

# New boundaries for the "ppK<sup>-</sup>" production in p+p collisions

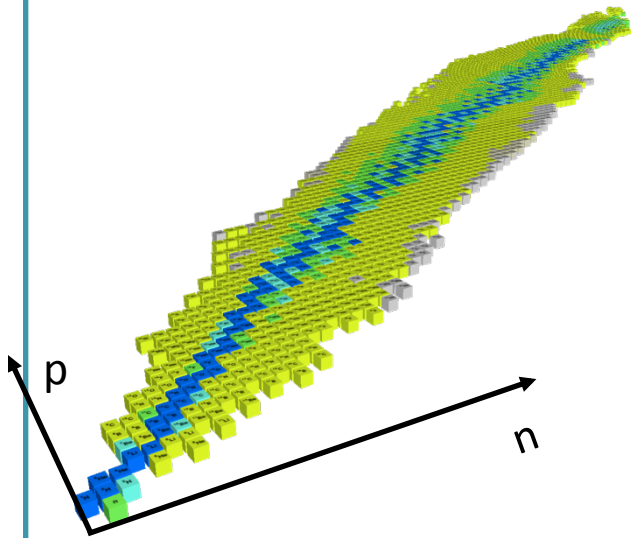
Eliane Epple  
for the HADES collaboration

Mo., 2.6.2014

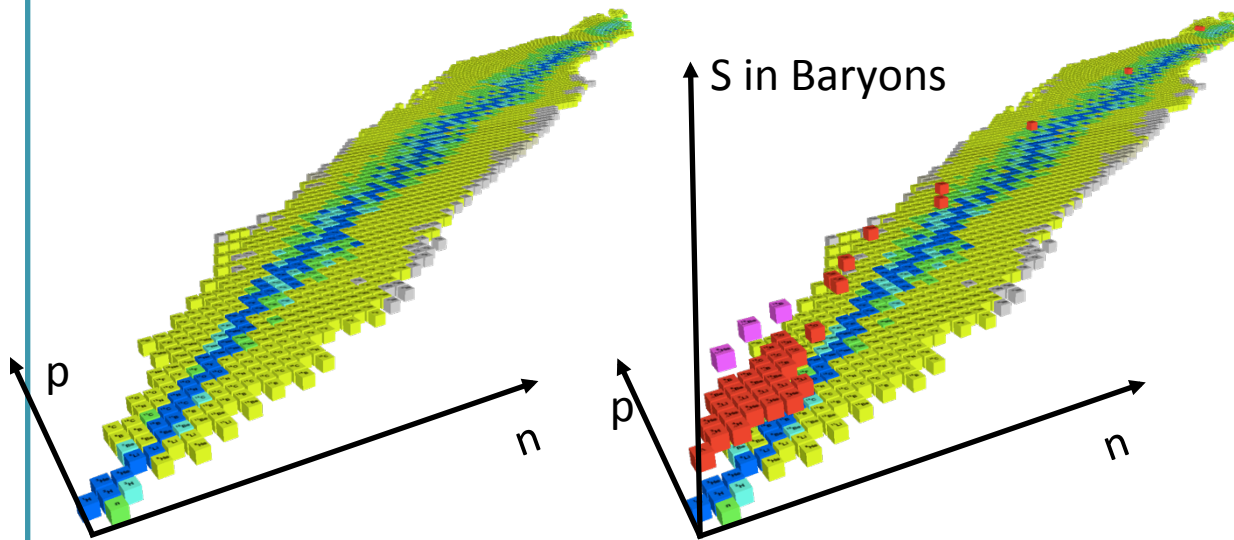


- Introduction
- Data
- Hypothesis Tests
- Conclusions

# Bound Objects



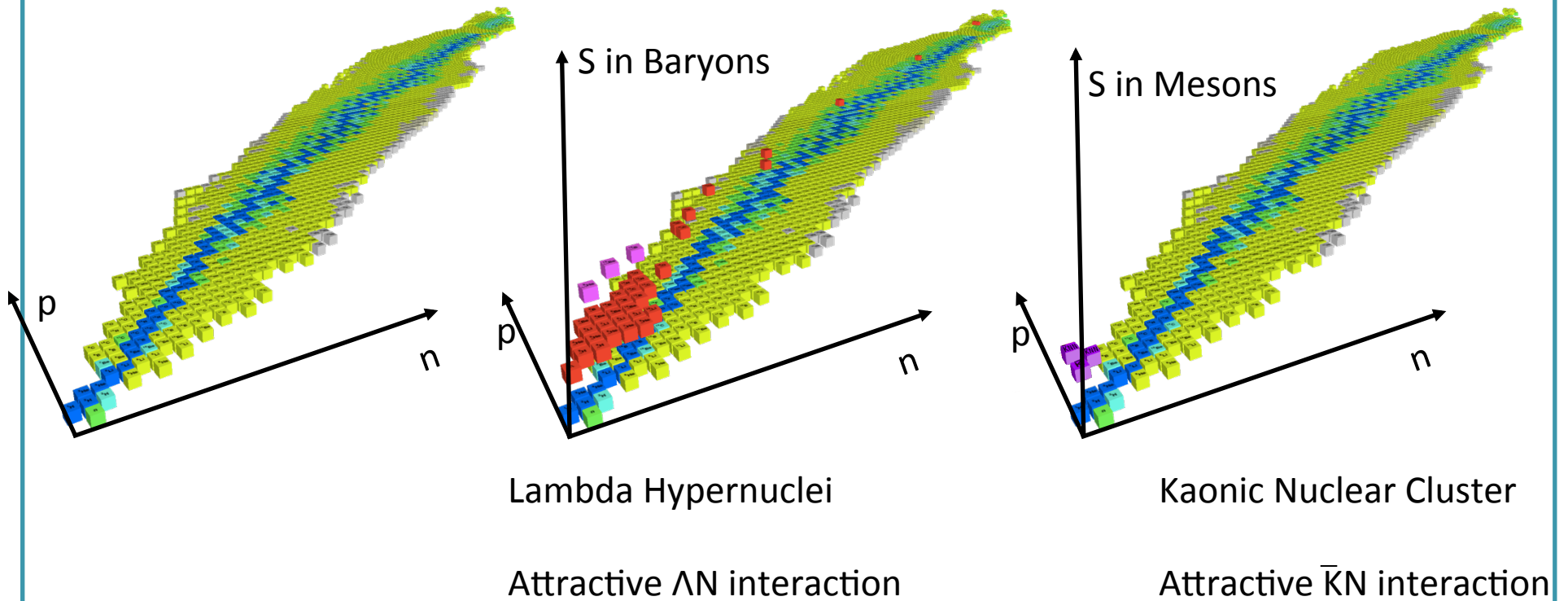
# Bound Objects



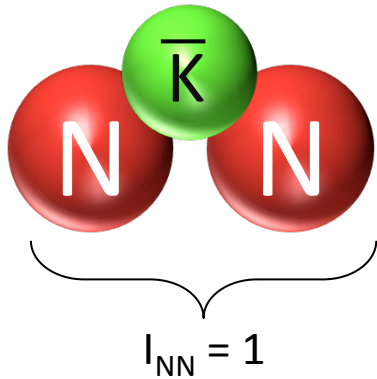
Lambda Hypernuclei

Attractive  $\Lambda N$  interaction

# Bound Objects

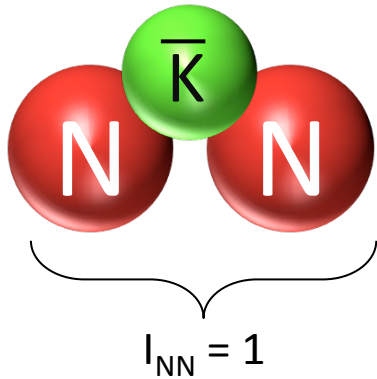


# The Smallest Cluster



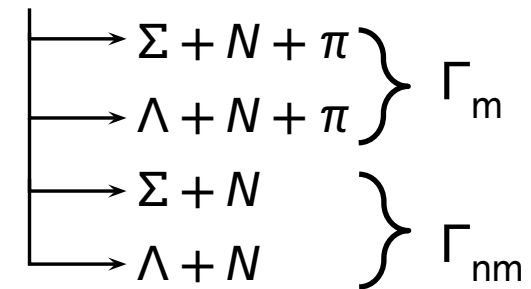
Property	Value
charge	+1
strangeness	-1
participants	$ppK^-$ , $pn\bar{K}^0$
$J^P$	$0^-$

# The Smallest Cluster

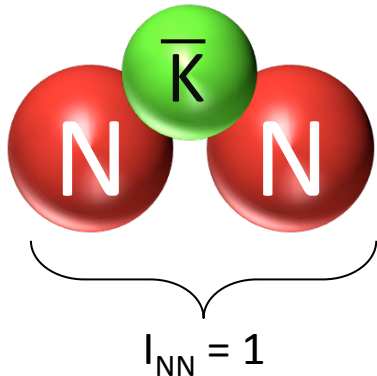


Property	Value
charge	+1
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participants	$ppK^-, pn\bar{K}^0$
$J^P$	$0^-$

$\bar{K}NN$

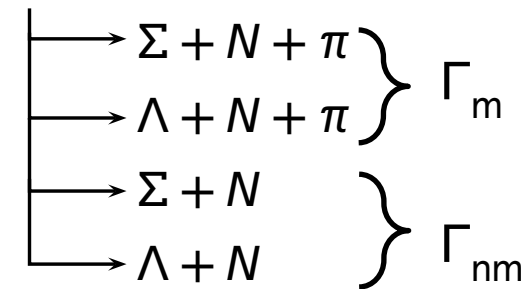


# The Smallest Cluster



Property	Value
charge	+1
strangeness	-1
participants	$ppK^-$ , $pn\bar{K}^0$
$J^P$	$0^-$

$\bar{K}NN$



Chiral, energy dependent

	var. [DHW09, DHW08]	Fad. [BO12b, BO12a]	var. [BGL12]	Fad. [IKS10]	Fad. [RS14]
$BE$	17–23	26–35	16	9–16	32
$\Gamma_m$	40–70	50	41	34–46	49
$\Gamma_{nm}$	4–12	30			

Non-chiral, static calculations

	var. [YA02, AY02]	Fad. [SGM07, SGMR07]	Fad. [IS07, IS09]	var. [WG09]	var. [FIK+11]
$BE$	48	50–70	60–95	40–80	40
$\Gamma_m$	61	90–110	45–80	40–85	64–86
$\Gamma_{nm}$	12			~20	~21

**Binding Energy (BE):**

10-100 MeV

**Mesonic Decay ( $\Gamma_m$ )**

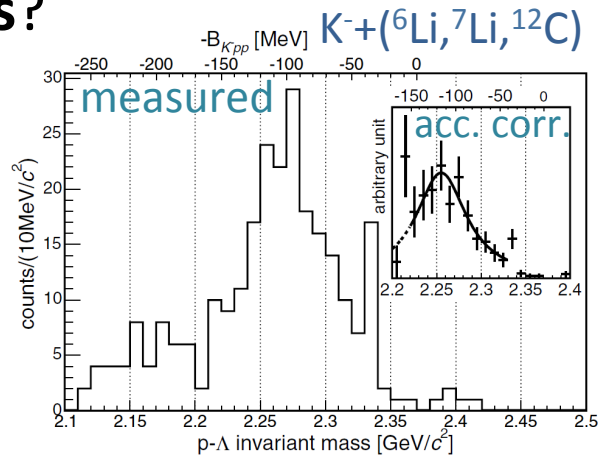
30-110 MeV

**Non-Mesonic Decay ( $\Gamma_{nm}$ )**

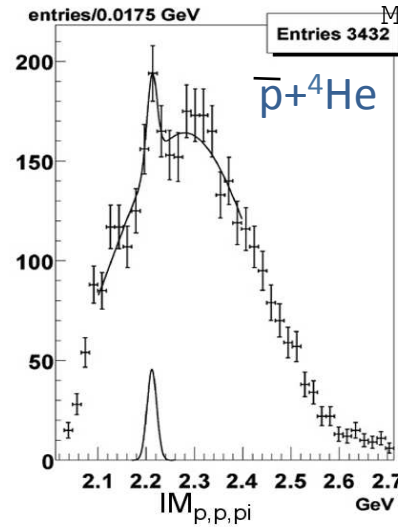
4-30 MeV

# Is there a $\bar{K}NN$ ?

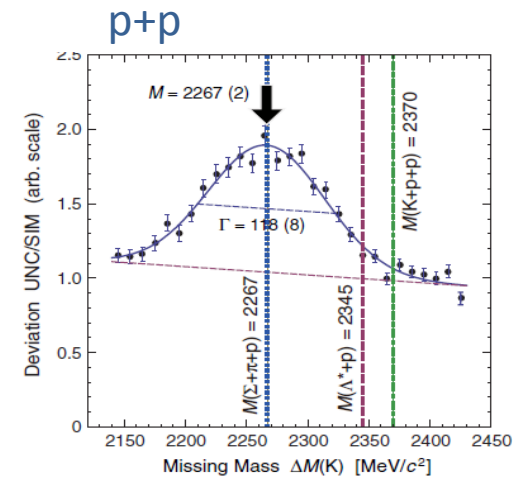
## Hints?



M. Agnello et al. Phys. Rev. Lett. **94** (2005)



T. Yamazaki et al. Phys. Rev. Lett. **104**, (2010);  
M. Maggiora et al. Nucl. Phys. **A 835** (2010)

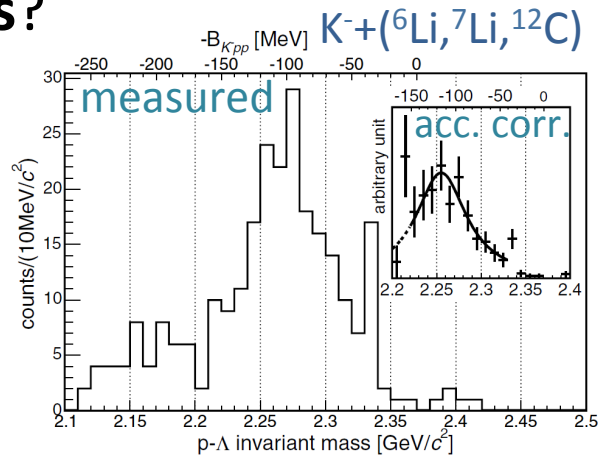


G. Bendiscioli et al. Nucl. Phys., **A 789** (2007)  
G. Bendiscioli et al. Eur.Phys.J., **A 40** (2009)

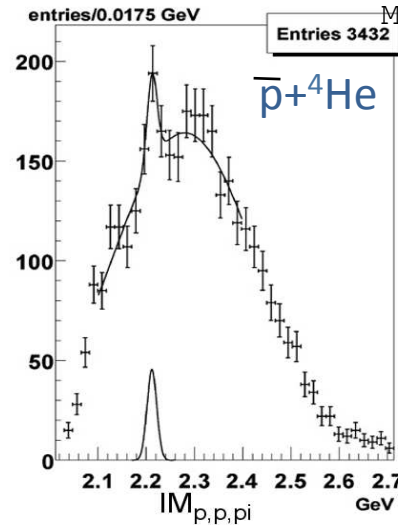


# Is there a $\bar{K}NN$ ?

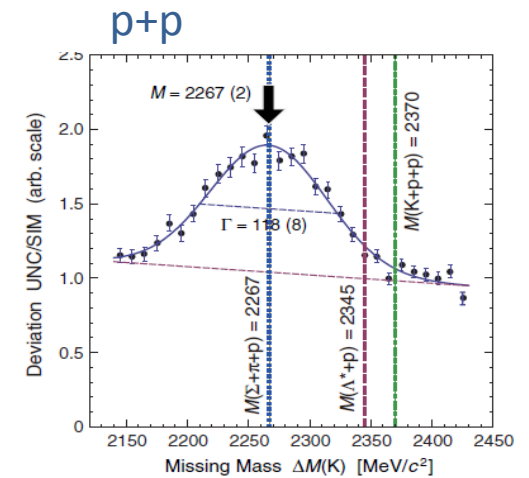
## Hints?



M. Agnello et al. Phys. Rev. Lett. **94** (2005)



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G. Bendiscioli et al. Nucl. Phys., **A 789** (2007)  
G. Bendiscioli et al. Eur.Phys.J., **A 40** (2009)



$$M(ppK^-) = 2.267 \text{ GeV}/c^2$$

$$B(ppK^-) = 103 \text{ MeV}$$

$$\Gamma(ppK^-) = 118 \text{ MeV}/c^2$$



$$M(ppK^-) = 2.212 \text{ GeV}/c^2$$

$$B(ppK^-) = 158 \text{ MeV}$$

$$\Gamma(ppK^-) = <24.4 \text{ MeV}/c^2$$



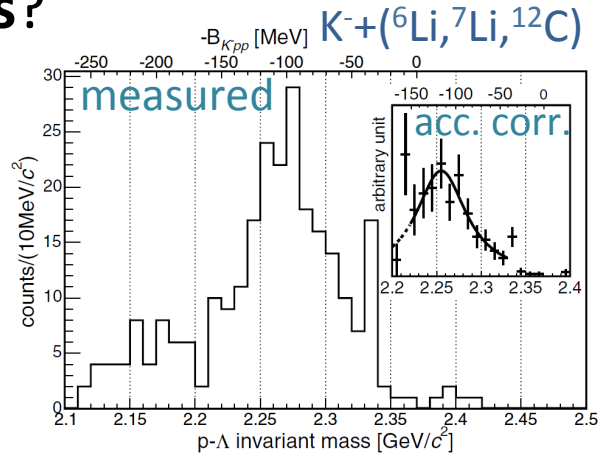
$$M(ppK^-) = 2.255 \text{ GeV}/c^2$$

$$B(ppK^-) = 115 \text{ MeV}$$

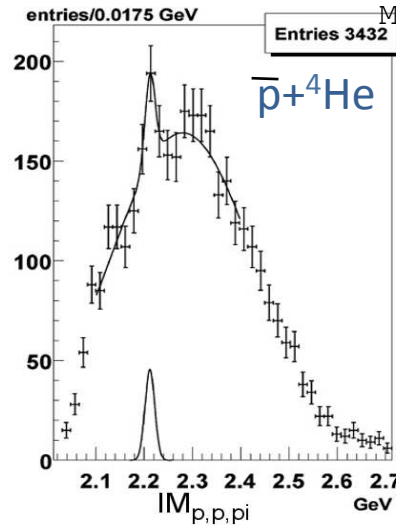
$$\Gamma(ppK^-) = 67 \text{ MeV}/c^2$$

# Is there a $\bar{K}NN$ ?

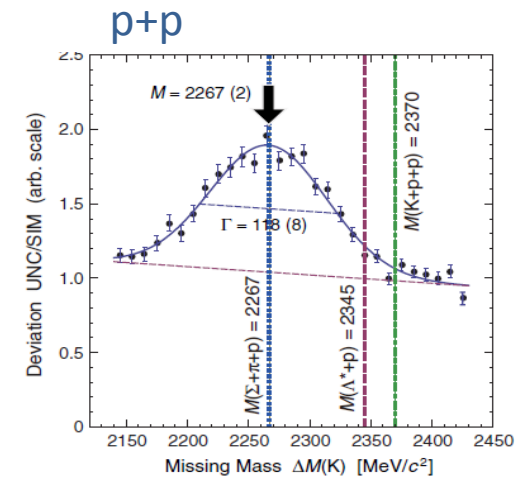
## Hints?



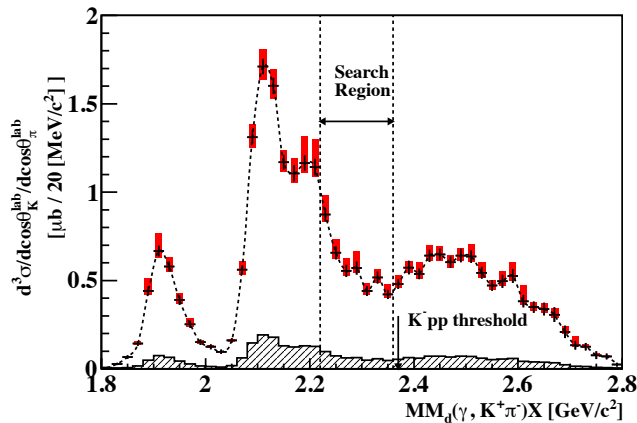
M. Agnello et al. Phys. Rev. Lett. **94** (2005)



T. Yamazaki et al. Phys. Rev. Lett. **104**, (2010);  
M. Maggiora et al. Nucl. Phys. **A 835** (2010)

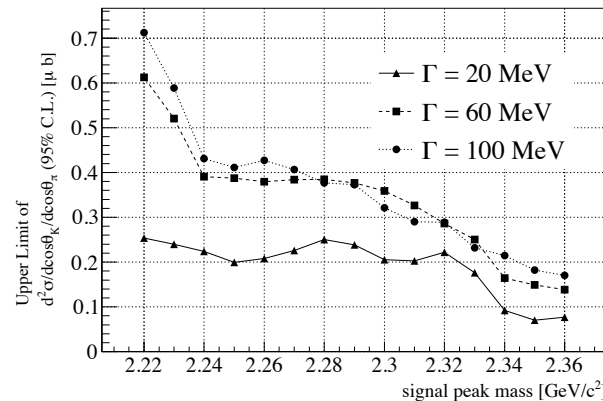


## Exclusions



G. Bendiscioli et al. Nucl. Phys., **A 789** (2007)

G. Bendiscioli et al. Eur.Phys.J., **A 40** (2009)

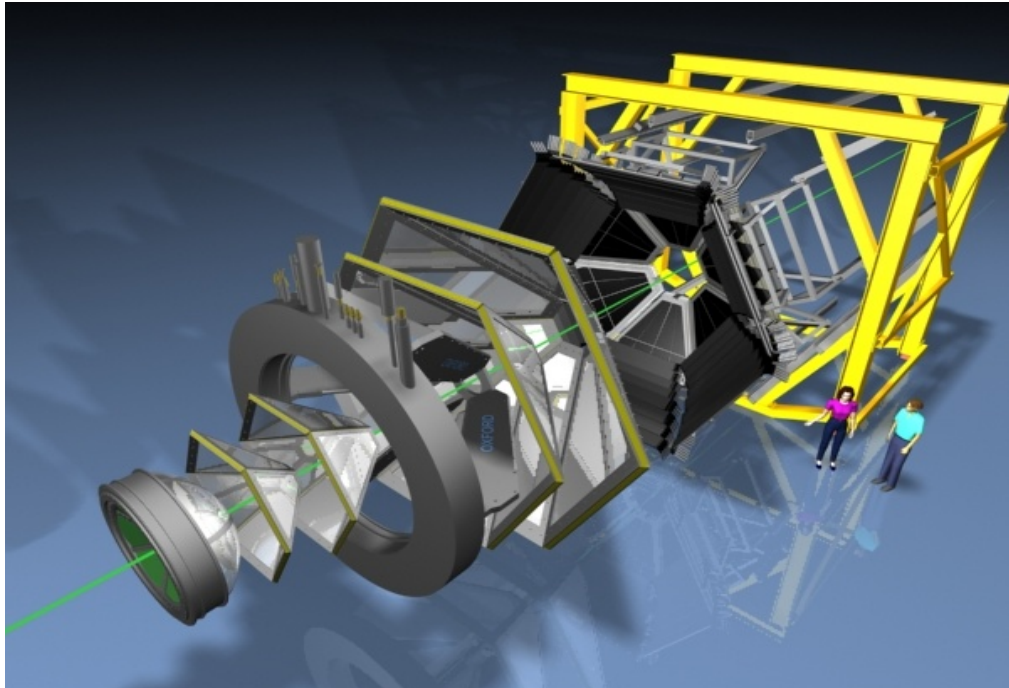


A.O. Tokiyasu et al. Phys.Lett. **B728** 616-621 (2014)

0.5-5% of the cross section of typical hadron photo-production

# The HADES experiment

High Acceptance Di-electron Spectrometer  
GSI, Darmstadt



Accelerator  
SIS18 at GSI  
Colliding system  
p+p at 3.5GeV

HADES Coll. (G. Agakishiev et al.),  
Eur. Phys. **J.** **A41** (2009)

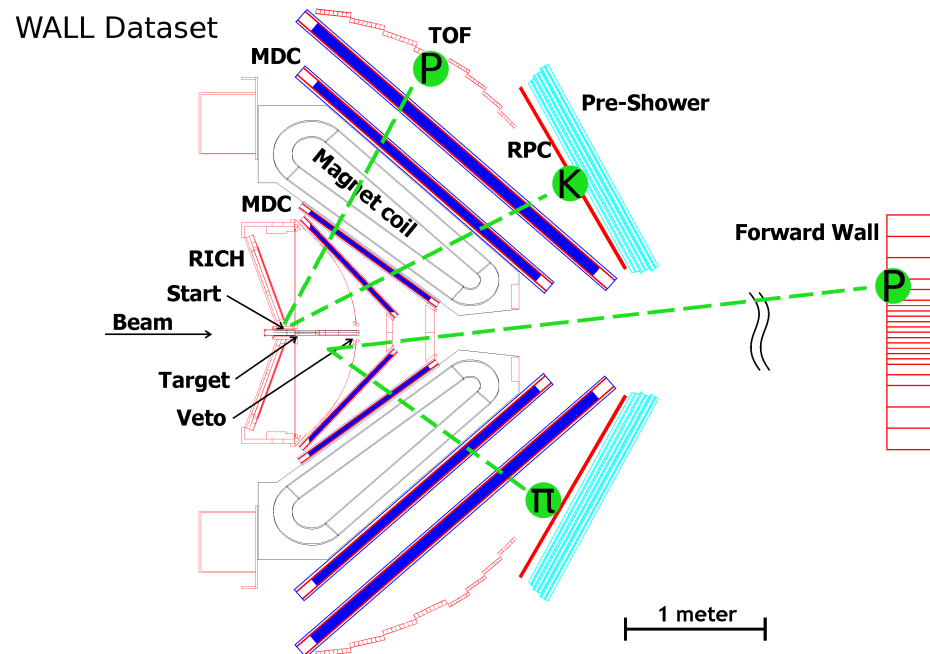
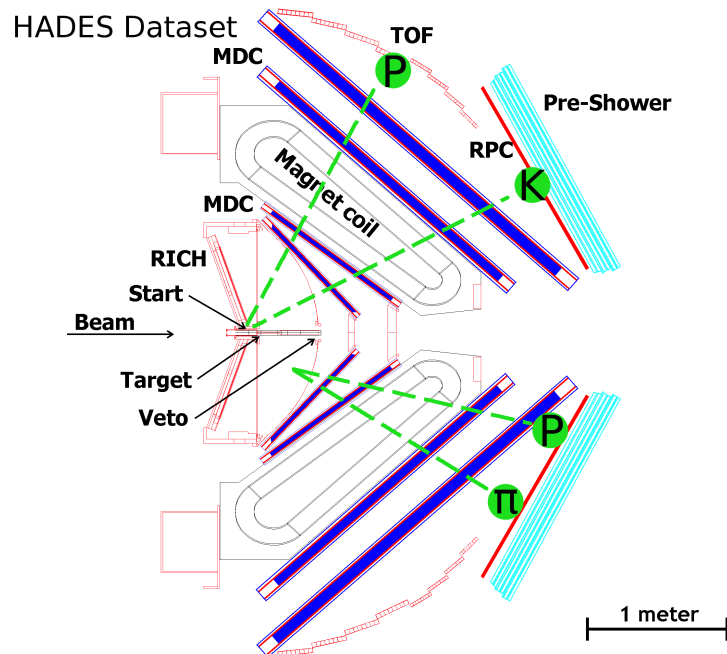
- Fixed-target experiment
- Full azimuthal coverage,  $15^\circ$  -  $85^\circ$  in polar angle
- Momentum resolution  $\approx 1\%$  -  $5\%$

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# The Data

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# Data Sample



## HADES data

13,000 events of  $pK^+\Lambda$   
 Background from wrong PID  $\approx 6\%$   
 Background from  $pK^+\Sigma^0$   $\approx 1\%$

## WALL data

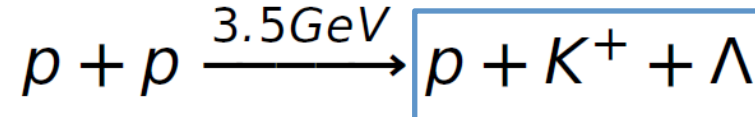
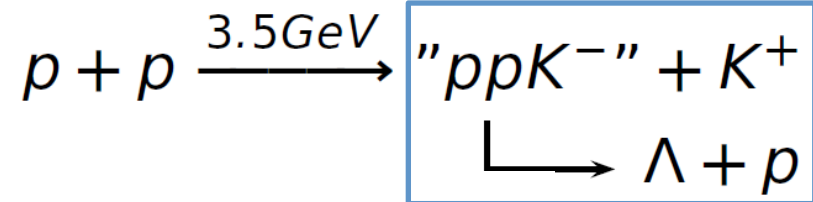
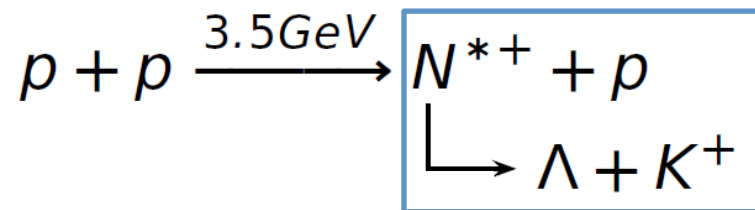
8000 events of  $pK^+\Lambda$   
 Background from wrong PID  $\approx 11.7\%$   
 Background from  $pK^+\Sigma^0$   $\approx 3\%$

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# A Model for the Process

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# Bonn-Gatchina PWA



<http://pwa.hiskp.uni-bonn.de/>

A.V. Anisovich, V.V. Anisovich, E. Klempt, V.A. Nikonov and A.V. Sarantsev  
Eur. Phys. J. A 34, 129152 (2007)

## What we included to model the $PK^+\Lambda$ process:

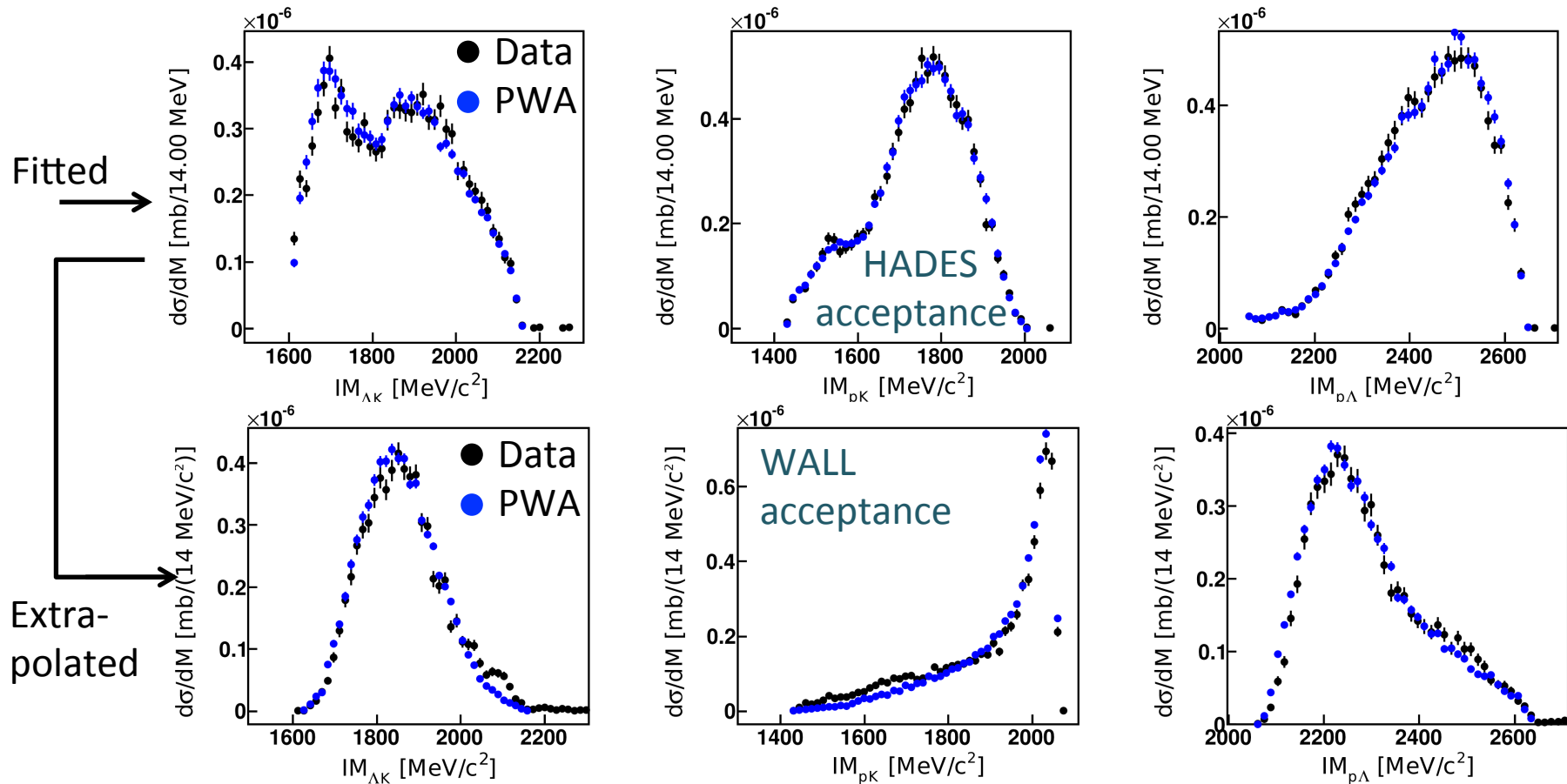
$N^*$  Resonances in the PDG with measured decay into  $K^+\Lambda$

$N(1650)$ ,  $N(1710)$ ,  $N(1720)$ ,  $N(1875)$ ,  $N(1880)$ ,  $N(1895)$ ,  $N(1900)$

Non-resonant  $PK^+\Lambda$  production waves

Interferences

# The best solution



included resonances:

Non-resonant waves:

$N(1650)$ ,  $N(1710)$ ,  $N(1720)$ ,  $N(1900)$ ,  $N(1895)$

$(pL)(^1S_0) - K$     $(pL)(^3S_1) - K$     $(pL)(^1P_1) - K$

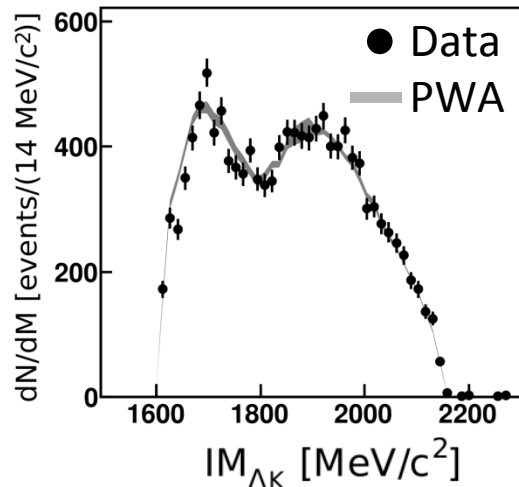
$(pL)(^3P_0) - K$     $(pL)(^3P_2) - K$     $(pL)(^3P_1) - K$

$(pL)(^3D_1) - K$     $(pL)(^1D_2) - K$     $(pL)(^3D_2) - K$

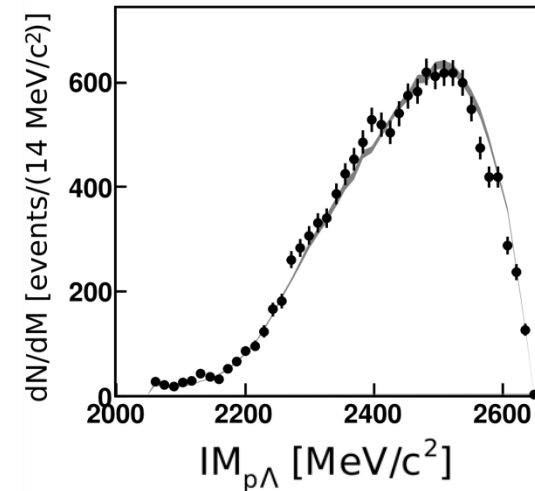
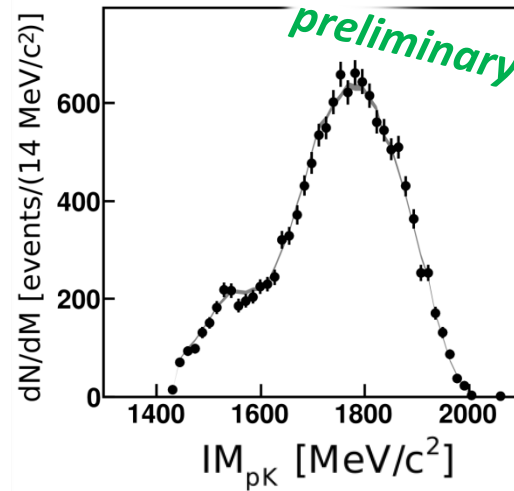


# Four Best PWA Solutions

Inside HADES acceptance

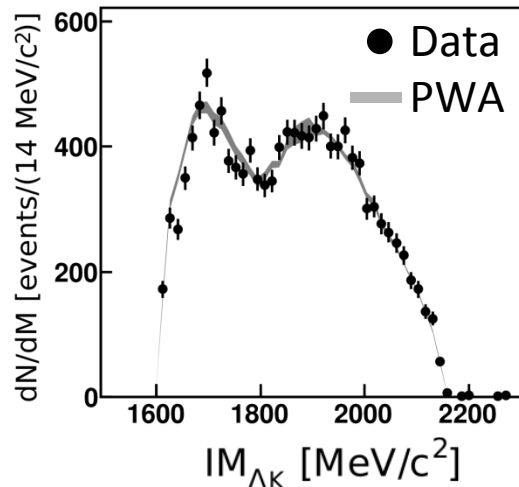


Measured data  
PWA solutions

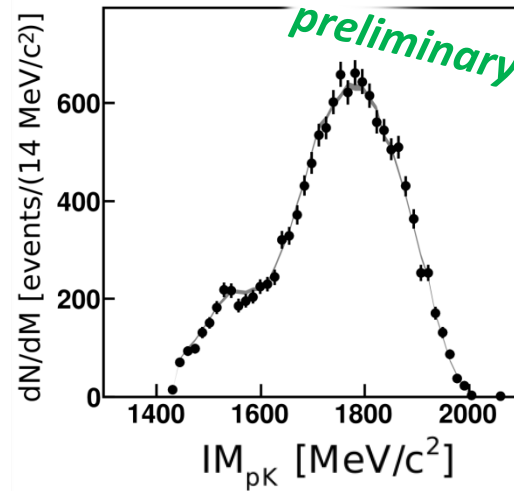


Name	N* combination
1/8	N(1650), N(1710), N(1720), N(1900)
3/8	N(1650), N(1710), N(1720), N(1880)
6/9	N(1650), N(1710), N(1720), N(1900), N(1895)
8/8	N(1650), N(1710), N(1720), N(1895), N(1880)

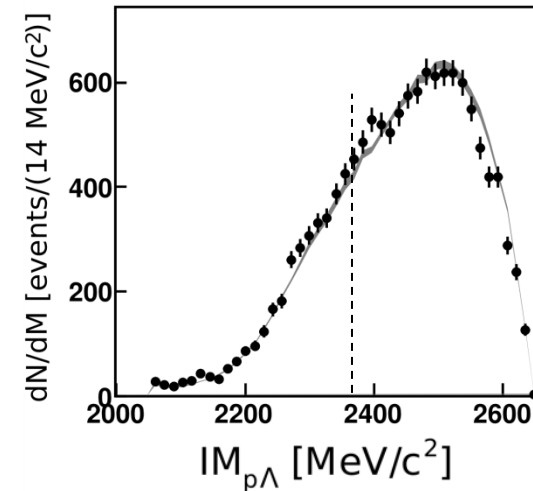
# Four Best PWA Solutions



Measured data  
PWA solutions

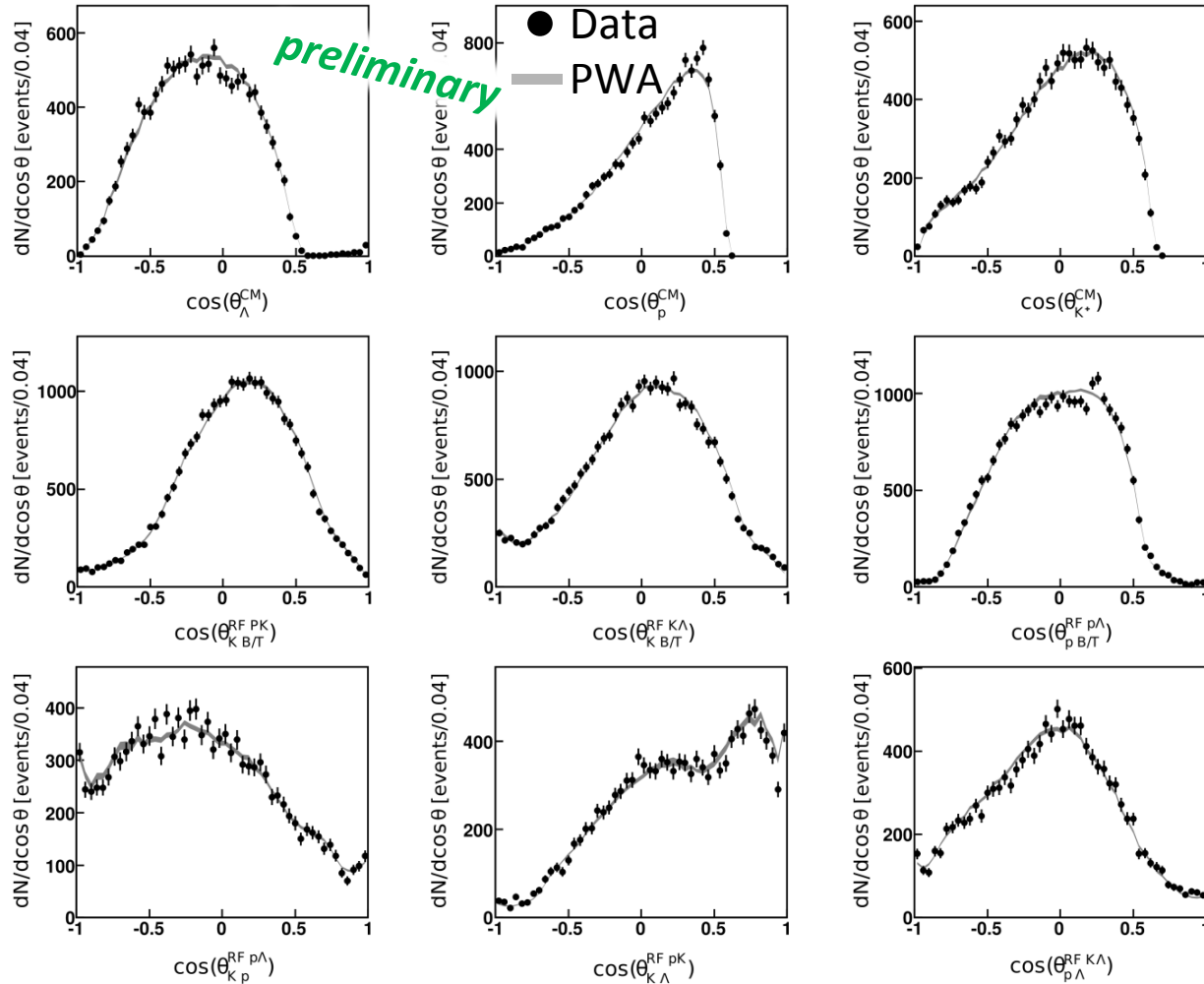


Inside HADES acceptance



mass of  $\Lambda+p = 2053.96 \text{ MeV}/c^2$   
 mass of  $\Sigma^0+p = 2130.82 \text{ MeV}/c^2$   
 mass of  $p+p+K^- = 2370.22 \text{ MeV}/c^2$

# Four Best PWA Solutions



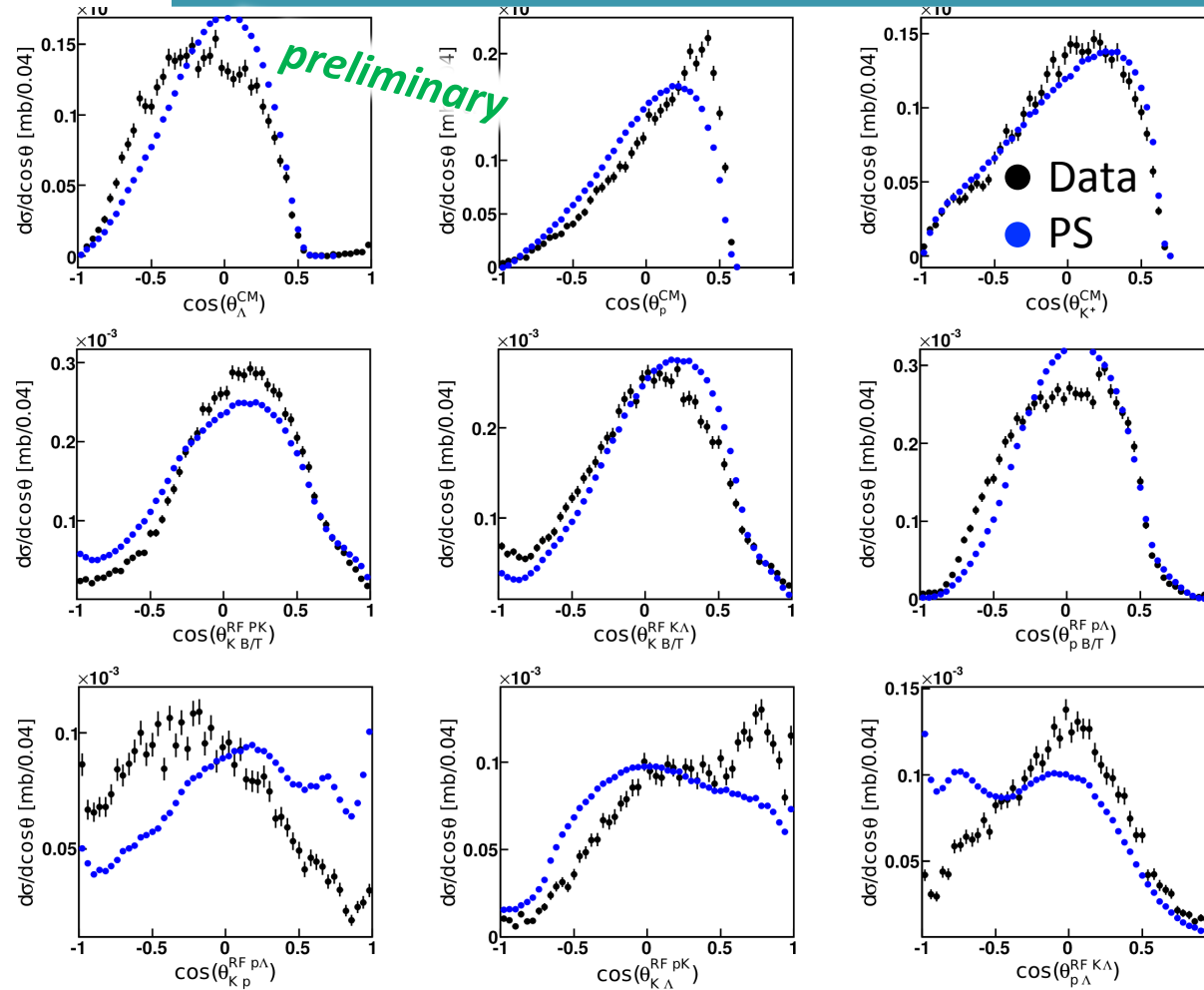
CM Angle

Jackson Angle

Helicity Angle

Measured Data  
PWA solutions  
Inside HADES acceptance

# Phase Space Model



CM Angle

Inside HADES acceptance

Jackson Angle

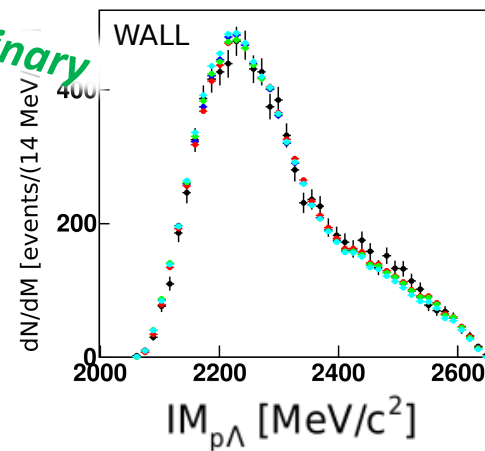
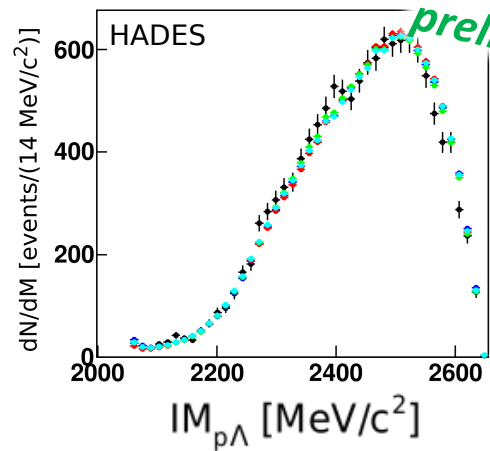
Helicity Angle

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# Test of the Null Hypothesis

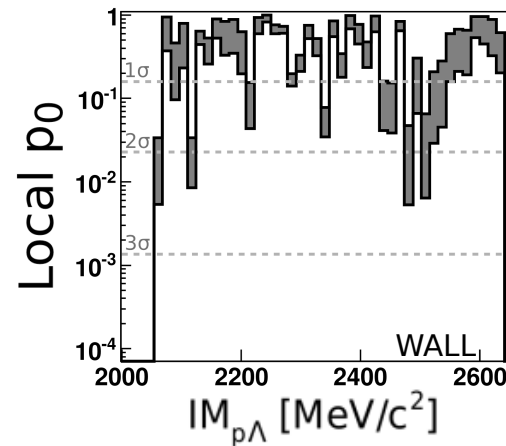
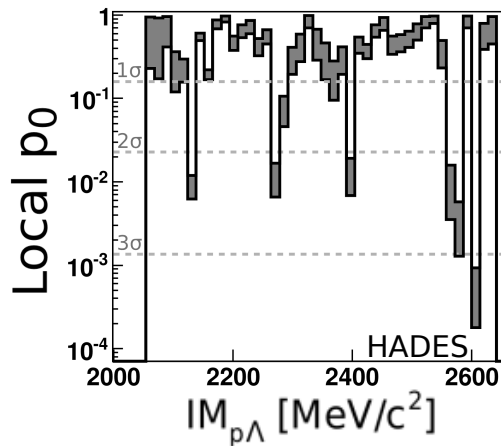
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# Test of the Null Hypothesis



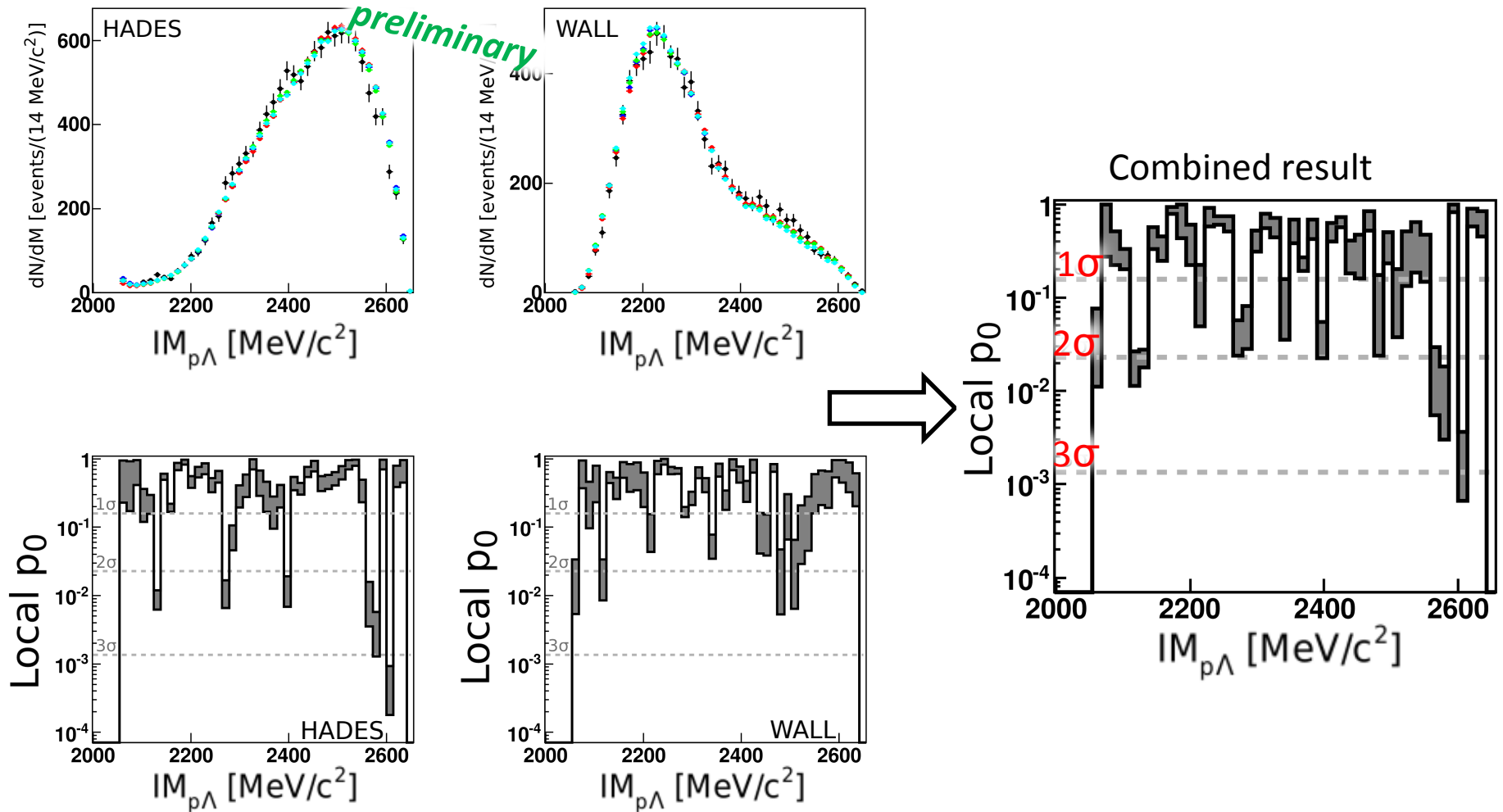
$$\chi_P^2 = \frac{(m - \lambda)^2}{\lambda}$$

$$p - value = \int_{\chi_{P,d}^2}^{\infty} P(\chi^2, Ndf) d\chi^2$$

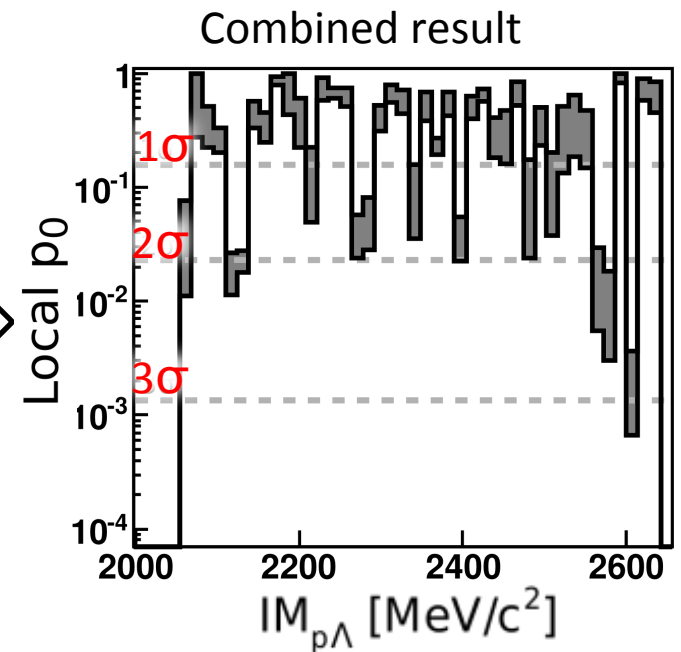
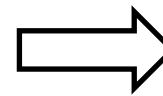
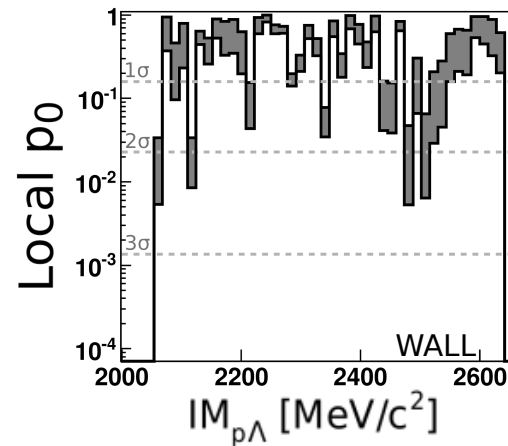
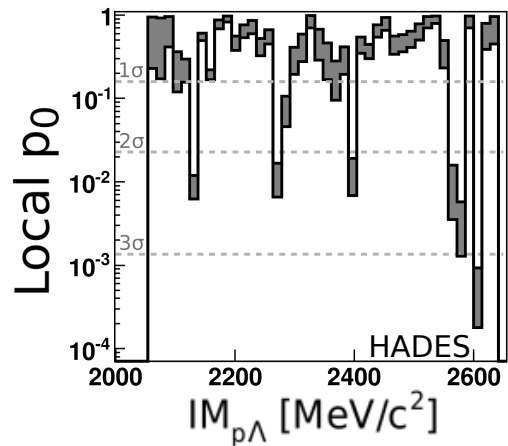
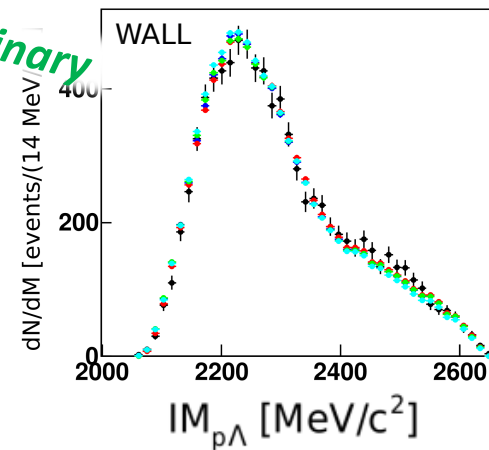
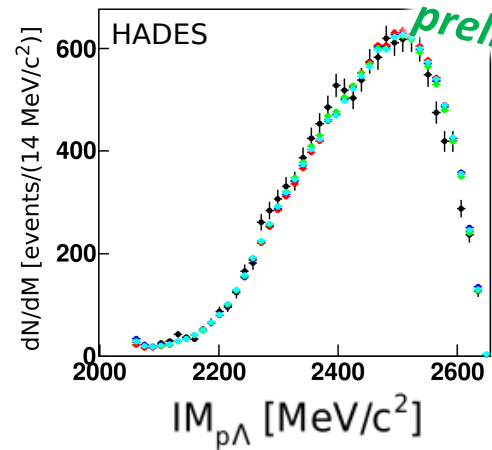


$m_i$  measured events in bin  $i$   
 $\lambda_i$  expected events in bin  $i$   
 according to the model

# Test of the Null Hypothesis



# Test of the Null Hypothesis



We found no new signal in the data

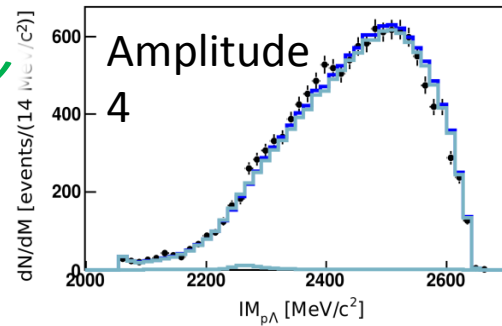
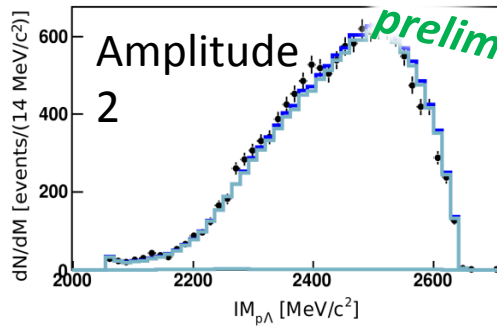


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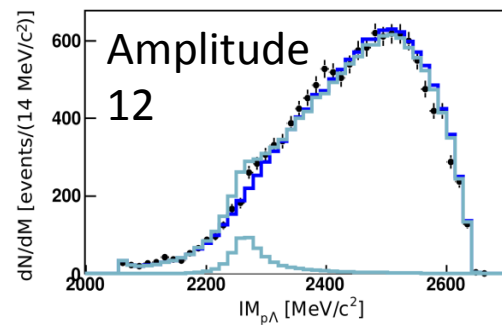
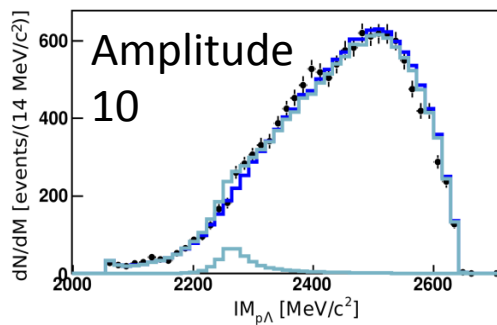
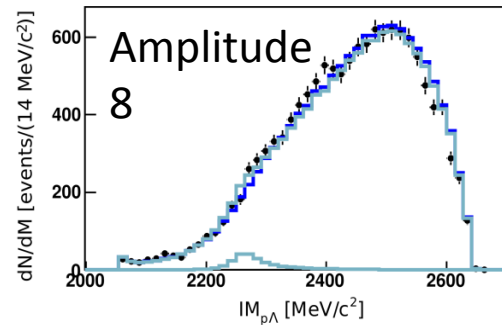
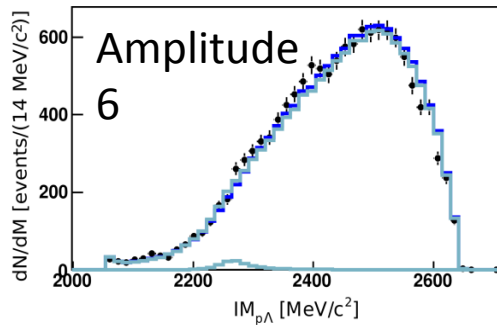
# Test of the Signal Hypothesis

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# Inclusion of a new State

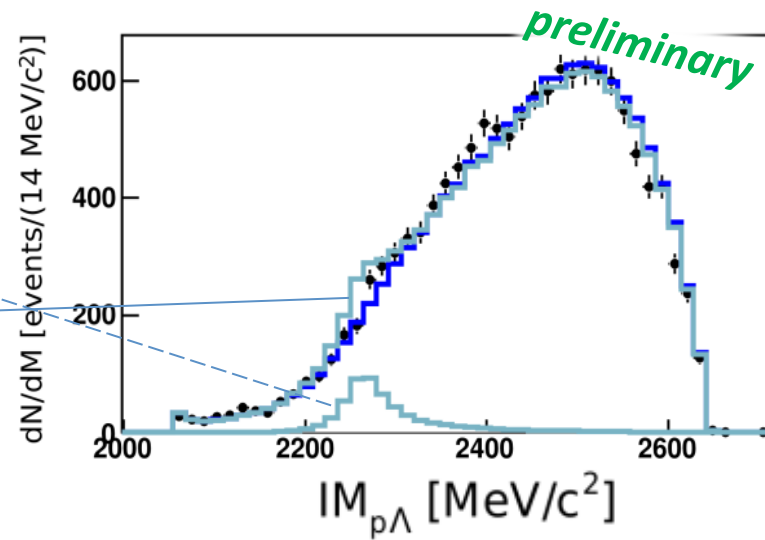
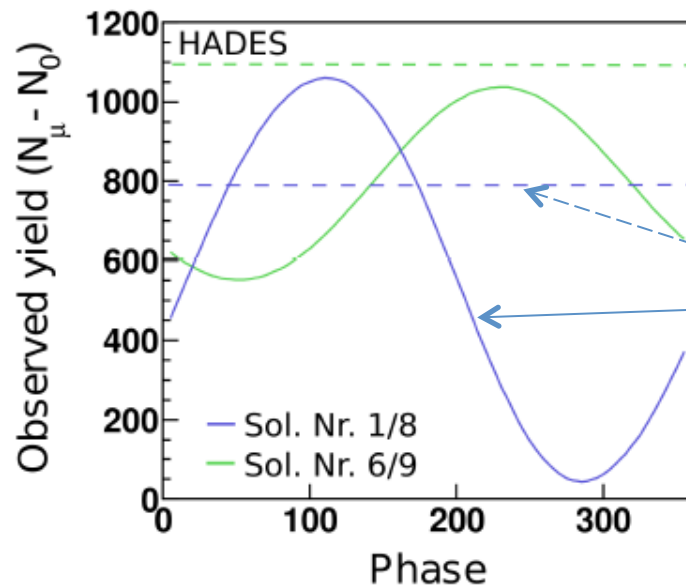


Data Points  
 Null Hypothesis  
 Hypothesis with ppK-



# Feature of a PWA...

... Interferences



The minimum has to be found by the fit

# Upper limit at $CL_s$ 95%

These waves are included into the four best solutions of the PWA

$${}^{2S+1}L_J$$

$$\text{WaveA : } 'p + p' \quad {}^1S_0 \rightarrow 'ppK(2250) - K' \quad {}^1S_0$$

$$\text{WaveB : } 'p + p' \quad {}^3P_1 \rightarrow 'ppK(2250) - K' \quad {}^1P_1$$

$$\text{WaveC : } 'p + p' \quad {}^1D_2 \rightarrow 'ppK(2250) - K' \quad {}^1D_2$$

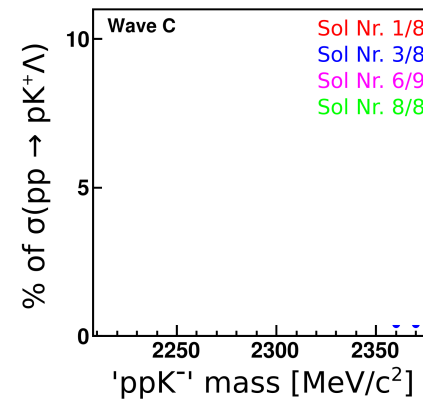
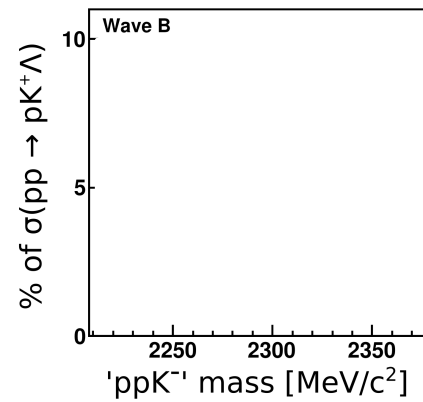
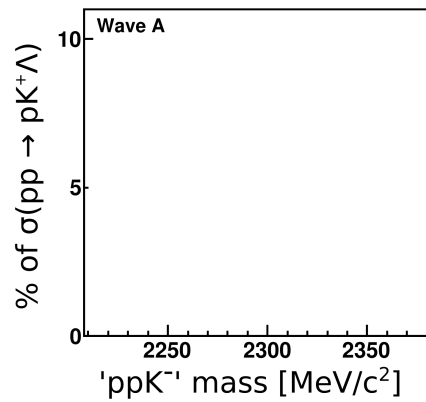
Scanned masses:

2220 – 2370 MeV/c<sup>2</sup> (in steps of 10 MeV/c<sup>2</sup>)

Scanned widths:

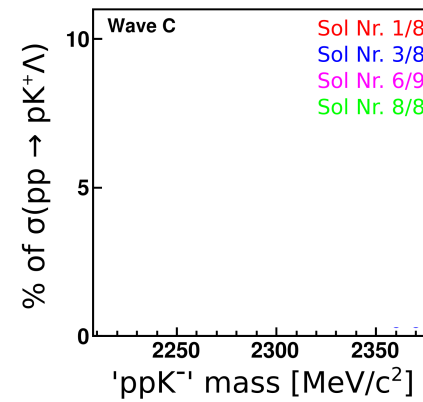
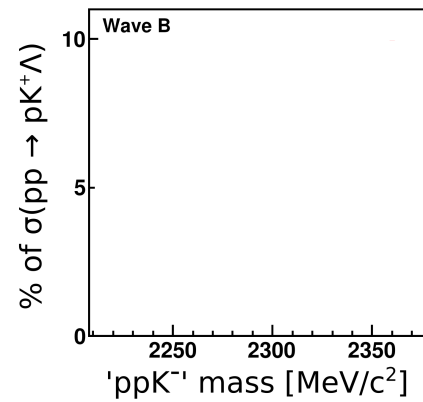
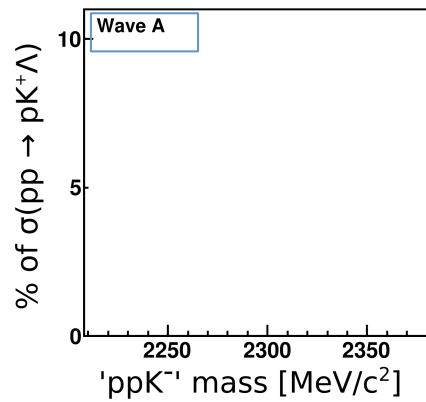
30 MeV, 50 MeV, and 70 MeV

# Upper Limit



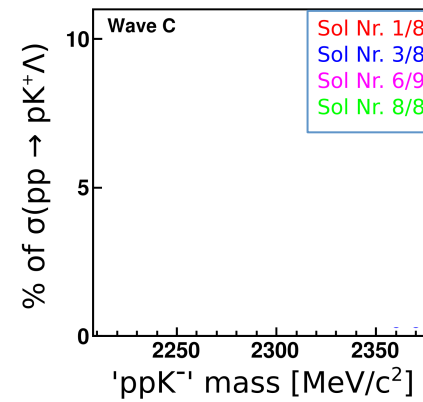
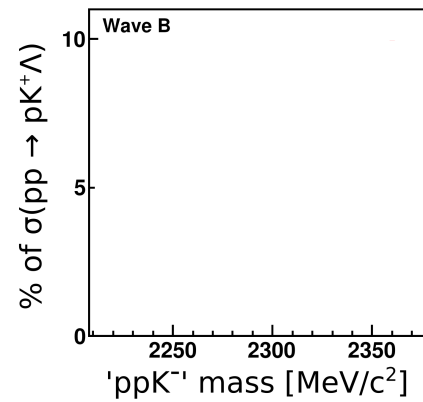
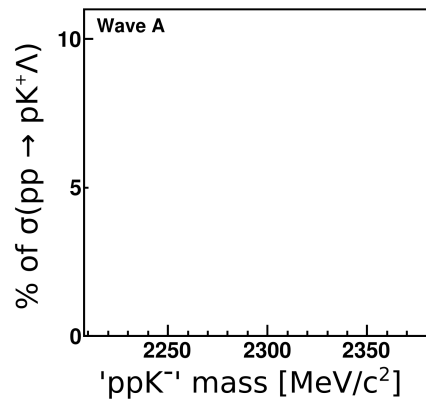
$\Gamma(ppK^-) = 50 \text{ MeV}$

# Upper Limit



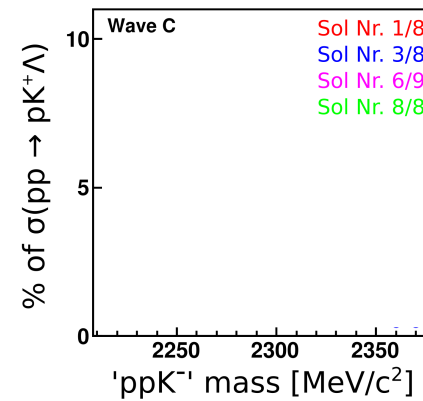
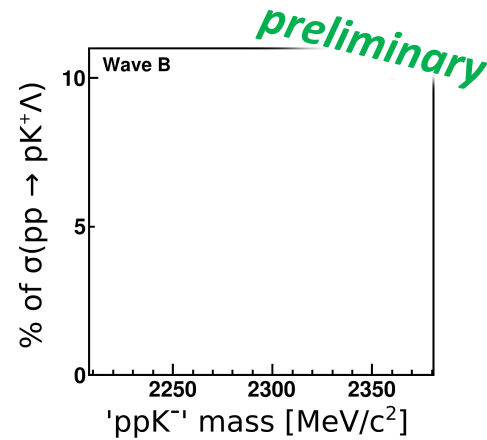
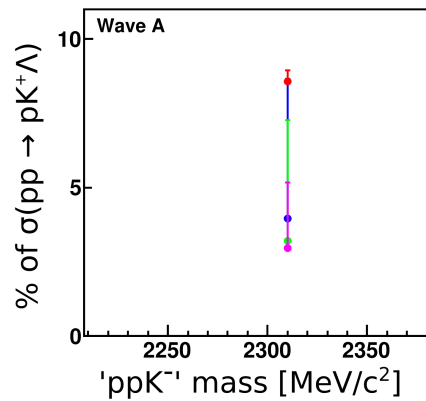
$\Gamma(ppK^-) = 50 \text{ MeV}$

# Upper Limit



$\Gamma(ppK^-) = 50 \text{ MeV}$

# Upper Limit

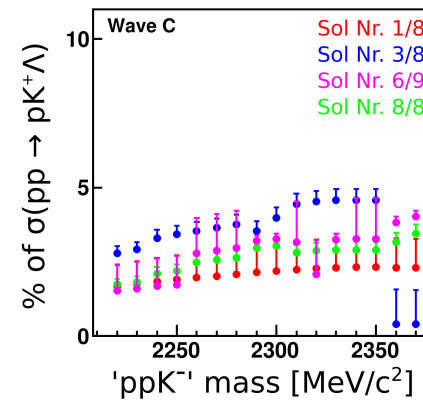
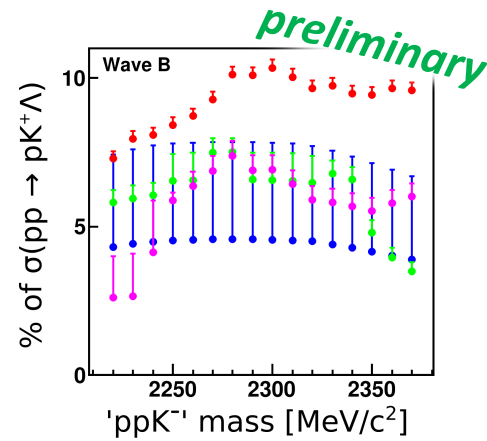
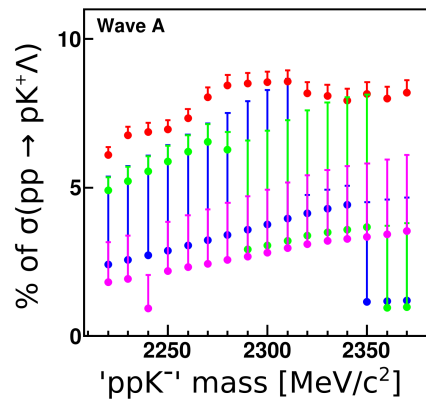


$\Gamma(ppK^-) = 50 \text{ MeV}$

Mass:  
2310 MeV/c<sup>2</sup>

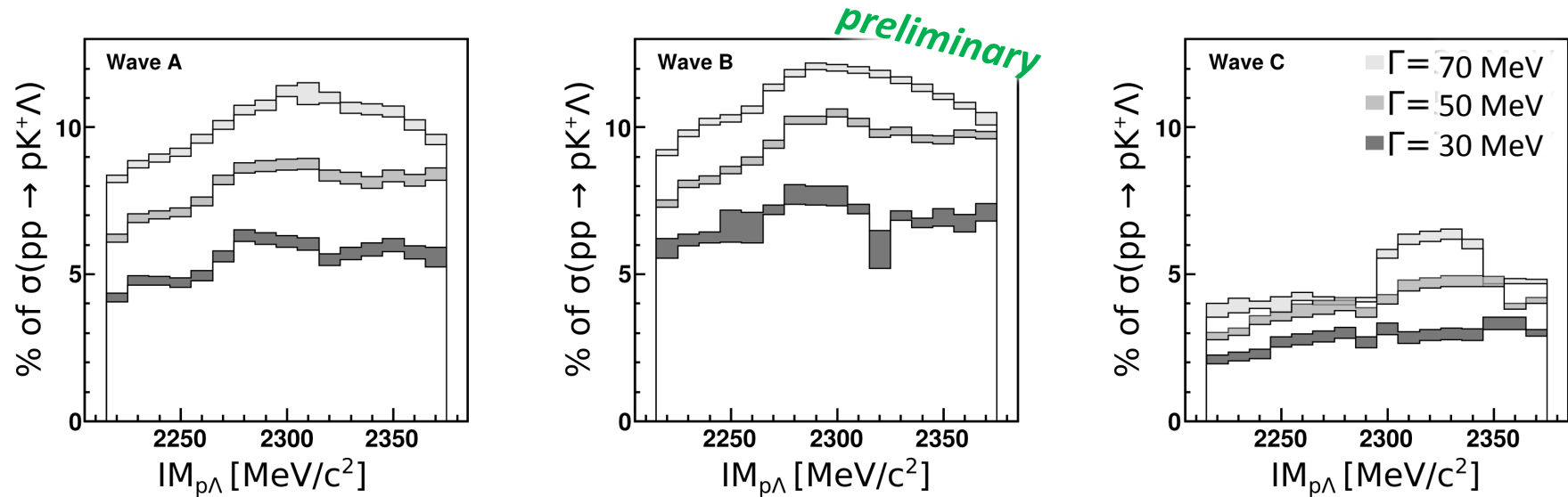


# Upper Limit



$\Gamma(ppK^-) = 50 \text{ MeV}$

# Upper Limit



Exclusion of a 'ppK' at a sensitivity level of 95% ( $CL_s$ )  
 This means in 95% of the experiments we would be sensitive to a kaonic cluster of that strength

$$\sigma_{pK^+\Lambda} = 38.12 \pm 0.43_{-2.83}^{+3.55} \pm 2.67(p+p\text{-error}) - 2.9(\text{background}) \mu\text{b}$$

→ 12%  $\approx 4\mu\text{b}$

# Summary and Outlook

First PWA of  $pK^+\Lambda$  production with Bonn-Gatchina-PWA  
First coherent description of a “ppK<sup>-</sup>” production

The PWA fit yields an excellent description of the data  
→ no new signal needed

The Upper limit for a broad KNN is in the order  
of <12% ( $\Gamma = 70\text{MeV}$ ) of the total  $pK^+\Lambda$  cross section  $\approx 4\mu\text{b}$

## Outlook:

More experimental data at J-Parc, KLOE, LEPS and BELLEII coming up  
A combined PWA of several  $pK^+\Lambda$  data is currently prepared  
(different energies, Experiments, polarization)

DFG Proposal: "Partialwellenanalyse von Ereignissen in Proton-Proton  
Reaktionen für Energien zwischen 1.9 und 3.5 GeV." FA 898/2-1

# Thanks to the HADES Collaboration

Jörn Adamczewski-Musch, Geydar Agakishiev, Claudia Behnke, Alexander Belyaev, **Jia-Chii Berger-Chen**, Alberto Blanco, Christoph Blume, Michael Böhmer, Pablo Cabanelas, Nuno Carolino, Sergey Chernenko, Jose Díaz, Adrian Dybczak, **Eliane Epple**, **Laura Fabbietti**, Oleg Fateev, Paulo Fonte, Jürgen Friese, Ingo Fröhlich, Tetyana Galatyuk, Juan A. Garzón, Roman Gernhäuser, Alejandro Gil, Marina Golubeva, Fedor Guber, Malgorzata Gumberidze, Szymon Harabasz, Klaus Heidelberg, Thorsten Heinz, Thierry Hennino, Romain Holzmann, Jochen Hutsch, Claudia Höhne, Alexander Ierusalimov, Alexander Ivashkin, Burkhard Kämpfer, Marcin Kajetanowicz, Tatiana Karavicheva, Vladimir Khomyakov, Ilse Koenig, Wolfgang Koenig, Burkhard W. Kolb, Vladimir Kolganov, Grzegorz Korcyl, Georgy Kornakov, Roland Kotte, Erik Krebs, Hubert Kuc, Wolfgang Kühn, Andrej Kugler, Alexei Kurepin, Alexei Kurilkin, Pavel Kurilkin, Vladimir Ladygin, **Rafal Lalik**, **Kirill Lapidus**, Alexander Lebedev, Ming Liu, Luís Lopes, Manuel Lorenz, Gennady Lykasov, Ludwig Maier, Alexander Malakhov, Alessio Mangiarotti, Jochen Markert, Volker Metag, Jan Michel, Christian Müntz, **Rober Münzer**, Lothar Naumann, Marek Palka, Vladimir Pechenov, Olga Pechenova, Americo Pereira, Jerzy Pietraszko, Witold Przygoda, Nicolay Rabin, Béatrice Ramstein, Andrei Reshetin, Laura Rehnisch, Philippe Rosier, Anar Rustamov, Alexander Sadovsky, Piotr Salabura, Timo Scheib, Alexander Schmah, Heidi Schuldes, Erwin Schwab, **Johannes Siebenson**, Vladimir Smolyankin, Manfred Sobiella, Yuri Sobolev, Stefano Spataro, Herbert Ströbele, Joachim Stroth, Christian Sturm, Khaled Teilab, Vladimir Tiflov, Pavel Tlusty, Michael Traxler, Alexander Troyan, Haralabos Tsertos, Evgeny Usenko, Taras Vasiliev, Vladimir Wagner, Christian Wendisch, Jörn Wüstenfeld, Yuri Zanevsky



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# Backup

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# N\* resonances

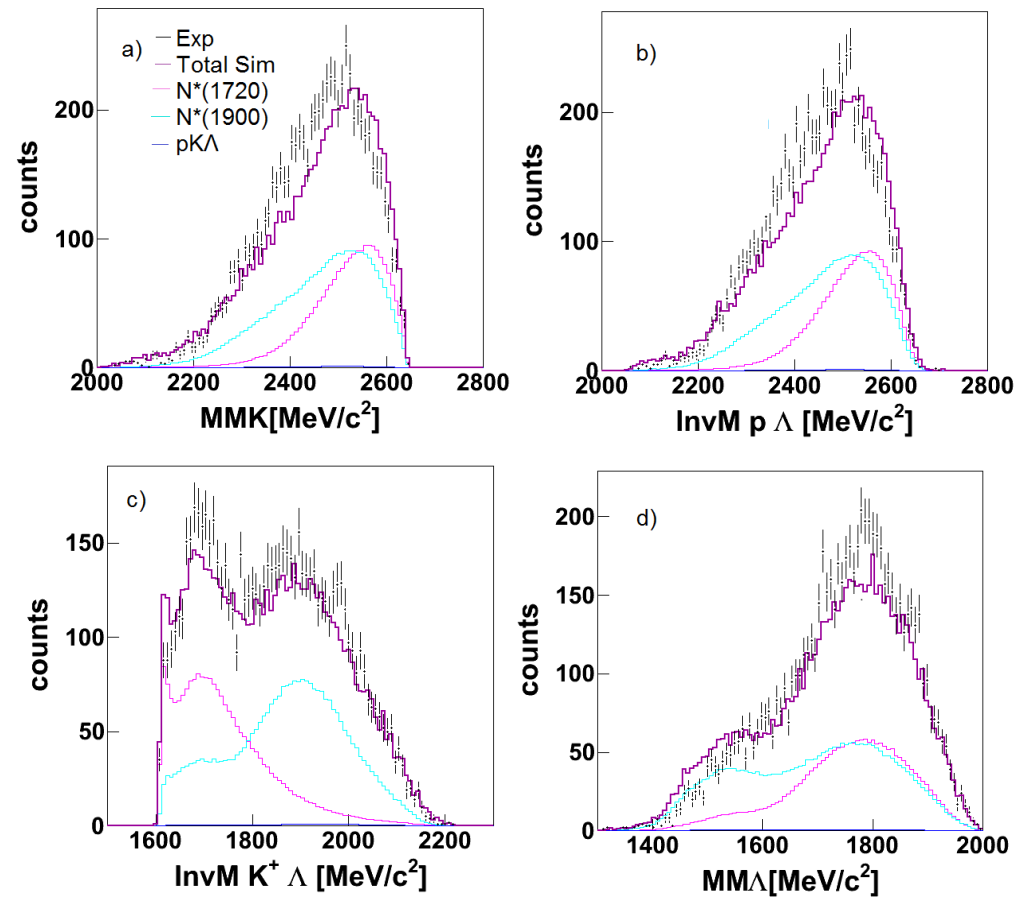


Figure 6.10: a)  $IM_{K+\Lambda}$ , b)  $IM_{p\Lambda}$ , c)  $MM_{K^+}$  and d)  $MM_\Lambda$  fitted with the sum of the four  $N^{*+}$ -resonances from table 6.2 and the simulation of a direct  $pK^+\Lambda$  production.

Master Thesis A. Solaguren-Beascoa Negre

# Bonn-Gatchina PWA

**Cross Section for the production of three particles out of a collision of two particle**

$$d\sigma = \frac{(2\pi)^4 |A|^2}{4|k|\sqrt{s}} d\Phi_3(P, q_1, q_2, q_3), \quad P = k_1 + k_2$$

*A* - reaction amplitude

*k* – 3-momentum of the initial particle in the CM

*s* –  $P^2 = (k_1 + k_2)^2$

$d\Phi_3(P, q_1, q_2, q_3)$  – invariant three-particles phase space

**The decomposition of the scattering amplitude into partial waves can be written as follows:**

$$A = \sum A_{tr}^{\alpha}(s) Q_{\mu_1 \dots \mu_J}^{in}(SLJ) A_{2b}(i, S_2 L_2 J_2)(s_i) \times Q_{\mu_1 \dots \mu_J}^{fin}(i, S_2 L_2 J_2 S' L' J). \quad (2)$$

*S, L, J* – spin, orbital mom. and total angular momentum of the pp system

*S<sub>2</sub>, L<sub>2</sub>, J<sub>2</sub>* – spin, orbital mom. and total angular momentum of the two particle system in fin. state

*S', L'* – spin, orbital mom. between the two particle system and the third particle with four mom. *q<sub>i</sub>*

multiindex *α* – possible combinations of the *S, L, J, S<sub>2</sub>, L<sub>2</sub>, J<sub>2</sub>, S', L'* and *i*

*A<sub>tr</sub><sup>α</sup>(s)* – transition Amplitude

*A<sub>2b</sub><sup>α</sup>(i, S<sub>2</sub>, L<sub>2</sub>, J<sub>2</sub>)* – rescattering process in the final two-particle channel (e.g. production of  $\Delta$ )

<http://pwa.hiskp.uni-bonn.de/>

A.V. Anisovich, V.V. Anisovich, E. Klempt, V.A. Nikonov and A.V. Sarantsev  
Eur. Phys. J. A 34, 129152 (2007)



# Fitting Procedure

The transition Amplitude is parameterized as follows

$$A_{tr}^{\alpha}(s) = (a_1^{\alpha} + a_3^{\alpha} \sqrt{s}) e^{ia_2^{\alpha}}$$

This is a log-likelihood minimization on an event-by-event base

## What we included to model the $PK^+\Lambda$ process:

$N^*$  Resonances in the PDG with measured decay into  $K^+\Lambda$

Notation in PDG	Old notation	Mass [GeV/c <sup>2</sup> ]	Width [GeV/c <sup>2</sup> ]	$\Gamma_{\Lambda K}/\Gamma_{All}$ %
$N(1650) \frac{1}{2}^{-}$	$N(1650)S_{11}$	1.655	0.150	3-11
$N(1710) \frac{1}{2}^{+}$	$N(1710)P_{11}$	1.710	0.200	5-25
$N(1720) \frac{3}{2}^{+}$	$N(1720)D_{13}$	1.720	0.250	1-15
$N(1875) \frac{3}{2}^{-}$	$N(1875)D_{13}$	1.875	0.220	4±2
$N(1880) \frac{1}{2}^{+}$	$N(1880)P_{11}$	1.870	0.235	2±1
$N(1895) \frac{1}{2}^{-}$	$N(1895)S_{11}$	1.895	0.090	18±5
$N(1900) \frac{3}{2}^{+}$	$N(1900)P_{13}$	1.900	0.250	0-10

And the production of  $pK^+\Lambda$  via non resonant waves

# Systematic

## N\* content

No.	Combination
0	N(1650), N(1710), N(1720)
1	N(1650), N(1710), N(1720), N(1900)
2	N(1650), N(1710), N(1720), N(1895)
3	N(1650), N(1710), N(1720), N(1880)
4	N(1650), N(1710), N(1720), N(1875)
5	N(1650), N(1710), N(1720), N(1900), N(1880)
6	N(1650), N(1710), N(1720), N(1900), N(1895)
7	N(1650), N(1710), N(1720), N(1900), N(1875)
8	N(1650), N(1710), N(1720), N(1895), N(1880)
9	N(1650), N(1710), N(1720), N(1895), N(1875)
10	N(1650), N(1710), N(1720), N(1880), N(1875)

## non-resonant content

No.	Combination
0	no non-resonant waves
1	$(pL)(^1S_0) - K$
2	previous wave + $(pL)(^3S_1) - K$
3	previous waves + $(pL)(^1P_1) - K$
4	previous waves + $(pL)(^3P_0) - K$
5	previous waves + $(pL)(^3P_1) - K$
6	previous waves + $(pL)(^3P_2) - K$
7	previous waves + $(pL)(^1D_2) - K$
8	previous waves + $(pL)(^3D_1) - K$
9	previous waves + $(pL)(^3D_2) - K$

	No. of N* combination	No. of non-res. waves	Log-likelih.
	0	7	-2415.74
<b>Best Solutions</b>	<b>1</b>	<b>8</b>	<b>-2708.49</b>
	2	8	-2524.59
	<b>3</b>	<b>8</b>	<b>-2712.49</b>
	4	4	-2671.05
	5	8	-2310.4
	<b>6</b>	<b>9</b>	<b>-2754.37</b>
	7	8	-2657.77
	<b>8</b>	<b>8</b>	<b>-2734.97</b>
	9	6	-2698.86
	10	4	-2642.58

# Solution inside WALL acceptance

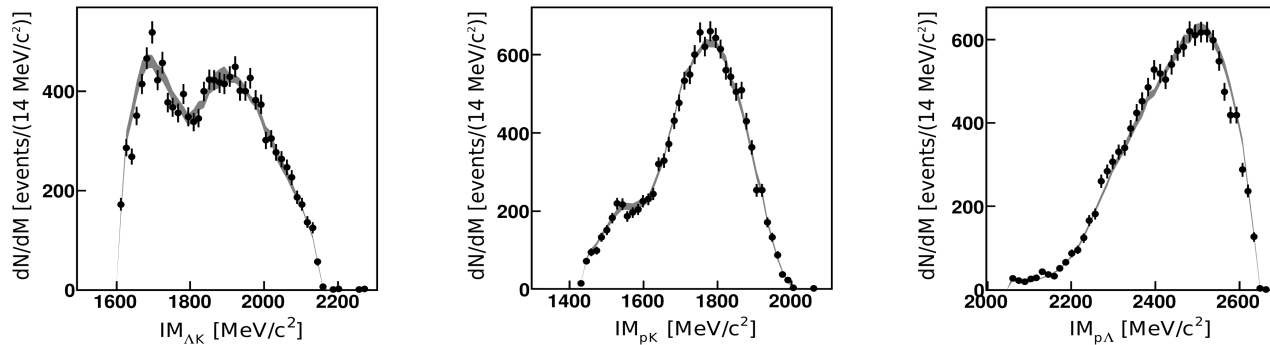


Figure 2.18: Two-particle masses for the **HADES data set** (black points) shown with the **four best PWA solutions** (gray band), obtained by a fit to the HADES and WALL data.

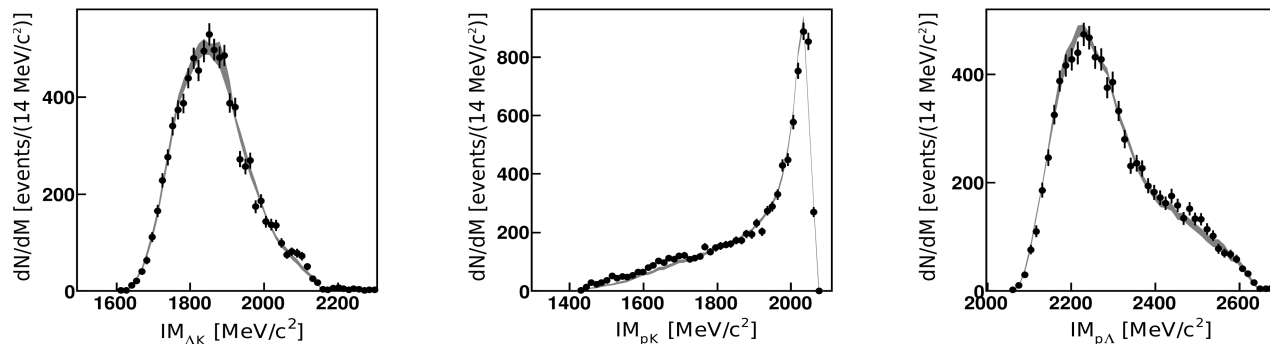
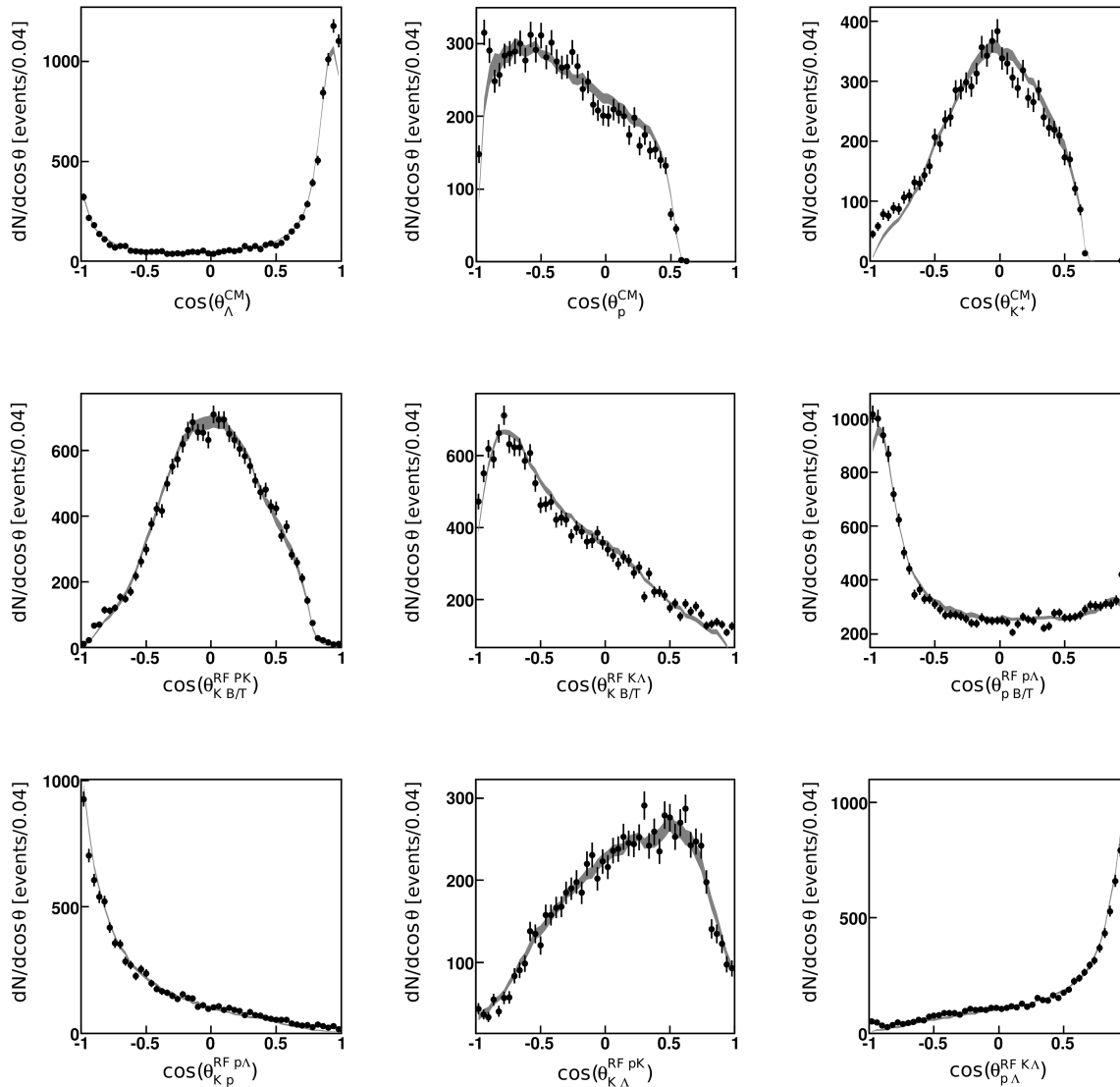
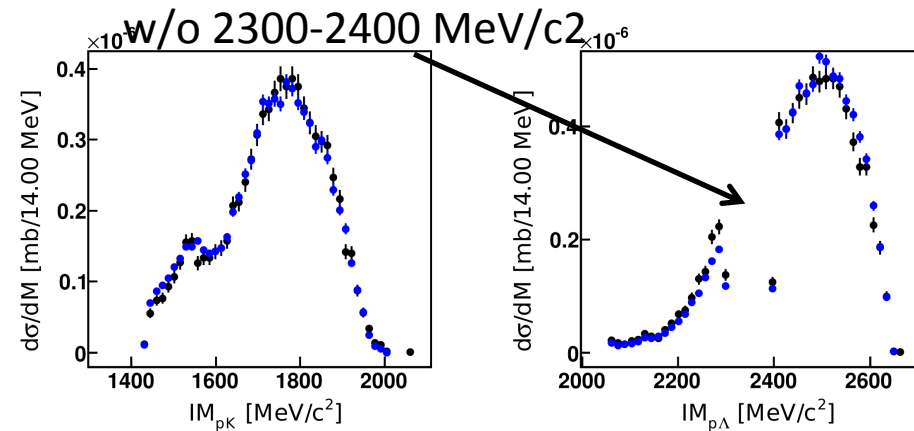
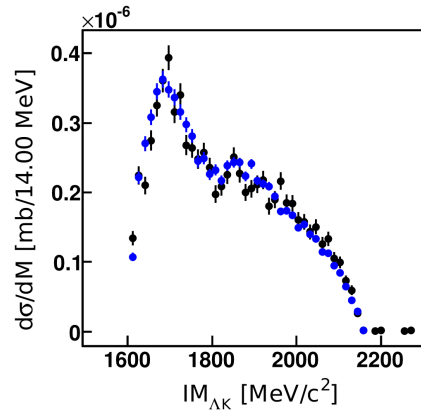
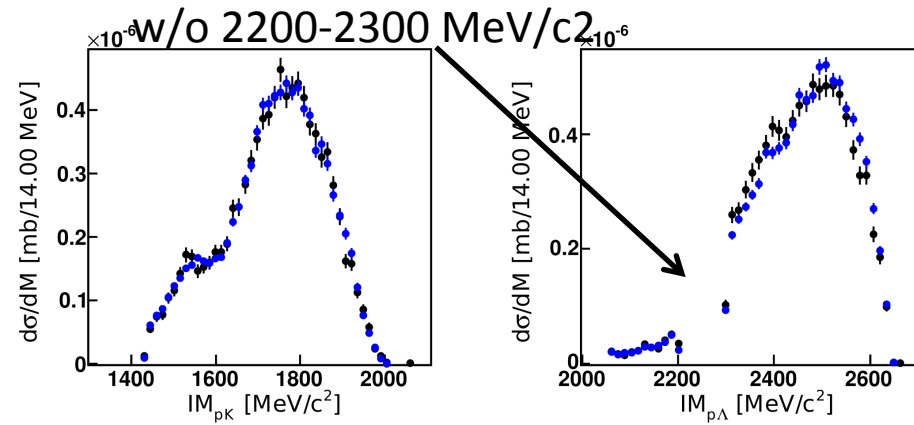
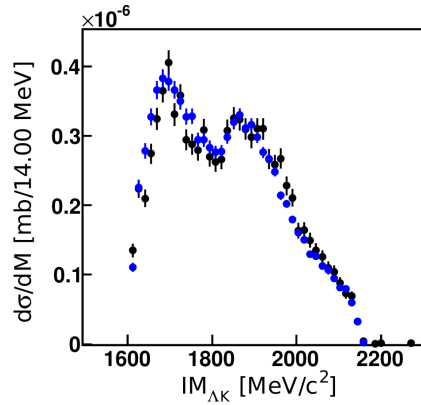


Figure 2.19: Two-particle masses for the **WALL data set** (black points) shown with the **four best PWA solutions** (gray band), obtained by a fit to the HADES and WALL data.

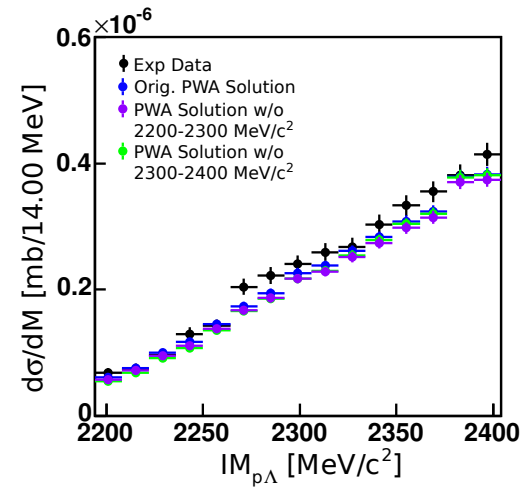
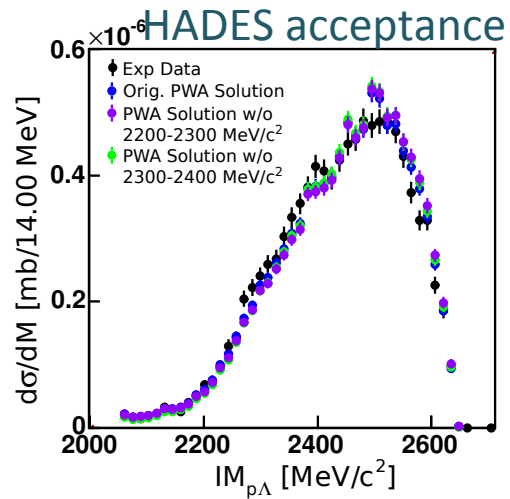
# Solution inside WALL acceptance



# Cross Check

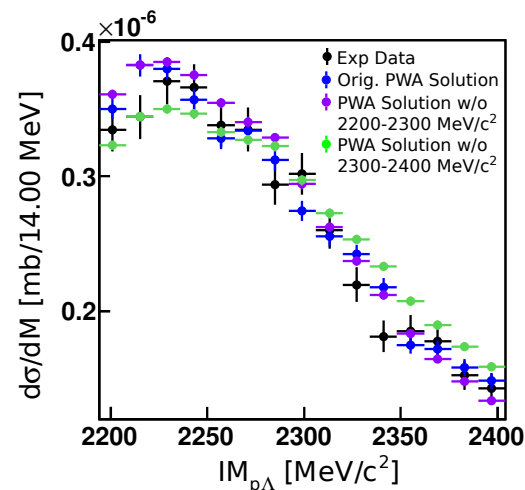
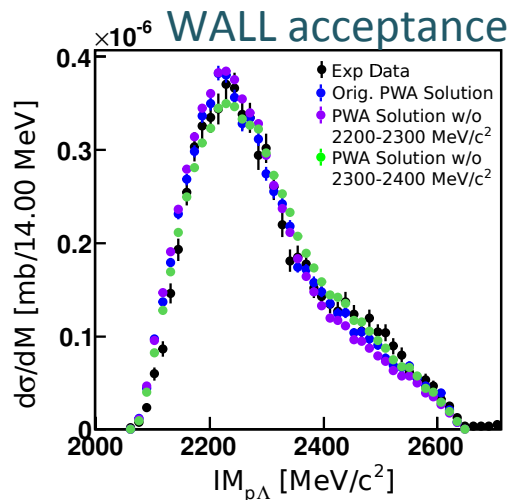


# Cross Check

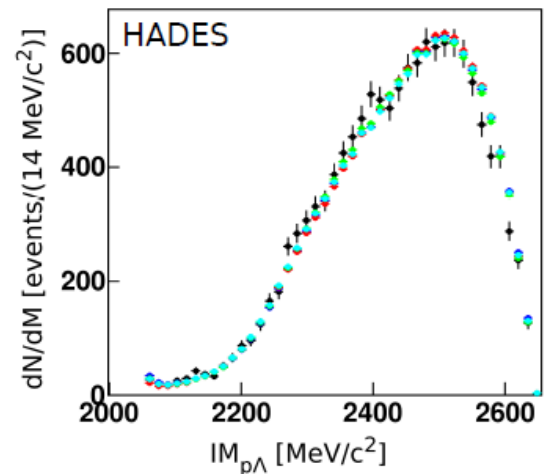


Good consistency among the results.

The solution is not biased by a possible signal in the excluded mass range

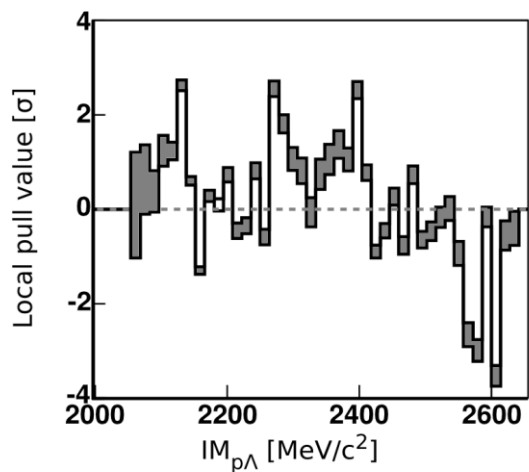


# Result

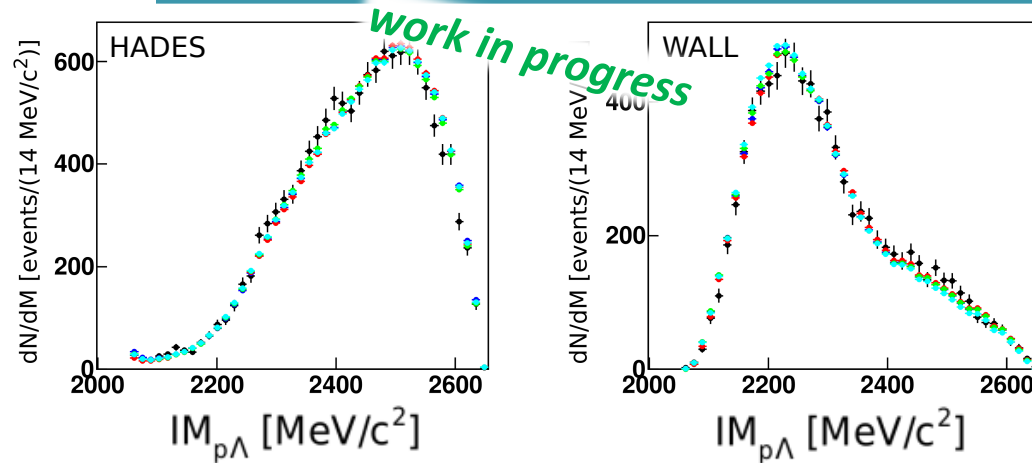


$$pull = \sum_{i=1}^{N_b} \frac{(m_i - \lambda_i)}{\lambda_i}$$

$m_i$  are the number of measured events in the bin  $i$   
 $\lambda_i$  number of expected events in the bin according to the model  
 $N_b$  is the number of bins

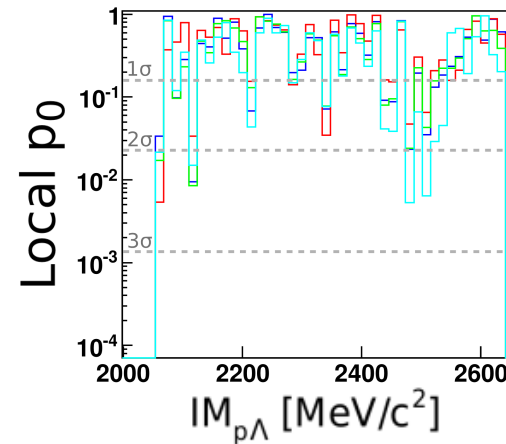
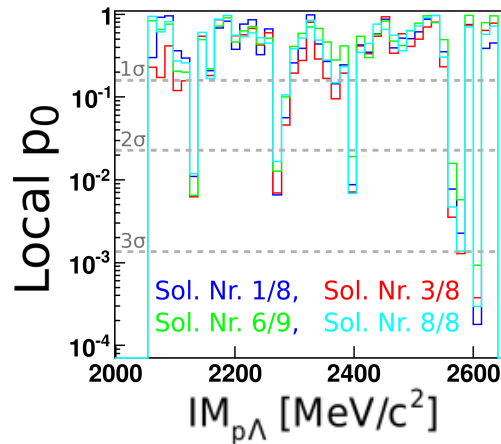


# Test of the Null Hypothesis



$$\chi_P^2 = \frac{(m - \lambda)^2}{\lambda}$$

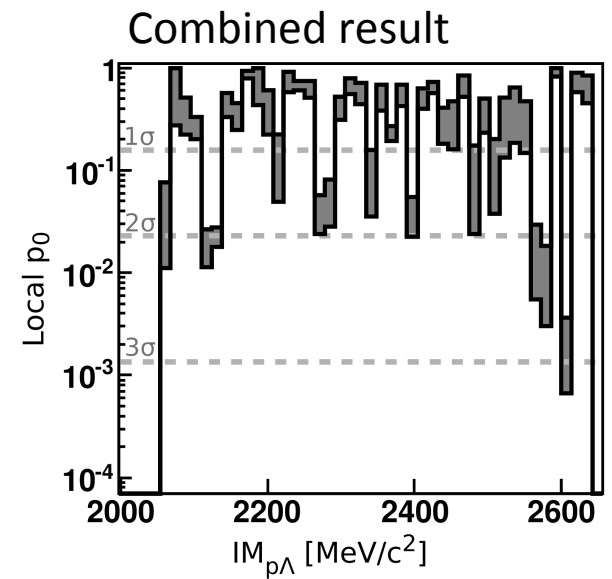
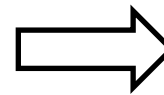
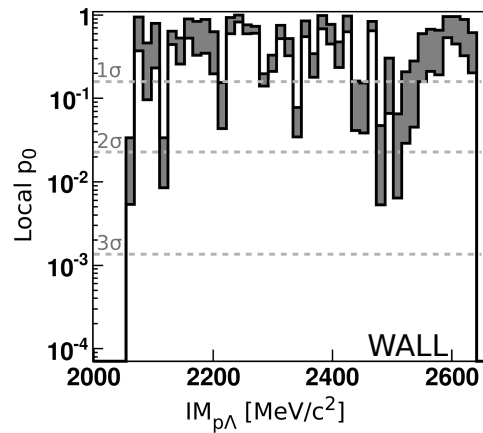
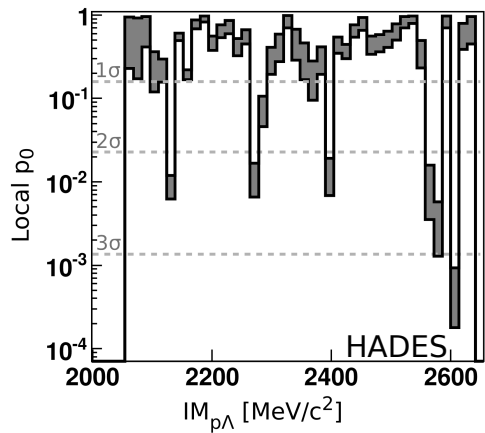
$$p - value = \int_{\chi_{P,d}^2}^{\infty} P(\chi^2, Ndf) d\chi^2$$

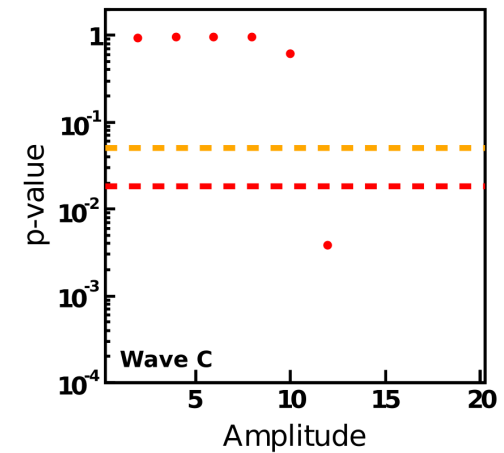
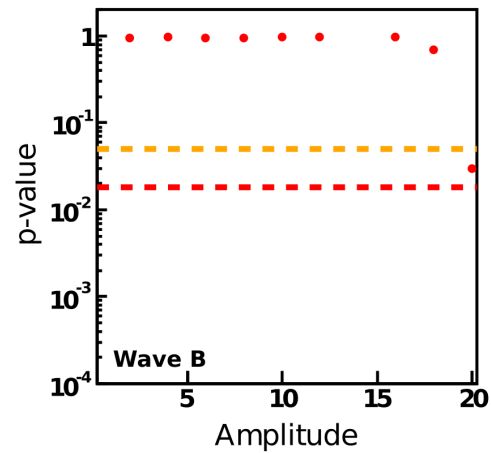
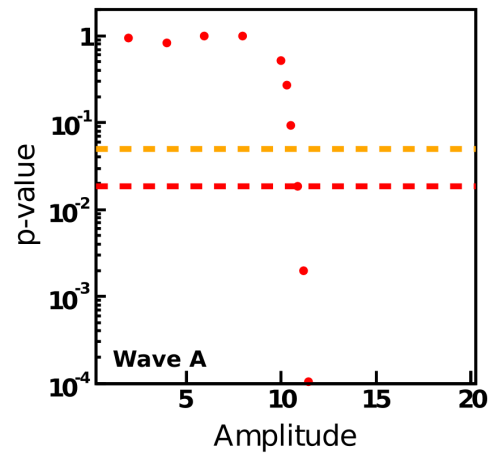


$m_i$  measured events in bin  $i$   
 $\lambda_i$  expected events in bin  $i$   
 according to the model



$$\chi_P^2 = \frac{(m - \lambda)^2}{\lambda} \Rightarrow \chi_P^2 = \sum_{i=1}^{N_b} \frac{(m_i - \lambda_i)^2}{\lambda_i}$$



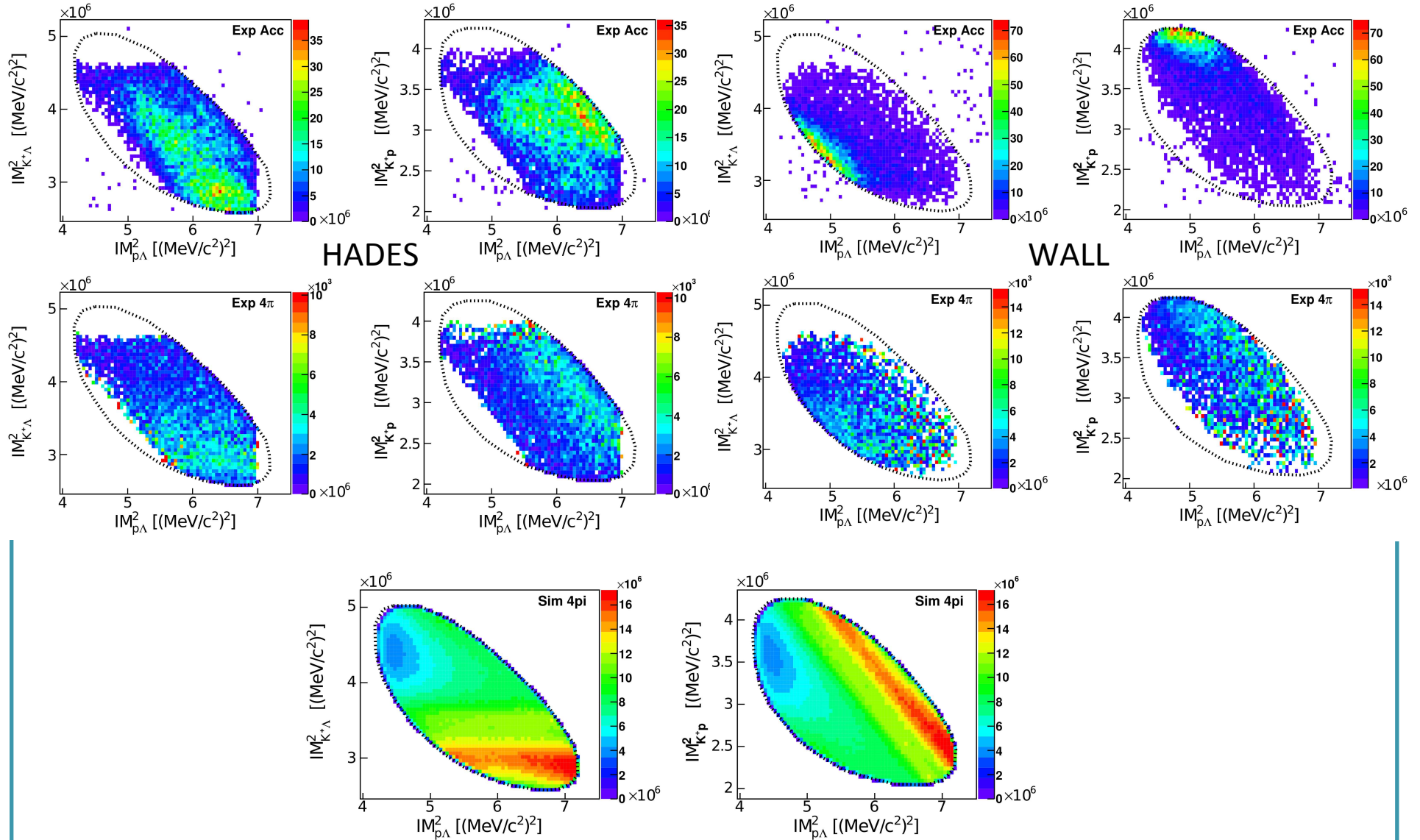


$$CL_S = \frac{p_\mu}{1 - p_0}.$$

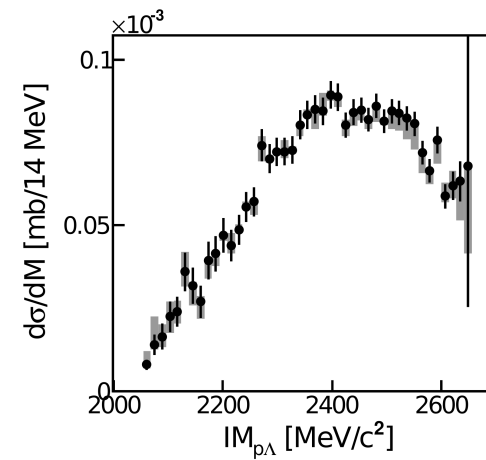
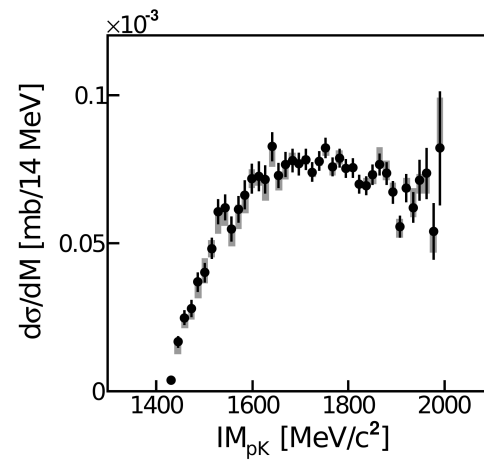
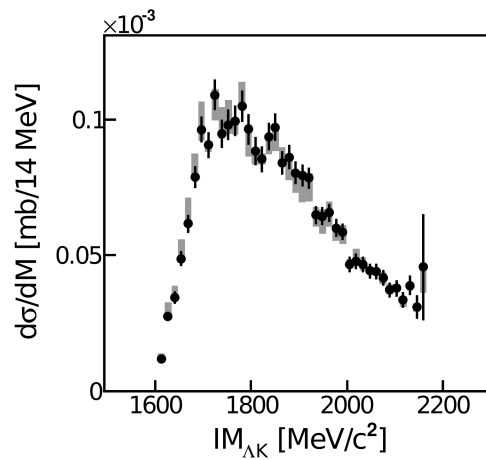
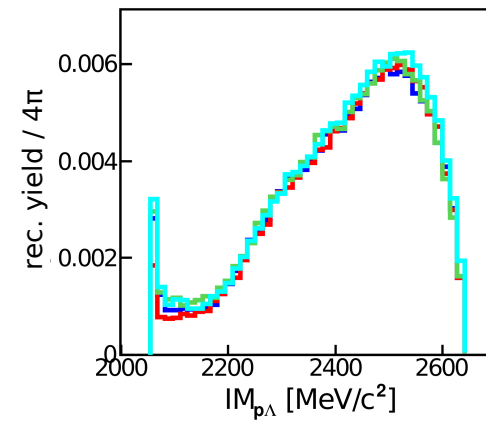
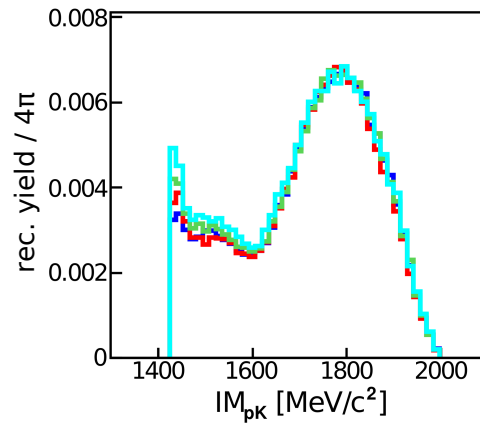
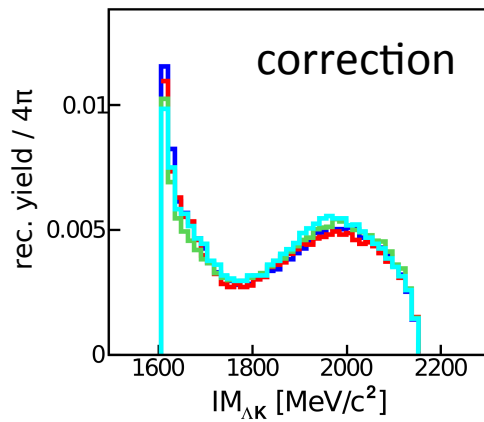
Values are rejected in a test if  $CL_S \leq \alpha$ .

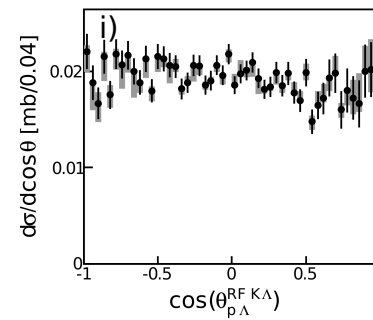
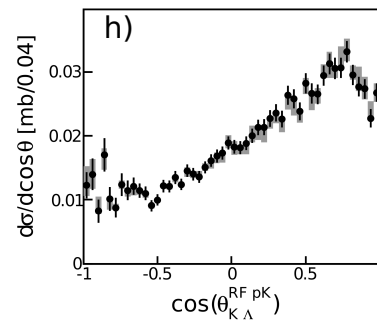
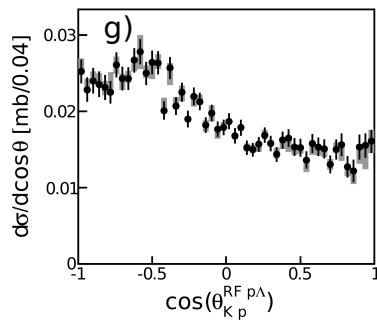
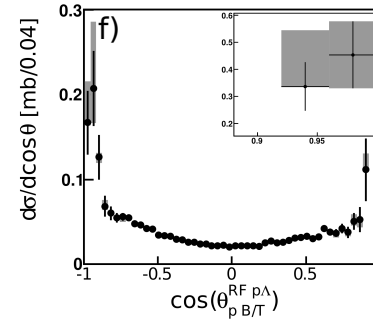
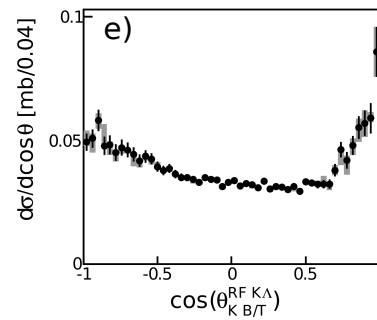
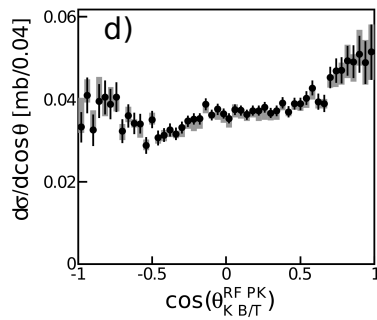
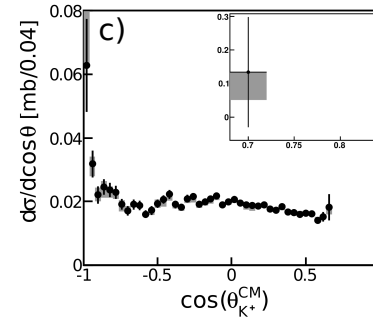
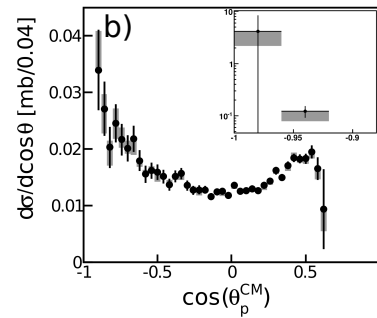
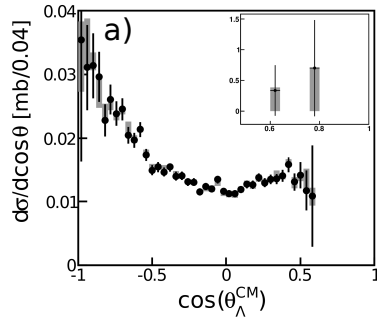
$$p_\mu \leq \alpha \cdot (1 - p_0).$$

# Dalitz Plots



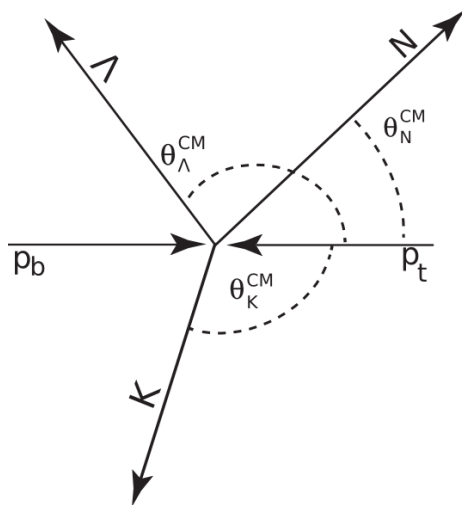
# Cross Section



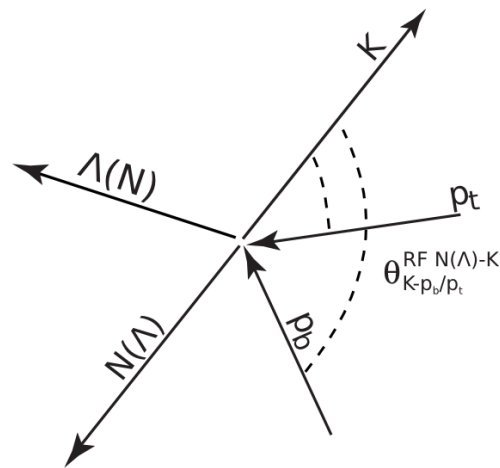


# Definition of Angles

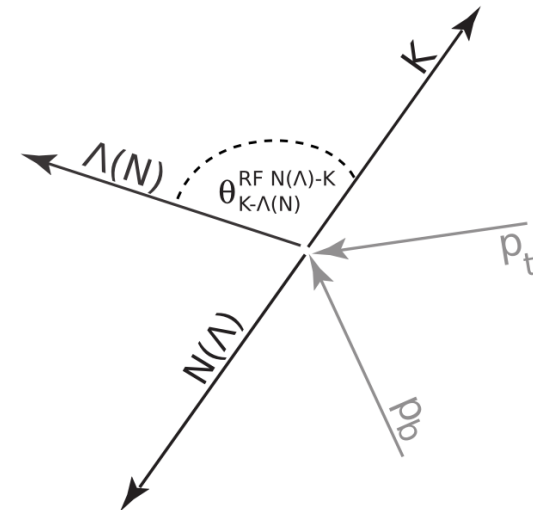
I) CM Angle



II) Jackson Angle

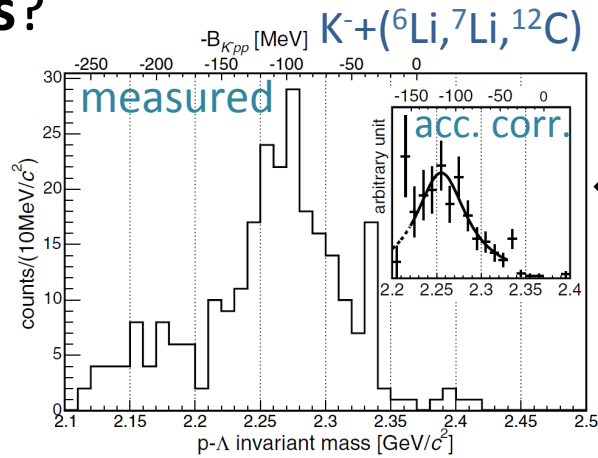


III) Helicity Angle



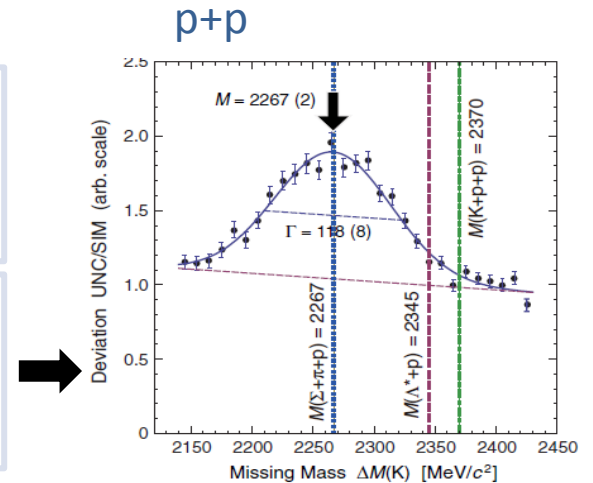
# Is there a $\bar{K}NN$ ?

## Hints?



M. Agnello et al. Phys. Rev. Lett. **94** (2005)

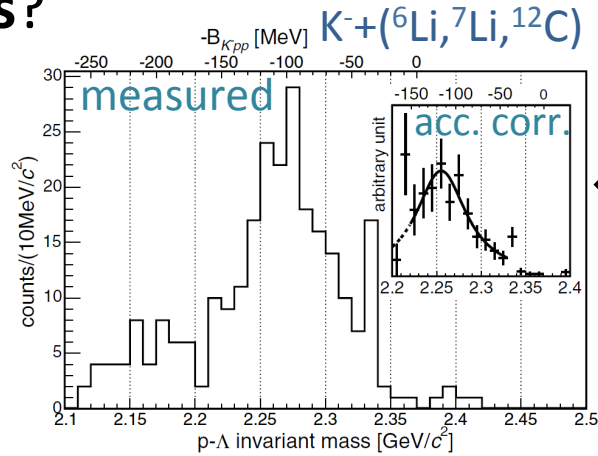
- $M(ppK) = 2.255 \text{ GeV}/c^2$
  - $B(ppK) = 115 \text{ MeV}$
  - $\Gamma(ppK) = 67 \text{ MeV}/c^2$
- 
- $M(ppK) = 2.267 \text{ GeV}/c^2$
  - $B(ppK) = 103 \text{ MeV}$
  - $\Gamma(ppK) = 118 \text{ MeV}/c^2$



T. Yamazaki et al. Phys. Rev. Lett. **104**, (2010)  
 M. Maggiora et al. Nucl. Phys. **A 835** (2010)

# Is there a $\bar{K}NN$ ?

## Hints?

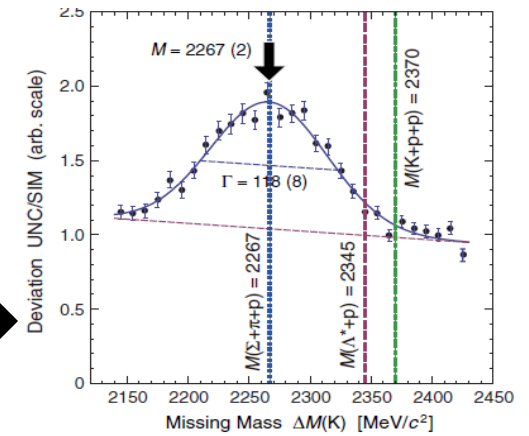


M. Agnello et al. Phys. Rev. Lett. **94** (2005)

$M(ppK) = 2.255 \text{ GeV}/c^2$   
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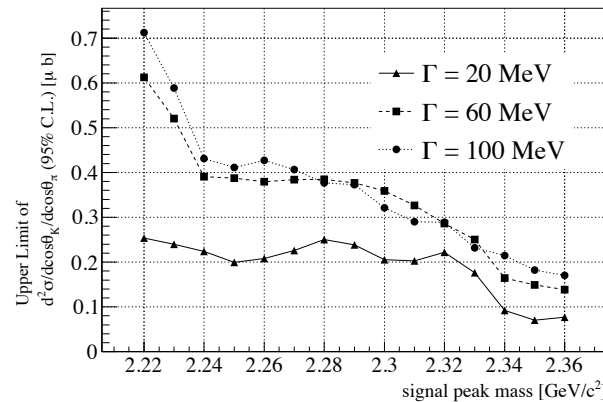
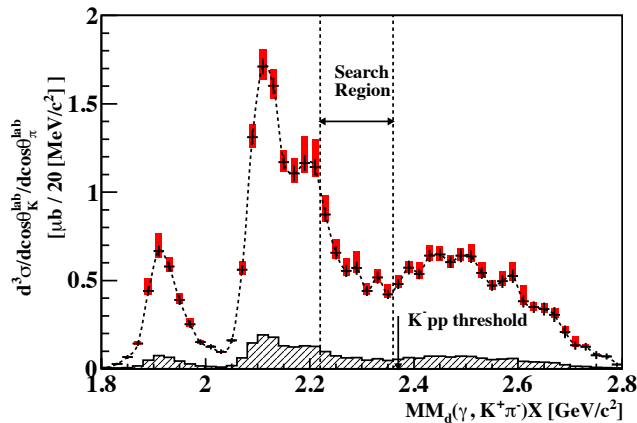
$M(ppK) = 2.267 \text{ GeV}/c$   
 $B(ppK) = 103 \text{ MeV}$   
 $\Gamma(ppK) = 118 \text{ MeV}/c^2$

p+p



T. Yamazaki et al. Phys. Rev. Lett. **104**, (2010)  
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## Exclusions



A.O. Tokiyasu et al.  
Phys.Lett. **B728** 616-621 (2014)

0.5-5% of the cross section of typical hadron photo-production