

M E S O N
2 0 1 4



13th International Workshop
on Meson Production,
Properties and Interaction

| Kraków, Poland

| 29th May – 3rd June 2014

STUDY OF RARE AND SUPPRESSED PROCESSES IN B meson decays WITH ATLAS

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on behalf of the ATLAS Collaboration

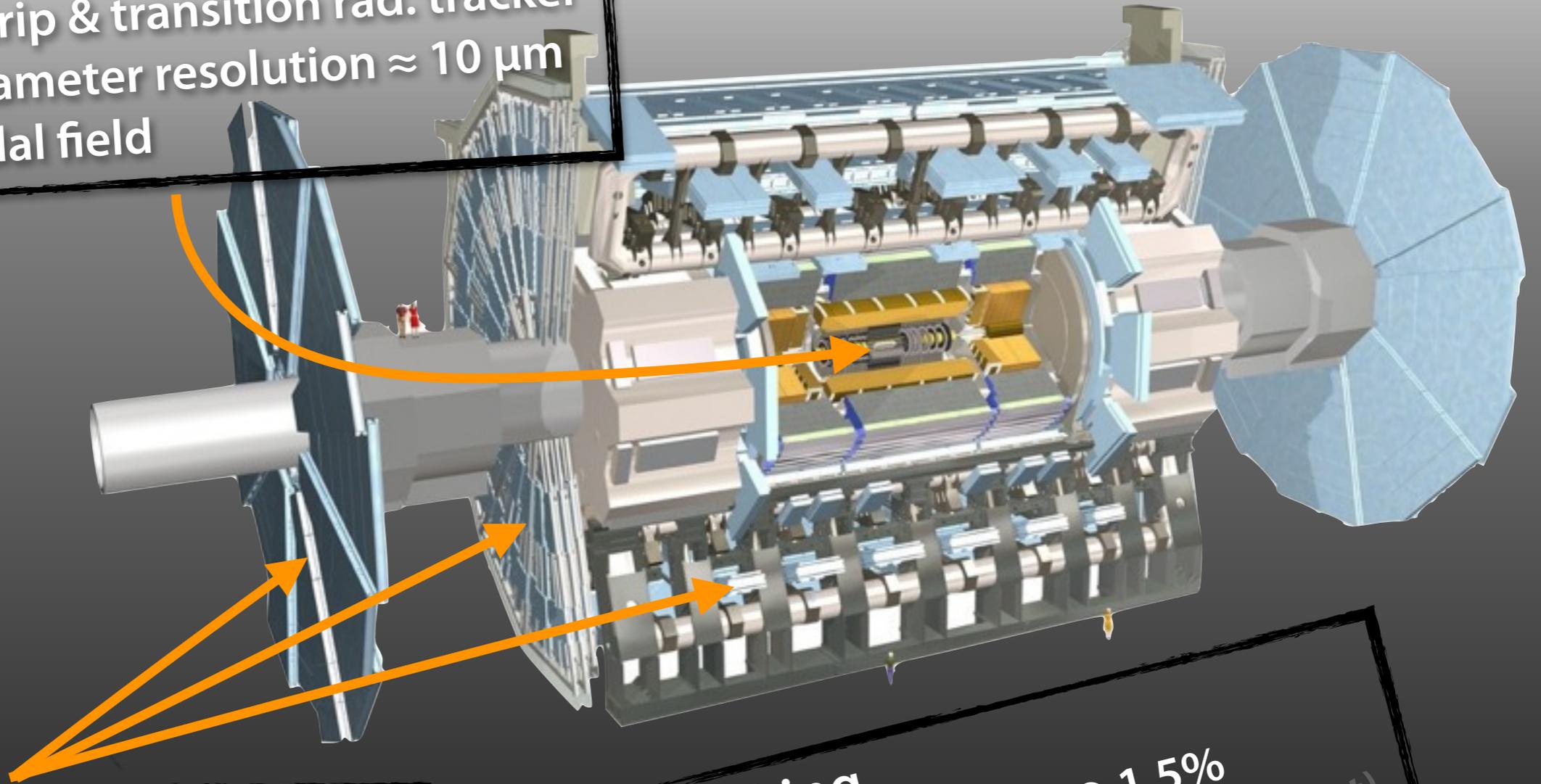


- ◆ ATLAS detector at LHC
- ◆ Study of the decay $B_d \rightarrow K^* (\rightarrow K^+\pi^-) \mu^+\mu^-$
- ◆ Search for $B_s \rightarrow \mu^+\mu^-$
- ◆ Conclusions

The ATLAS Detector

Inner Detector ($|\eta| < 2.4$)

- silicon pixel, strip & transition rad. tracker
- Impact parameter resolution $\approx 10 \mu\text{m}$
- 2T solenoidal field



Muon Spectrometer ($|\eta| < 2.7$)

- Trigger chambers (RPC, TGC),
- Tracking chambers (MDT, CSC)
- 0.5-2 T toroidal field

Tracking

- $\sigma_{p_T}/p_T \sim 0.05\% p_T \oplus 1.5\%$
(for $p_T < 100 \text{ GeV}$, ID dominant)
- $\sigma_M(J/\psi-\gamma) \sim 60-120 \text{ MeV}$

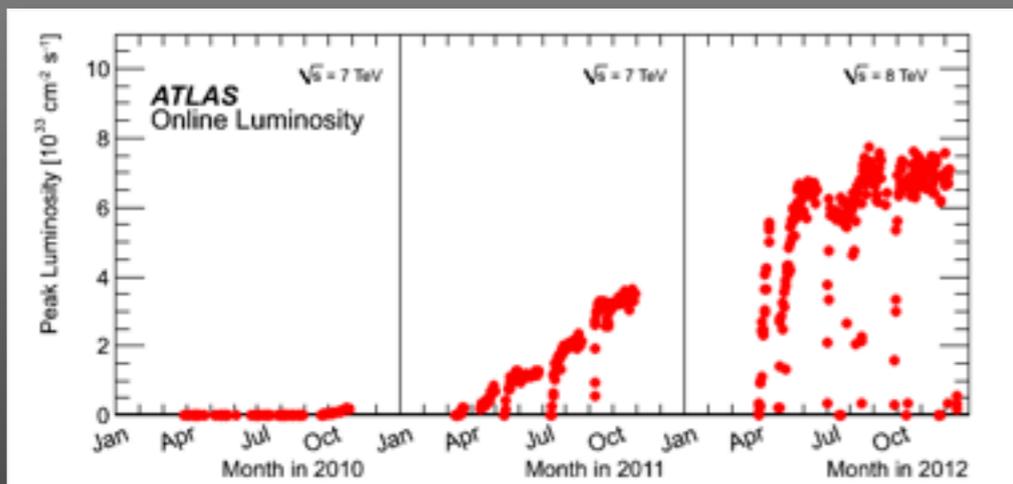
ATLAS Data Taking

2011

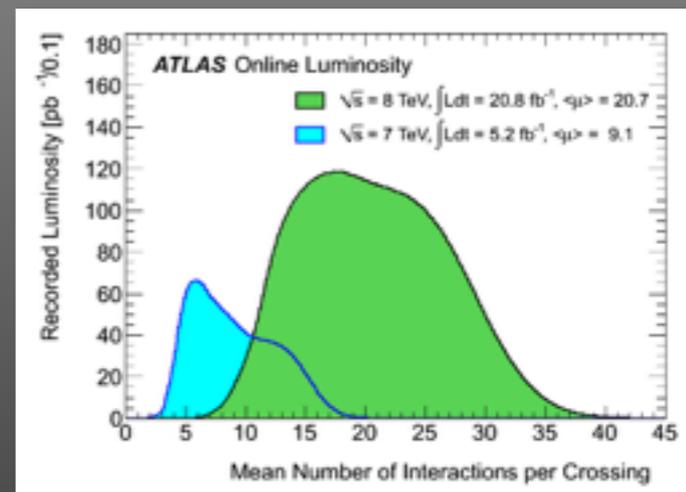
- $> 5 \text{ fb}^{-1}$ recorded
- instantaneous luminosity & pile-up steadily increasing

2012

- $\sim 20 \text{ fb}^{-1}$ recorded
- Flatter instantaneous luminosity profile
- Challenging pile-up conditions!

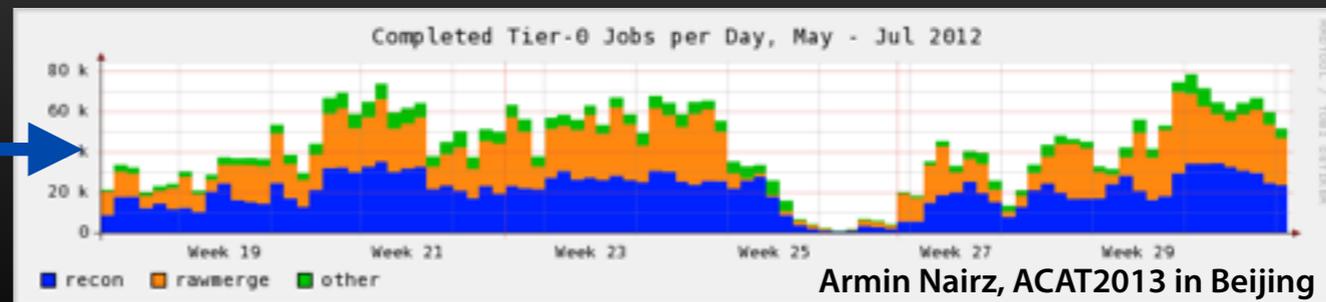
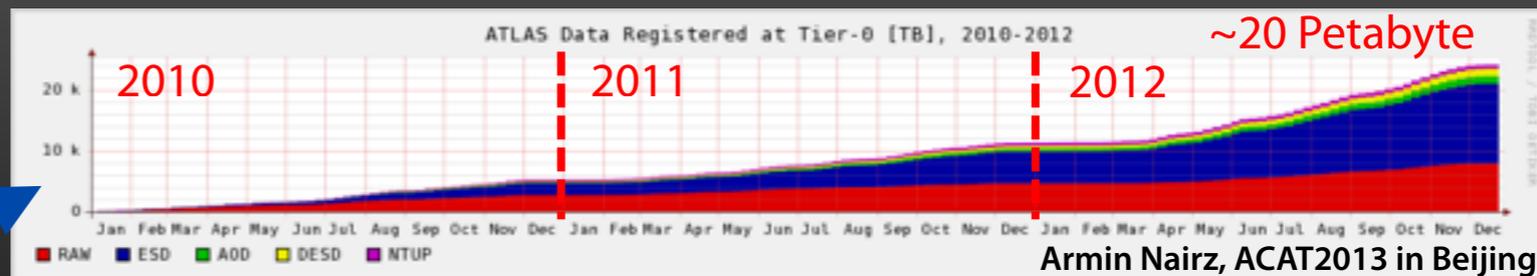


di-muon trigger selection

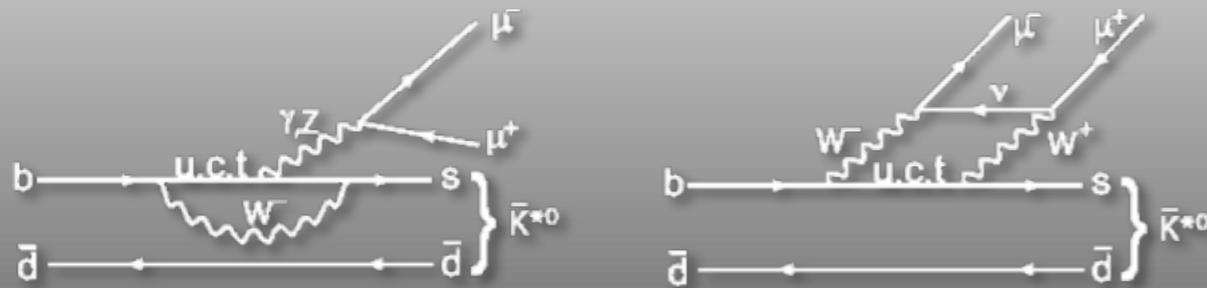


Tier-0 processing

- RAW and derived data products registered for export (2010-12)
- Up-to 80k Tier-0 jobs completed/day (May to July 2012)



STUDY OF THE DECAY $B_d \rightarrow K^* (\rightarrow K^+ \pi^-) \mu^+ \mu^-$



Motivation

- relatively small SM BR $\approx 1.1 \cdot 10^{-6}$
- provides exclusive final state for $b \rightarrow s + l^+ l^-$ transition
- only loop-mediated within SM

Observables sensitive to NP:

- Lepton forward-backward asymmetry – A_{FB}
- K^{*0} longitudinal polarization fraction – F_L
(hadronic uncertainties drop out - at some order)

$$\frac{d^4\Gamma}{dq^2 d\cos\theta_\ell d\cos\theta_{K^*} d\phi}$$

Measurement:

- differential angular distributions of the 4-particle final state as a function of di-muon mass (q^2)

$B_D \rightarrow K^* (\rightarrow K^+ \pi^-) \mu^+ \mu^-$ decay & analysis method

Kinematic observables:

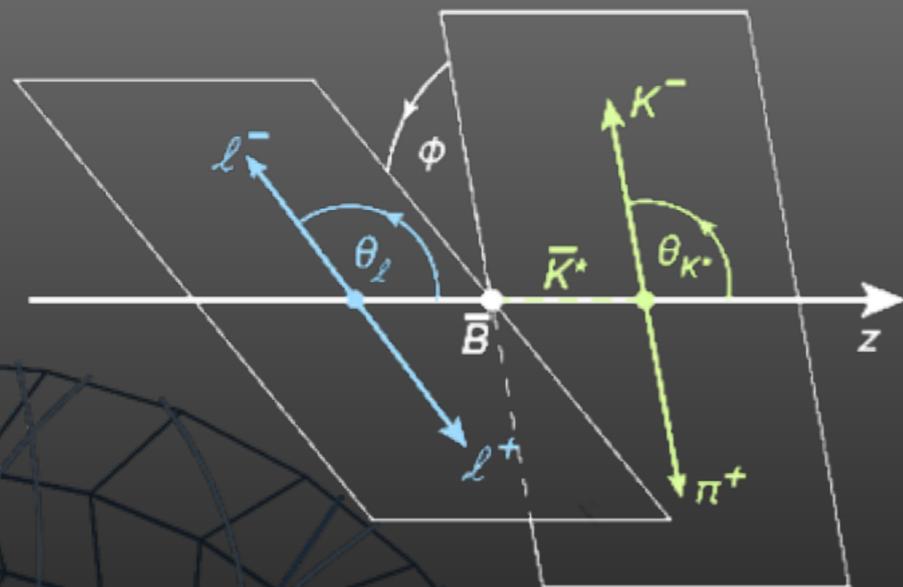
- 3 angles (θ_L, θ_K, Φ)
- dimuon mass q^2 (K^{*0} on shell)
- differential decay rate

Measured angular distributions:

- insufficient statistics 2 out of 3 angles integrated out from the 4 diff. decay rate

$$\frac{1}{\Gamma} \frac{d^2\Gamma}{dq^2 d\cos\theta_K} = \frac{3}{2} F_L(q^2) \cos^2\theta_K + \frac{3}{4} (1 - F_L(q^2)) (1 - \cos^2\theta_K)$$

$$\frac{1}{\Gamma} \frac{d^2\Gamma}{dq^2 d\cos\theta_l} = \frac{3}{4} F_L(q^2) (1 - \cos^2\theta_l) + \frac{3}{8} (1 - F_L(q^2)) (1 + \cos^2\theta_l) + A_{FB}(q^2) \cos\theta_l$$



$$\frac{d^4\Gamma}{dq^2 d\cos\theta_l d\cos\theta_{K^*} d\phi}$$

$\langle A_{FB} \rangle$ & $\langle F_L \rangle$ extraction:

- extended unbinned maximum-likelihood fits
- 1-D fits in bins of q^2 to mass and the 2 angles θ_l, θ_K

$B_D \rightarrow K^* (\rightarrow K^+ \pi^-) \mu^+ \mu^-$ SIGNAL YIELD

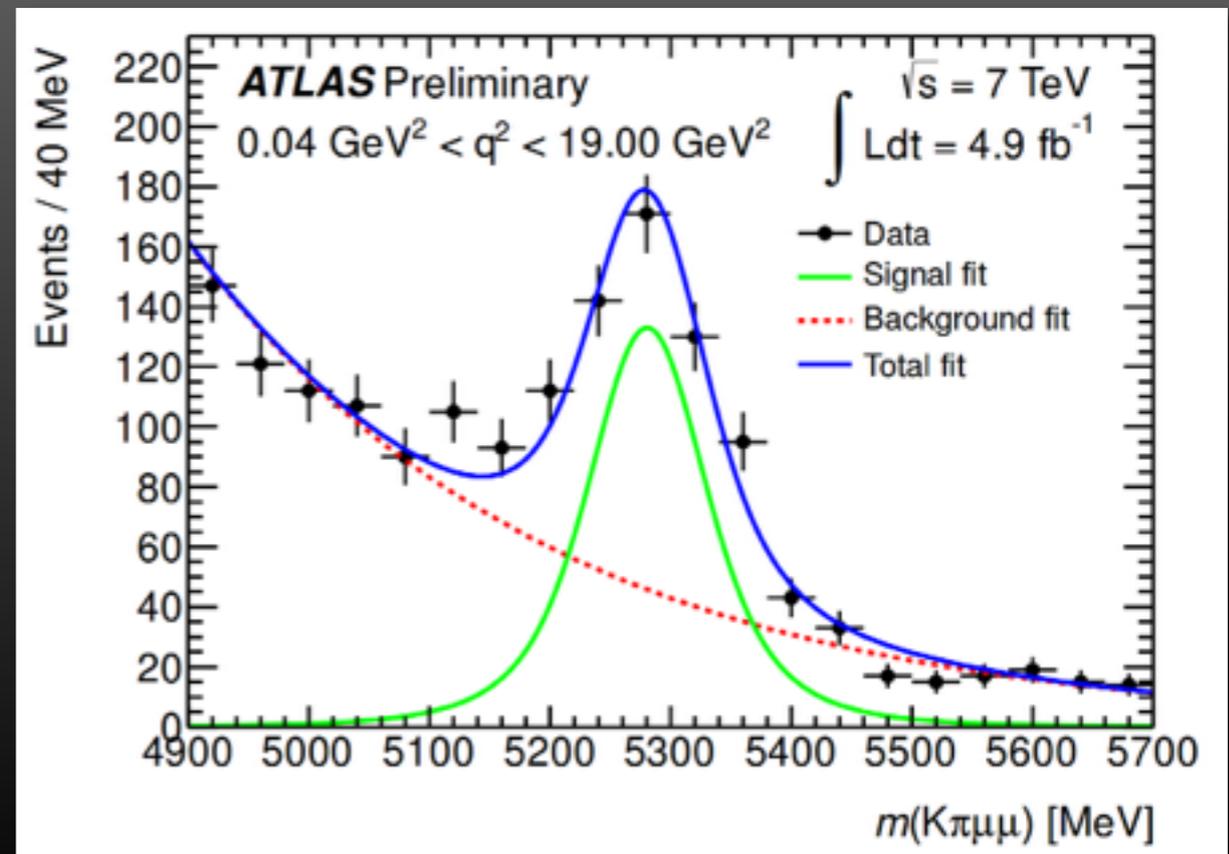
Constraints on measurement:

- $q^2 < 2 \text{ GeV}^2$, limited statistics due to trigger acceptance
- experimental veto on J/ψ & $\psi(2S)$ ($c\bar{c}$ regions)
 - $8.68 < q^2 < 10.09$ $J/\psi \rightarrow \mu^+ \mu^-$ (3σ)
 - $12.86 < q^2 < 14.18$ $\psi(2S) \rightarrow \mu^+ \mu^-$ (3σ)
- to remove radiative c-decays and remaining J/ψ & $\psi(2S)$ in tails:
 - cut $| (m(B_D)_{\text{REC}} - m(B_D)_{\text{PDG}}) - (m(\mu^+ \mu^-)_{\text{REC}} - m(c\bar{c})_{\text{PDG}}) | < \Delta m$

B_D mass likelihood fit:

- cut based selection optimised on MC
- Gaussian for signal (with per-event errors)
- Exponential for the background
- K^{*0} accepted if $m(K^+ \pi^-) \in (846, 946) \text{ MeV}$
- $N_{\text{sig}} = 466 \pm 34$
- $N_{\text{bkg}} = 1132 \pm 43$

ATLAS-CONF-2013-038

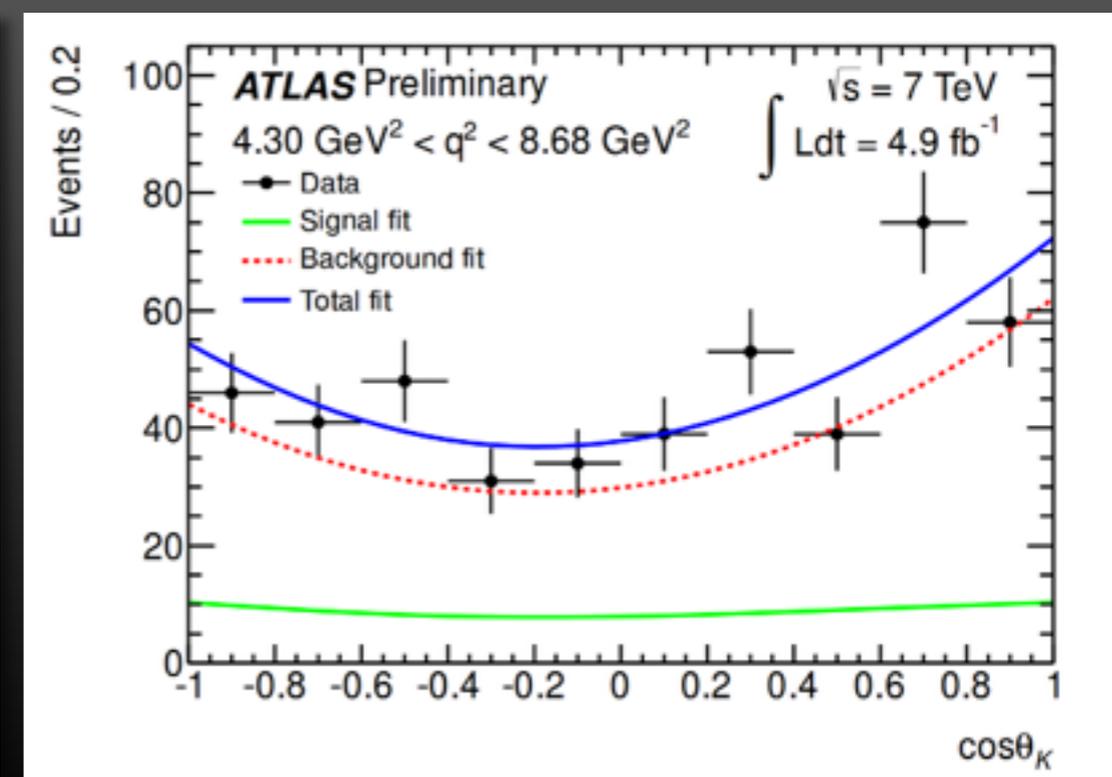
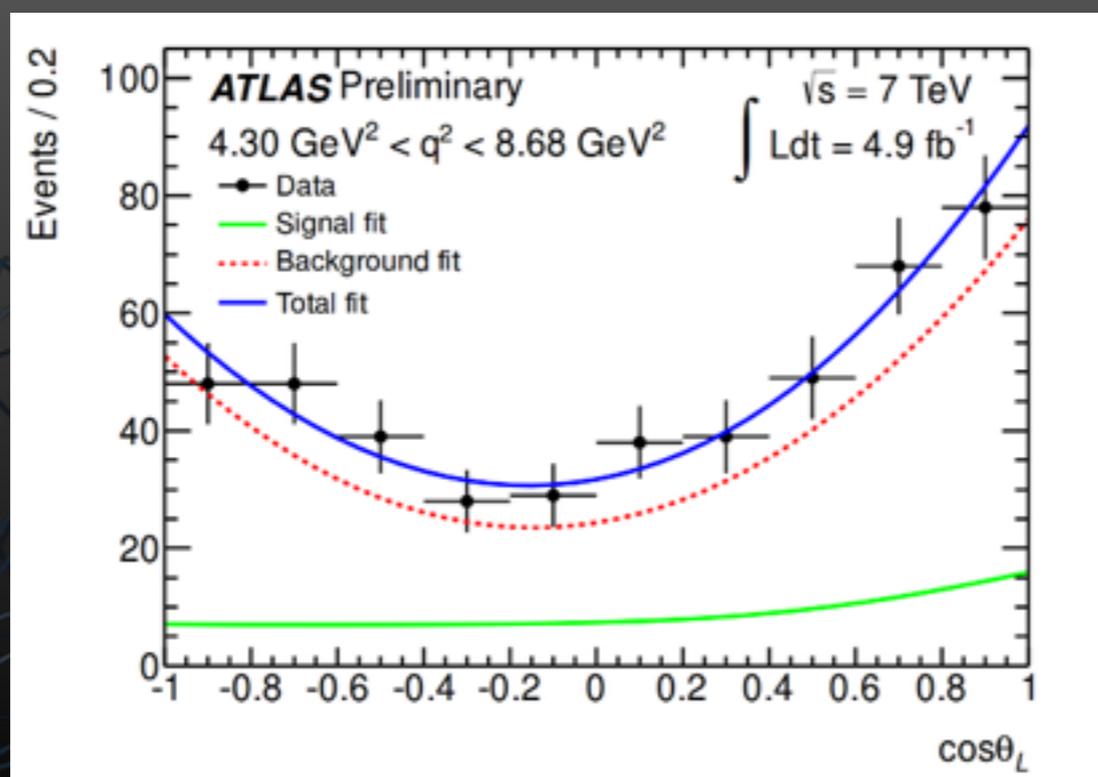
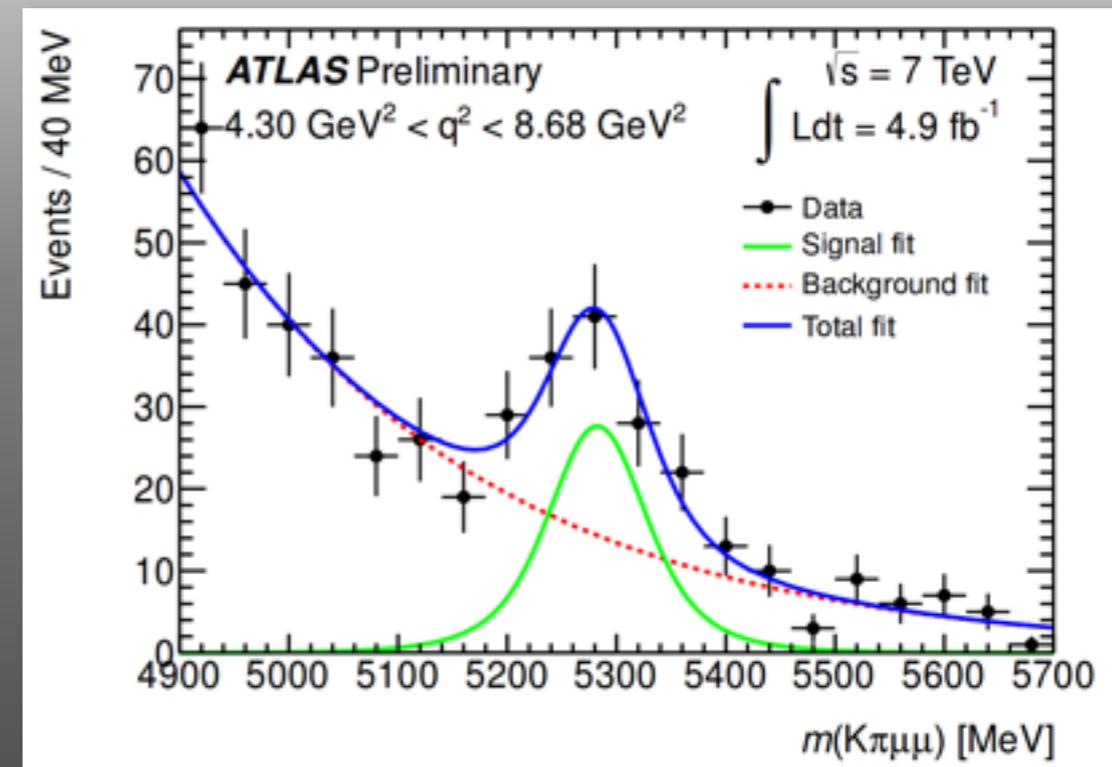


$B_D \rightarrow K^* (\rightarrow K^+ \pi^-) \mu^+ \mu^-$ LIKELIHOOD FIT

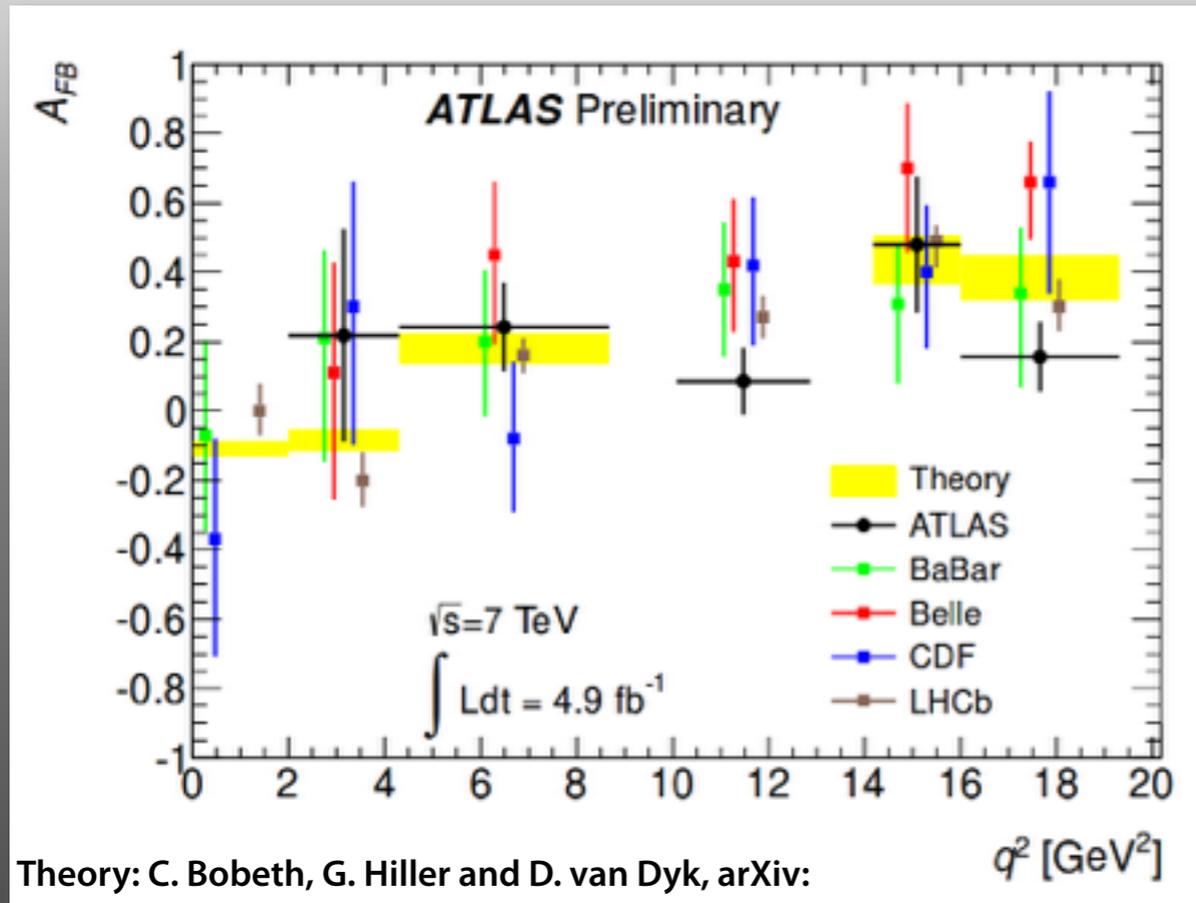
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Extended unbinned max-likelihood fit :

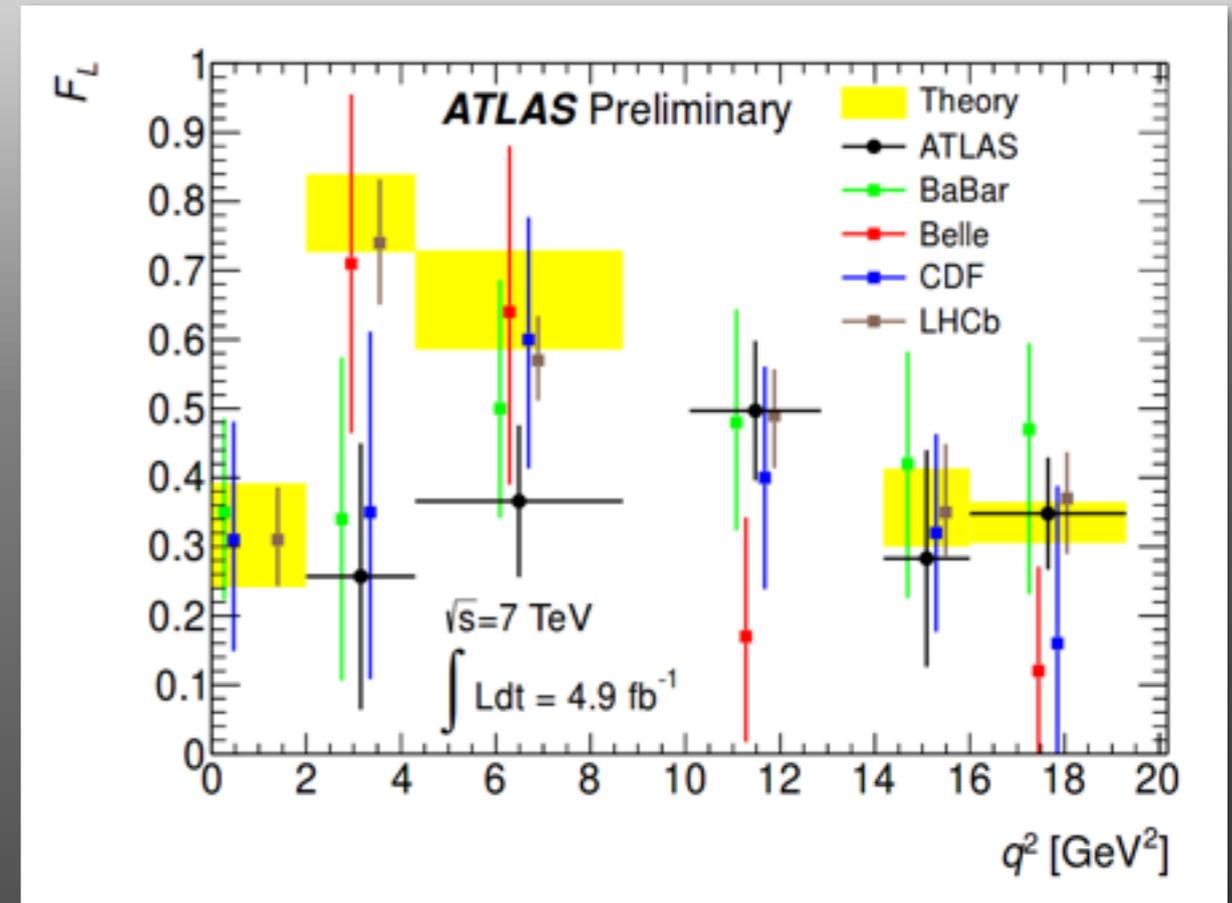
- performed sequentially
 - fit mass distribution, & fixed signal yield
 - simultaneous unbinned mass-angular fit (a la "BaBar")
(the mass PDF param. & signal fraction kept fixed from previous fit)
- done separately in each of 6 q^2 bins



$B_D \rightarrow K^* (\rightarrow K^+ \pi^-) \mu^+ \mu^-$, $\langle A_{FB} \rangle$ & $\langle F_L \rangle$ FIT RESULT



Theory: C. Bobeth, G. Hiller and D. van Dyk, arXiv: 1105.2659



Fit Results:

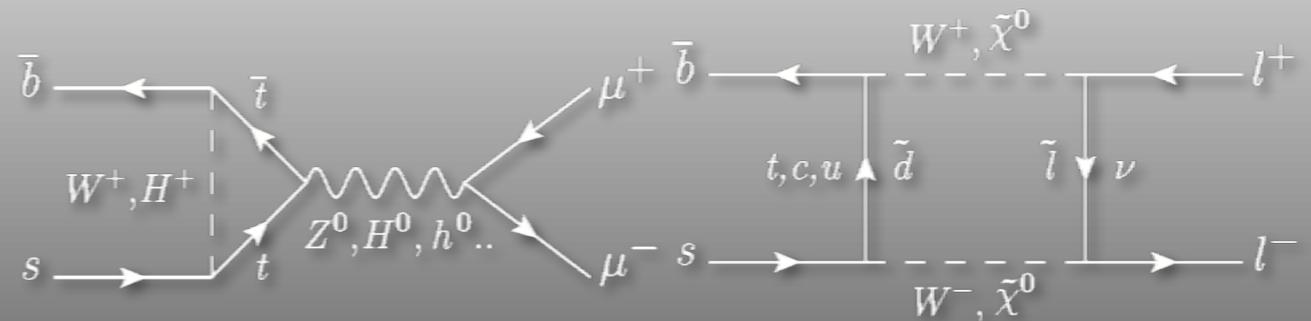
- statistical uncertainty dominates
- ATLAS measurement in agreement with SM

q^2 range (GeV^2)	N_{sig}	A_{FB}	F_L
$2.00 < q^2 < 4.30$	19 ± 8	$0.22 \pm 0.28 \pm 0.14$	$0.26 \pm 0.18 \pm 0.06$
$4.30 < q^2 < 8.68$	88 ± 17	$0.24 \pm 0.13 \pm 0.01$	$0.37 \pm 0.11 \pm 0.02$
$10.09 < q^2 < 12.86$	138 ± 31	$0.09 \pm 0.09 \pm 0.03$	$0.50 \pm 0.09 \pm 0.04$
$14.18 < q^2 < 16.00$	32 ± 14	$0.48 \pm 0.19 \pm 0.05$	$0.28 \pm 0.16 \pm 0.03$
$16.00 < q^2 < 19.00$	149 ± 24	$0.16 \pm 0.10 \pm 0.03$	$0.35 \pm 0.08 \pm 0.02$
$1.00 < q^2 < 6.00$	42 ± 11	$0.07 \pm 0.20 \pm 0.07$	$0.18 \pm 0.15 \pm 0.03$

SEARCH FOR $B_s \rightarrow \mu^+ \mu^-$

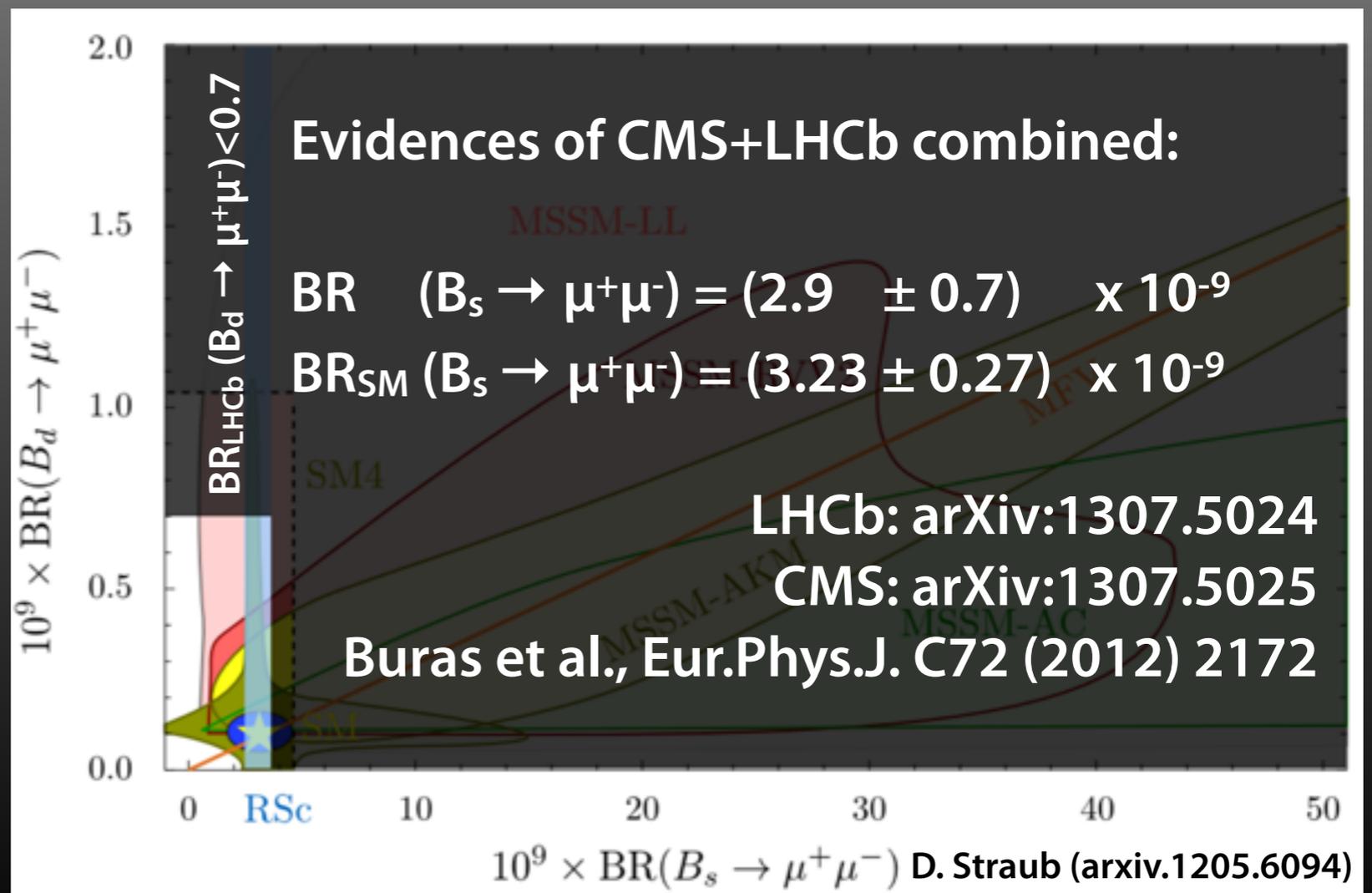
Motivation

- (SM) helicity suppressed FCNC
- strong QCD-free constraint on NP
- genuine probe of Yukawa interactions
- EW precision test (wrt. Z penguin)



Recent results

- very consistent with SM
- hope for $>$ BR due to NP (pseudo-)scalar op.
- room for NP also in :
 - destructive interference between NP and SM
 - $BR \ll BR_{SM} ???$
 - waits for LHC RUN II data



$B_s \rightarrow \mu^+ \mu^-$ STRATEGY @ ATLAS

Analysis Features:

- Blind analysis technique - B_s signal mass region excluded (± 300 MeV)
- sideband events – split in 1/2 :
 - even # events = bkg. interpolation, odd # = selection optimization
- Multivariate analysis (BDT)
- Relative BR measurement:
 - reference signal decay = $B^+ \rightarrow J/\psi K^+$ (large stat.)
 - partial cancelation of syst. uncertainties on lumi, cross-sec, efficiencies

Data

- efficient di-muon trigger
→ 4.9fb^{-1} (2011)

$$\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) = N_{B_s \rightarrow \mu^+ \mu^-} \times \frac{1}{N_{B^+ \rightarrow J/\psi K^+}}$$

Monte Carlo

$$(\epsilon_{tot} \times A_{tot}) = \frac{N_{\text{SELECT \& RECON}}}{N_{\text{GENERATED}}}$$

- derived from simulation
- “calibrated” on data
- systematics taken from data-MC discrepancies

$$\times \frac{(\epsilon_{tot} \times A_{tot})_{B^+ \rightarrow J/\psi K^+}}{(\epsilon_{tot} \times A_{tot})_{B_s \rightarrow \mu^+ \mu^-}}$$

$$\times \mathcal{B}(B^+ \rightarrow J/\psi K^+) \times \frac{f_u}{f_s}$$

PDG, LHCb

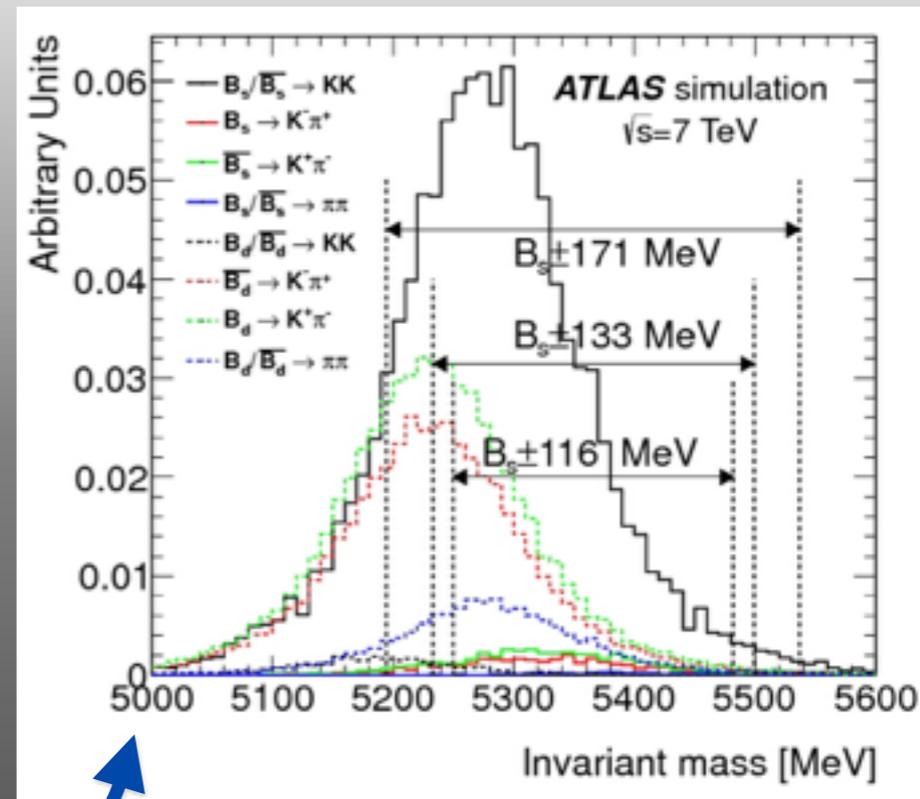
ATLAS-CONF-2013-076

$B_s \rightarrow \mu^+ \mu^-$ SIGNAL & BACKGROUND

Signal extraction:

- N_{B_s} is a CLs limit derived from :
 - candidate count &
 - background estimation in signal region
- N_{B^+} is an unbinned extended maximum-likelihood fit

$$N_{B_s \rightarrow \mu^+ \mu^-} \times \frac{1}{N_{B^+ \rightarrow J/\psi K^+}}$$



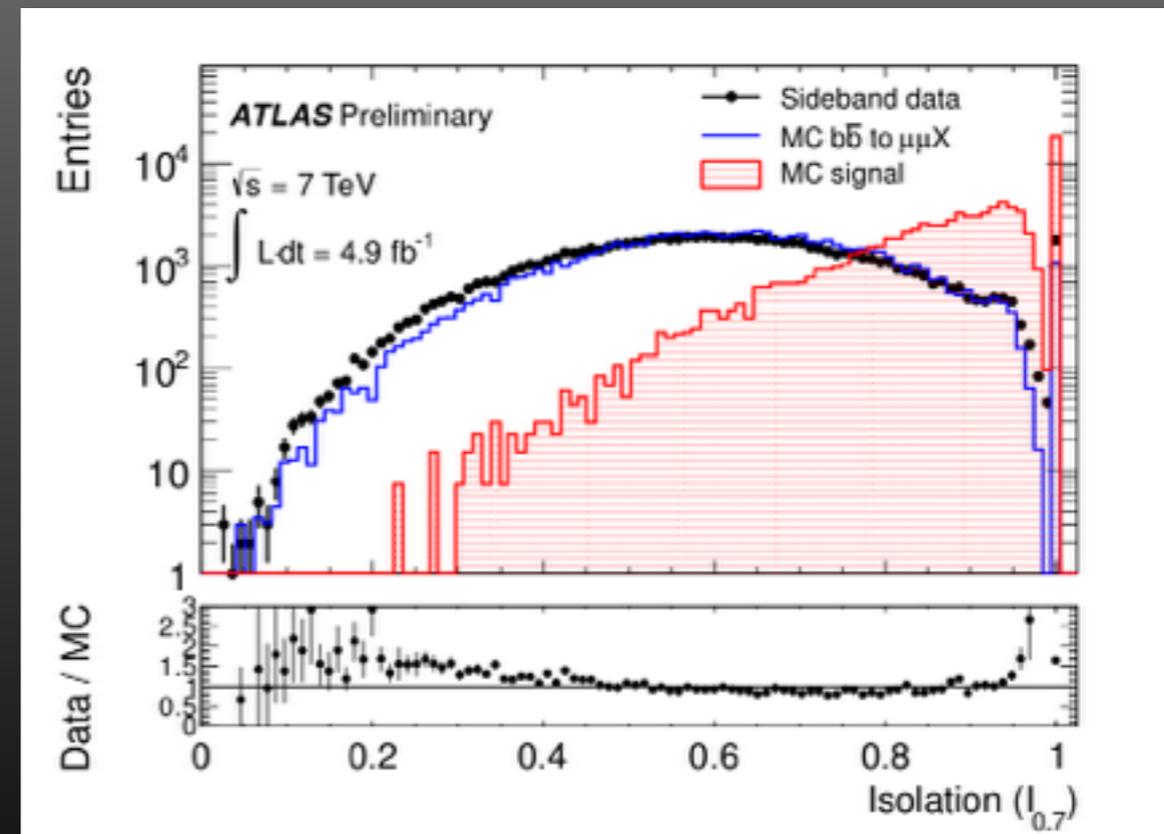
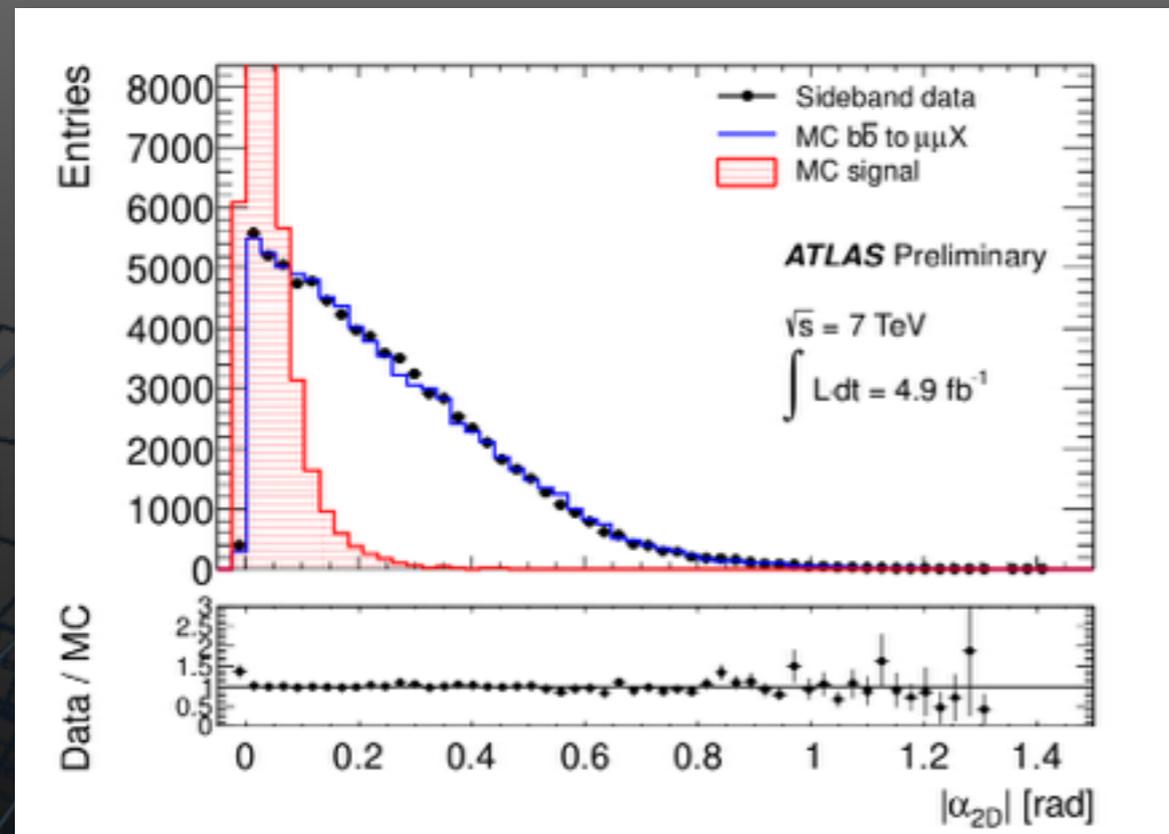
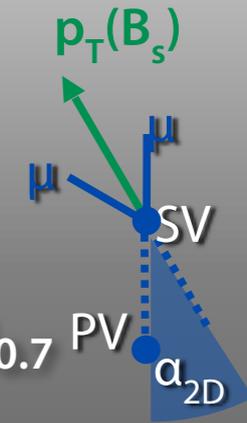
Background composition:

- resonant: $B \rightarrow hh'$ (K/ π)
 - 'fake'-muon rates (MC) $\pi^\pm / K^+ / K^- \sim 2.1/4.1/3.3 \%$
 - 0.3 $B \rightarrow hh'$ events expected in the signal region
- continuum: non resonant $b\bar{b} \rightarrow \mu^+ \mu^- X$
 - smooth in dimuon mass
 - sideband interpolation (even # events)

$B_s \rightarrow \mu^+ \mu^-$ BACKGROUND DISCRIMINATION

Continuum discrimination:

- 13 best performing discriminating variables chosen by MVA
- BDT shown as most powerful event classifier
 - trained on MC
- plots show Data/MC agreement of pointing angle α_{2D} and Isolation $I_{0.7}$ (among most discriminant variables)



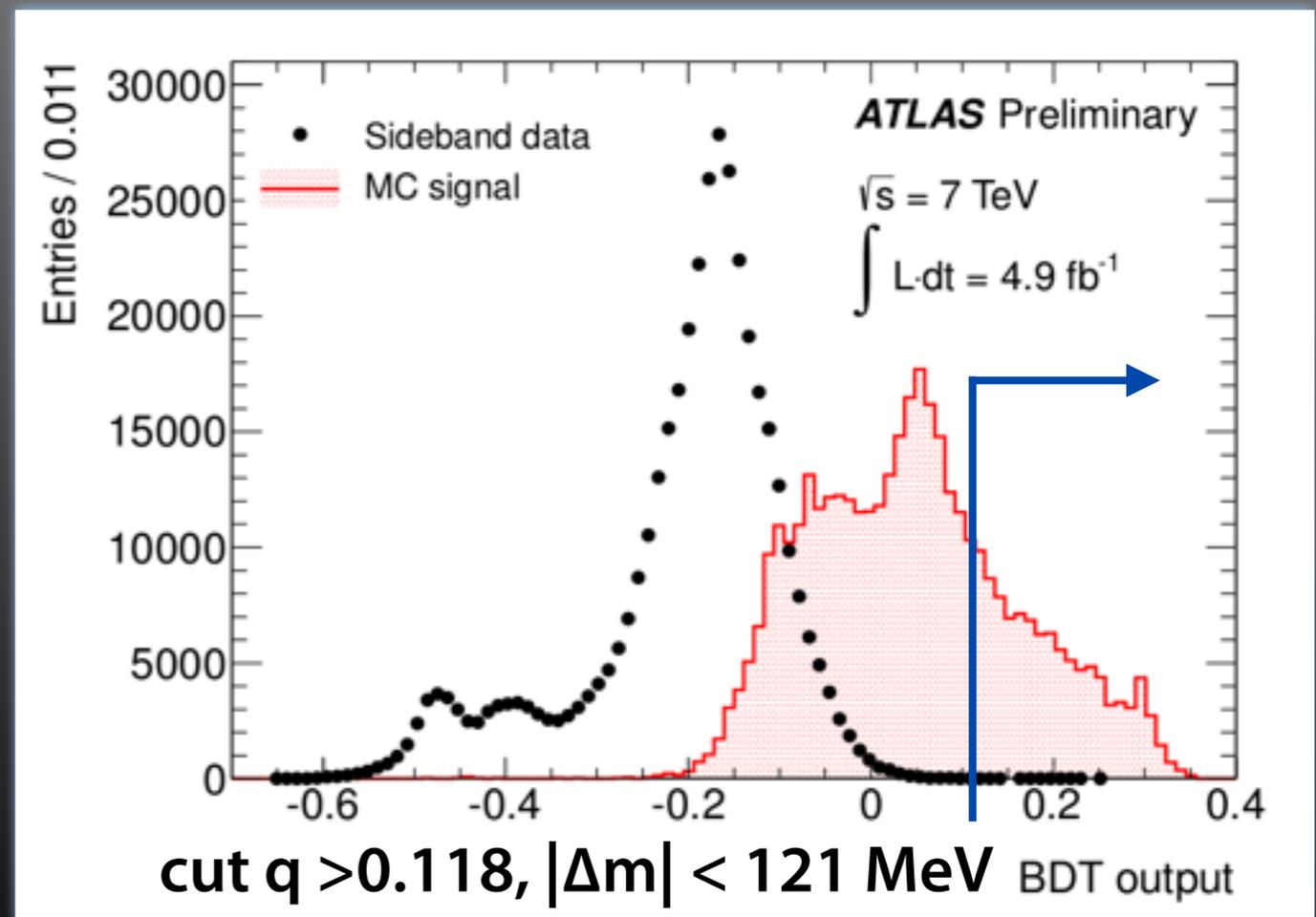
$B_s \rightarrow \mu^+ \mu^-$ BDT selection

Selection optimised in 2D space ($\Delta m, q$):

- Δm = signal mass window width
- q = BDT output (event classifier)
- odd-numbered sideband events and signal MC used

Working point ($\Delta m, q$):

- = max of Punzi estimator
 - $P(\Delta m, q) = \epsilon_{\text{sig}} / (1 + \sqrt{N_{\text{bkg}}})$ (@95% CL)
- ϵ_{sig} calculated directly on simulated signal events
- N_{bkg} in sig. region estimated from sideband data



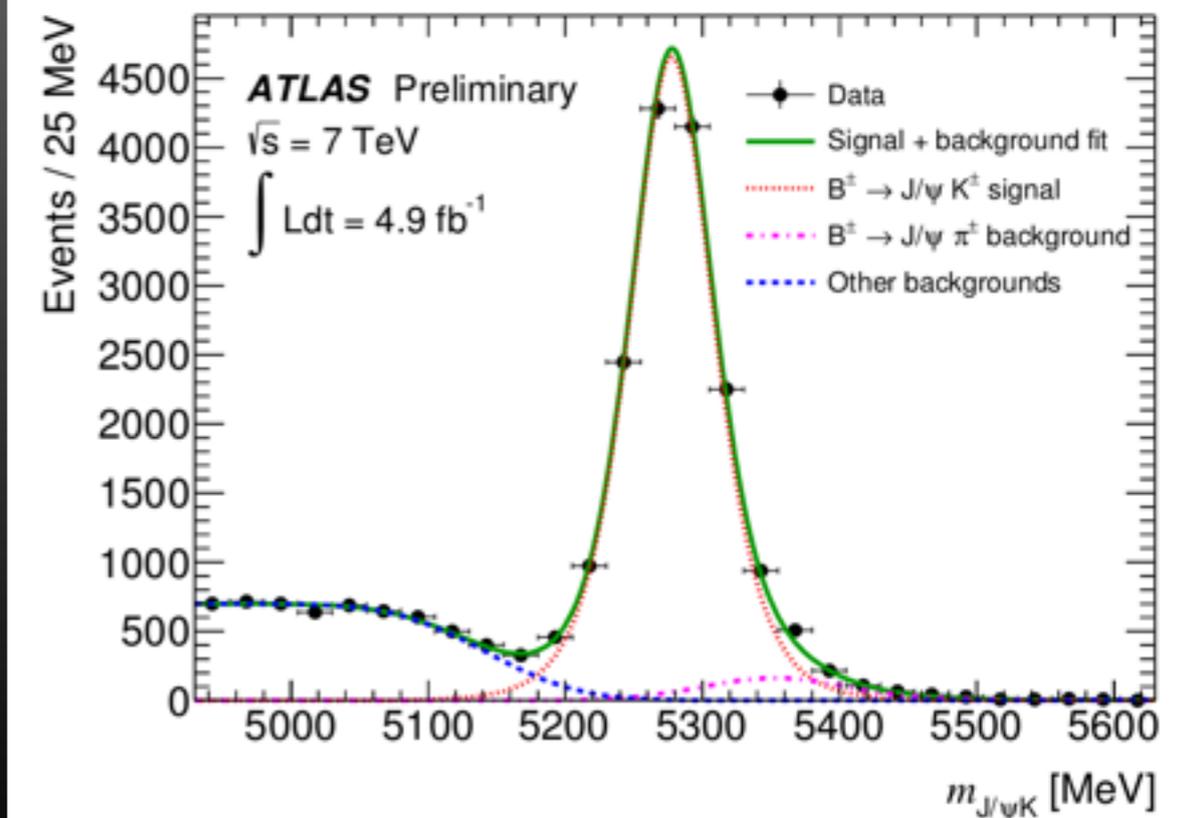
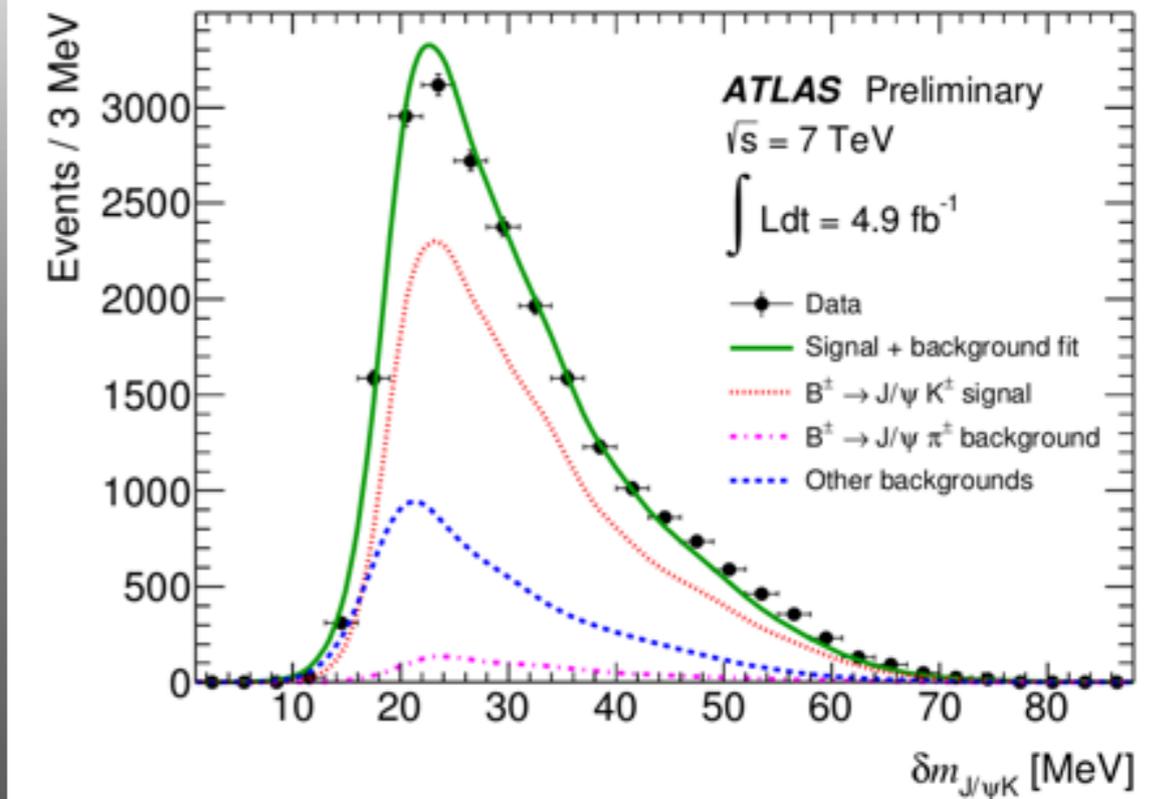
$B_s \rightarrow \mu^+ \mu^-$ Reference Decay Yield

$N_{B^+ \rightarrow J/\psi K^+}$ extraction:

- by unbinned maximum likelihood fit
- per-event mass resolution δm in the fit
- selection as close as possible to B_s
- same B_s -trained BDT used to min. systematics
- main systematics from varying continuum background fit models

$B^\pm \rightarrow J/\psi (\rightarrow \mu^+ \mu^-) K^\pm$ yield:

- $N_{B^\pm \rightarrow J/\psi (\rightarrow \mu^+ \mu^-) K^\pm} = 15214 \pm 1.1\%(\text{stat}) \pm 2.4\%(\text{syst})$



$B_s \rightarrow \mu^+ \mu^-$ Box opening

N_{B_s} extraction:

- Single Event Sensitivity
 $SES = (2.07 \pm 26\%(\text{stat}) \pm 12.5\%(\text{syst})) \times 10^{-9}$
- Systematic uncertainty dominated by
 - reference channel BR contribution
 - acceptance and efficiency ratio
- N_{bkg} expected in signal window = 6.75
- N_{obs} in signal window = 6

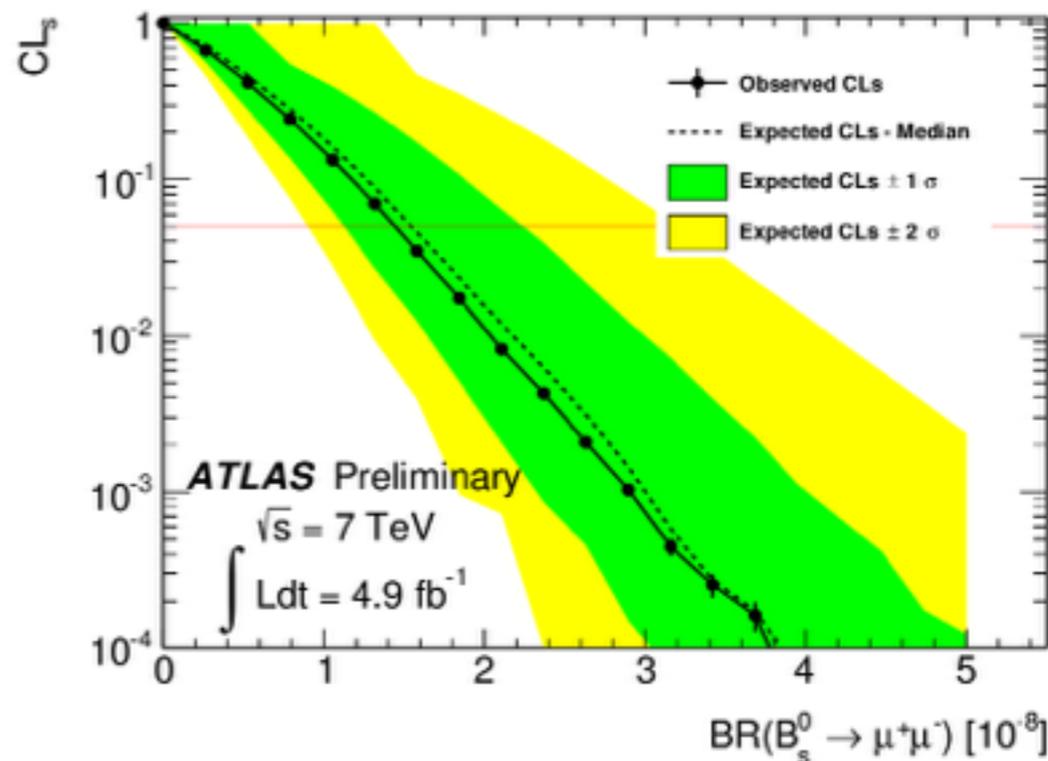
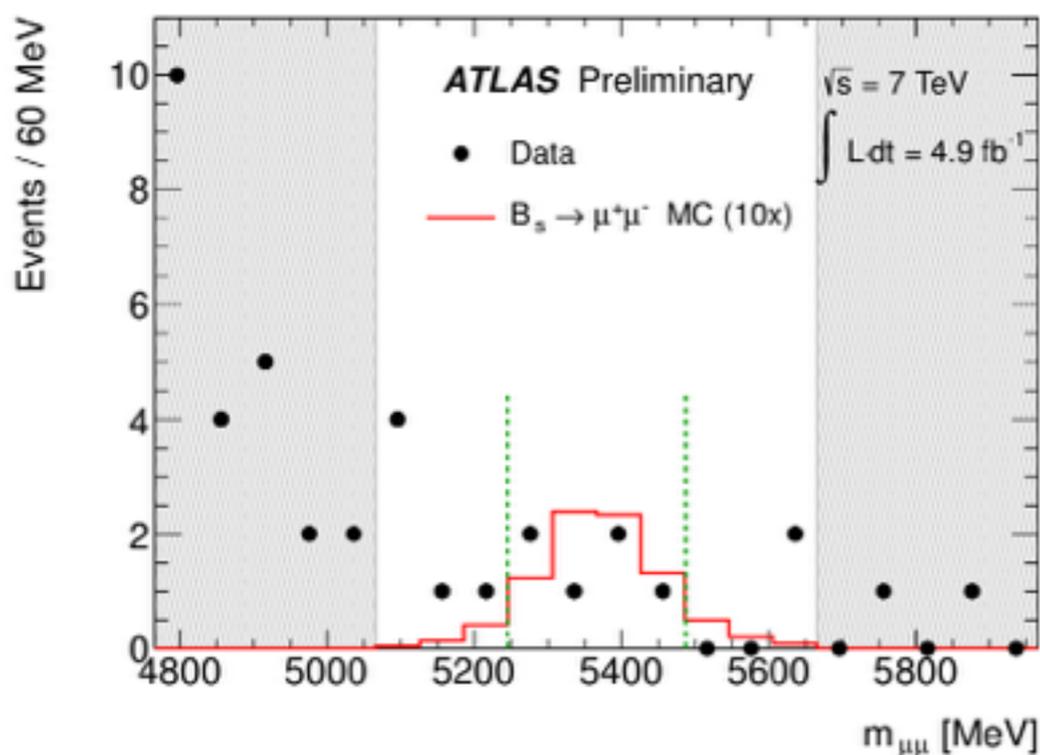
$$\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) = N_{B_s \rightarrow \mu^+ \mu^-} \times \frac{1}{N_{B^+ \rightarrow J/\psi K^+}} \times \frac{(\epsilon_{\text{tot}} \times A_{\text{tot}})_{B^+ \rightarrow J/\psi K^+}}{(\epsilon_{\text{tot}} \times A_{\text{tot}})_{B_s \rightarrow \mu^+ \mu^-}} \times \mathcal{B}(B^+ \rightarrow J/\psi K^+) \times \frac{f_u}{f_s}$$

CLs @ 95% CL:

$$\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) < 1.6 \times 10^{-9}$$

$$\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) < 1.5 \times 10^{-9}$$

New ATLAS result on 2012 data soon!



CONCLUSIONS

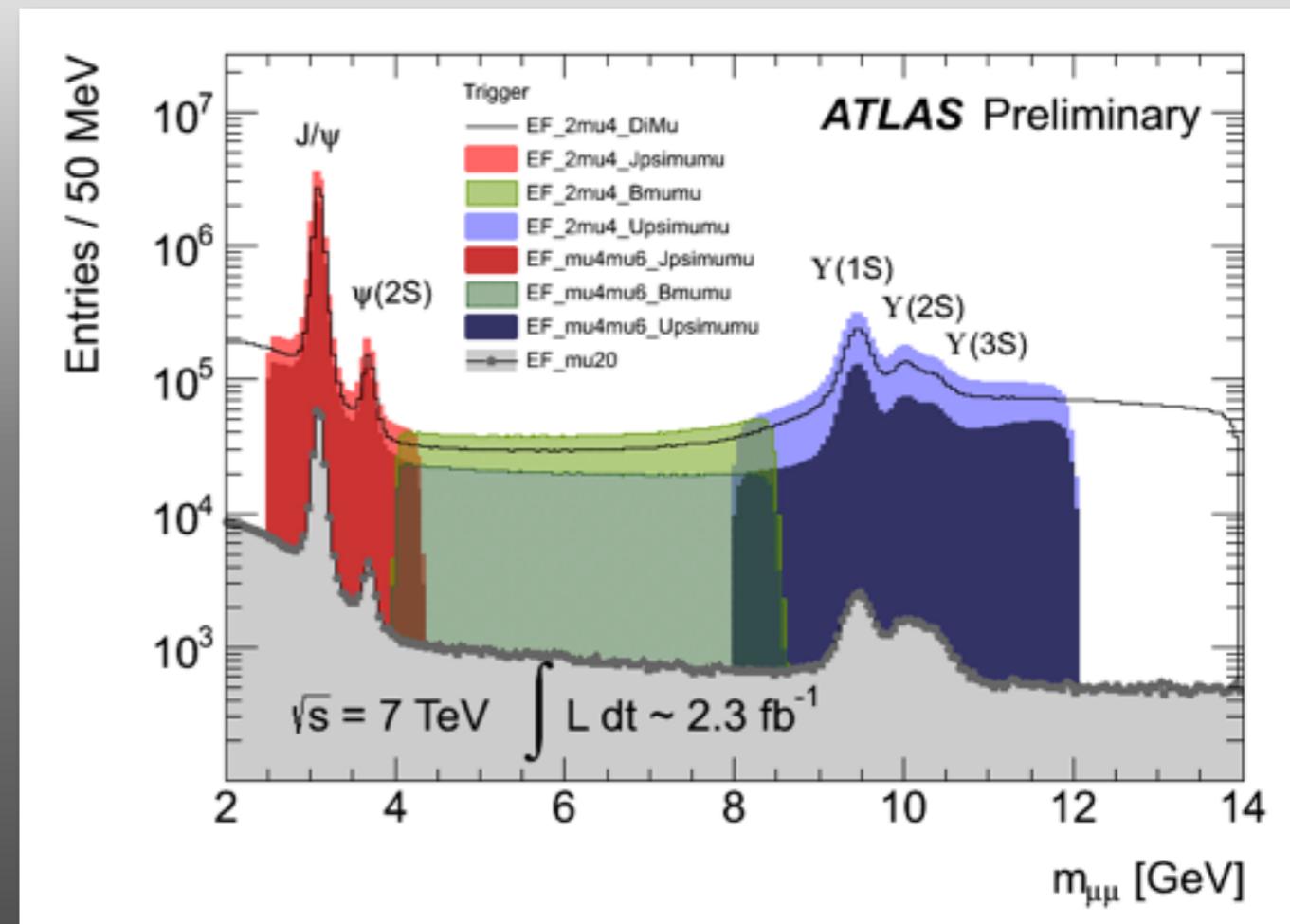
- ◆ Results from the full 2011 dataset
- ◆ No NP signs or significant deviation from SM predictions
- ◆ ATLAS has high quality b-physics program
 - ◆ search for the rare decay $B_s \rightarrow \mu^+\mu^-$
 - ✓ ATLAS-CONF-2013-076
 - ◆ angular analysis of the decay $B_d \rightarrow K^{*0} (\rightarrow K^+\pi^-) \mu^+\mu^-$
 - ✓ ATLAS-CONF-2013-038
- ◆ Improved analysis techniques are being developed
- ◆ Plans :
 - ✓ Publish result on the full 2012 dataset ($>20\text{fb}^{-1}$) ASAP
 - stay tuned !

THANK YOU FOR YOUR ATTENTION!

Theory: C. Bobeth, G. Hiller and D. van Dyk, arXiv:1105.2659

BACKUP SLIDES

Theory: C. Bobeth, G. Hiller and D. van Dyk, arXiv:1105.2659



di-muon trigger event selection :

- 5 fb⁻¹ ~ 150G B⁰-pairs, ~ 30M B_s → J/ψ Φ
- specific dimuon selections with Barrel/Endcap logic introduced in 2012
- new dedicated μ+μ-X trigger introduced in 2012
- B-physics trigger (mu4mu4) thresholds unprescaled during 2011 despite the increasing instantaneous luminosity

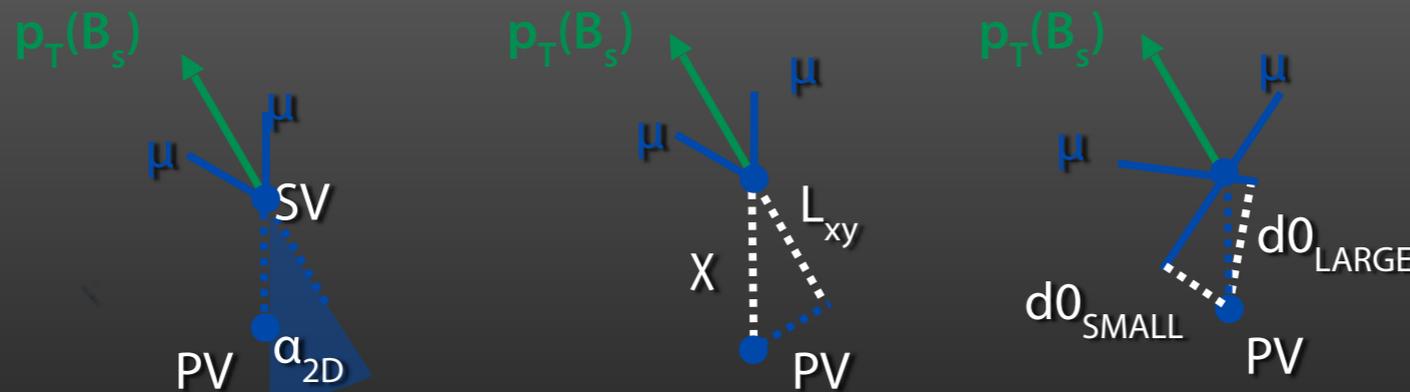
Signal candidate selection

- 2, 3 or 4 prong vertex constraint depending on decay topology
- Primary vertex selection:
 - Closest in z to the B candidate
 - Re-fit excluding B daughters
- Tracks:
 - At least 1 pixel, 6 SCT and 9 TRT hits (good tracks)
 - $|\eta| < 2.5$ and $p_T > 4$ (2.5) GeV for muons (kaons)
 - tracks from the tracking systems matched to muon spectrometer tracks
- B candidates $p_T > 8$ GeV and $|\eta| < 2.5$
 - Events selected based on their decay topology using many discriminating variables

$B_s \rightarrow \mu^+ \mu^-$ SEL. OF DISCRIMINATING VARIABLES

Discriminating variables:

- Distinguish B and continuum events
- Highest discriminating power
- Exclusion of highly correlated variables
- Only variables not correlated with invariant mass were taken
- Exploit PV-SV separation (L_{xy}), symmetry of the final state (d_0), pointing angle, b-hadronisation features (isolation, p_T of the B)



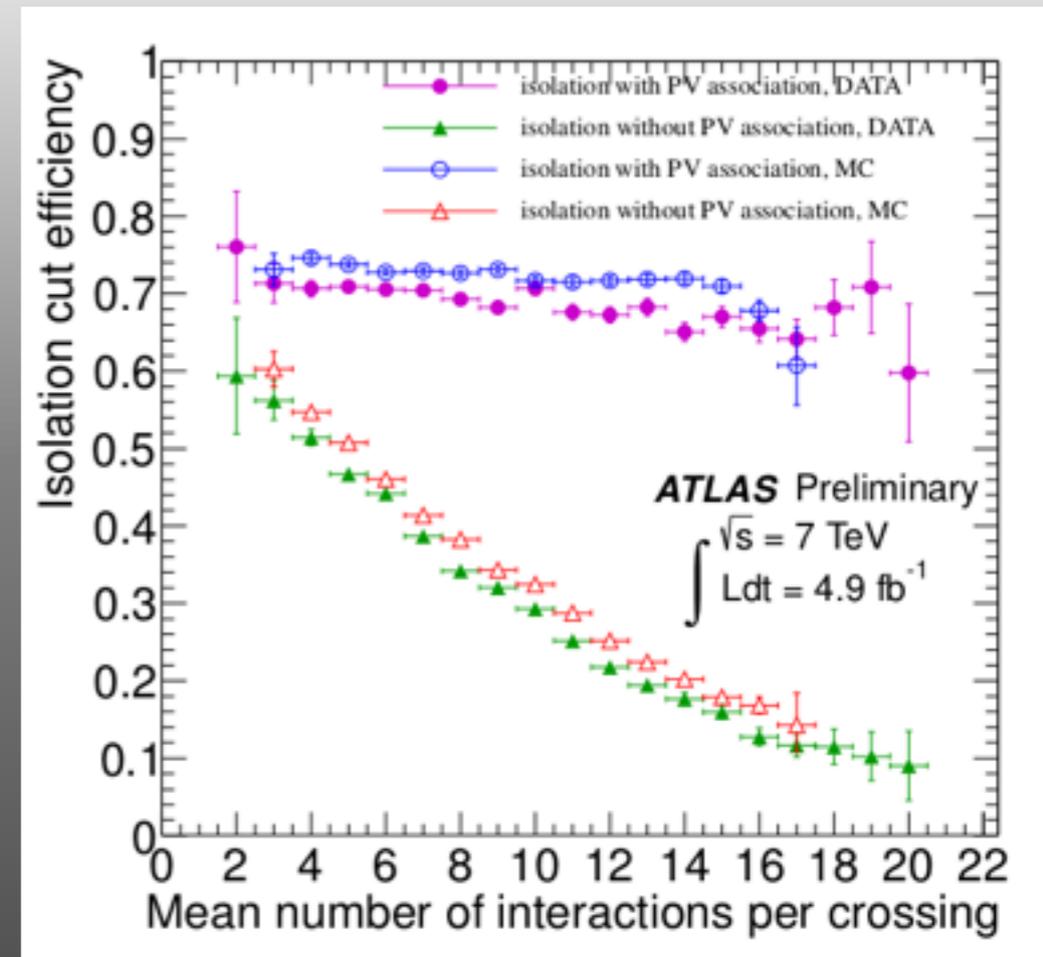
$B_s \rightarrow \mu^+ \mu^-$ DISCRIMINATING VARIABLES

Variable	Description	Ranking
L_{xy}	Scalar product in the transverse plane of $(\Delta\vec{x} \cdot \vec{p}^B)/ \vec{p}_T^B $	1
$I_{0.7}$ isolation	Ratio of $ \vec{p}_T^B $ to the sum of $ \vec{p}_T^B $ and the transverse momenta of all tracks with $p_T > 0.5$ GeV within a cone $\Delta R < 0.7$ from the B direction, excluding B decay products	2
$ \alpha_{2D} $	Absolute value of the angle in the transverse plane between $\Delta\vec{x}$ and \vec{p}^B	3
p_L^{\min}	Minimum momentum of the two muon candidates along the B direction	4
p_T^B	B transverse momentum	5
ct significance	Proper decay length $ct = L_{xy} \times m_B / p_T^B$ divided by its uncertainty	6
χ_z^2, χ_{xy}^2	Significance of the separation between production (PV) and decay vertex (SV) $\Delta\vec{x}^T \cdot (\sigma_{\Delta\vec{x}}^2)^{-1} \cdot \Delta\vec{x}$, in z and (x, y) , respectively	7, 13
$ D_{xy} ^{\min}, D_z ^{\min}$	Absolute values of the minimum distance of closest approach in the xy plane or along z of tracks in the event to the B vertex	8, 11
ΔR	Angle $\sqrt{(\Delta\phi)^2 + (\Delta\eta)^2}$ between $\Delta\vec{x}$ and \vec{p}^B	9
$ d_0 ^{\max}, d_0 ^{\min}$	Absolute values of the maximum and minimum impact parameter in the transverse plane of the B decay products relative to the primary vertex	10, 12

$B_s \rightarrow \mu^+ \mu^-$ ISOLATION VARIABLE

Isolation variable:

- Tracks with $p_T > 0.5$ GeV excluding B daughters in cone $\Delta R < 0.7$
 $\Delta R = \sqrt{(\Delta\eta^2 + \Delta\phi^2)}$
- Only tracks associated with the corresponding PV are taken to avoid isolation cut efficiency to depend on pile-up



$B_s \rightarrow \mu^+ \mu^-$ (acceptance x efficiency) ratio

$$\frac{(\epsilon_{tot} \times A_{tot})_{B^+ \rightarrow J/\psi K^+}}{(\epsilon_{tot} \times A_{tot})_{B_s \rightarrow \mu^+ \mu^-}}$$

- Determined on reweighted B_s and B^+ MC samples wrt the fiducial volume
- Systematic uncertainties:
 - Dominant contribution from data-MC discrepancies of separation variables
 - Main discrepancies come from : Isolation and L_{xy}
 - Isolation is B-flavour dependent
 - L_{xy} is correlated with the vertex reconstruction (\rightarrow with other discriminant variables) but is it B-flavour independent

Channel	$A \times \epsilon$	$R_{A\epsilon}$
B^+	$1.317 \pm 0.008\%$ (stat)	$0.267 \pm 1.8\%$ (stat) $\pm 6.9\%$ (syst)
B_s^0	$4.929 \pm 0.084\%$ (stat)	

SES systematic uncertainties

- Table shows summary of $\Delta\text{SES}/\text{SES}$ uncertainty (due to syst. uncertainty sources) \rightarrow SES statistical uncertainty of 2.1%

description	contribution
PDG branching fractions and f_s/f_d	8.5%
K^\pm tracking efficiency	5%
vertexing efficiency	2%
K^\pm charge asymmetry. in $B^\pm \rightarrow J/\psi K^\pm$	1%
$B^\pm \rightarrow J/\psi K^\pm$ yield	2.4%
$R_{A\epsilon}$	6.9%
total (comb. in quadrature)	12.5%

- contributions from backgrounds:
 - background interpolation from sidebands \rightarrow 4% on Rbkg
 - $B \rightarrow hh'$ negligible
- Mainly contribute: BRref and f_u/f_s , acc-vs-eff ratio (data-MC discrepancies), K tracking efficiency

$B_s \rightarrow \mu^+ \mu^-$ UPPER LIMIT EXTRACTION

CLs method with profile likelihood function

$$\mathcal{L} = \text{Poisson}(N_{SR}^{obs} | \epsilon \mathcal{B} + N_{bkg} + N_{B \rightarrow hh}) \text{Poisson}(N_{bkg,SB}^{obs} | R_{bkg} N_{bkg}) \times$$

$$\text{Gauss}(\epsilon^{obs} | \epsilon, \sigma_\epsilon) \text{Gauss}(R_{bkg}^{obs} | R_{bkg}, \sigma_{R_{bkg}})$$

$$\epsilon = 1/\text{SES}$$

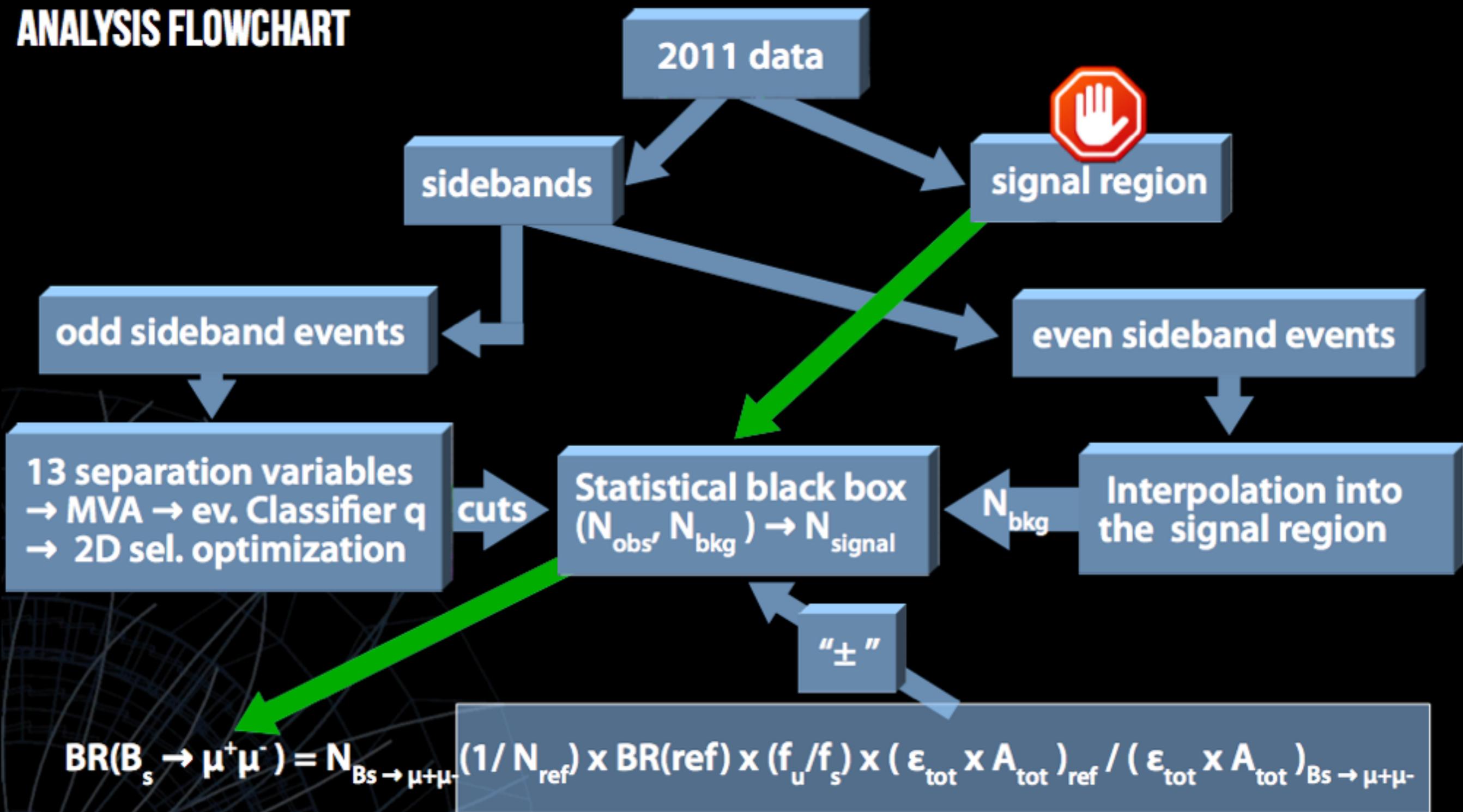
$$R = \Delta_{SB} / \Delta_{SR}$$

- the expected UL is calculated assuming the number of events in the signal region as the number of expected events obtained from the sideband interpolation (6.75 events):
- peeking background negligible, but included in the optimization procedure and in the upper limit calculation

quantity	value
$N_{J/\psi K^\pm}$	$15\,214 \pm 1.10\% \pm 2.39\%$
$R_{A\epsilon}$	$0.267 \pm 1.8\% \pm 6.9\%$
SES	$(2.07 \pm 0.26) \cdot 10^{-9}$
R_{bkg}^{obs}	1.240 ± 0.050
$N_{SR}^{exp} N_{SR}^{obs}$	6.75 6
$N_{bkg,SB}^{obs}$	8
$N_{B \rightarrow hh}$	0.30

$B_s \rightarrow \mu^+ \mu^-$ ANALYSIS FLOWCHART

ANALYSIS FLOWCHART



$B_D \rightarrow K^* (\rightarrow K^+ \pi^-) \mu^+ \mu^-$ BASELINE CUTS

Anna Usanova

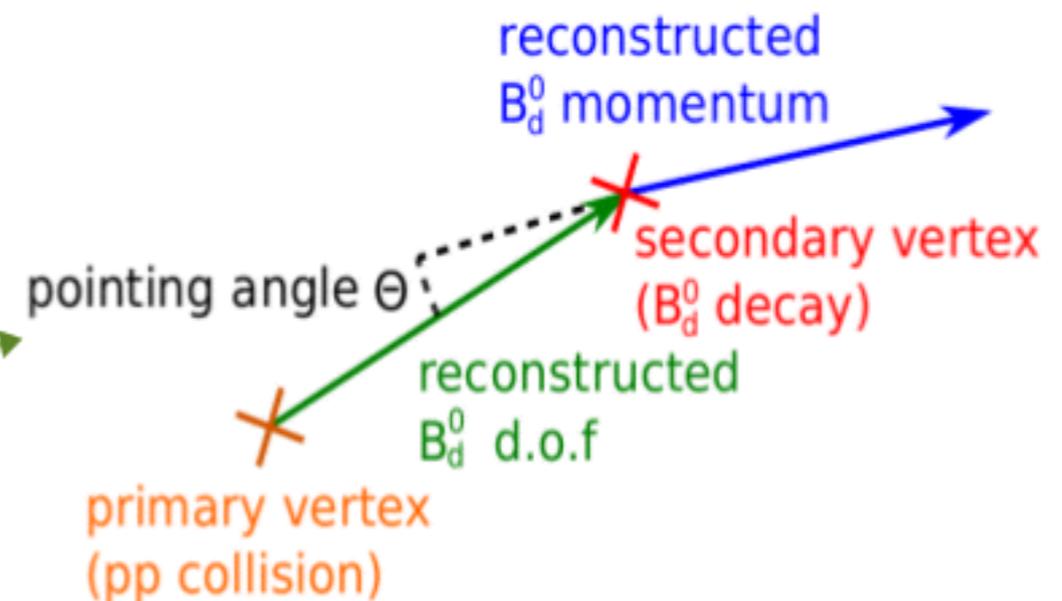
- Baseline:

- $p_T(\mu) > 3.5$ GeV
- $|\eta| < 2.5$ for all tracks
- $\chi^2/n.d.f(\mu\mu) < 10$
- $846 < M(K^{*0}) < 946$ MeV
- $p_T(K) > 0.5$ GeV
- $p_T(\pi) > 0.5$ GeV

- $J/\psi, \Psi'(2S)$ regions are excluded

- Selection (cut values are optimized):

- $\tau/\Delta\tau(B_d) > 12.75$
- $\cos(\theta) > 0.999$
- $\chi^2/n.d.f.(B_d) < 2.0$
- $p_T(K^*) > 3$ GeV
- $|(M(B^0)_{rec} - M(B^0)_{PDG})| - |(M(\mu\mu)_{rec} - M(J/\psi)_{PDG})| > 130$ MeV



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$B_D \rightarrow K^* (\rightarrow K^+ \pi^-) \mu^+ \mu^-$ FIT STRATEGY

- Extended unbinned maximum likelihood fit (performed sequentially):
 - 1) mass ($K\pi\mu\mu$) distribution fitted to separate signal and background yields
 - 2) mass-angular simultaneous fit performed on the signal events from the previous fit (fixed mass)
- Done separately for each of the 6 q^2 bins
- The procedure checked to give the same results as single-step fit except the lowest q^2 bin (included in systematics there).

$$\mathcal{M}_{\text{sig}}(m_i, \delta m_i) = \frac{1}{\sqrt{2\pi} s_m \delta m_i} \exp\left(\frac{-(m_i - m_{B_D^0})^2}{2(s_m \delta m_i)^2}\right)$$

$$\mathcal{L} = \prod_{i=1}^N \left[N_{\text{sig}} \cdot \mathcal{M}_{\text{sig}}(m_i, \delta m_i) + N_{\text{bckg}} \cdot \mathcal{M}_{\text{bckg}}(m_i) \right], \quad \mathcal{M}_{\text{bckg}}(m_i) = e^{-\lambda \cdot m_i}$$

$B_D \rightarrow K^* (\rightarrow K^+ \pi^-) \mu^+ \mu^-$ FIT STRATEGY

- Angular fit (in each q^2 bin):
$$\mathcal{L} = \prod_{i=1}^N [N_{\text{sig}}^{\text{fix}} \cdot \mathcal{M}_{\text{sig}}(m_i, \delta_{m_i} | \text{fixed}) \cdot \mathcal{A}_{L,\text{sig}}(\cos \theta_{L,i}) \cdot \alpha_L(\cos \theta_{L,i}) \cdot \mathcal{A}_{K,\text{sig}}(\cos \theta_{K,i}) \cdot \alpha_K(\cos \theta_{K,i}) + N_{\text{bckg}}^{\text{fix}} \cdot \mathcal{M}_{\text{bckg}}(m_i | \text{fixed}) \cdot \mathcal{A}_{L,\text{bckg}}(\cos \theta_{L,i}) \cdot \mathcal{A}_{K,\text{bckg}}(\cos \theta_{K,i})]$$

- Signal PDFd:
$$\mathcal{A}_{L,\text{sig}}(\cos \theta_{L,i}) = \frac{3}{4} F_L(q^2) (1 - \cos^2 \theta_{L,i}) + \frac{3}{8} (1 - F_L(q^2)) (1 + \cos^2 \theta_{L,i}) + A_{FB}(q^2) \cos \theta_{L,i}$$

$$\mathcal{A}_{K,\text{sig}}(\cos \theta_{K,i}) = \frac{3}{2} F_L(q^2) \cos^2 \theta_{K,i} + \frac{3}{4} (1 - F_L(q^2)) (1 - \cos^2 \theta_{K,i})$$

- Background PDF – linear combination of Chebyshev polynomials (to 2nd order)

$$\mathcal{A}_{L(K),\text{bkg}} = 1 + p_{1L(K)} \cos \theta_{L(K),i} + p_{2L(K)} (2 \cos^2 \theta_{L(K),i} - 1)$$

- detector and selection effects on the angular shapes taken into account via the acceptance functions $\alpha_L(\cos \theta_{L,i}), \alpha_K(\cos \theta_{K,i})$

$B_D \rightarrow K^* (\rightarrow K^+ \pi^-) \mu^+ \mu^-$ SYSTEMATIC

- Ranges of the mass fit region
 - Differ in q^2 bins due to ΔM cut effect
- Angular background shapes
 - Varied between 2nd and 3rd Chebyshev polynomials
- Contribution of $B_{\pm} \rightarrow \mu^+ \mu^- K_{\pm}$ events
 - estimated by removing potential $B_{\pm} \rightarrow \mu^+ \mu^- K_{\pm}$ candidates
- Angular acceptance effects
 - Mainly from limited MC statistics
 - Various signal angular shapes tested
- Sequential fitting approach
 - Non-negligible effect only in $2.00 < q^2 < 4.30 \text{ GeV}^2$ bin due to low statistics

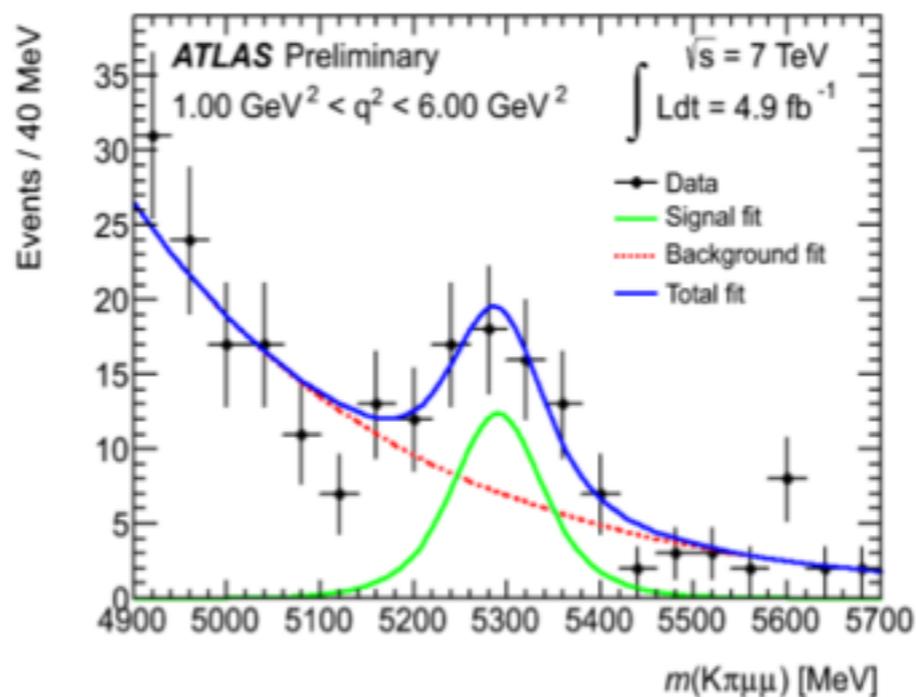
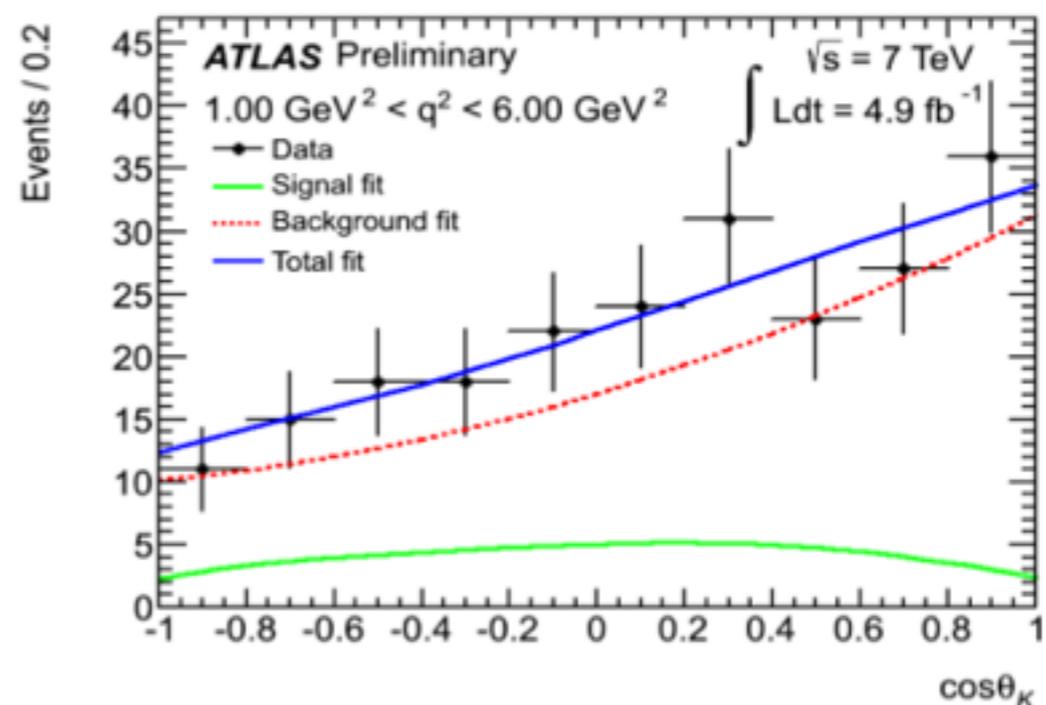
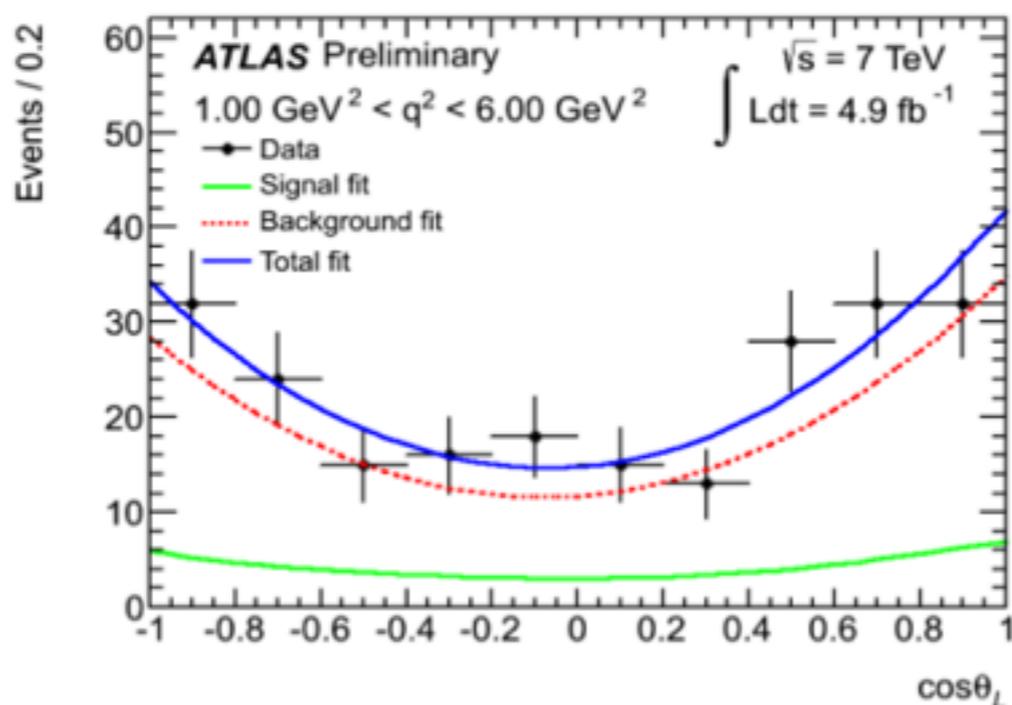
Negligible sources:

- Contribution from S-wave ($B_D \rightarrow K^+ \pi^- \mu^+ \mu^-$)
- Contribution from $B_S \rightarrow \Phi (\rightarrow K^+ K^-) \mu^+ \mu^-$
- Background mass shape
- Possible bias due to angular fit approach (neglecting correlation)

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$B_D \rightarrow K^* (\rightarrow K^+ \pi^-) \mu^+ \mu^-$ LIKELIHOOD FIT - OTHER BINS

$1.00 < q^2 < 6.00$



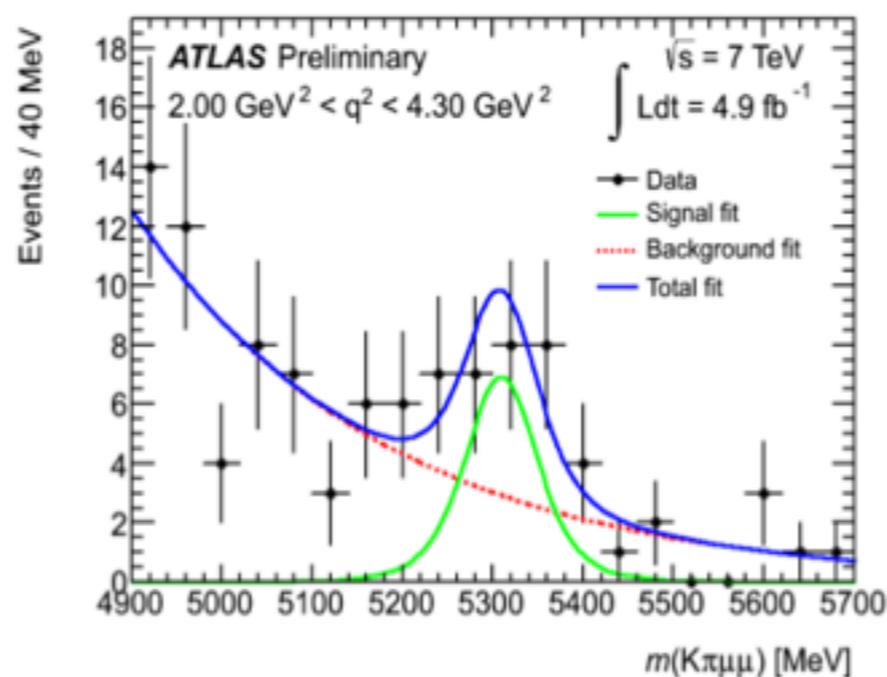
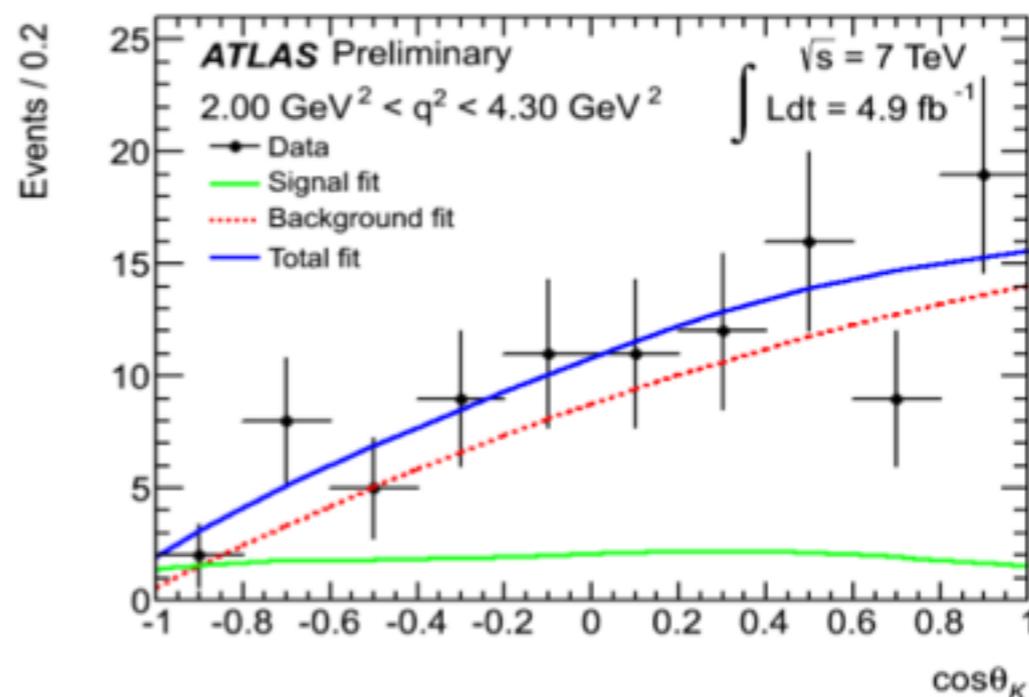
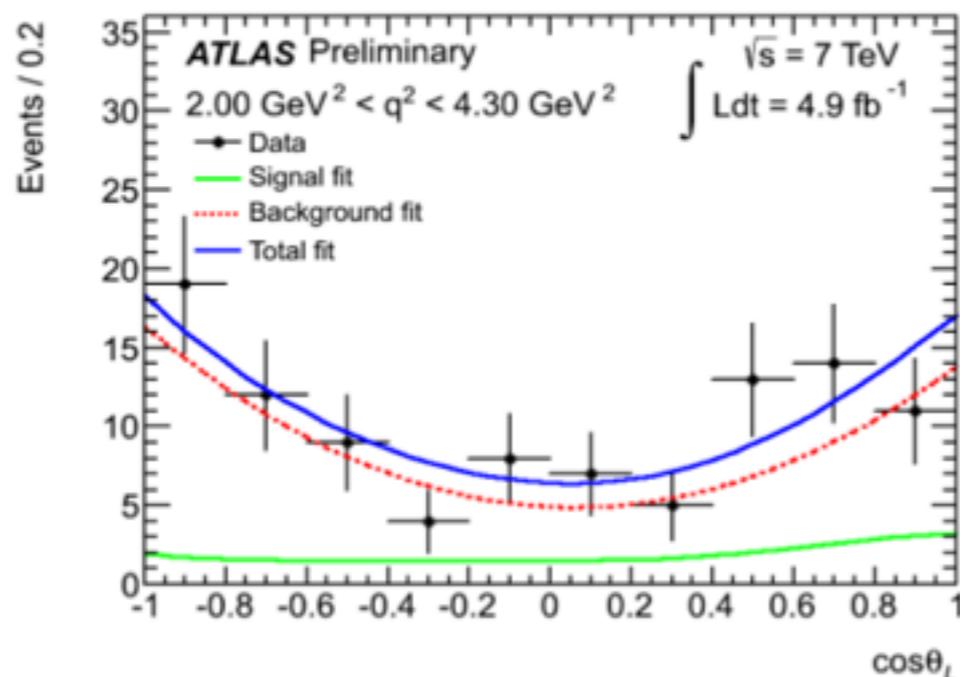
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$B_D \rightarrow K^* (\rightarrow K^+ \pi^-) \mu^+ \mu^-$ LIKELIHOOD FIT - OTHER BINS

$2.00 < q^2 < 4.30$



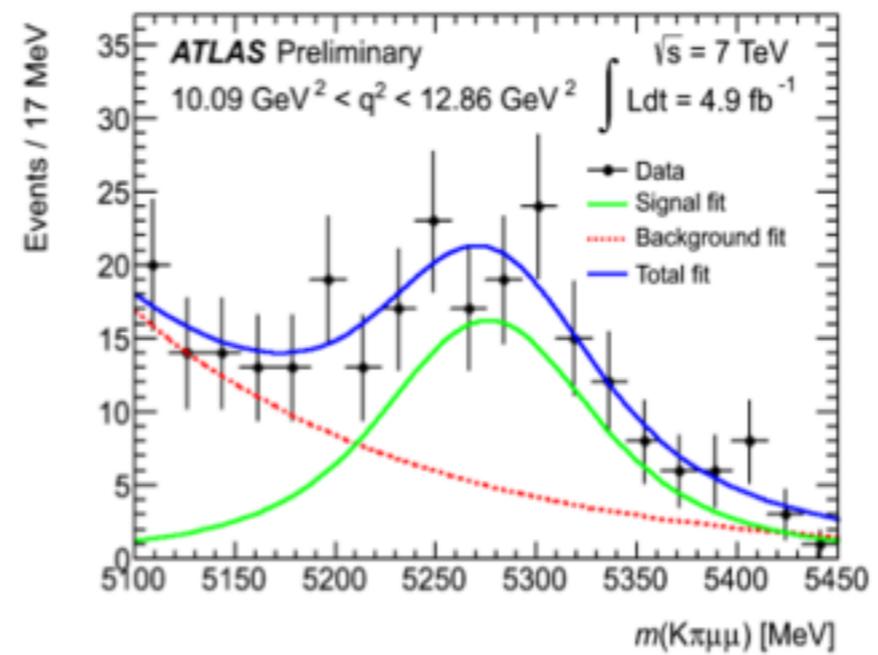
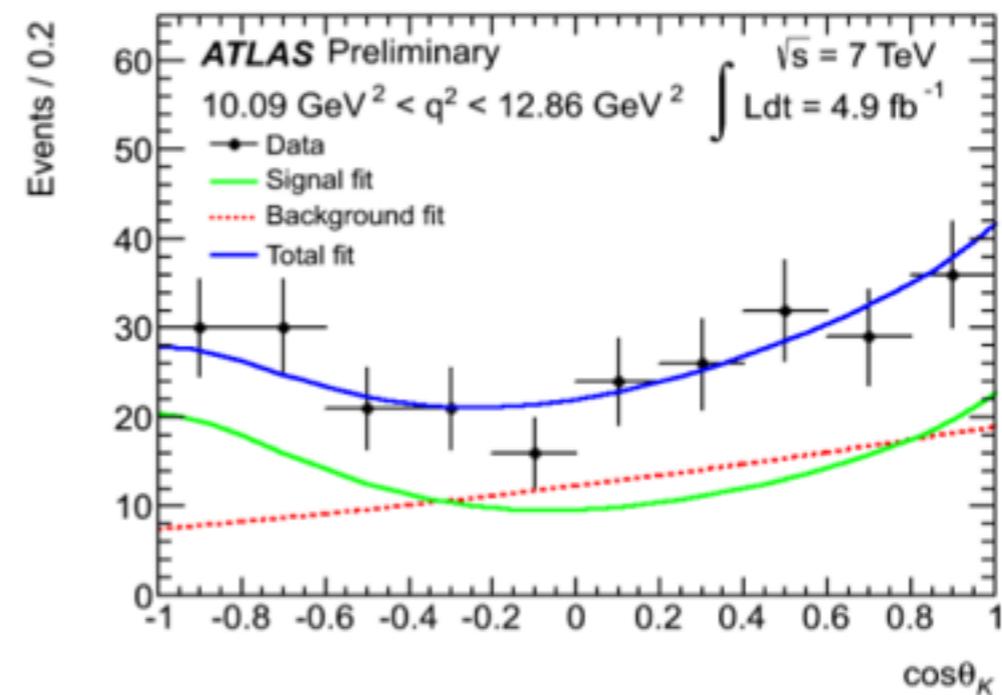
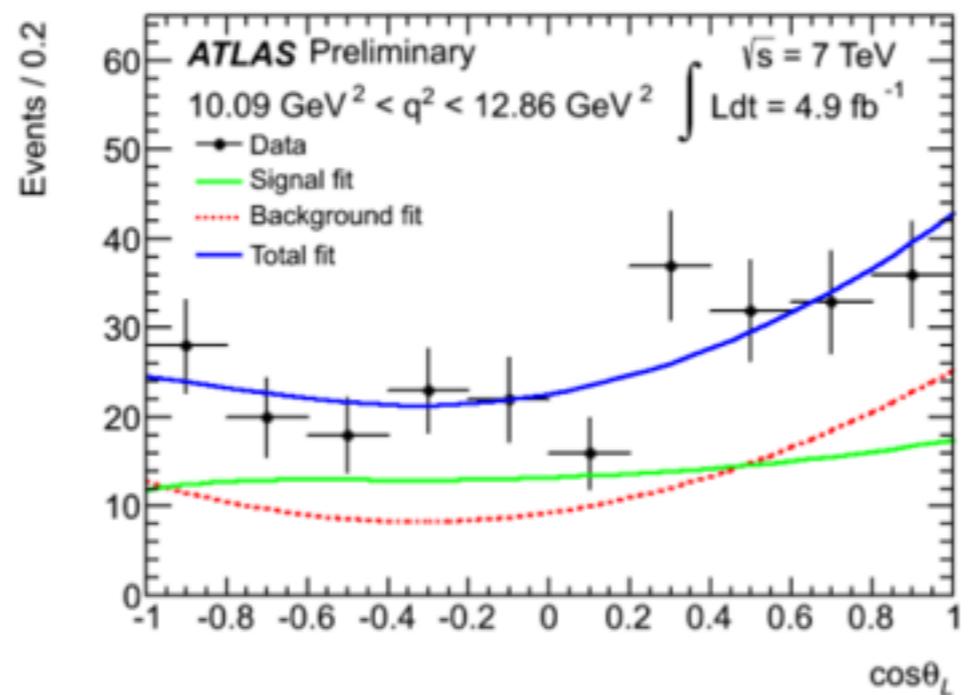
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$B_D \rightarrow K^* (\rightarrow K^+ \pi^-) \mu^+ \mu^-$ LIKELIHOOD FIT - OTHER BINS

$10.09 < q^2 < 12.86$

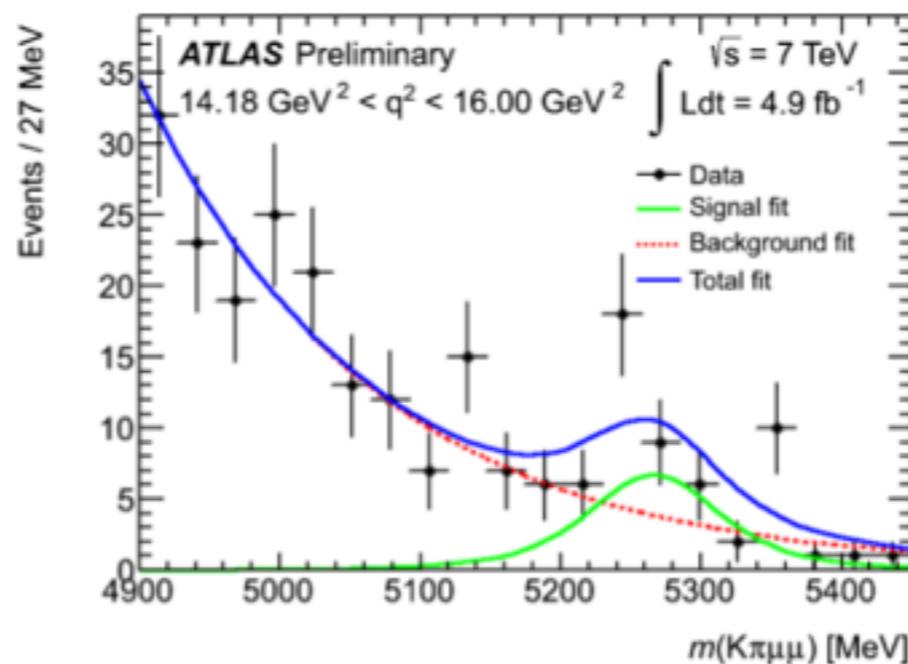
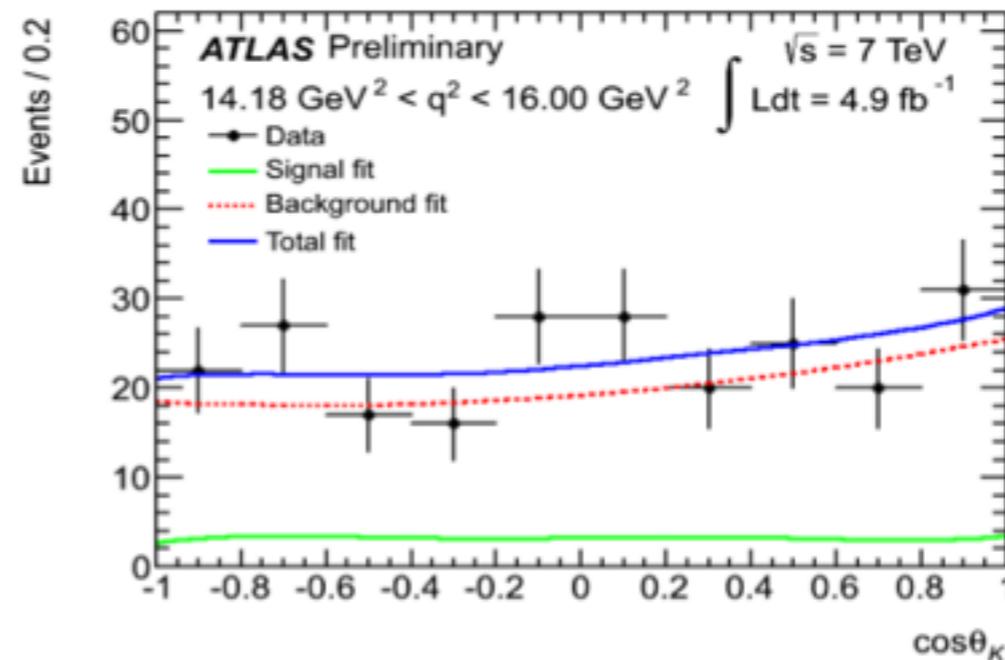
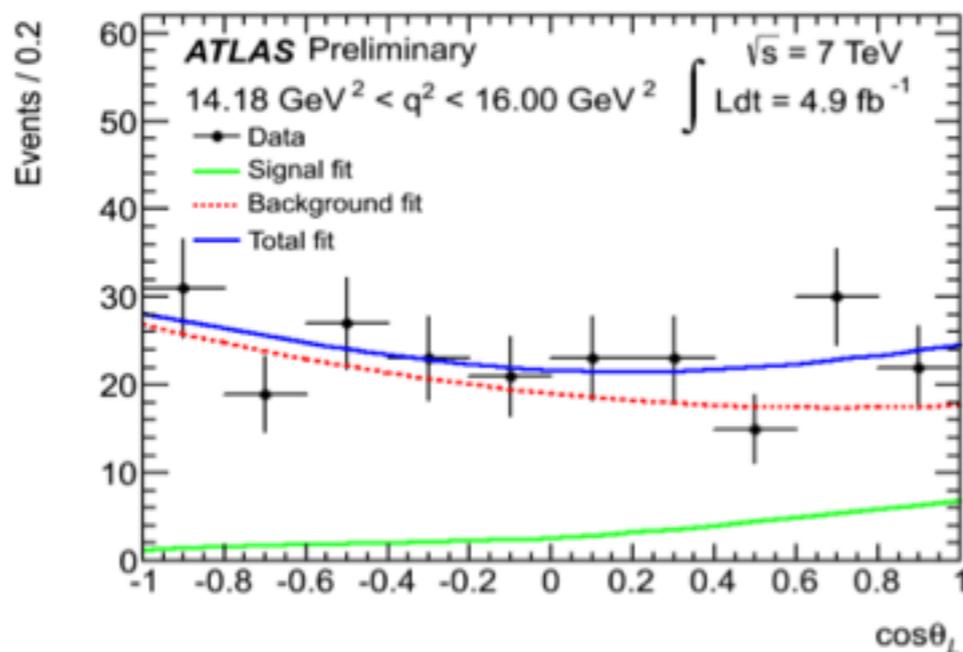


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$B_D \rightarrow K^* (\rightarrow K^+ \pi^-) \mu^+ \mu^-$ LIKELIHOOD FIT - OTHER BINS

$14.18 < q^2 < 16.00$



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