (**more channels, NLO Lagrangian, s-channel, u-channel Born terms...**), all of them obtaining in general similar features.
  - E. Oset and A. Ramos, Nucl. Phys. A635 (1998) 99
  - J.A. Oller and U.G. Meissner, Phys. Lett. B500 (2001) 263
  - M.F.M. Lutz, E.E. Kolomeitsev, Nucl. Phys. A700 (2002) 193
  - C.Garcia-Recio et al., Phys. Rev. D (2003) 07009
  - B.Borasoy, R. Nissler, and W. Weise, Phys. Rev. Lett. 94, 213401 (2005); Eur. Phys. J. A25, 79 (2005)
  - J.A. Oller, J. Prades, and M. Verbeni, Phys. Rev. Lett. 95, 172502 (2005)
  - B. Borasoy, U. G. Meissner and R. Nissler, Phys. Rev. C74, 055201 (2006).
  
- Recently, the **more precise, SIDDHARTA measurement** of the energy shift  $\Delta E$  and width  $\Gamma$  of the 1s state in **kaonic hydrogen** [M. Bazzi et al, Phys. Lett. B704 (2011) 113], clarifying the inconsistency between earlier KEK and DEAR experiments, has injected a renovated interest in the field  $\rightarrow$  the parameters of the NLO meson-baryon Lagrangian can be better constrained  $\rightarrow$  better knowledge of the  $K\bar{b}N$  interaction.
  - Y. Ikeda, T. Hyodo, W. Weise, Nucl.Phys. A881 (2012) 98-114,
  - Z-H. Guo, J.A. Oller, Phys.Rev. C87 (2013) 3, 035202
  - M. Mai, U-G. Meissner, Nucl.Phys. A900 (2013) 51 - 64
  - V.K. Magas, A. Feijoo, A. Ramos, arXiv:1402.3971

# Essence of the non-perturbative chiral approach

## 1. Meson-baryon effective chiral Lagrangian:

Lowest order (LO),  $\mathcal{O}(q)$

$$\mathcal{L}_{MB}^{(1)}(B, U) = \langle \bar{B} i \gamma^\mu \nabla_\mu B \rangle - M_B \langle \bar{B} B \rangle + \frac{1}{2} D \langle \bar{B} \gamma^\mu \gamma_5 \{u_\mu, B\} \rangle + \frac{1}{2} F \langle \bar{B} \gamma^\mu \gamma_5 [u_\mu, B] \rangle$$

$$\nabla_\mu B = \partial_\mu B + [\Gamma_\mu, B]$$

$$\Gamma_\mu = \frac{1}{2} (u^\dagger \partial_\mu u + u \partial_\mu u^\dagger)$$

$$U = u^2 = \exp\left(\frac{i\sqrt{2}\Phi}{f}\right)$$

$$u_\mu = i u^\dagger \partial_\mu U u^\dagger$$

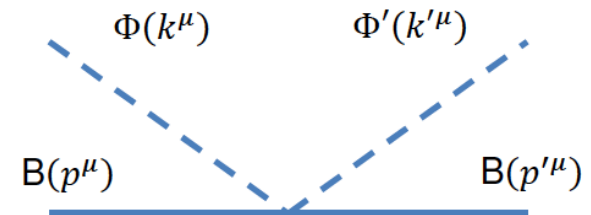
$$\Phi = \begin{pmatrix} \frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta_8 & \pi^+ & K^+ \\ \pi^- & -\frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta_8 & K^0 \\ K^- & \bar{K}^0 & -\frac{2}{\sqrt{6}}\eta_8 \end{pmatrix}$$

$$B = \begin{pmatrix} \frac{1}{\sqrt{2}}\Sigma^0 + \frac{1}{\sqrt{6}}\Lambda^0 & \Sigma^+ & p \\ \Sigma^- & -\frac{1}{\sqrt{2}}\Sigma^0 + \frac{1}{\sqrt{6}}\Lambda^0 & n \\ \Xi^- & \Xi^0 & -\frac{2}{\sqrt{6}}\Lambda^0 \end{pmatrix}$$

→ LO meson-baryon potential in s-wave (contact term):

$$V_{ij} = -C_{ij} \frac{1}{4f^2} \bar{u}(p) \gamma^\mu u(p) (k_\mu + k'_\mu)$$

One parameter: f



## Next to leading order (NLO), $\mathcal{O}(q^2)$

$$\mathcal{L}_{MB}^{(2)}(B, U) = b_D \langle \bar{B} \{ \chi_+, B \} \rangle + b_F \langle \bar{B} [ \chi_+, B ] \rangle + b_0 \langle \bar{B} B \rangle \langle \chi_+ \rangle + d_1 \langle \bar{B} \{ u_\mu, [ u^\mu, B ] \} \rangle + d_2 \langle \bar{B} [ u_\mu, [ u^\mu, B ] ] \rangle + d_3 \langle \bar{B} u_\mu \rangle \langle u^\mu B \rangle + d_4 \langle \bar{B} B \rangle \langle u^\mu u_\mu \rangle$$

$d_1, d_2, d_3, d_4$ : two-derivative terms

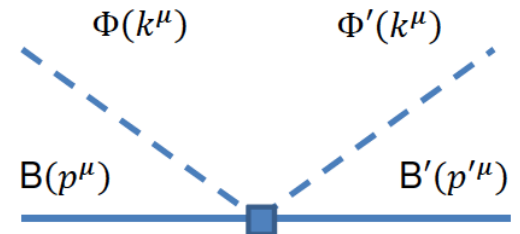
$$\chi_+ = -\frac{1}{4f^2} \{ \Phi, \{ \Phi, \chi \} \}$$

explicit chiral symmetry breaking terms:  $b_D, b_F, b_0$

$$\chi = \begin{pmatrix} m_\pi^2 & 0 & 0 \\ 0 & m_\pi^2 & 0 \\ 0 & 0 & 2m_K^2 - m_\pi^2 \end{pmatrix}$$

→ NLO contribution to the meson-baryon potential:

$$\tilde{V}_{ij} = \frac{1}{f^2} (D_{ij} - 2(k_\mu k'^\mu) L_{ij}) \sqrt{\frac{M_i + E_i}{2M_i}} \sqrt{\frac{M_j + E_j}{2M_j}}$$



$D_{ij}, L_{ij}$ : matrices which depend on the 7 NLO parameters:  $b_D, b_F, b_0, d_1, d_2, d_3, d_4$

## 2. Unitarization:

N/D, Bethe-Salpeter...

$$T_{ij} = V_{ij} + V_{il} G_l T_{lj}$$

Coupled channels in S=-1 meson-baryon sector:

$$K^- p, \bar{K}^0 n, \pi^0 \Lambda, \pi^0 \Sigma^0, \pi^+ \Sigma^-, \pi^- \Sigma^+, \eta \Lambda, \eta \Sigma^0, K^+ \Xi^-, K^0 \Xi^0$$

## 3. Regularization of loop function:

$$G_l = i2M_l \int \frac{d^4 q}{(2\pi)^4} \frac{1}{(P-q)^2 - M_l^2 + i\epsilon} \frac{1}{q^2 - m_l^2 + i\epsilon}$$

Dimensional regularization :

$$G_l = \frac{2M_l}{16\pi^2} \left\{ a_l(\mu) + \ln \frac{M_l^2}{\mu^2} + \frac{m_l^2 - M_l^2 + s}{2s} \ln \frac{m_l^2}{M_l^2} + \right. \\ \left. + \frac{\bar{q}_l}{\sqrt{s}} \left[ \ln(s - (M_l^2 - m_l^2) + 2\bar{q}_l\sqrt{s}) + \ln(s + (M_l^2 - m_l^2) + 2\bar{q}_l\sqrt{s}) \right. \right. \\ \left. \left. - \ln(-s + (M_l^2 - m_l^2) + 2\bar{q}_l\sqrt{s}) - \ln(-s - (M_l^2 - m_l^2) + 2\bar{q}_l\sqrt{s}) \right] \right\}$$

subtraction constants  
(to be fitted)

$$a_l(\mu) \simeq -2 \quad \text{"natural size } (\mu \sim 700 \text{ MeV})$$



# Parameters

- Decay constant  $f$
- 7 parameters of the NLO Lagrangian:  $b_D, b_F, b_0, d_1, d_2, d_3, d_4$
- 6 subtraction constants (isospin symmetry)

$$a_{K^-p} = a_{\bar{K}^0 n} = a_{\bar{K}N}$$

$$a_{\pi\Lambda}$$

$$a_{\pi^+\Sigma^-} = a_{\pi^-\Sigma^+} = a_{\pi^0\Sigma^0} = a_{\pi\Sigma}$$

$$a_{\eta\Lambda}$$

$$a_{\eta\Sigma}$$

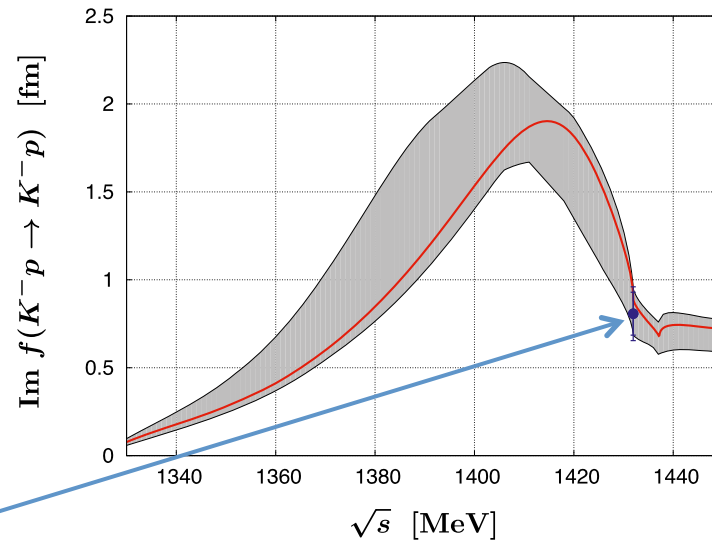
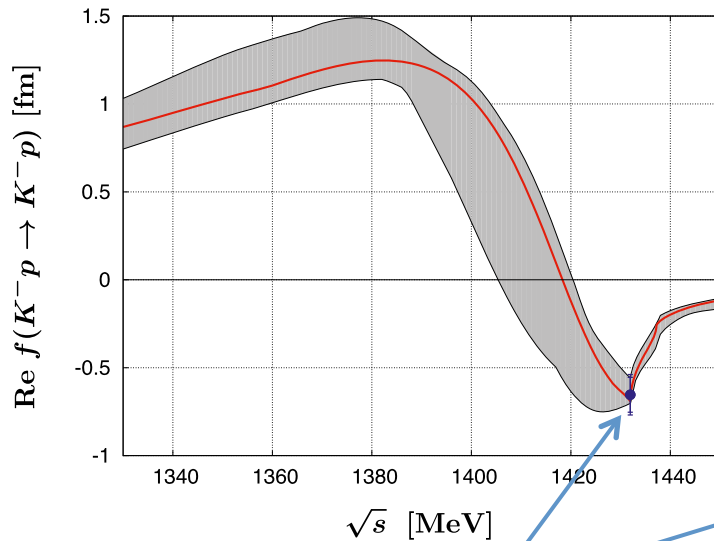
$$a_{K^+\Xi^-} = a_{K^0\Xi^0} = a_{K\Xi}$$

# Observables (threshold)

$$\gamma = \frac{\Gamma(K^- p \rightarrow \pi^+ \Sigma^-)}{\Gamma(K^- p \rightarrow \pi^- \Sigma^+)}$$

$$R_n = \frac{\Gamma(K^- p \rightarrow \pi^0 \Lambda)}{\Gamma(K^- p \rightarrow \text{neutral states})}$$

$$R_c = \frac{\Gamma(K^- p \rightarrow \pi^+ \Sigma^-, \pi^- \Sigma^+)}{\Gamma(K^- p \rightarrow \text{all inelastic channels})}$$



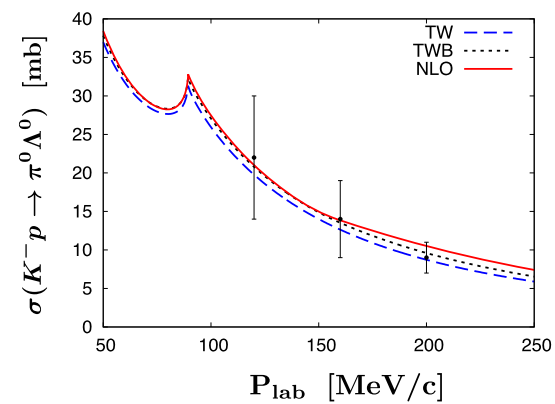
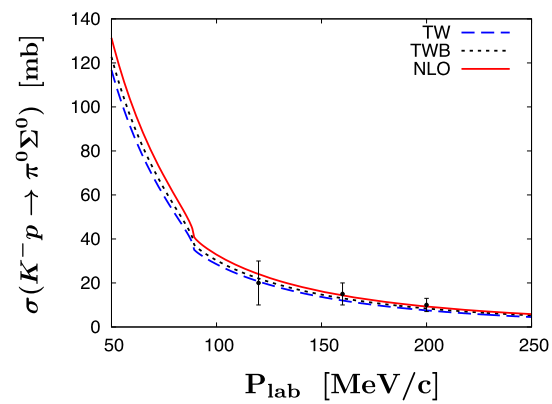
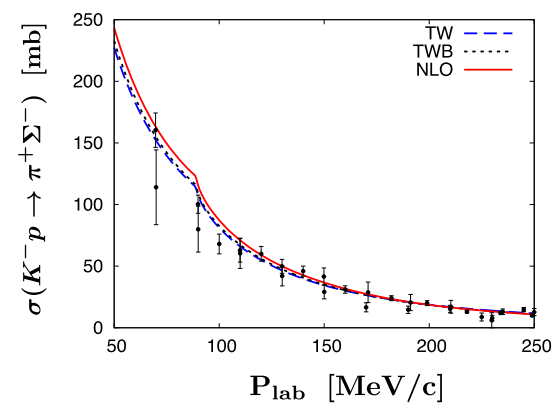
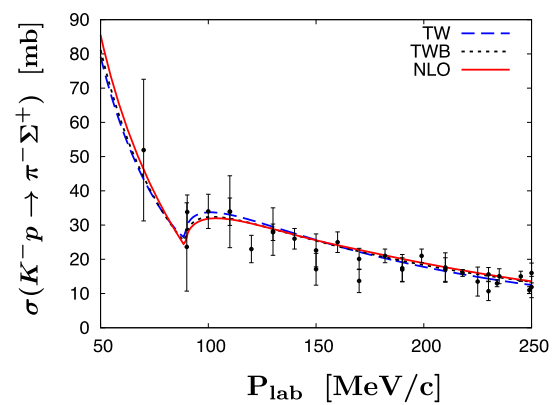
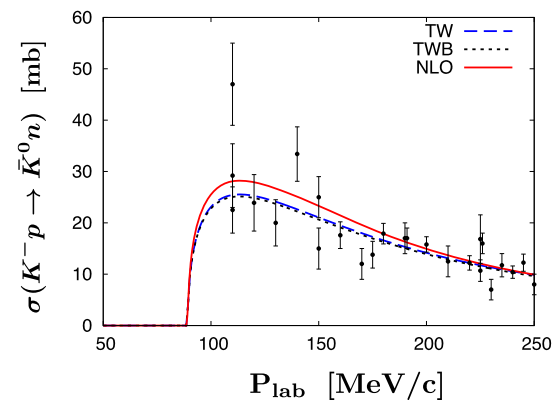
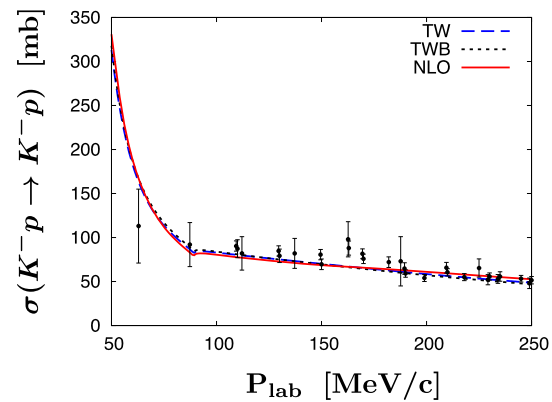
SIDDHARTA kaonic hydrogen,  
M. Bazzi et al. Phys. Lett. B704 (2011) 113

Branching ratios:

$\Delta E$ [eV]	$\Gamma$ [eV]	$\gamma$	$R_n$	$R_c$
EXP: $283 \pm 36 \pm 6$	$541 \pm 89 \pm 22$	$2.36 \pm 0.04$	$0.189 \pm 0.015$	$0.664 \pm 0.011$
THEO: 306	591	2.37	0.19	0.66

Y. Ikeda, T. Hyodo and W. Weise, Nucl.Phys. A881 (2012) 98

# Observables (beyond threshold)



# The two-pole structure of the $\Lambda(1405)$

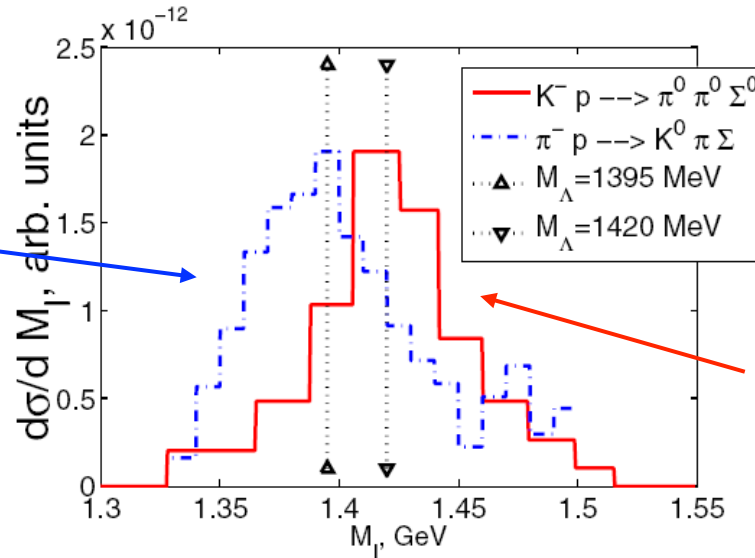
T-matrix poles and couplings to physical states with  $l=0$

$$T_{ij} = \frac{g_i g_j}{\sqrt{s} - M_R + i\Gamma/2},$$

$z_R$ ( $l=0$ )	1390 - 66i	1426 - 16i
$\pi\Sigma$	2.9	1.5
$KN$	2.1	2.7
$\eta\Lambda$	0.77	1.4
$K\Xi$	0.61	0.35

Experimental evidence

Magas, Oset, Ramos, PRL 95 (2005) 052301



$\pi p \rightarrow K^0 \pi \Sigma$

D.W.Thomas et al.  
Nucl. Phys. B56, 15 (1973)

$M \sim 1385$  MeV

$\Gamma \sim 50$  MeV

$K^- p \rightarrow \pi^0 \pi^0 \Sigma^0$

S. Prakhov et al.,  
Phys.Rev. C70,034605 (2004)

$M \sim 1420$  MeV

$\Gamma \sim 38$  MeV

- The  $\Lambda(1405)$  resonance shows different properties (position, width) in different reactions
- Success of meson-baryon coupled-channel models!

# $K^- p \rightarrow K \Xi$ channels

V.K. Magas, A. Feijoo, A. Ramos, arXiv:1402.3971

- Differently than the other works, we incorporate the  $K \Xi$  channels in the NLO fit
- They are particularly interesting because the LO (Weinberg-Tomozawa) terms are zero

	$K^- p$	$\bar{K}^0 n$	$\pi^0 \Lambda$	$\pi^0 \Sigma^0$	$\eta \Lambda$	$\eta \Sigma^0$	$\pi^+ \Sigma^-$	$\pi^- \Sigma^+$	$K^+ \Xi^-$	$K^0 \Xi^0$
$K^- p$	2	1	$\sqrt{3}/2$	1/2	3/2	$\sqrt{3}/2$	0	1	0	0
$\bar{K}^0 n$		2	$-\sqrt{3}/2$	1/2	3/2	$-\sqrt{3}/2$	1	0	0	0
$\pi^0 \Lambda$			0	0	0	0	0	0	$\sqrt{3}/2$	$-\sqrt{3}/2$
$\pi^0 \Sigma^0$				0	0	0	2	2	1/2	1/2
$\eta \Lambda$					0	0	0	0	3/2	3/2
$\eta \Sigma^0$						0	0	0	$\sqrt{3}/2$	$-\sqrt{3}/2$
$\pi^+ \Sigma^-$							2	0	1	0
$\pi^- \Sigma^+$								2	0	1
$K^+ \Xi^-$									2	1
$K^0 \Xi^0$										2

→ Therefore, these channels are especially sensitive to NLO parameters !!

# NLO coefficients

$D_{ij}$

	$K^-p$	$\bar{K}^0n$	$\pi^0\Lambda$	$\pi^0\Sigma^0$	$\eta\Lambda$	$\eta\Sigma^0$	$\pi^+\Sigma^-$	$\pi^-\Sigma^+$	$K^+\Xi^-$	$K^0\Xi^0$
$K^-p$	$4(b_0 + b_D)m_K^2$	$2(b_D + b_F)m_K^2$	$\frac{-(b_D + 3b_F)\mu_1^2}{2\sqrt{3}}$	$\frac{(b_D - b_F)\mu_1^2}{2}$	0	$(b_D - b_F)\mu_1^2$	$\frac{(b_D + 3b_F)\mu_2^2}{6}$	$-\frac{(b_D - b_F)\mu_2^2}{2\sqrt{3}}$	0	0
$\bar{K}^0n$		$4(b_0 + b_D)m_K^2$	$\frac{(b_D + 3b_F)\mu_1^2}{2\sqrt{3}}$	$\frac{(b_D - b_F)\mu_1^2}{2}$	$(b_D - b_F)\mu_1^2$	0	$\frac{(b_D + 3b_F)\mu_2^2}{6}$	$\frac{(b_D - b_F)\mu_2^2}{2\sqrt{3}}$	0	0
$\pi^0\Lambda$			$\frac{4(3b_0 + b_D)m_\pi^2}{3}$	0	0	0	0	$\frac{4b_D m_\pi^2}{3}$	$-\frac{(b_D - 3b_F)\mu_1^2}{2\sqrt{3}}$	$\frac{(b_D - 3b_F)\mu_1^2}{2\sqrt{3}}$
$\pi^0\Sigma^0$				$4(b_0 + b_D)m_\pi^2$	0	0	$\frac{4b_D m_\pi^2}{3}$	0	$\frac{(b_D + b_F)\mu_1^2}{2}$	$\frac{(b_D + b_F)\mu_1^2}{2}$
$\eta\Lambda$					$4(b_0 + b_D)m_\pi^2$	0	$\frac{4b_D m_\pi^2}{3}$	$\frac{4b_F m_\pi^2}{\sqrt{3}}$	$(b_D + b_F)\mu_1^2$	0
$\eta\Sigma^0$						$4(b_0 + b_D)m_\pi^2$	$\frac{4b_D m_\pi^2}{3}$	$-\frac{4b_F m_\pi^2}{\sqrt{3}}$	0	$(b_D + b_F)\mu_1^2$
$\pi^+\Sigma^-$							$\frac{4(3b_0\mu_3^2 + b_D\mu_4^2)}{9}$	0	$\frac{(b_D - 3b_F)\mu_2^2}{6}$	$\frac{(b_D - 3b_F)\mu_2^2}{6}$
$\pi^-\Sigma^+$								$\frac{4(b_0\mu_3^2 + b_D m_\pi^2)}{3}$	$\frac{(b_D + b_F)\mu_2^2}{2\sqrt{3}}$	$\frac{(b_D + b_F)\mu_2^2}{2\sqrt{3}}$
$K^+\Xi^-$									$4(b_0 + b_D)m_K^2$	$2(b_D - b_F)m_K^2$
$K^0\Xi^0$										$4(b_0 + b_D)m_K^2$

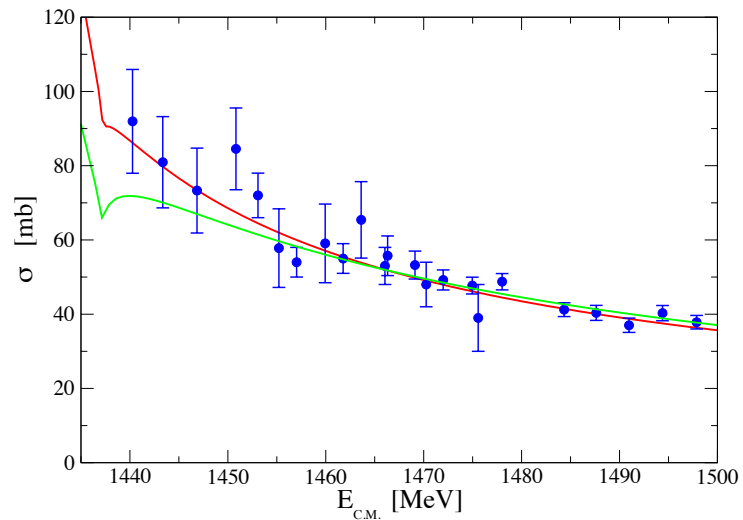
$L_{ij}$

	$K^-p$	$\bar{K}^0n$	$\pi^0\Lambda$	$\pi^0\Sigma^0$	$\eta\Lambda$	$\eta\Sigma^0$	$\pi^+\Sigma^-$	$\pi^-\Sigma^+$	$K^+\Xi^-$	$K^0\Xi^0$
$K^-p$	$2d_2 + d_3 + 2d_4$	$d_1 + d_2 + d_3$	$-\frac{\sqrt{3}(d_1 + d_2)}{2}$	$\frac{-d_1 - d_2 + 2d_3}{2}$	$-2d_2 + d_3$	$-d_1 + d_2 + d_3$	$\frac{d_1 - 3d_2 + 2d_3}{2}$	$\frac{d_1 - 3d_2}{2\sqrt{3}}$	$-4d_2 + 2d_3$	$-2d_2 + d_3$
$\bar{K}^0n$		$2d_2 + d_3 + 2d_4$	$\frac{\sqrt{3}(d_1 + d_2)}{2}$	$\frac{-d_1 - d_2 + 2d_3}{2}$	$-d_1 + d_2 + d_3$	$-2d_2 + d_3$	$\frac{d_1 - 3d_2 + 2d_3}{2}$	$-\frac{(d_1 - 3d_2)}{2\sqrt{3}}$	$-2d_2 + d_3$	$-4d_2 + 2d_3$
$\pi^0\Lambda$			$2d_4$	0	0	0	0	$d_3$	$\frac{\sqrt{3}(d_1 - d_2)}{2}$	$-\frac{\sqrt{3}(d_1 - d_2)}{2}$
$\pi^0\Sigma^0$				$2(d_3 + d_4)$	$-2d_2 + d_3$	$-2d_2 + d_3$	$d_3$	0	$\frac{d_1 - d_2 + 2d_3}{2}$	$\frac{d_1 - d_2 + 2d_3}{2}$
$\eta\Lambda$					$2d_2 + d_3 + 2d_4$	$-4d_2 + 2d_3$	$d_3$	$\frac{2d_1}{\sqrt{3}}$	$d_1 + d_2 + d_3$	$-2d_2 + d_3$
$\eta\Sigma^0$						$2d_2 + d_3 + 2d_4$	$d_3$	$-\frac{2d_1}{\sqrt{3}}$	$-2d_2 + d_3$	$d_1 + d_2 + d_3$
$\pi^+\Sigma^-$							$2(d_3 + d_4)$	0	$\frac{-d_1 - 3d_2 + 2d_3}{2}$	$\frac{-d_1 - 3d_2 + 2d_3}{2}$
$\pi^-\Sigma^+$								$2d_4$	$-\frac{(d_1 + 3d_2)}{2\sqrt{3}}$	$\frac{d_1 + 3d_2}{2\sqrt{3}}$
$K^+\Xi^-$									$2d_2 + d_3 + 2d_4$	$-d_1 + d_2 + d_3$
$K^0\Xi^0$										$2d_2 + d_3 + 2d_4$

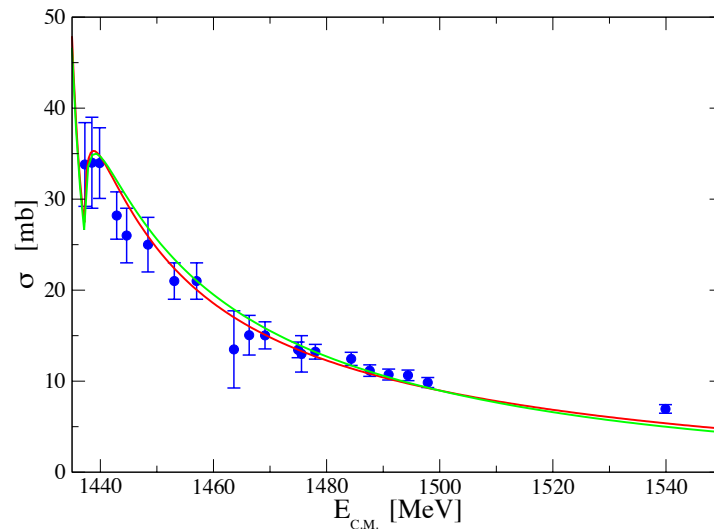
# Results

- LO fit
- LO + NLO (including  $K\Xi$  channels)

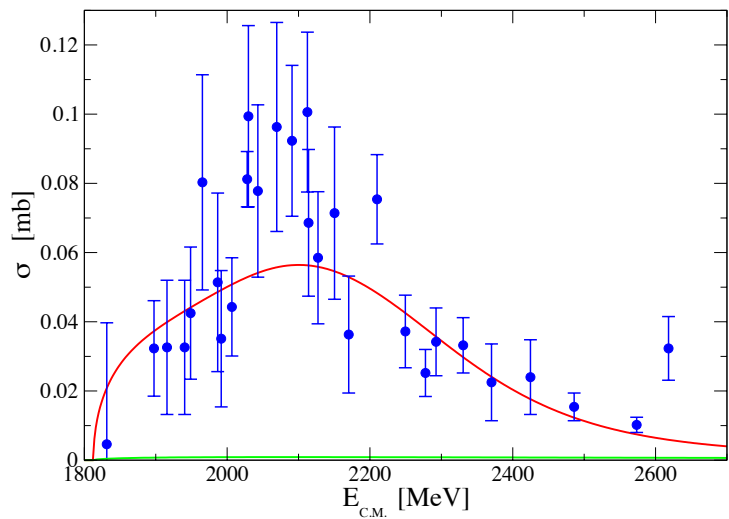
$K^- p \rightarrow K^- p$



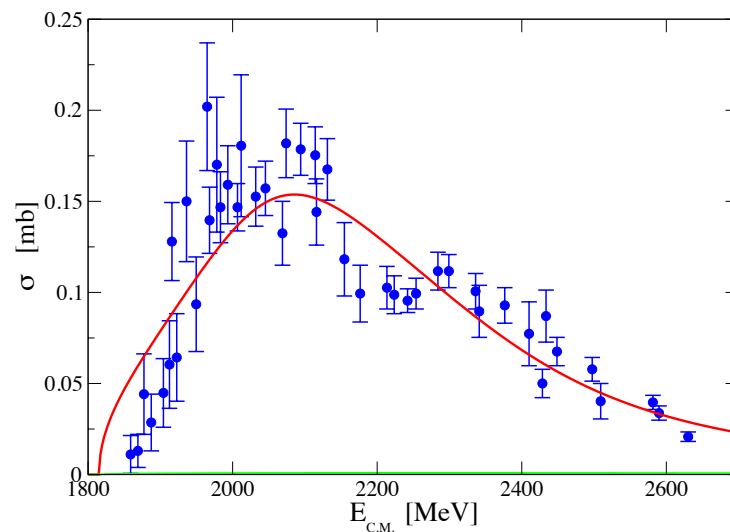
$K^- p \rightarrow \pi^- \Sigma^+$

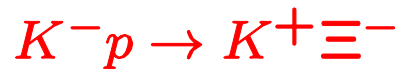


$K^- p \rightarrow K^0 \Xi^0$

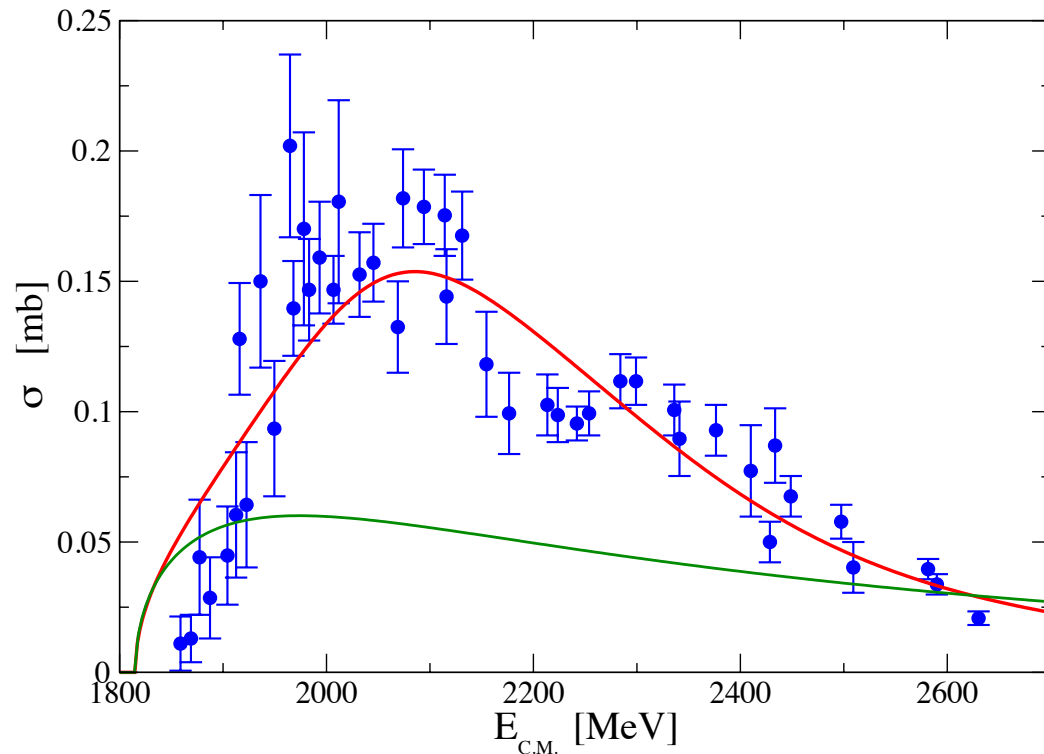
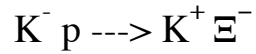


$K^- p \rightarrow K^+ \Xi^-$





- LO + NLO (including  $K\Xi$  channels)
- switching off NLO:  $b_i=0$   $d_i=0$



NLO terms contribute sizably in this channel!

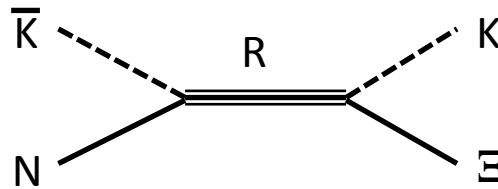
But the shape of the cross section indicates that there are resonant structures.

→ Need to include genuine resonances and refit!



# Resonances in $K\Xi$ channels

From the PDG we see many 3\* and 4\* resonances in the region of interest!



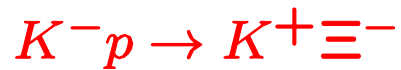
Resonancia	$I(J^P)$	Mass (MeV)	$\Gamma$ (MeV)	Fraction ( $\Gamma_{K\Xi}/\Gamma$ )
$\Lambda(1890)$	$0\left(\frac{3^+}{2}\right)$	1850 – 1910	60 – 200	–
$\Lambda(2100)$	$0\left(\frac{7^-}{2}\right)$	2090 – 2110	100 – 250	< 3%
$\Lambda(2110)$	$0\left(\frac{5^+}{2}\right)$	2090 – 2140	150 – 250	–
$\Lambda(2350)$	$0\left(\frac{9^+}{2}\right)$	2340 – 2370	100 – 250	–
$\Sigma(1915)$	$1\left(\frac{5^+}{2}\right)$	1900 – 1935	80 – 160	–
$\Sigma(1940)$	$1\left(\frac{3^-}{2}\right)$	1900 – 1950	150 – 300	–
$\Sigma(2030)$	$1\left(\frac{7^+}{2}\right)$	2025 – 2040	150 – 200	< 2%
$\Sigma(2250)$	$1(?)\left(\frac{5^-}{2}\right)$	2210 – 2280	60 – 150	–

In the resonant model of [Sharov, Korotkikh, Lanskoj, EPJA 47 \(2011\) 109](#) for the  $\bar{K}N \rightarrow K\Xi$  reaction several combinations were tested  $\rightarrow \Sigma(2030)$  and  $\Sigma(2250)$  were the more relevant!

The  $\Sigma(2030)$  also plays a relevant role in the  $\gamma p \rightarrow K^+ K^+ \Sigma^-$  reaction

[K. Nakayama, Y. Oh, H. Habertzettl, Phys. Rev. C74, 035205 \(2006\)](#)

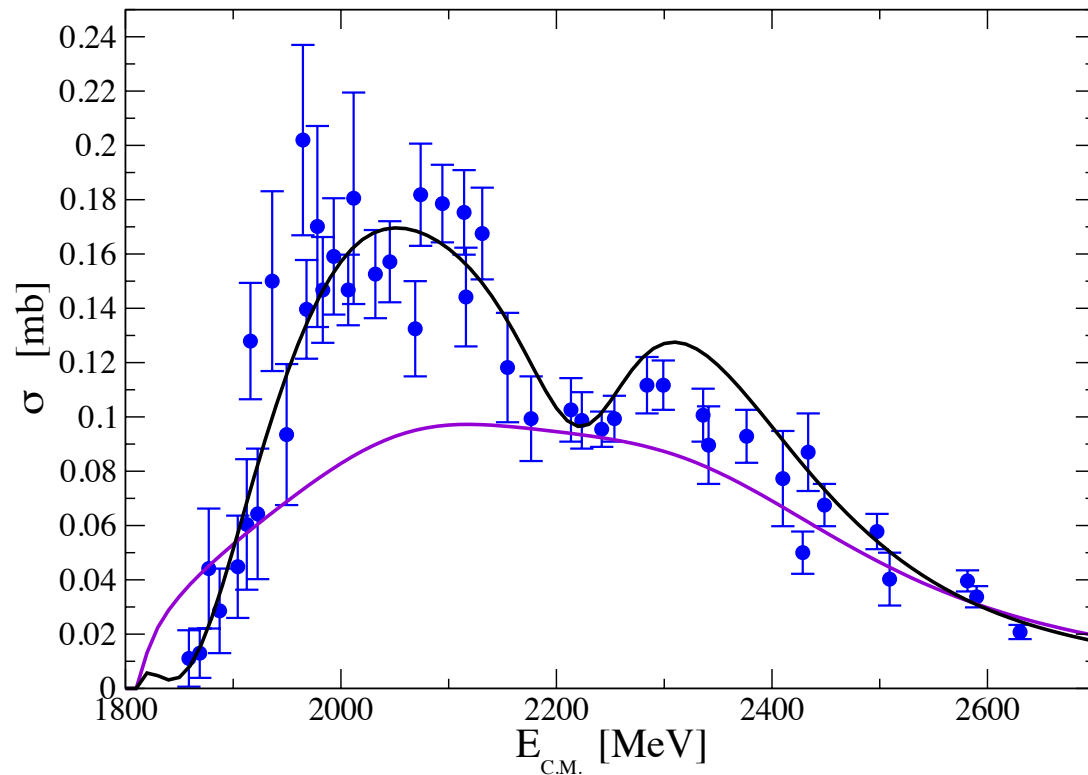
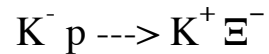
[K. Shing Man, Y. Oh, K. Nakayama,, Phys. Rev. C83, 055201 \(2011\)](#)



We supplement the LO+NLO Lagrangian with two resonances:

One of  $J^P=7/2^+$  around 2030 MeV and one of  $J^P=5/2^-$  around 2250 MeV

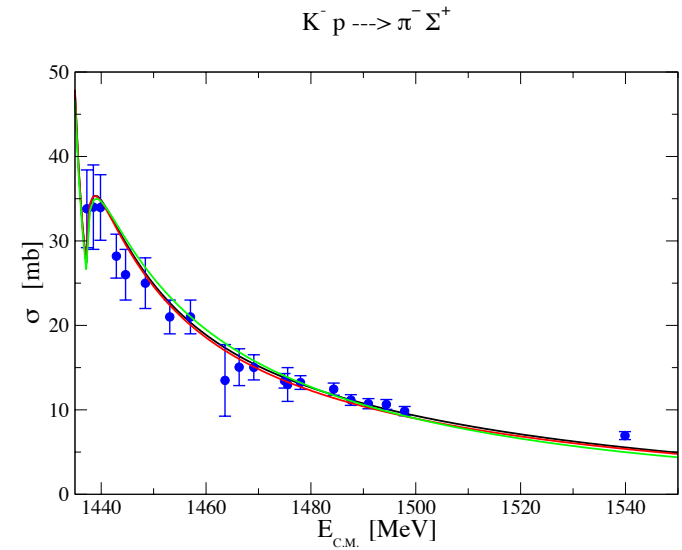
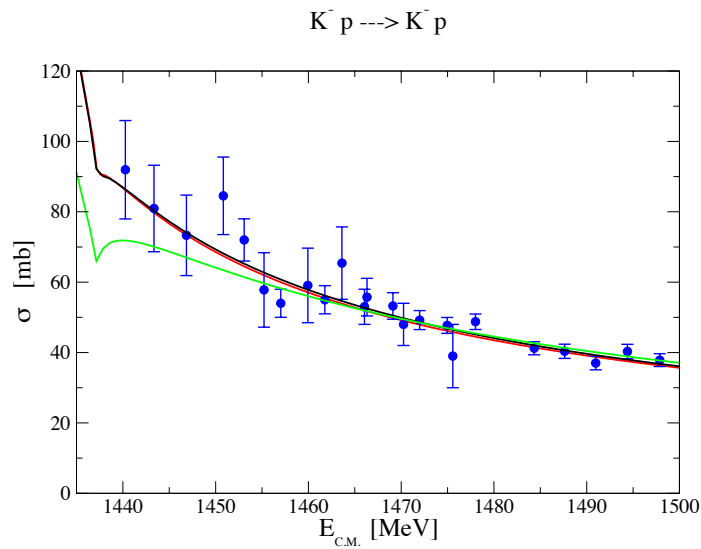
→ the fit determines masses, widths and couplings of resonances



— LO + NLO + Resonances  
— LO + NLO

Background due to NLO chiral  
Lagrangian reduced and more  
realistic!

The incorporation of these resonances in the fitting procedure does not alter the other cross sections (black lines: LO+NLO+resonances),



nor the threshold ratios:

Ramos-Magas-Feijoo MODEL	$\gamma$	$R_n$	$R_c$
WT	2.34	0.185	0.665
WT+ NLO + $\Xi$ channels	2.36	0.197	0.659
WT+NLO+ $\Xi$ channels + Resonances	2.36	0.193	0.661
Experimental	$2.36 \pm 0.04$	$0.189 \pm 0.015$	$0.664 \pm 0.011$

# Parameters (Preliminary!)

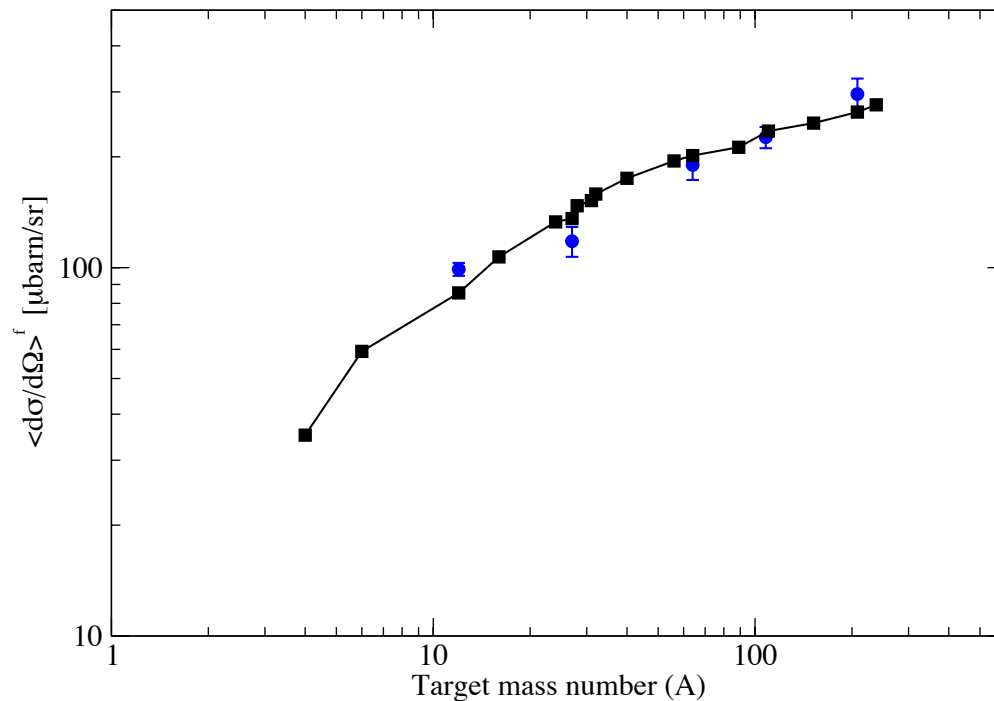
	WT	WT+NLO+ $\Xi$ chann.	WT+NLO+ $\Xi$ chann. + Resonances
$a_{\bar{K}N}$ ( $10^{-3}$ )	-1.79	4.64	4.72
$a_{\pi\Lambda}$ ( $10^{-3}$ )	-39.83	24.52	26.01
$a_{\pi\Sigma}$ ( $10^{-3}$ )	0.06	2.06	2.27
$a_{\eta\Lambda}$ ( $10^{-3}$ )	1.18	-9.10	-7.82
$a_{\eta\Sigma}$ ( $10^{-3}$ )	38.04	-8.43	-7.68
$a_{K\Xi}$ ( $10^{-3}$ )	239.00	37.54	42.90
$f$ (MeV)	$1.21f_\pi$	$1.19f_\pi$	$1.2f_\pi$
$b_0$ ( $GeV^{-1}$ )	-	-0.37	-0.44
$b_D$ ( $GeV^{-1}$ )	-	-0.04	-0.05
$b_F$ ( $GeV^{-1}$ )	-	0.37	0.37
$d_1$ ( $GeV^{-1}$ )	-	0.24	0.22
$d_2$ ( $GeV^{-1}$ )	-	0.41	0.40
$d_3$ ( $GeV^{-1}$ )	-	0.74	0.76
$d_4$ ( $GeV^{-1}$ )	-	-0.58	-0.60
$f_{KYB5}$	-	-	-2.72
$f_{KYB7}$	-	-	402.05
$\Lambda_{5/2}$ (MeV)	-	-	720.02
$\Lambda_{7/2}$ (MeV)	-	-	298.13
$M_{5/2}$ (MeV)	-	-	2216.4
$M_{7/2}$ (MeV)	-	-	2040.0
$\Gamma_{5/2}$ (MeV)	-	-	146.24
$\Gamma_{7/2}$ (MeV)	-	-	150.00
$\chi_{d.o.f}$	1.23 (no $\Xi$ )	1.88	0.73

# Production of $\Xi$ in nuclei: $(K^-, K^+)$ reaction on nuclear targets

- These reactions are employed to produce double  $\Lambda$  hypernuclei
- They may inform us on the size of the  $\Xi$  optical potential in the nucleus

$p_{K^-} = 1.65 \text{ GeV}/c$

$K^- A \rightarrow K^+ \Xi^- A'$   
 $0.95 < p_{K^-} < 1.30 \text{ GeV}/c$



Blue points: T.Iijima et al. Nucl.Phys. A546 (1992) 588

# Conclusions

- Chiral Perturbation Theory with unitarization in coupled channels is a very powerful technique to describe low energy hadron dynamics.
- More precise data has become available → NLO calculations become more meaningful (NLO terms in the Lagrangian do improve agreement with data)
- The  $\bar{K}N \rightarrow K\Xi$  reaction is very interesting and important for fitting NLO parameters (Work in progres ... )