

# Exclusive central diffractive production of scalar, pseudoscalar and vector mesons

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P. Lebiedowicz, O. Nachtmann and A. Szczurek, Ann. Phys. 344 (2014) 301
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P. Lebiedowicz, O. Nachtmann and A. Szczurek, in preparation  
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# The soft pomeron model

For  $pp$  elastic scattering we get (T-matrix element):

effective vector pomeron exchange

vs

effective tensor pomeron exchange

$$\begin{aligned} \mathcal{M}_{\lambda_a \lambda_b \rightarrow \lambda_1 \lambda_2}^{pp \rightarrow pp} |_{\mathcal{P}_V} &= (-i) \bar{u}(p_1, \lambda_1) i\Gamma_{\mu}^{(\mathcal{P}_V pp)}(p_1, p_a) u(p_a, \lambda_a) \\ &\times i\Delta^{(\mathcal{P}_V) \mu\nu}(s, t) \\ &\times \bar{u}(p_2, \lambda_2) i\Gamma_{\nu}^{(\mathcal{P}_V pp)}(p_2, p_b) u(p_b, \lambda_b) \end{aligned}$$

$$\begin{aligned} \mathcal{M}_{\lambda_a \lambda_b \rightarrow \lambda_1 \lambda_2}^{pp \rightarrow pp} |_{\mathcal{P}_T} &= (-i) \bar{u}(p_1, \lambda_1) i\Gamma_{\mu_1 \nu_1}^{(\mathcal{P}_T pp)}(p_1, p_a) u(p_a, \lambda_a) \\ &\times i\Delta^{(\mathcal{P}_T) \mu_1 \nu_1, \mu_2 \nu_2}(s, t) \\ &\times \bar{u}(p_2, \lambda_2) i\Gamma_{\mu_2 \nu_2}^{(\mathcal{P}_T pp)}(p_2, p_b) u(p_b, \lambda_b) \end{aligned}$$

$$i\Gamma_{\mu}^{(\mathcal{P}_V pp)}(p', p) = -i 3\beta_{\mathcal{P}NN} F_1((p' - p)^2) M_0 \gamma_{\mu}$$

$$i\Delta_{\mu\nu}^{(\mathcal{P}_V)}(s, t) = \frac{1}{M_0^2} g_{\mu\nu} (-is\alpha'_{\mathcal{P}})^{\alpha_{\mathcal{P}}(t)-1}$$

$$i\Gamma_{\mu\nu}^{(\mathcal{P}_T pp)}(p', p) = -i 3\beta_{\mathcal{P}NN} F_1((p' - p)^2)$$

$$\times \left\{ \frac{1}{2} [\gamma_{\mu}(p' + p)_{\nu} + \gamma_{\nu}(p' + p)_{\mu}] - \frac{1}{4} g_{\mu\nu} (\not{p}' + \not{p}) \right\}$$

$$i\Delta_{\mu\nu, \kappa\lambda}^{(\mathcal{P}_T)}(s, t) = \frac{1}{4s} \left( g_{\mu\kappa} g_{\nu\lambda} + g_{\mu\lambda} g_{\nu\kappa} - \frac{1}{2} g_{\mu\nu} g_{\kappa\lambda} \right) (-is\alpha'_{\mathcal{P}})^{\alpha_{\mathcal{P}}(t)-1}$$

The Donnachie - Landschoff pomeron is frequently called a 'C = +1 photon' → problems from the point of view of QFT

*C. Ewerz, M. Maniatis and O. Nachtmann, Ann. Phys. 342 (2014) 31*

*O. Nachtmann, High-energy soft reactions: A model with tensor pomeron and vector odderon, WE-Heraeus-Summerschool, Heidelberg, 2013*

Effective  $\mathcal{P}_T pp$  vertex and  $\mathcal{P}_T$  propagator

respect the standard C parity and crossing rules of QFT

In QFT a second rank tensor - like for gravity - gives the same sign for the coupling of particles and of antiparticles

$$\beta_{\mathcal{P}NN} = 1.87 \text{ GeV}^{-1}, \quad M_0 = 1 \text{ GeV},$$

$$\alpha_{\mathcal{P}}(t) = \alpha_{\mathcal{P}}(0) + \alpha'_{\mathcal{P}} t,$$

$$F_1(t) = \frac{4m_p^2 - 2.79t}{(4m_p^2 - t)(1 - t/m_D^2)}$$

$$\alpha_{\mathcal{P}}(0) = 1.0808, \quad \alpha'_{\mathcal{P}} = 0.25 \text{ GeV}^{-2},$$

$$m_D^2 = 0.71 \text{ GeV}^2$$

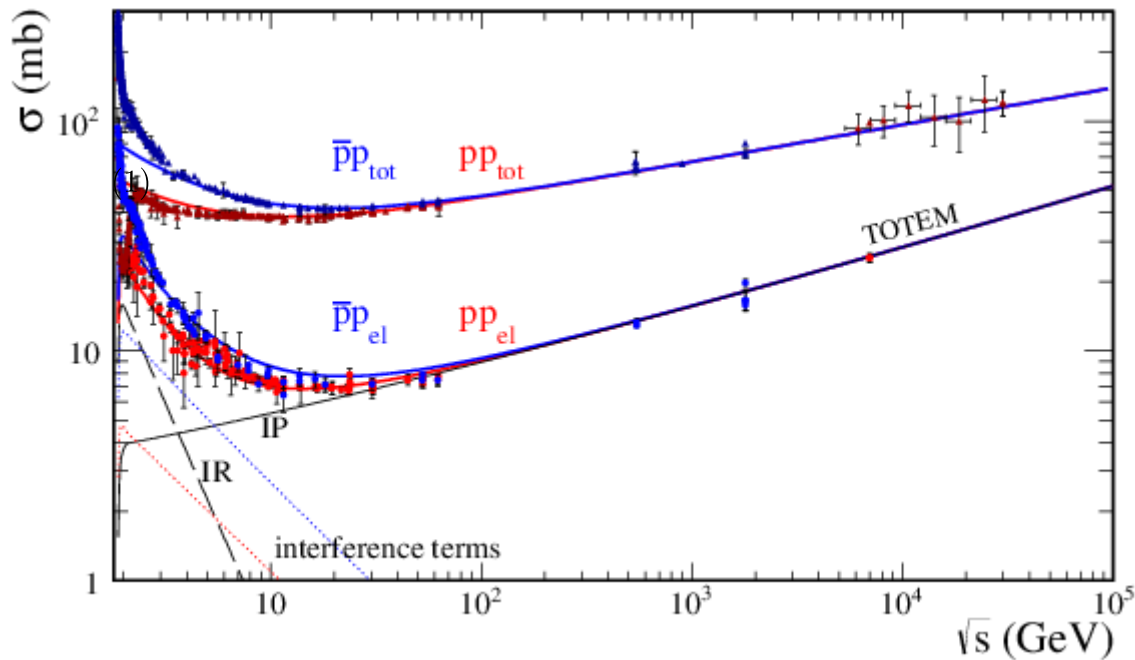
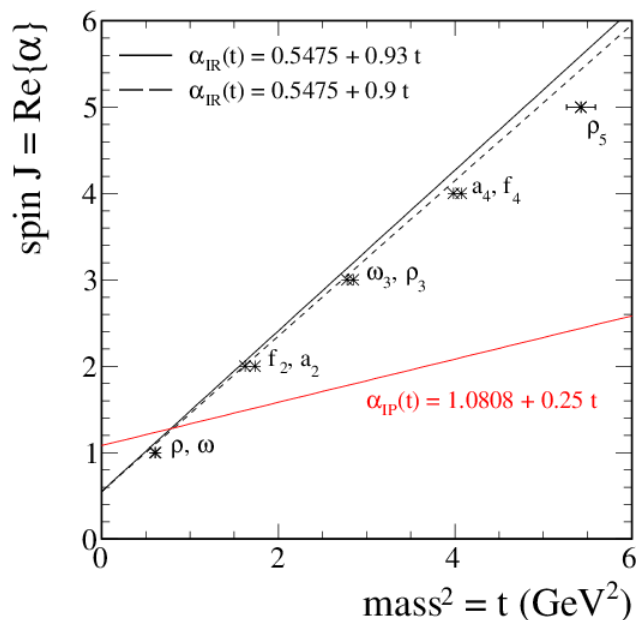
# Total and elastic scattering

For high energies, we have

$$\sigma_{tot}(s) \sim s^{-1} \text{Im}M_{ab \rightarrow ab}(s, t=0)$$

$$M_{pp \rightarrow pp}(s) = A_{IP}(s) + A_{f_{2R}}(s) + A_{a_{2R}}(s) - A_{\omega_{IR}}(s) - A_{\rho_{IR}}(s)$$

$$M_{\bar{p}p \rightarrow \bar{p}p}(s) = A_{IP}(s) + A_{f_{2R}}(s) + A_{a_{2R}}(s) + A_{\omega_{IR}}(s) + A_{\rho_{IR}}(s)$$



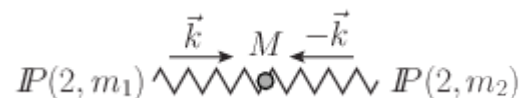
Tensor pomeron gives, at high energies, the same results for the  $pp$  and  $p\bar{p}$  elastic amplitudes as the standard DL pomeron

$$\mathcal{M}_{\lambda_a \lambda_b \rightarrow \lambda_1 \lambda_2}^{2 \rightarrow 2}(s, t) \xrightarrow{s \gg 4m_p^2} i 2s [3\beta_{IPNN} F_1(t)]^2 (-is\alpha'_{IP})^{\alpha_{IP}(t)-1} \delta_{\lambda_1 \lambda_a} \delta_{\lambda_2 \lambda_b}$$

In the Regge theory the t-channel Regge exchanges ( $IR$ ) form so-called linear Regge trajectories and correspond to a sum of ordinary mesons with the same quantum numbers (see the Chew-Frautschi plot);  $C = +1$  ( $f_2, a_2$ ) and  $C = -1$  ( $\omega, \rho$ ) secondary trajectories are all degenerate with intercept  $\sim 0.5$ .

There is belief that the pomeron rather is associated with the exchange of family of glueballs.

# $IP_V IP_V$ fusion vs $IP_T IP_T$ fusion



$IP_V IP_V \rightarrow M$

$l$	$S$	$J$	$P$
0	0	0	+
	2	2	
1	1	0, 1, 2	-
2	0	2	+
	2	0,1,2,3,4	
3	1	2,3,4	-
4	0	4	+
	2	2,3,4,5,6	

$IP_T IP_T \rightarrow M$

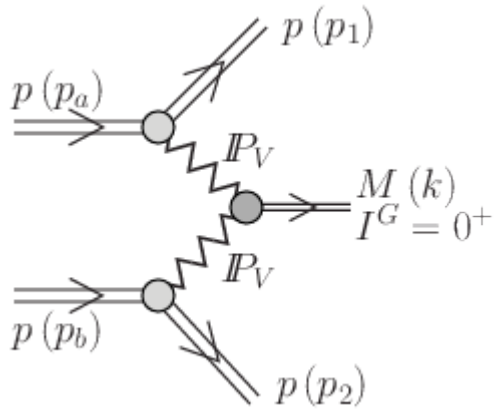
$l$	$S$	$J$	$P$
0	0	0	+
	2	2	
	4	4	
1	1	0, 1, 2	-
	3	2, 3, 4	
2	0	2	+
	2	0,1,2,3,4	
	4	2,3,4,5,6	
3	1	2,3,4	-
	3	0,1,2,3,4,5,6	
4	0	4	+
	2	2,3,4,5,6	
	4	0,1,2,3,4,5,6,7,8	

$J^{PC}$	meson $M$	$IP_V$		$IP_T$	
		$l$	$S$	$l$	$S$
$0^{-+}$	$\eta$	1	1	1	1
	$\eta'(958)$			3	3
$0^{++}$	$f_0(980)$	0	0	0	0
	$f_0(1370)$	2	2	2	2
	$f_0(1500)$			4	4
$1^{++}$	$f_1(1285)$	2	2	2	2
	$f_1(1420)$			4	4
$2^{++}$	$f_2(1270)$	0	2	0	2
	$f_2'(1525)$	2	0	2	0
		2	2	2	2
		4	2	2	4
				4	2
		4	4		
$4^{++}$	$f_4(2050)$	2	2	0	4
		4	0	2	2
		4	2	2	4
				4	0
				4	2
		4	4		

The values, for orbital angular momentum ( $l$ ), total spin ( $S$ ) of the two “pomeron particles”, total angular momentum ( $J$ ) and parity ( $P$ ) of the state, respectively, possible in the annihilation reaction of two “pomeron particles” into a meson.

$$|l - S| \leq J \leq l + S, \quad P = (-1)^l$$

# Exclusive production of resonances via $IP_V IP_V$ fusion

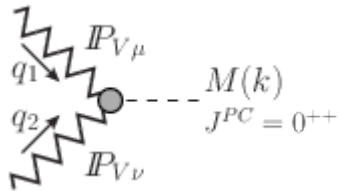


$$\begin{aligned} \mathcal{M}_{\lambda_a \lambda_b \rightarrow \lambda_1 \lambda_2 M}^{2 \rightarrow 3} |_{IP_V} &= (-i) \bar{u}(p_1, \lambda_1) i \Gamma_{\mu_1}^{(IP_V PP)}(p_1, p_a) u(p_a, \lambda_a) \\ &\times i \Delta^{(IP_V) \mu_1 \nu_1}(s_{13}, t_1) \quad i \Gamma_{\nu_1 \nu_2}^{(IP_V IP_V \rightarrow M)}(q_1, q_2) \quad i \Delta^{(IP_V) \nu_2 \mu_2}(s_{23}, t_2) \\ &\times \bar{u}(p_2, \lambda_2) i \Gamma_{\mu_2}^{(IP_V PP)}(p_2, p_b) u(p_b, \lambda_b) \end{aligned}$$

$$i \Gamma_{\mu\nu}^{(IP_V IP_V \rightarrow M)}(q_1, q_2) = \left( i \Gamma_{\mu\nu}'^{(IP_V IP_V \rightarrow M)} |_{bare} + i \Gamma_{\mu\nu}''^{(IP_V IP_V \rightarrow M)}(q_1, q_2) |_{bare} \right) F_{IPVM}(q_1^2, q_2^2)$$

$$F_{IPVM}(t_1, t_2) = F_M(t_1) F_M(t_2), \quad F_M(t) = F_\pi(t) = \frac{1}{1 - t/\Lambda_0^2}, \quad \Lambda_0^2 = 0.5 \text{ GeV}^2$$

The “bare” vertices were obtained from a covariant Lagrangians corresponding to the  $l$  and  $S$  values.



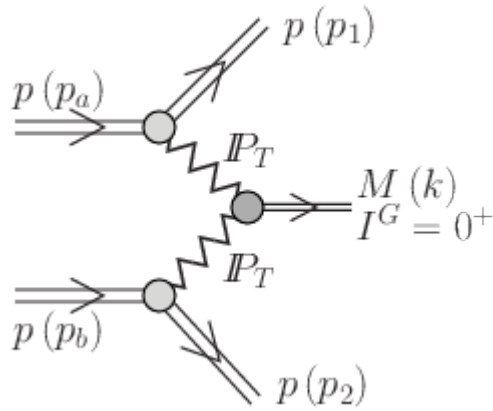
$$J^{PC} = 0^{++} : \quad i \Gamma_{\mu\nu}'^{(IP_V IP_V \rightarrow M)} |_{bare} = i g'_{IP_V IP_V M} M_0 2g_{\mu\nu} \quad \Leftarrow (l, S) = (0, 0) \text{ term}$$

$$i \Gamma_{\mu\nu}''^{(IP_V IP_V \rightarrow M)}(q_1, q_2) |_{bare} = \frac{2i g''_{IP_V IP_V M}}{M_0} [q_{2\mu} q_{1\nu} - (q_1 q_2) g_{\mu\nu}] \quad \Leftarrow (l, S) = (2, 2) \text{ term}$$

$$J^{PC} = 0^{-+} : \quad i \Gamma_{\mu\nu}'^{(IP_V IP_V \rightarrow \tilde{M})}(q_1, q_2) |_{bare} = i \frac{g'_{IP_V IP_V \tilde{M}}}{2M_0} \varepsilon_{\mu\nu\rho\sigma} q_1^\rho q_2^\sigma \quad \Leftarrow (l, S) = (1, 1) \text{ term}$$

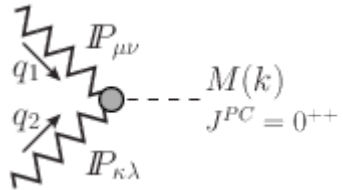
The dimensionless coupling constants  $g_{IP_V IP_V M}$  can be fixed from the meson production data.

# Exclusive production of resonances via $IP_T IP_T$ fusion



$$\begin{aligned} \mathcal{M}_{\lambda_a \lambda_b \rightarrow \lambda_1 \lambda_2 M}^{2 \rightarrow 3} |_{IP_T} &= (-i) \bar{u}(p_1, \lambda_1) i \Gamma_{\mu_1 \nu_1}^{(IP_T PP)}(p_1, p_a) u(p_a, \lambda_a) \\ &\times i \Delta^{(IP_T) \mu_1 \nu_1, \kappa_1 \lambda_1}(s_{13}, t_1) i \Gamma_{\kappa_1 \lambda_1, \kappa_2 \lambda_2}^{(IP_T IP_T \rightarrow M)}(q_1, q_2) i \Delta^{(IP_T) \kappa_2 \lambda_2, \mu_2 \nu_2}(s_{23}, t_2) \\ &\times \bar{u}(p_2, \lambda_2) i \Gamma_{\mu_2 \nu_2}^{(IP_T PP)}(p_2, p_b) u(p_b, \lambda_b) \end{aligned}$$

$$i \Gamma_{\mu\nu, \kappa\lambda}^{(IP_T IP_T \rightarrow M)}(q_1, q_2) = \left( i \Gamma_{\mu\nu, \kappa\lambda}'^{(IP_T IP_T \rightarrow M)} |_{bare} + i \Gamma_{\mu\nu, \kappa\lambda}''^{(IP_T IP_T \rightarrow M)}(q_1, q_2) |_{bare} \right) F_{IPM}(q_1^2, q_2^2)$$



$$\begin{aligned} J^{PC} = 0^{++} : i \Gamma_{\mu\nu, \kappa\lambda}'^{(IP_T IP_T \rightarrow M)} |_{bare} &= i g'_{IP_T IP_T M} M_0 \left( g_{\mu\kappa} g_{\nu\lambda} + g_{\mu\lambda} g_{\nu\kappa} - \frac{1}{2} g_{\mu\nu} g_{\kappa\lambda} \right) \Leftarrow (l, S) = (0, 0) \text{ term} \\ i \Gamma_{\mu\nu, \kappa\lambda}''^{(IP_T IP_T \rightarrow M)}(q_1, q_2) |_{bare} &= \frac{i g''_{IP_T IP_T M}}{2M_0} [q_{1\kappa} q_{2\mu} g_{\nu\lambda} + q_{1\kappa} q_{2\nu} g_{\mu\lambda} + q_{1\lambda} q_{2\mu} g_{\nu\kappa} + q_{1\lambda} q_{2\nu} g_{\mu\kappa} - 2(q_1 q_2)(g_{\mu\kappa} g_{\nu\lambda} + g_{\nu\kappa} g_{\mu\lambda})] \Leftarrow (2, 2) \end{aligned}$$

$$\begin{aligned} J^{PC} = 0^{-+} : i \Gamma_{\mu\nu, \kappa\lambda}'^{(IP_T IP_T \rightarrow \tilde{M})}(q_1, q_2) |_{bare} &= i \frac{g'_{IP_T IP_T \tilde{M}}}{2M_0} (g_{\mu\kappa} \varepsilon_{\nu\lambda\rho\sigma} + g_{\nu\kappa} \varepsilon_{\mu\lambda\rho\sigma} + g_{\mu\lambda} \varepsilon_{\nu\kappa\rho\sigma} + g_{\nu\lambda} \varepsilon_{\mu\kappa\rho\sigma}) (q_1 - q_2)^\rho k^\sigma \Leftarrow (1, 1) \\ i \Gamma_{\mu\nu, \kappa\lambda}''^{(IP_T IP_T \rightarrow \tilde{M})}(q_1, q_2) |_{bare} &= i \frac{g''_{IP_T IP_T \tilde{M}}}{M_0^3} \{ \varepsilon_{\nu\lambda\rho\sigma} [q_{1\kappa} q_{2\mu} - (q_1 q_2) g_{\mu\kappa}] + \varepsilon_{\mu\lambda\rho\sigma} [q_{1\kappa} q_{2\nu} - (q_1 q_2) g_{\nu\kappa}] \\ &\quad + \varepsilon_{\nu\kappa\rho\sigma} [q_{1\lambda} q_{2\mu} - (q_1 q_2) g_{\mu\lambda}] + \varepsilon_{\mu\kappa\rho\sigma} [q_{1\lambda} q_{2\nu} - (q_1 q_2) g_{\nu\lambda}] \} (q_1 - q_2)^\rho k^\sigma \Leftarrow (3, 3) \end{aligned}$$

# $IP_V IP_V$ fusion vs $IP_T IP_T$ fusion

We shall now consider the **high-energy small-angle limit** for both the tensorial and vectorial pomeron fusion reactions giving the mesons  $M$  and  $\tilde{M}$ .

$$\left. \begin{aligned} |t_1|, |t_2| &\ll m_p^2, & m_M^2 &\ll s, & \xi_1, \xi_2 &= \mathcal{O}(m_M/\sqrt{s}) \\ \xi_1 &\cong \frac{s_{23}}{s}, & \xi_2 &\cong \frac{s_{13}}{s}, & m_M^2 &\cong s\xi_1\xi_2 = \frac{s_{13}s_{23}}{s}, & t_1 &\cong -\vec{q}_{1\perp}^2, & t_2 &\cong -\vec{q}_{2\perp}^2; \\ \bar{u}(p_1, \lambda_1)\gamma^\mu u(p_a, \lambda_a) &\cong (p_1 + p_a)^\mu \delta_{\lambda_1\lambda_a} \\ \bar{u}(p_2, \lambda_2)\gamma^\mu u(p_b, \lambda_b) &\cong (p_2 + p_b)^\mu \delta_{\lambda_2\lambda_b} \end{aligned} \right\} s_{13}, s_{23} = \mathcal{O}(m_M\sqrt{s})$$

$$\begin{aligned} \mathcal{M}_{\lambda_a\lambda_b \rightarrow \lambda_1\lambda_2 M}^{2 \rightarrow 3} |_{IP_T IP_T} &\cong -2s (3\beta_{IPNN})^2 F_1(t_1) F_1(t_2) F_{IPPM}(t_1, t_2) \\ &\times \frac{M_0}{m_M^2} \left( g'_{IP_T IP_T M} + g''_{IP_T IP_T M} \frac{1}{M_0^2} |\vec{p}_{1\perp}| |\vec{p}_{2\perp}| \cos \phi_{pp} \right) \\ &\times (-is_{13}\alpha'_{IP})^{\alpha_P(t_1)-1} (-is_{23}\alpha'_{IP})^{\alpha_P(t_2)-1} \\ &\times \delta_{\lambda_1\lambda_a} \delta_{\lambda_2\lambda_b} \end{aligned} \quad (1)$$

$$\begin{aligned} \mathcal{M}_{\lambda_a\lambda_b \rightarrow \lambda_1\lambda_2 \tilde{M}}^{2 \rightarrow 3} |_{IP_T IP_T} &\cong -2s (3\beta_{IPNN})^2 F_1(t_1) F_1(t_2) F_{IP\tilde{M}}(t_1, t_2) \\ &\times \frac{2}{m_{\tilde{M}}^2 M_0} |\vec{p}_{1\perp}| |\vec{p}_{2\perp}| \sin \phi_{pp} \left( g'_{IP_T IP_T \tilde{M}} + g''_{IP_T IP_T \tilde{M}} \frac{2}{M_0^2} |\vec{p}_{1\perp}| |\vec{p}_{2\perp}| \cos \phi_{pp} \right) \\ &\times (-is_{13}\alpha'_{IP})^{\alpha_P(t_1)-1} (-is_{23}\alpha'_{IP})^{\alpha_P(t_2)-1} \\ &\times \delta_{\lambda_1\lambda_a} \delta_{\lambda_2\lambda_b} \end{aligned} \quad (2)$$

For the vectorial pomeron we get in this limit the expressions (1) and (2), respectively, but with the replacements:

$$\begin{aligned} g'_{IP_T IP_T M} &\rightarrow \frac{2m_M^2}{M_0^2} g'_{IP_V IP_V M}, & g''_{IP_T IP_T M} &\rightarrow \frac{2m_M^2}{M_0^2} g''_{IP_V IP_V M}, \\ g'_{IP_T IP_T \tilde{M}} &\rightarrow \frac{m_{\tilde{M}}^2}{4M_0^2} g'_{IP_V IP_V \tilde{M}}, & g''_{IP_T IP_T \tilde{M}} &\rightarrow 0 \end{aligned}$$

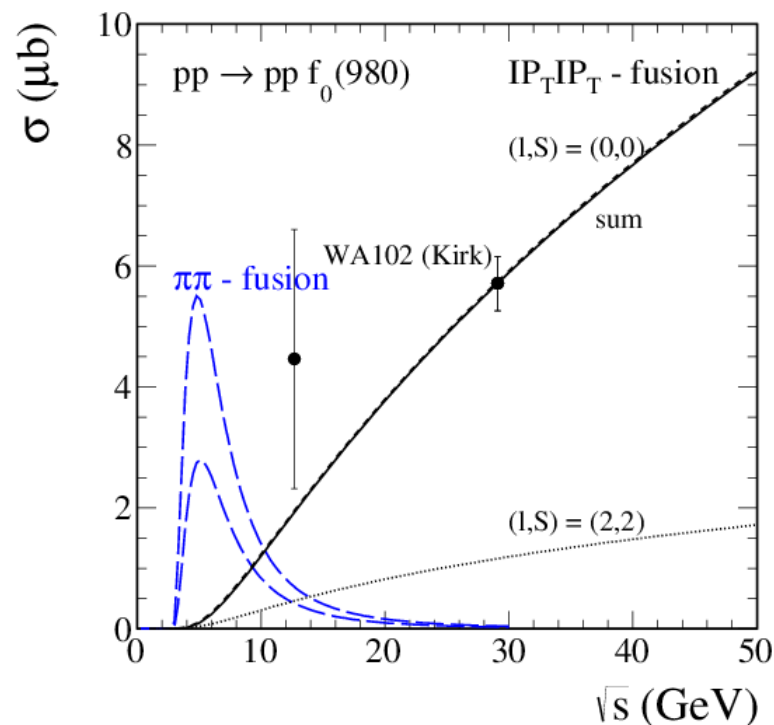
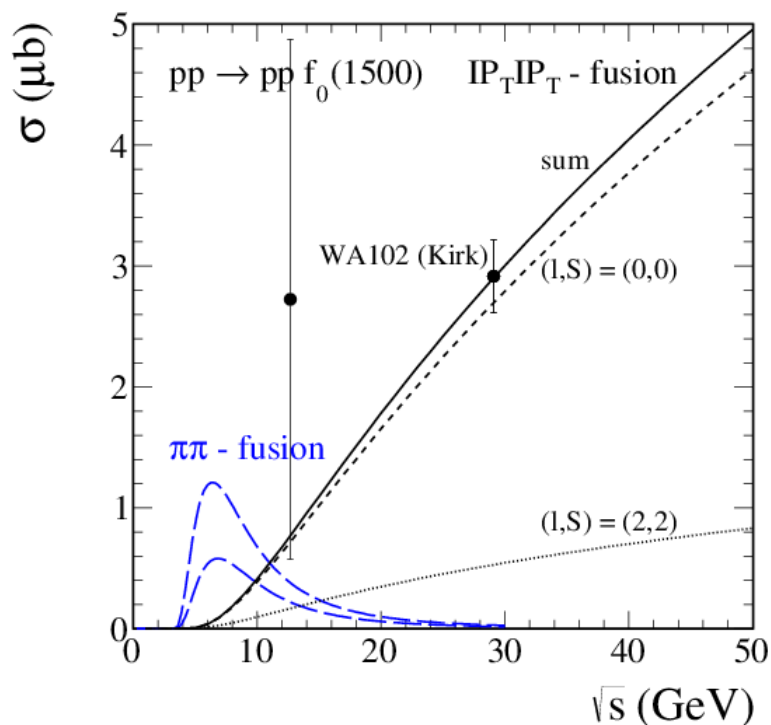
We see that for the vectorial pomeron the term  $\propto \cos \phi_{pp} \sin \phi_{pp}$  in (2) is absent.



Experimental results (WA102) for total cross sections of scalar mesons in  $pp$  collisions (29.1 GeV)

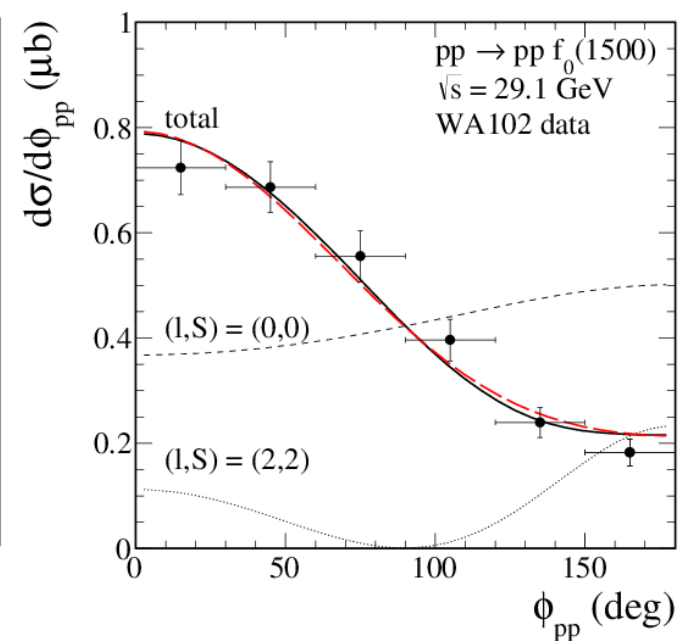
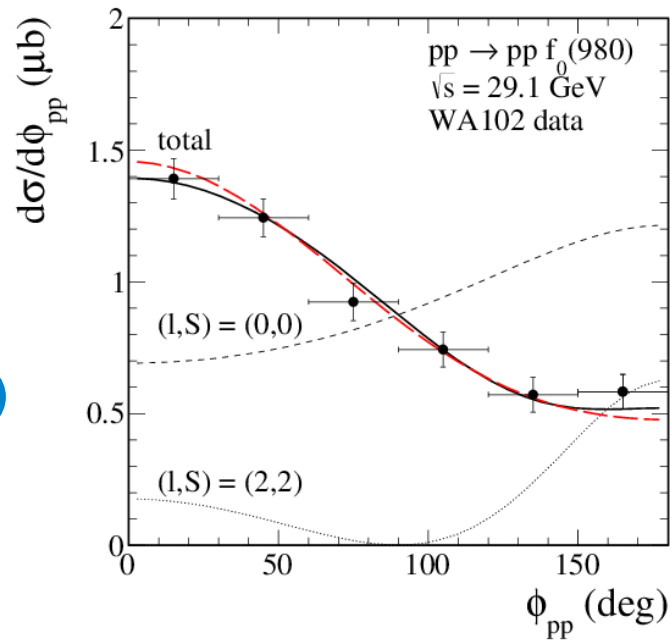
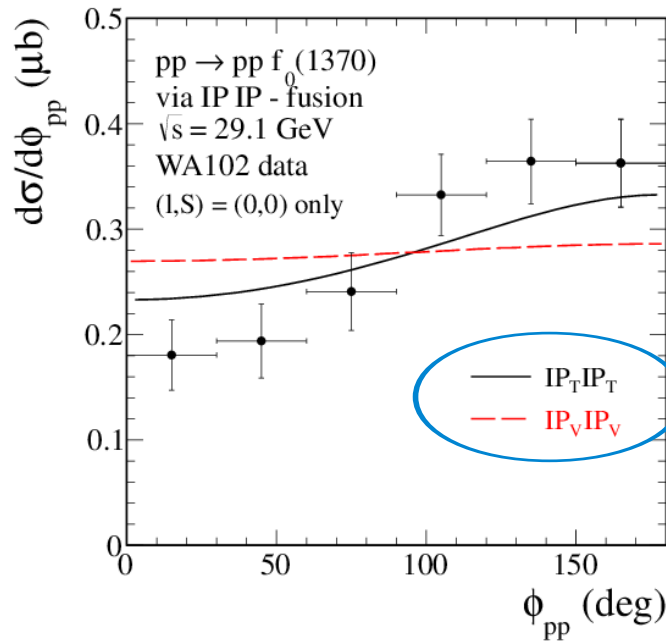
*A. Kirk, Phys. Lett. B489 (2000) 29*

	$f_0(980)$	$f_0(1370)$	$f_0(1500)$	$f_0(1710)$	$f_0(2000)$
$\sigma(\mu\text{b})$	$5.71 \pm 0.45$	$1.75 \pm 0.58$	$2.91 \pm 0.30$	$0.25 \pm 0.07$	$3.14 \pm 0.48$



$\pi\pi$  - fusion mechanism  $\rightarrow$  *A. Szczurek and P. L., Nucl. Phys. A826 (2009) 101, arXiv:0906.0286*

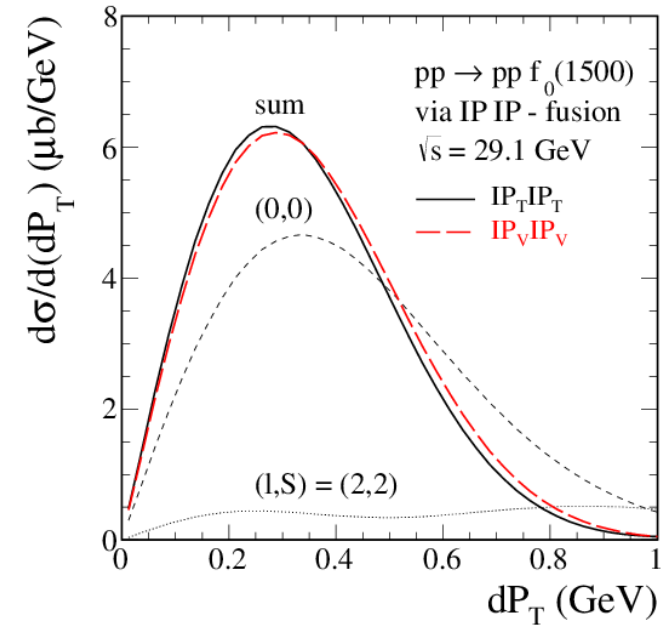
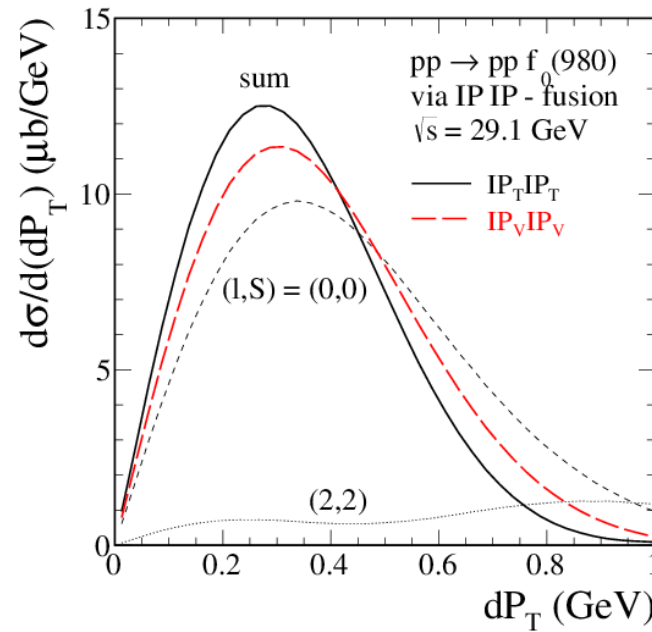
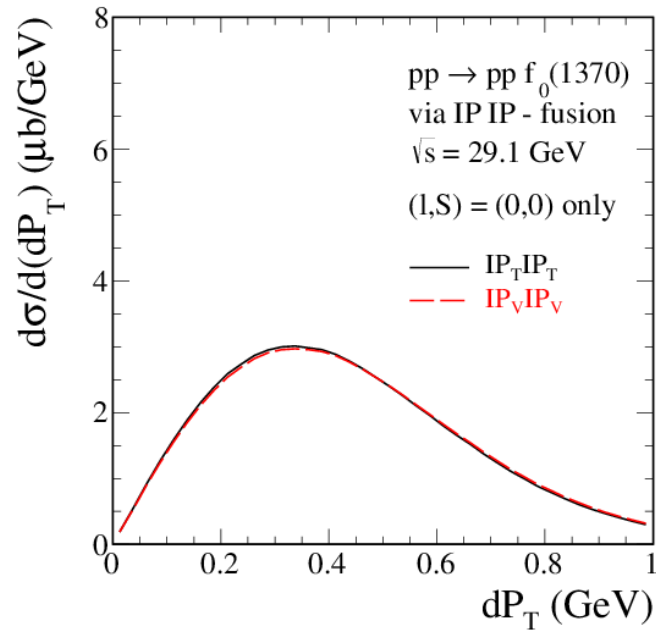
Our results and the WA102 exp. distributions have been normalized to the value of total cross sections given by Kirk.

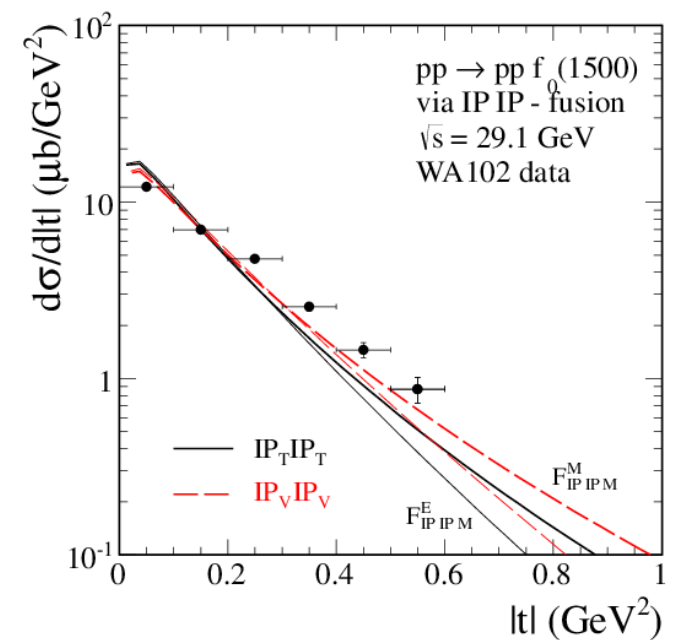
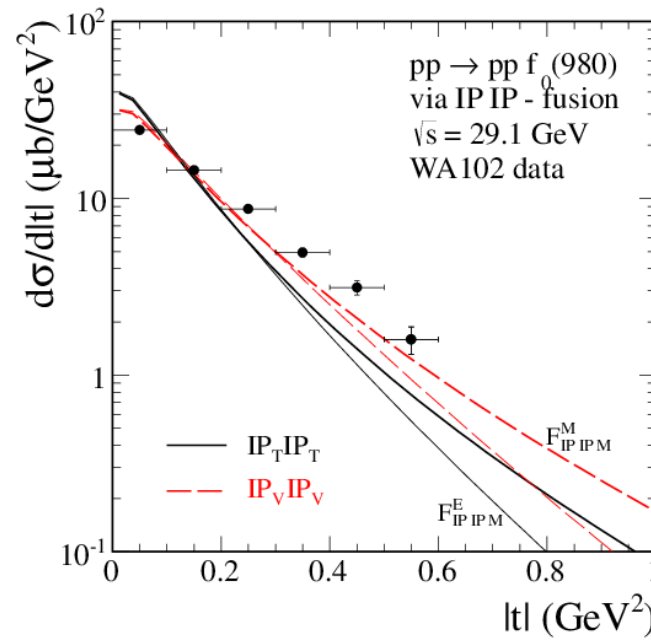
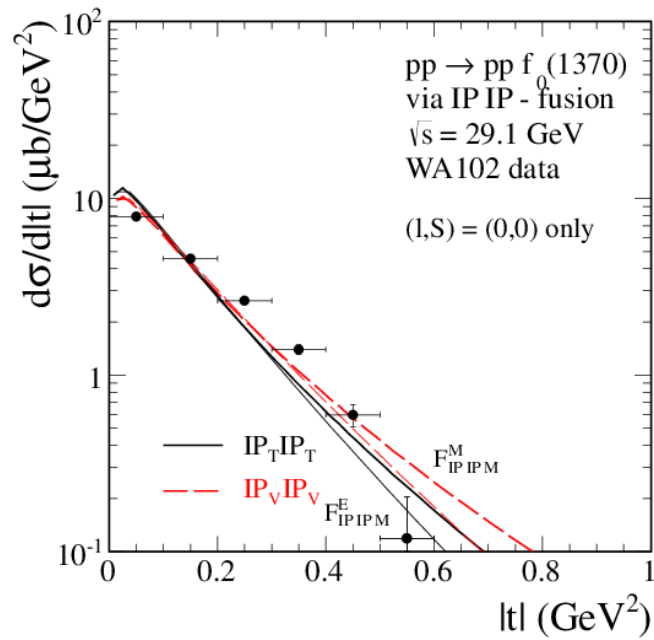


For  $f_0(1370)$  the tensorial pomeron with the  $(l, S) = (0, 0)$  coupling alone already describes data. The vectorial pomeron term is disfavoured here.

The “glueball filter” variable  $dP_{\perp} = |d\vec{P}_{\perp}| = |\vec{q}_{1\perp} - \vec{q}_{2\perp}| = |\vec{p}_{2\perp} - \vec{p}_{1\perp}|$

*F. E. Close and A. Kirk, Phys. Lett. B397 (1997) 333*

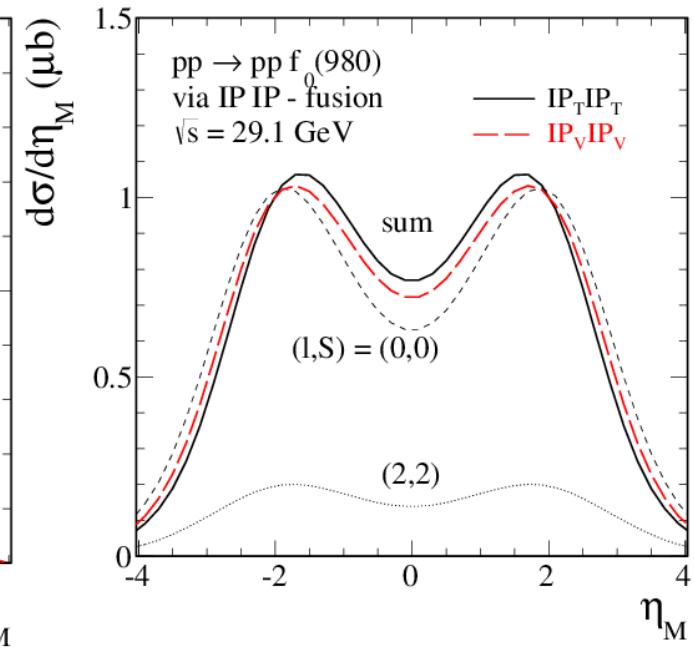
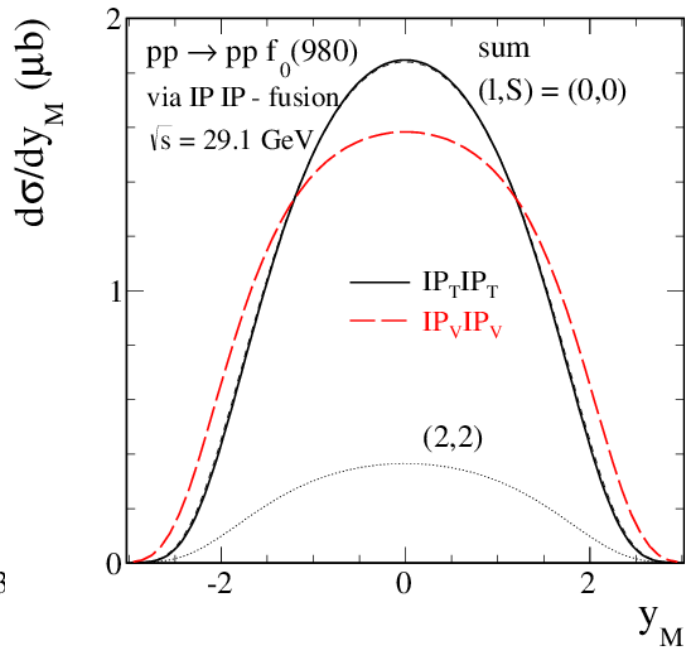
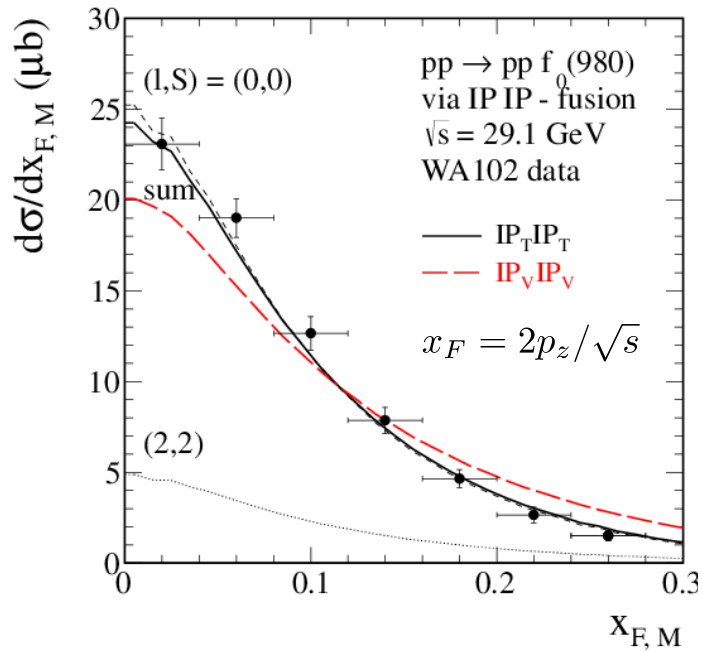




$$F_{IPM}^M(t_1, t_2) = F_M(t_1)F_M(t_2), \quad F_M(t) = F_\pi(t) = \frac{1}{1 - t/\Lambda_0^2}, \quad \Lambda_0^2 = 0.5 \text{ GeV}^2$$

$$F_{IPM}^E(t_1, t_2) = \exp\left(\frac{t_1 + t_2}{\Lambda_E^2}\right), \quad \Lambda_E^2 = 0.64 \text{ GeV}^2$$

# $J^{PC} = 0^{++}$ $x_{F,M}$ , $y_M$ and $\eta_M$ distributions



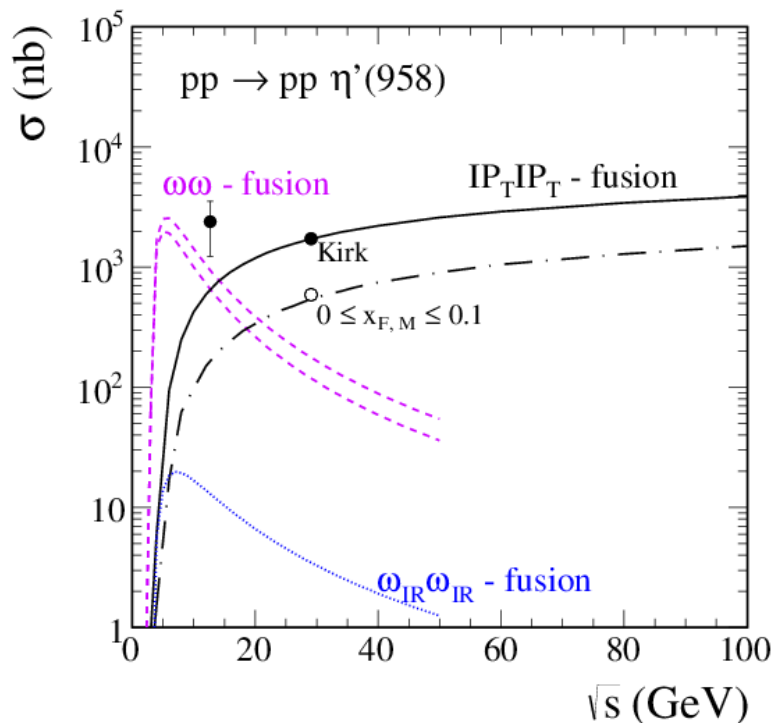
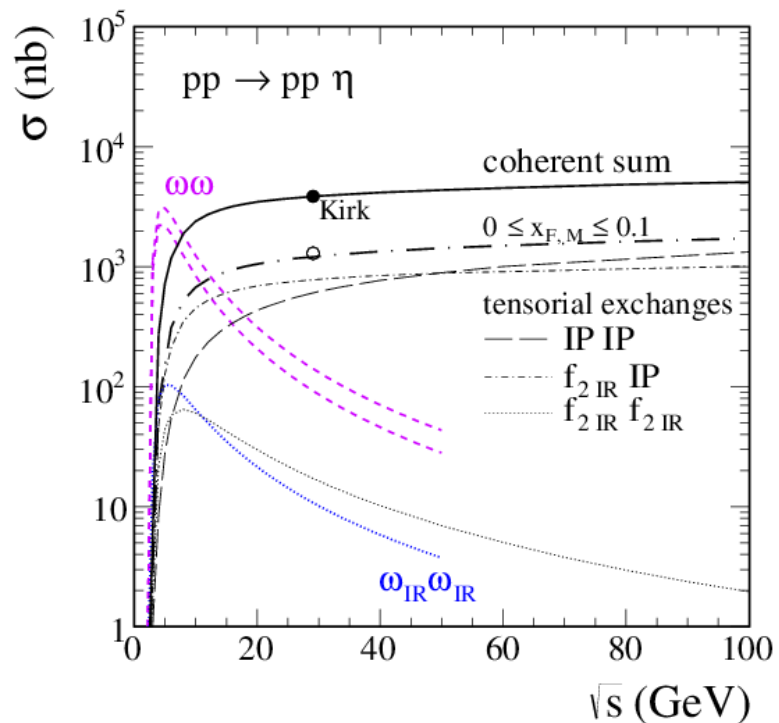
The dip in the  $\eta_M$  distribution for  $|\eta_M| \rightarrow 0$  is a kinematic effect.

Exp. results (WA102) for total cross sections of pseudoscalar mesons in  $pp$  collisions (29.1 GeV)

A. Kirk, *Phys. Lett. B*489 (2000) 29

$$\sigma(\eta) = 3.86 \pm 0.37 \mu\text{b}$$

$$\sigma(\eta') = 1.72 \pm 0.18 \mu\text{b}$$

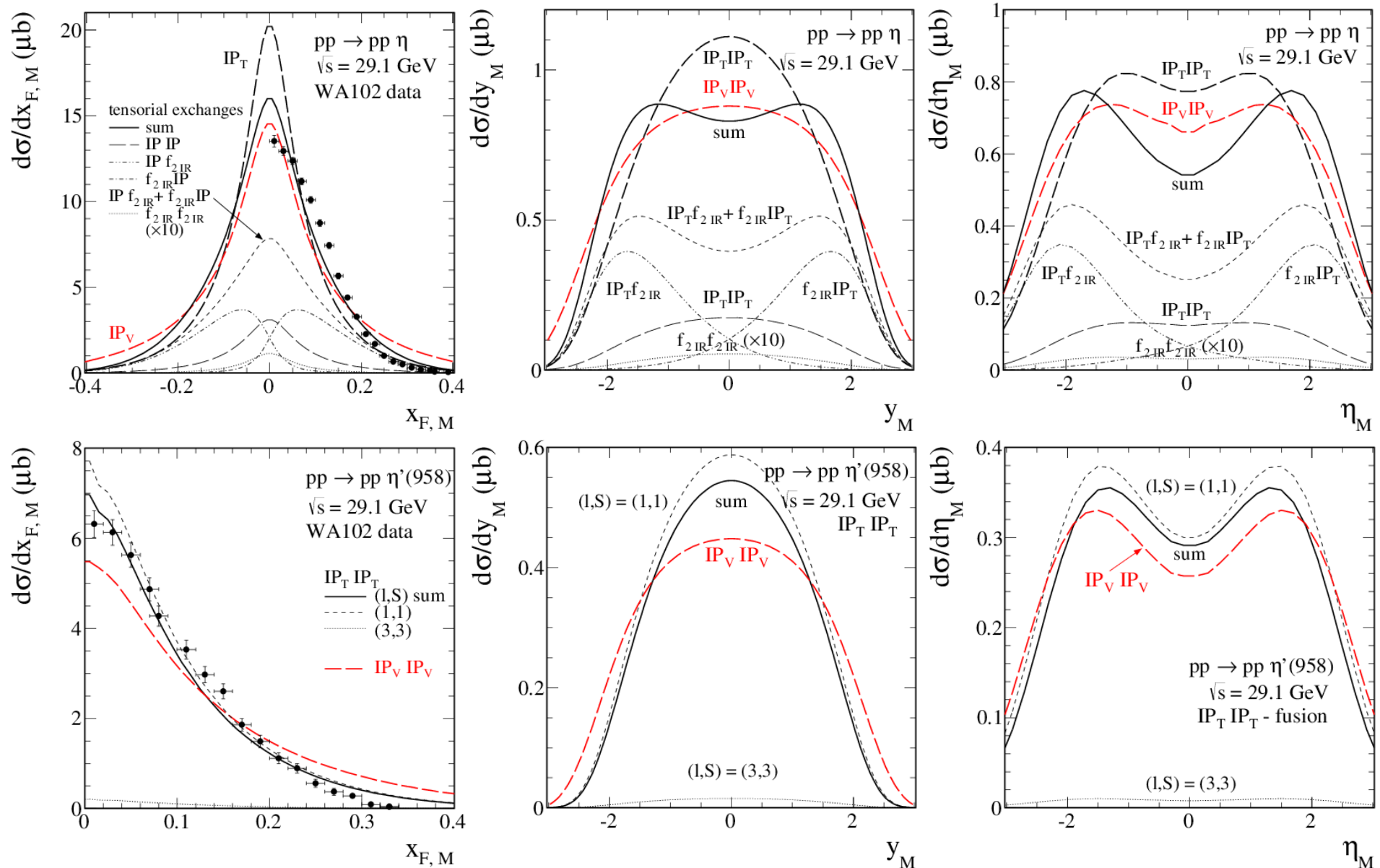


For  $\eta$  production we included subleading exchanges (reggeon-pomeron, pomeron-reggeon, and reggeon-reggeon) which improve the agreement with experimental data.

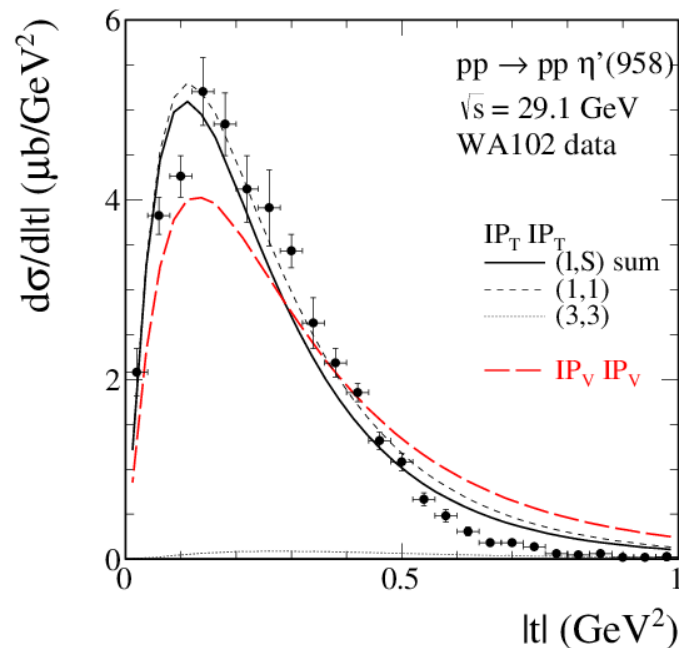
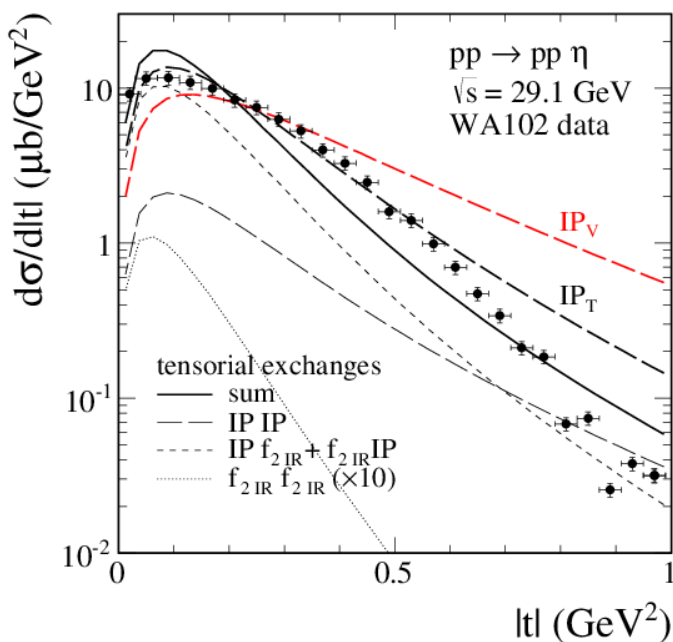
Production of  $\eta'$  seems to be less affected by contributions from subleading exchanges.

# $J^{PC} = 0^{-+}$ $X_{F,M}$ , $y_M$ and $\eta_M$ distributions

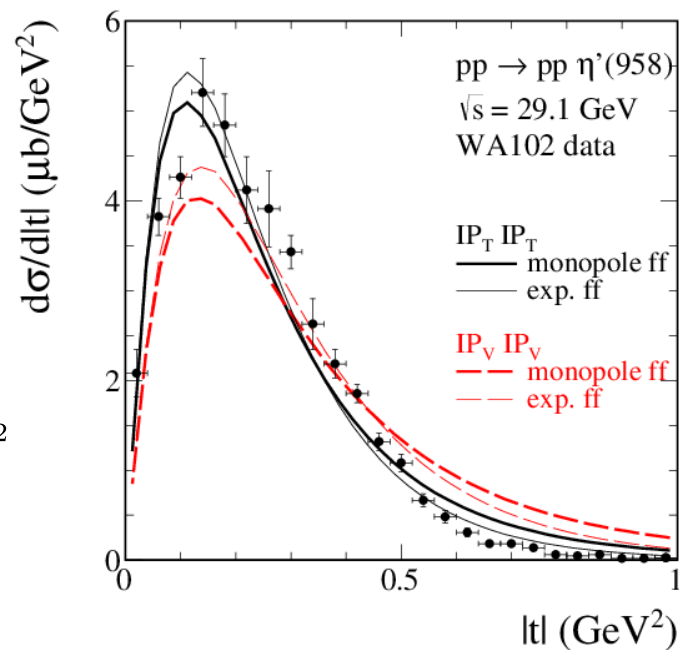
Our results and the WA102 exp. distributions have been normalized to the value of total cross sections given by Kirk.



For  $\eta$  meson the enhancement of distributions at larger values of  $x_{F,M}$  or  $y_M$  can be explained by the pomeron-reggeon exchanges



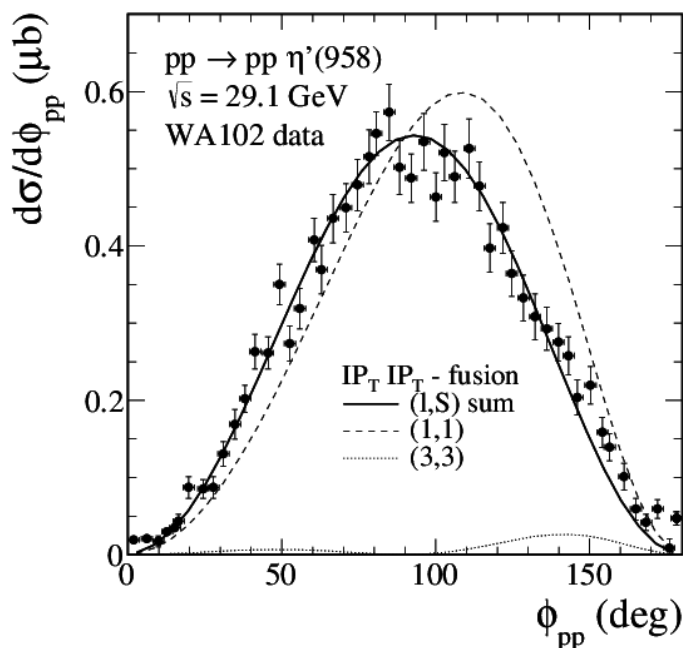
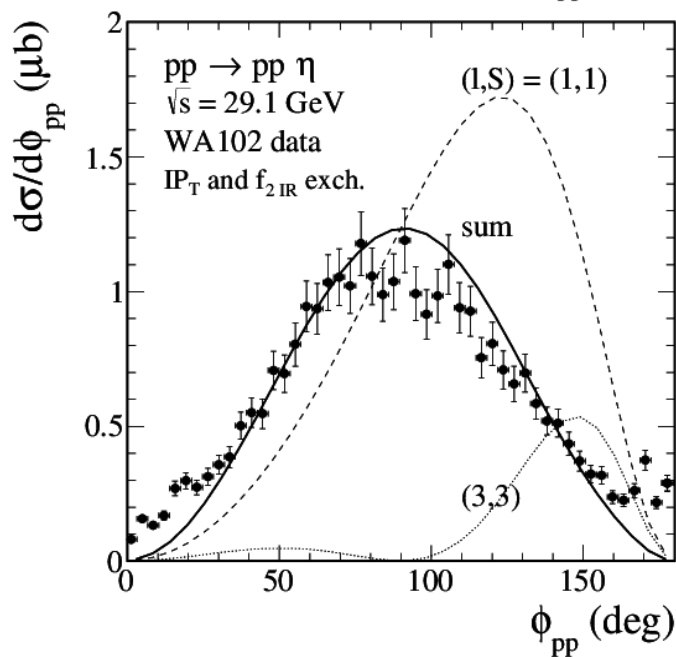
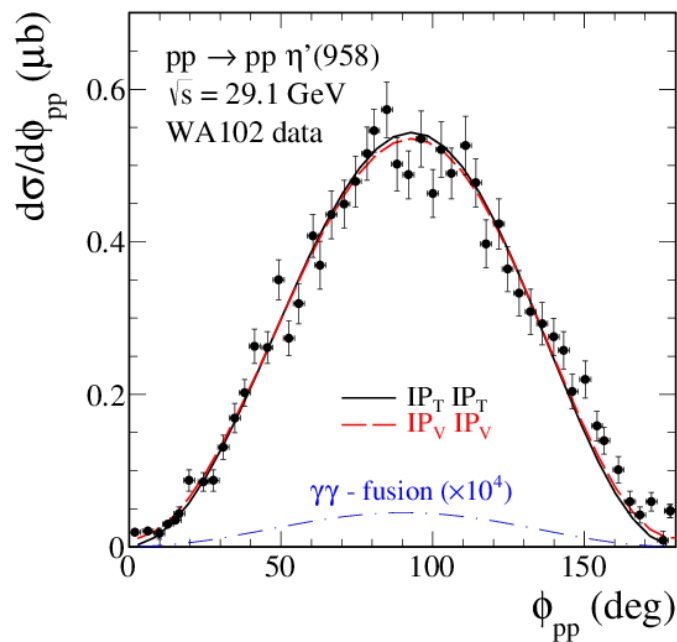
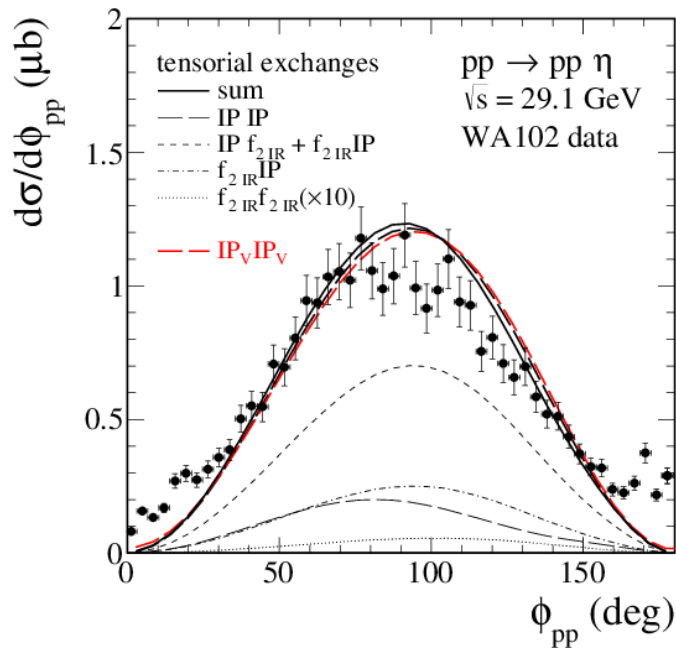
The vectorial pomeron term is disfavoured here.

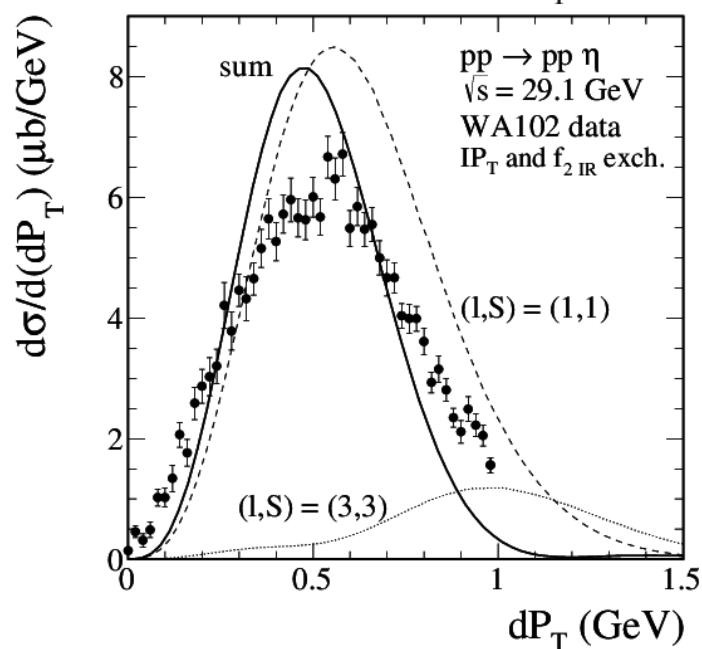
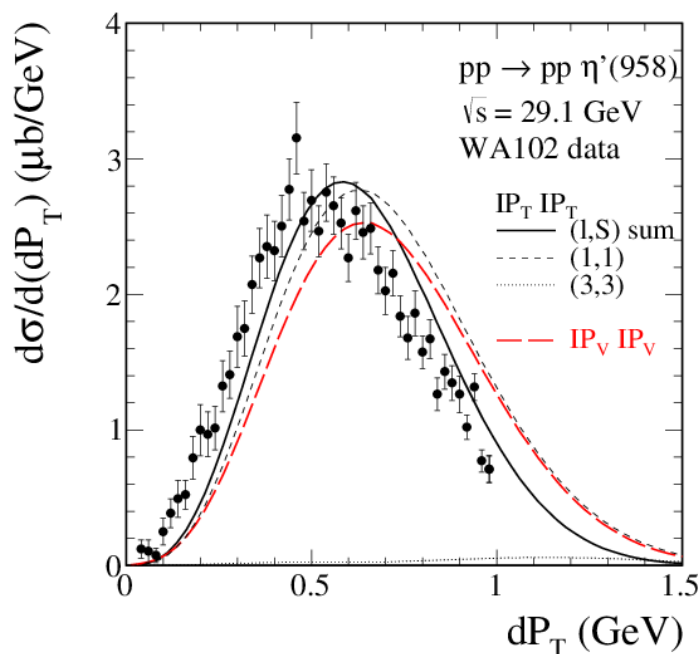
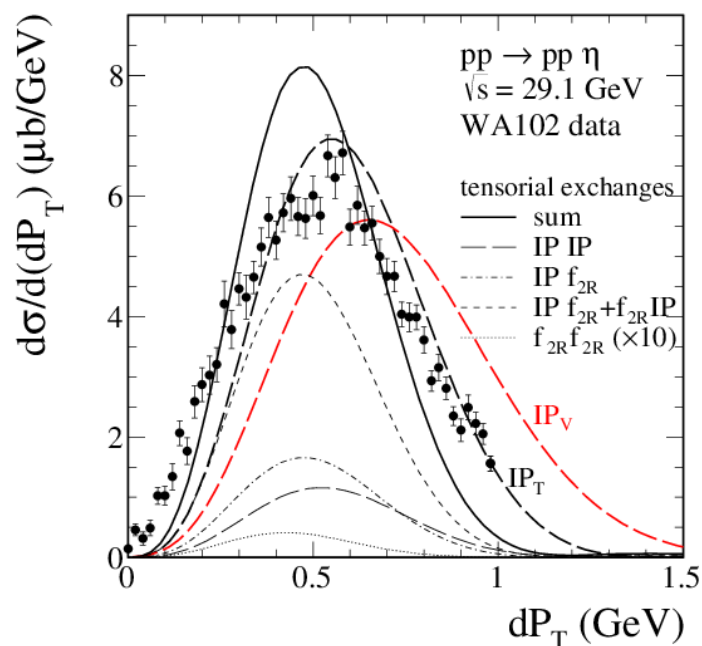


$$F_{IPM}^M(t_1, t_2) = F_M(t_1)F_M(t_2), \quad F_M(t) = F_\pi(t) = \frac{1}{1 - t/\Lambda_0^2}, \quad \Lambda_0^2 = 0.5 \text{ GeV}^2$$

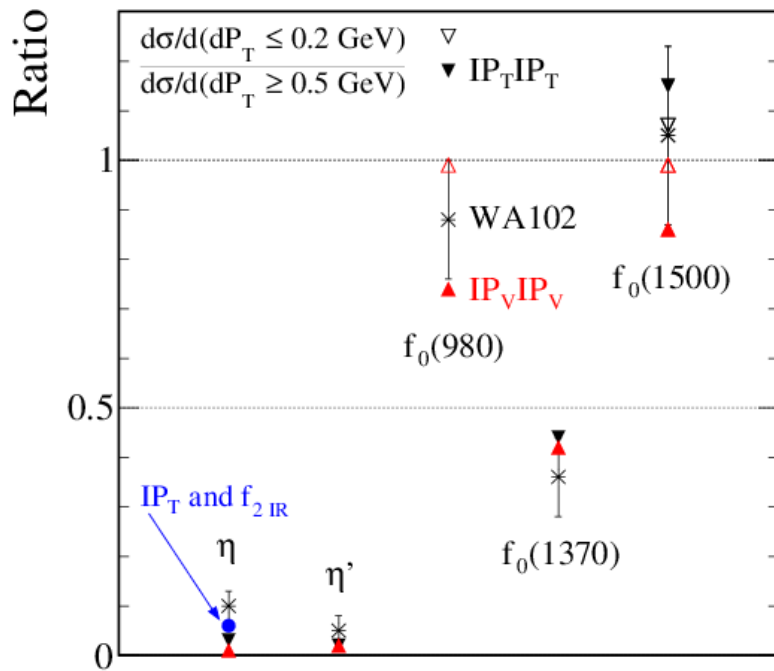
$$F_{IPM}^E(t_1, t_2) = \exp\left(\frac{t_1 + t_2}{\Lambda_E^2}\right), \quad \Lambda_E^2 = 0.64 \text{ GeV}^2$$







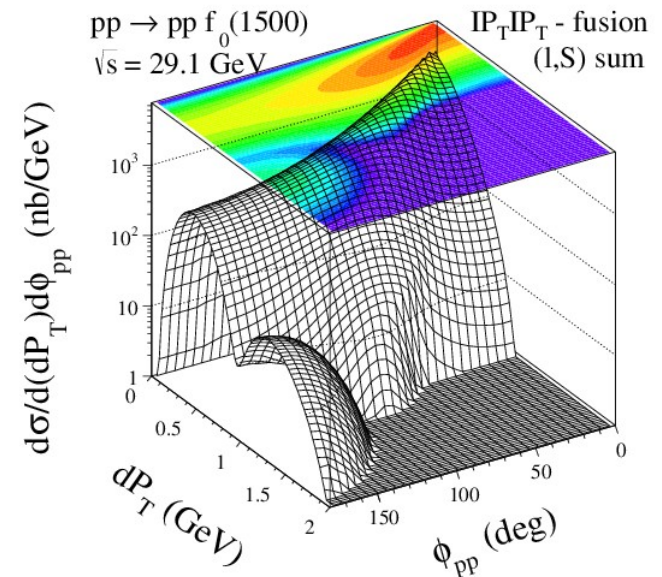
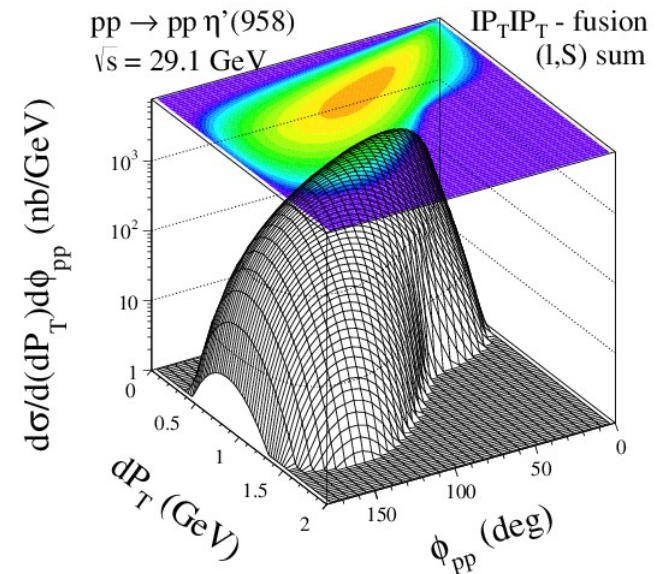
$$dP_{\perp} = |d\vec{P}_{\perp}| = |\vec{q}_{1\perp} - \vec{q}_{2\perp}| = |\vec{p}_{2\perp} - \vec{p}_{1\perp}|$$



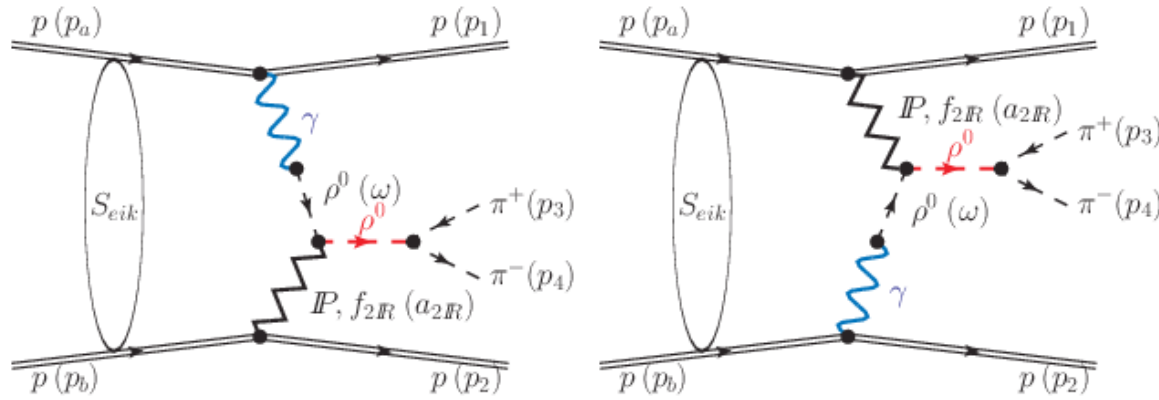
The ratio of mesons production at small  $dP_{\perp}$  to large  $dP_{\perp}$  for two models has been compared with the exp. results from [A. Kirk, Phys. Lett. B489 \(2000\) 29](#).

It was observed that all undisputed  $q\bar{q}$  states ( $\eta$ ,  $\eta'$ ,  $f_1(1285)$  etc.) are suppressed as  $dP_{\perp} \rightarrow 0$ , whereas the glueball candidates (e.g.  $f_0(1500)$ ,  $f_2(1950)$ ) are prominent.

The  $dP_{\perp}$  and  $\phi_{pp}$  effects  
 → in general more than one coupling structure  $IP IP M$  is possible.



# The $\rho^0$ contribution to CEP of $\pi^+\pi^-$ pairs in $pp$ collisions



$$\mathcal{M}^{(P\text{-wave})} = \mathcal{M}^{\gamma P} + \mathcal{M}^{P\gamma} + \mathcal{M}^{\gamma f_{2R}} + \mathcal{M}^{f_{2R}\gamma}$$

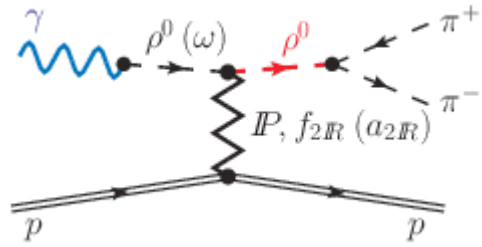
in the Born approximation

$$\begin{aligned} \mathcal{M}_{\lambda_a \lambda_b \rightarrow \lambda_1 \lambda_2 \pi^+ \pi^-}^{\gamma P} &= \bar{u}(p_1, \lambda_1) i\Gamma_{\mu}^{(\gamma pp)}(p_1, p_a) u(p_a, \lambda_a) i\Delta^{(\gamma) \mu\sigma}(q_1) i\Gamma_{\sigma\nu}^{(\gamma \rightarrow \rho)}(q_1) i\Delta^{(\rho) \nu\rho_1}(q_1) i\Delta^{(\rho) \rho_2\kappa}(p_{34}) i\Gamma_{\kappa}^{(\rho\pi\pi)}(p_3, p_4) \\ &\times i\Gamma_{\rho_1\rho_2\alpha\beta}^{(P\rho\rho)}(-q_1, -p_{34}) i\Delta^{(P) \alpha\beta\delta\eta}(s_2, t_2) \bar{u}(p_2, \lambda_2) i\Gamma_{\delta\eta}^{(Ppp)}(p_2, p_b) u(p_b, \lambda_b) \end{aligned}$$

$$\begin{aligned} \mathcal{M}_{\lambda_a \lambda_b \rightarrow \lambda_1 \lambda_2 \pi^+ \pi^-}^{\gamma P, \gamma f_{2R}} &\cong \pm e(p_1 + p_a)^\mu F_1(t_1) \delta_{\lambda_1 \lambda_a} \\ &\times e \frac{m_\rho^2}{\gamma_\rho} \frac{1}{t_1} \Delta_{\mu\rho_1}^{(\rho)}(q_1) \Delta_{\rho_2\kappa}^{(\rho)}(p_{34}) \frac{g_{\rho\pi\pi}}{2} (p_3 - p_4)^\kappa F_{\rho\pi\pi}(s_{34}) F_{\rho\pi\pi}(s_{34}) \\ &\times V^{\rho_1\rho_2\alpha\beta}(s_2, t_2) 2(p_2 + p_b)_\alpha (p_2 + p_b)_\beta F_M(t_2) F_1(t_2) \delta_{\lambda_2 \lambda_b} \end{aligned}$$

where the decay vertex for  $\rho \rightarrow \pi^+\pi^-$  is well known and the coupling constant is  $g_{\rho\pi\pi} = 11.51$

# Photoproduction of $\rho^0$ meson



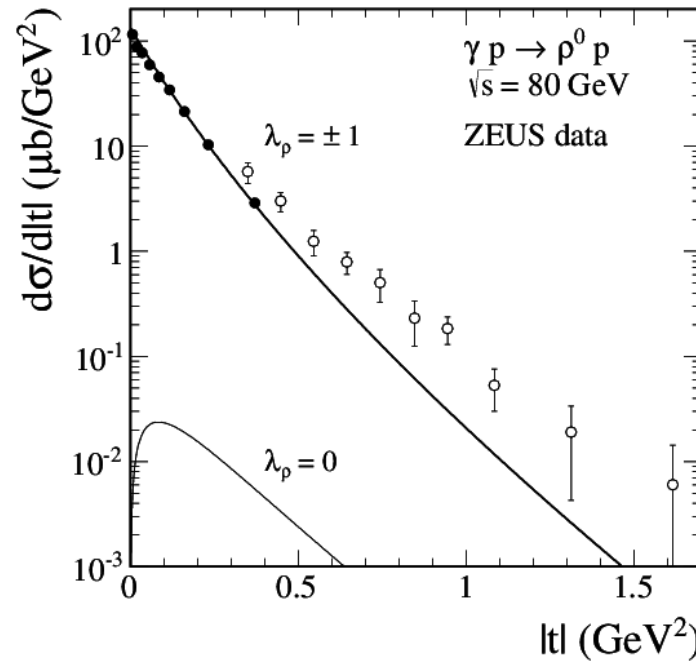
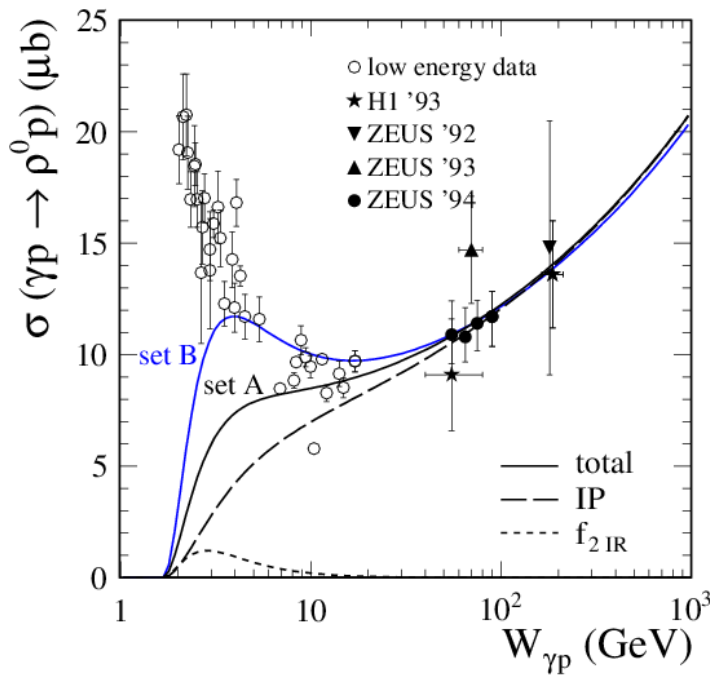
$$\mathcal{M}_{\lambda_\gamma \lambda_b \rightarrow \lambda_\rho \lambda_2}^{\gamma p \rightarrow \rho^0 p}(s, t) \cong c^{(\gamma \rightarrow \rho)} (\Delta_T^{(\rho)})^{-1} \epsilon_\gamma^\mu (\epsilon_\rho^\nu)^* V_{\mu\nu\kappa\lambda}(s, t) (p_2 + p_b)^\kappa (p_2 + p_b)^\lambda 2\delta_{\lambda_2 \lambda_b} F_1(t) F_M(t)$$

$$\text{where } c^{(\gamma \rightarrow \rho)} = -iem_\rho^2/\gamma_\rho, 4\pi/\gamma_\rho^2 = 0.496, \Delta_T^{(\rho)} = -m_\rho^2 + im_\rho\Gamma_{\rho, \text{tot}}$$

$$g_{f_{2R}PP} = 11.04$$

$$V_{\mu\nu\kappa\lambda}(s, t) = \frac{1}{4s} \left\{ 2\Gamma_{\mu\nu\kappa\lambda}^{(0)}(-p_\gamma, p_\rho) \left[ 3\beta_{PNN} a_{P\rho\rho} (-is\alpha'_{IP})^{\alpha_{IP}(t)-1} + M_0^{-1} g_{f_{2R}PP} a_{f_{2R}\rho\rho} (-is\alpha'_{IR})^{\alpha_{IR}(t)-1} \right] \right. \\ \left. - \Gamma_{\mu\nu\kappa\lambda}^{(2)}(-p_\gamma, p_\rho) \left[ 3\beta_{PNN} b_{P\rho\rho} (-is\alpha'_{IP})^{\alpha_{IP}(t)-1} + M_0^{-1} g_{f_{2R}PP} b_{f_{2R}\rho\rho} (-is\alpha'_{IR})^{\alpha_{IR}(t)-1} \right] \right\}$$

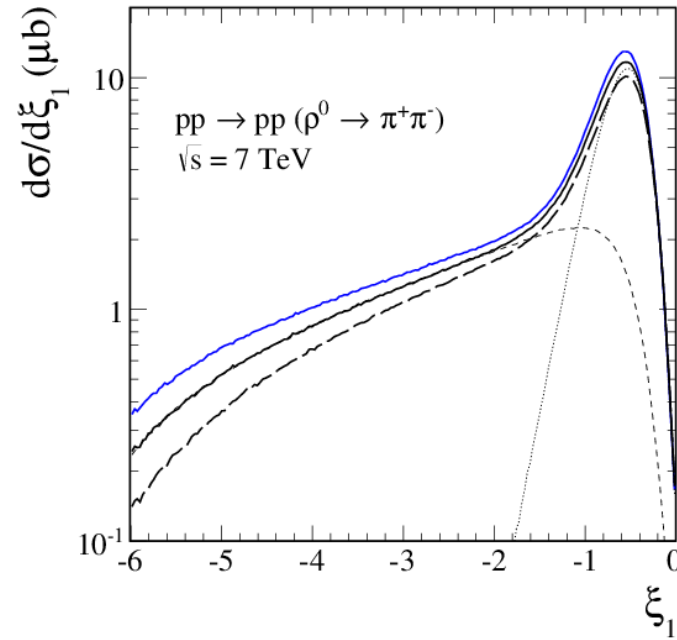
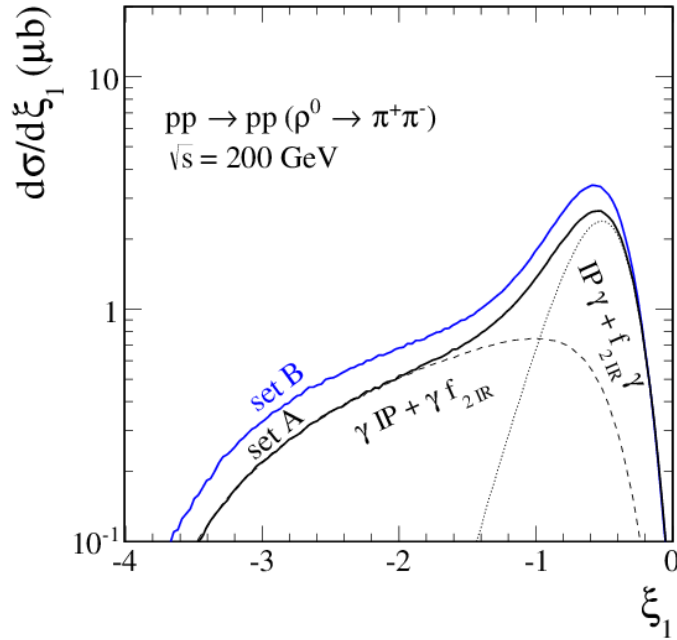
where two rank-four tensor functions: *C. Ewerz, M. Maniatis and O. Nachtmann, Ann. Phys. 342 (2014) 31*



$$\text{set A : } a_{P\rho\rho} = 0.45 \text{ GeV}^{-3}, a_{f_{2R}\rho\rho} = 2.91 \text{ GeV}^{-3}, b_{P\rho\rho} = 6.50 \text{ GeV}^{-1}, b_{f_{2R}\rho\rho} = 5.80 \text{ GeV}^{-1} \quad (\text{default values})$$

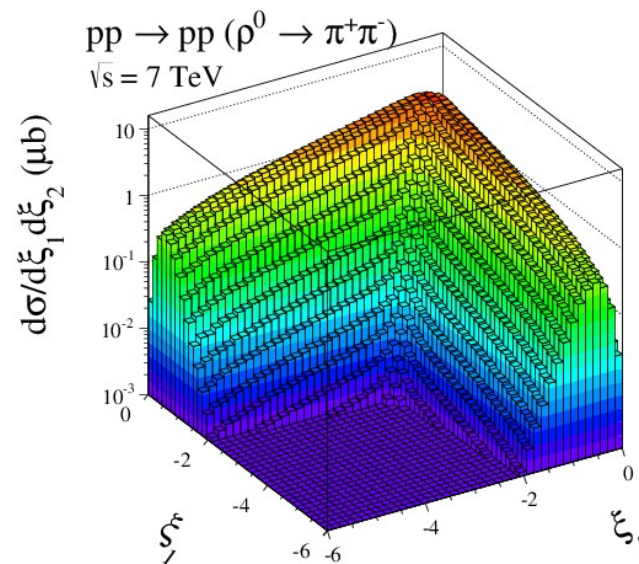
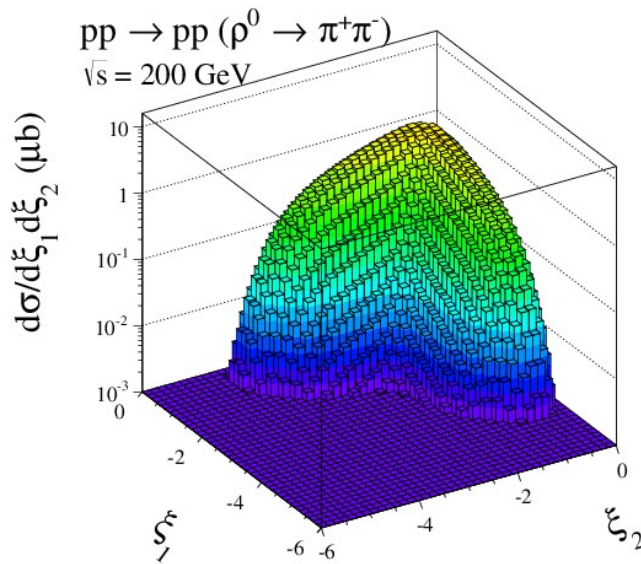
$$\text{set B : } a_{P\rho\rho} = a_{f_{2R}\rho\rho} = 0 \text{ GeV}^{-3}, b_{P\rho\rho} = 6.70 \text{ GeV}^{-1}, b_{f_{2R}\rho\rho} = 14.50 \text{ GeV}^{-1}$$

# $\xi$ distribution

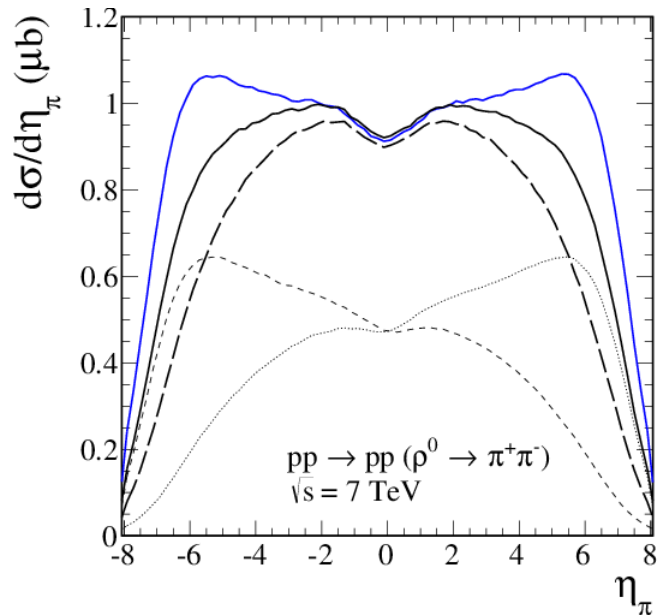
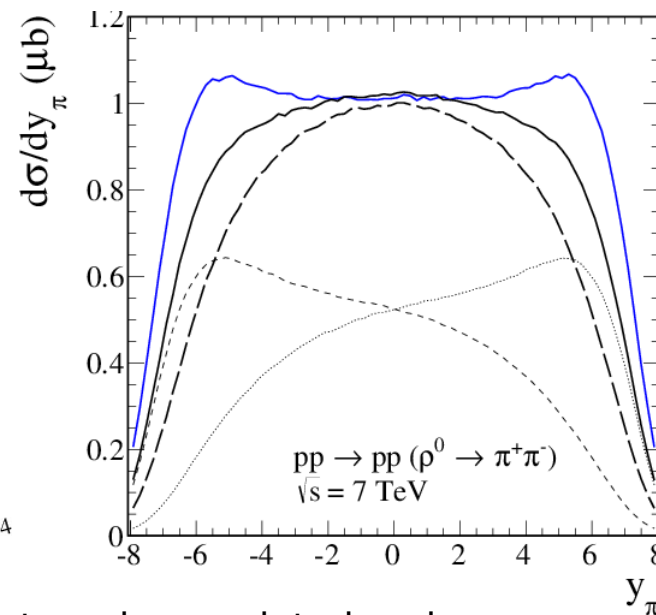
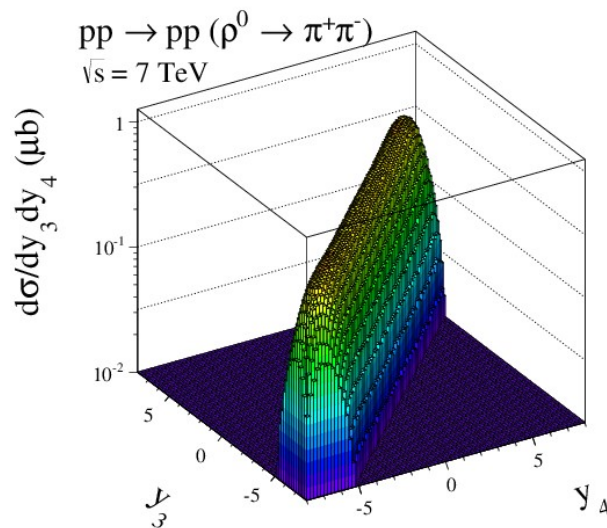
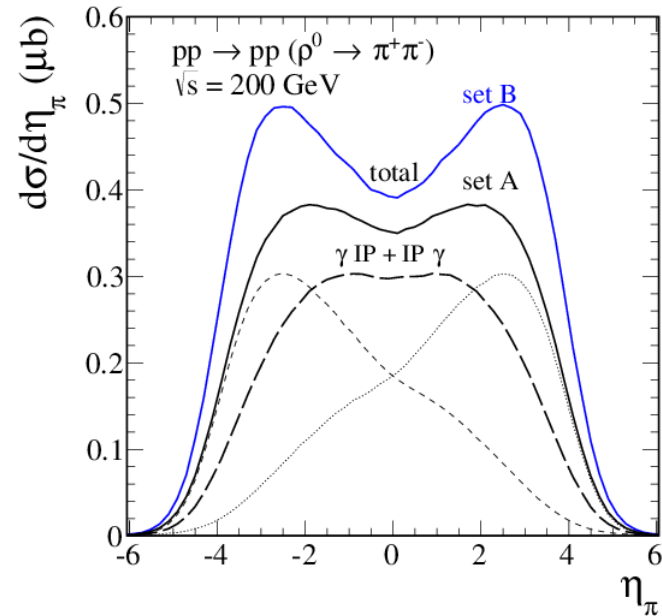
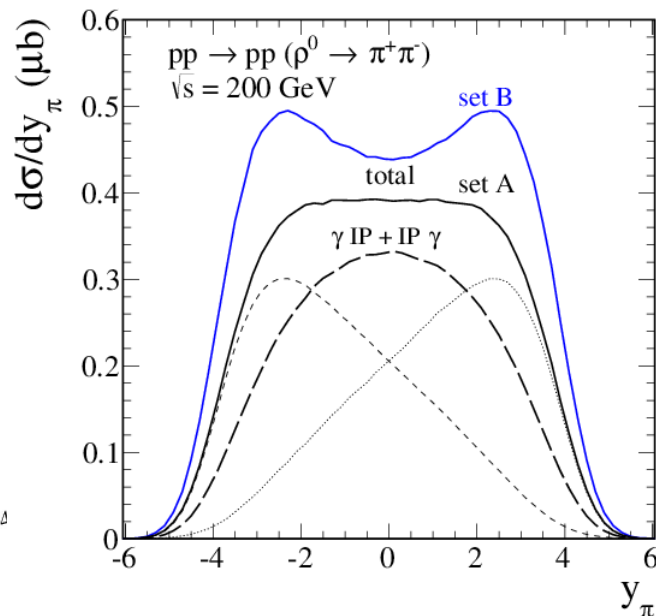
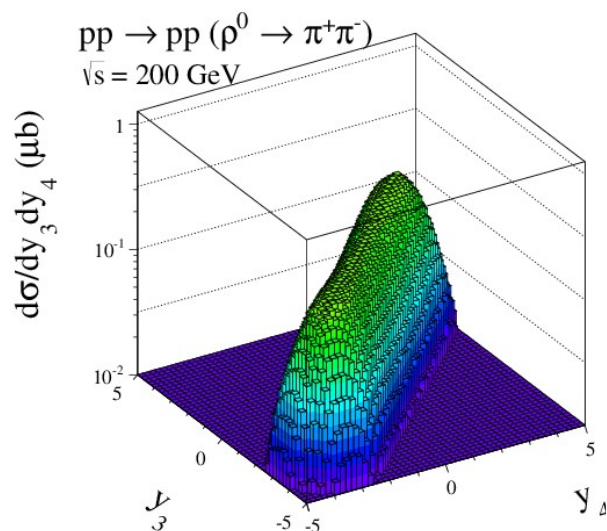


$\xi$  is auxiliary variable:

$$\xi_1 = \log_{10}(p_{1\perp}/1 \text{ GeV})$$



# $y_\pi$ and $\eta_\pi$ distributions

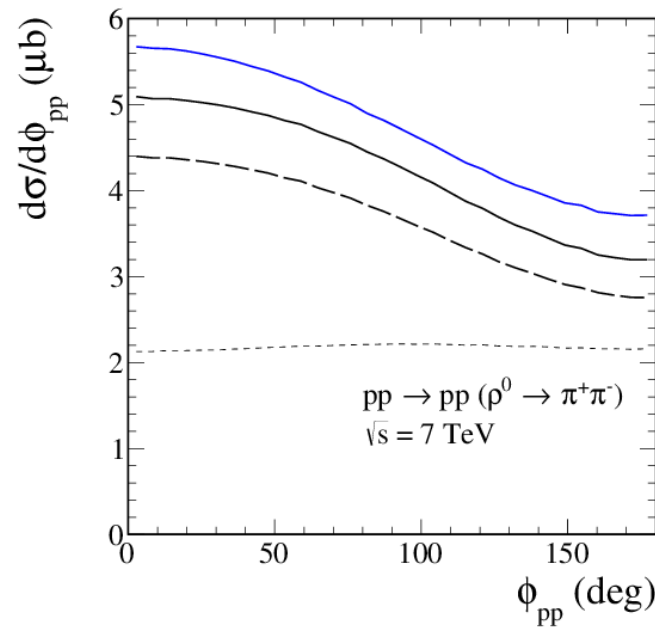
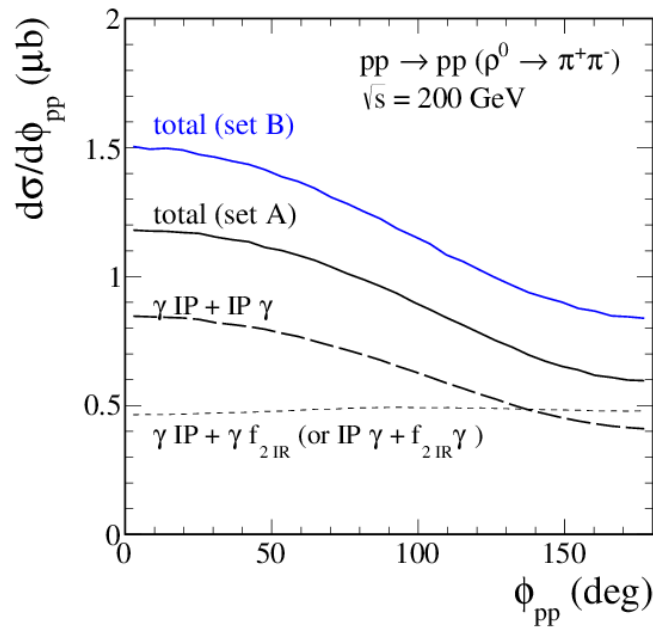


The rapidities of the two pions are strongly correlated and  $y_{\pi^+} \approx y_{\pi^-}$ .

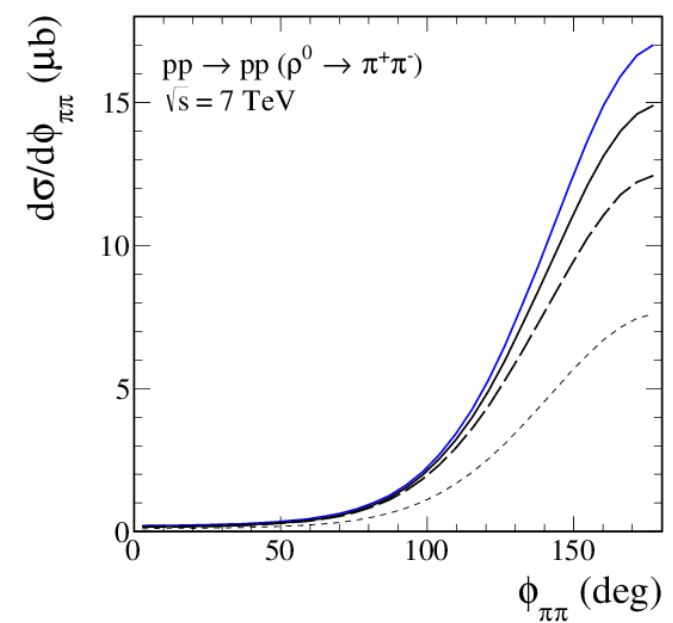
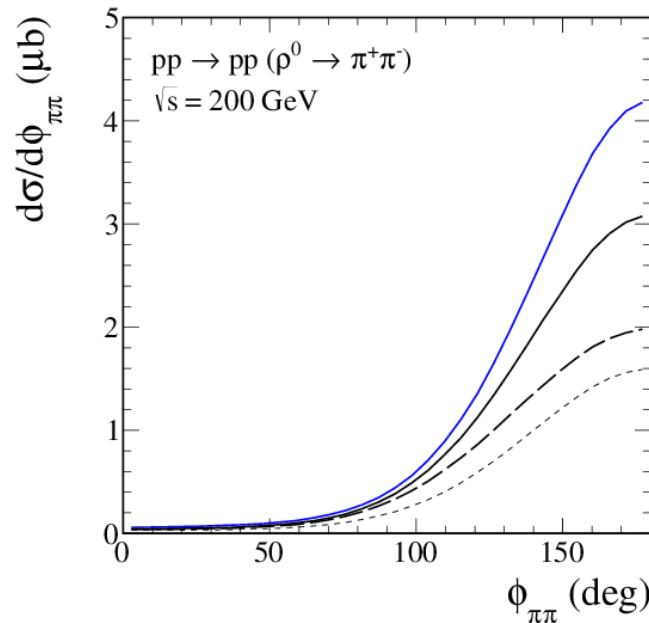
This is similar characteristic as for the double pomeron/reggeon exchanges in the fully diffractive mechanism

*P. L. and A. Szczurek, Phys. Rev. D81 (2010) 036003.*

# $\phi_{pp}$ and $\phi_{\pi\pi}$ distributions

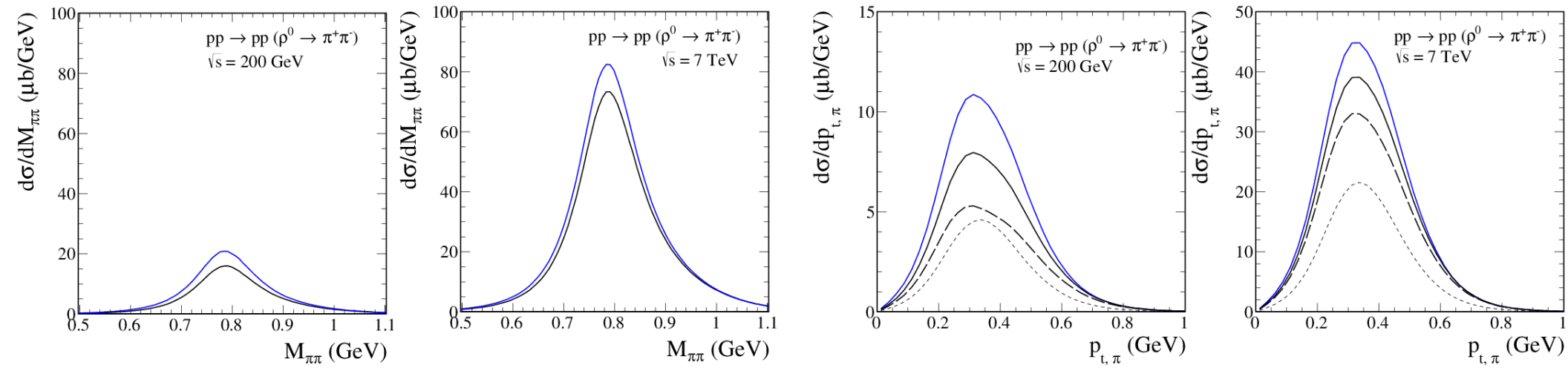


The effect of  $\phi_{pp}$  deviation from a constant is due to interference of  $\gamma$ - $IP$  and  $IP$ - $\gamma$  amplitudes. Similar effect was discussed in [W. Schäfer and A. Szczurek, Phys. Rev. D76 \(2007\) 094014](#) for the exclusive production of  $J/\psi$  meson.





# $M_{\pi\pi}$ and $p_{\perp\pi}$ distributions



$\sigma_{pp \rightarrow pp(\rho^0 \rightarrow \pi^+ \pi^-)}$  in  $\mu b$

$\sqrt{s}$ , TeV	cuts	$I^P$ and $f_{2R}$ set A (set B)	$I^P$ set A
0.2	—	2.88 (3.73)	2.03
0.5	—	4.67 (5.79)	3.52
1.96	—	8.48 (9.97)	6.88
7	—	13.28 (14.85)	11.45
0.2 (STAR I)	$ \eta_{\pi^\pm}  < 1, p_{\perp, \pi^\pm} > 0.15 \text{ GeV}, 0.003 < -t_{1,2} < 0.035 \text{ GeV}^2$	0.032 (0.038)	0.026
0.5 (STAR II)	$ \eta_{\pi^\pm}  < 1, p_{\perp, \pi^\pm} > 0.15 \text{ GeV}, 0.1 < -t_{1,2} < 1.5 \text{ GeV}^2$	0.004 (0.004)	0.004
7 (CMS)	$ y_{\pi^\pm}  < 2.5, p_{\perp, \pi^\pm} > 0.1 \text{ GeV}$	4.14 (4.11)	4.02
7 (ALICE)	$ \eta_{\pi^\pm}  < 0.9, p_{\perp, \pi^\pm} > 0.1 \text{ GeV}$	0.91 (0.89)	0.89

# Conclusions

- The tensorial pomeron  $IP_T$  can equally well describe existing experimental data on the exclusive meson production as the less theoretically justified vectorial pomeron  $IP_V$  frequently used in the literature.
- **Our study certainly shows the potential of  $pp \rightarrow pMp$  reactions for testing the nature of the soft pomeron.** Pseudoscalar meson production could be of particular interest in this respect since there the distribution in  $\phi_{pp}$  may contain, for the  $IP_T$ , a term which is not possible for the  $IP_V$ .  
In most cases ( $J^{PC} = 0^{++}, 0^{-+}$ ) one has to add coherently amplitudes for two lowest ( $I, S$ ) couplings. The corresponding coupling constants are not known and have been fitted to existing experimental data.
- We have made first estimates of central exclusive  $\rho^0$  meson production in the  $pp \rightarrow pp\pi^+\pi^-$  reaction. **The  $\rho^0$  contribution constitutes 10-20 % of the double pomeron/Reggeon contribution** calculated in a simple Regge model. Similar characteristic of rapidity and  $p_{\perp,\pi}$  distributions, but different dependence on  $p_{\perp,\rho}$  and  $\phi_{pp}$ .
- **Future experimental data** (COMPASS, STAR RHIC, CDF Tevatron, ALICE, CMS, ATLAS, etc.) on exclusive meson production **should thus provide good information on the spin structure of the soft pomeron and on its couplings to the nucleon and the mesons.**

[see R. Schicker and M. Żurek talks](#)

## To-do list

- To extend the studies of central meson production in diffractive processes to higher energies, where the dominance of the  $IP$  exchange can be better justified. The deviation from “bare” distributions is more significant at high energies, where the absorptive corrections should be more important.
- **A consistent model of the resonances decaying into the  $\pi\pi/KK$  channels** (other mesons like  $f_2(1270)$ ) **and the non-resonant background.** The interference of the resonance signals with the  $\pi\pi/KK$  continuum.
- Other mechanisms → see backup slide.

# Other mechanisms to $pp \rightarrow pp\pi^+\pi^-$ reaction

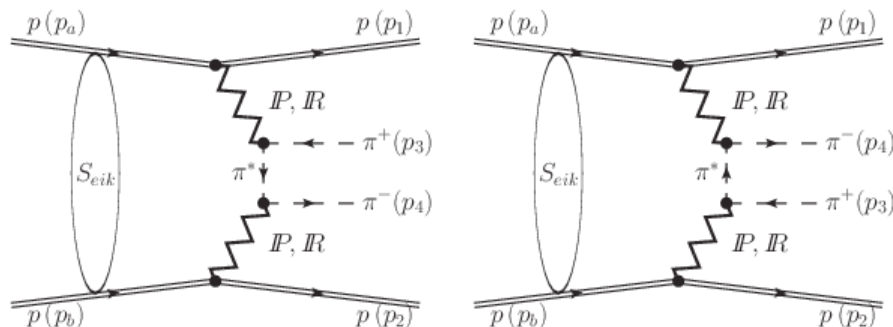
The measurement of forward/backward protons is crucial in better understanding of the mechanism reaction  
*R. Staszewski, P.L., M. Trzebiński, J. Chwastowski, A. Szczurek, Acta Phys. Polon. B42 (2011) 1861 (ATLAS + ALFA)*

- (background for scalar and tensor resonances)

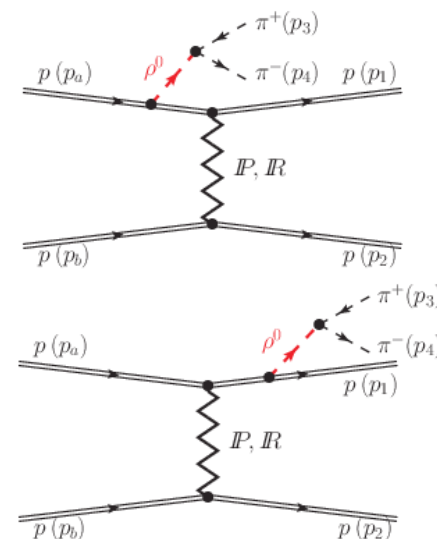
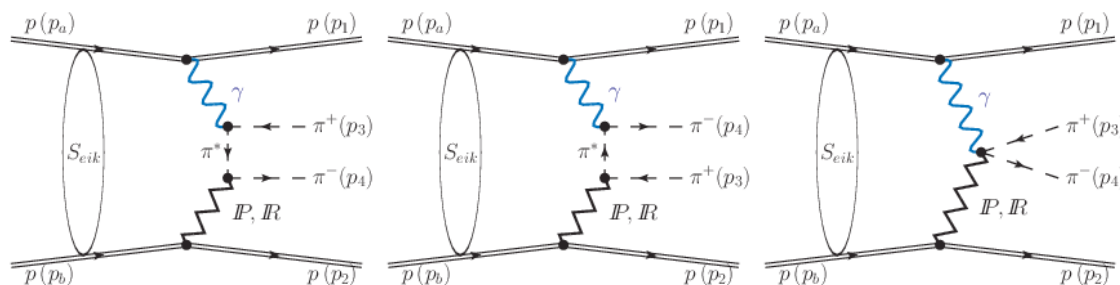
*P. L. and A. Szczurek, Phys. Rev. D81 (2010) 036003 ( $pp \rightarrow pp\pi^+\pi^-$ )*

*P. L., R. Pasechnik and A. Szczurek, Phys. Lett. B701 (2011) 434 ( $pp \rightarrow pp(\chi_{c0} \rightarrow \pi^+\pi^-)$ )*

*P. L. and A. Szczurek, Phys. Rev. D85 (2012) 014026 ( $pp \rightarrow ppK^+K^-$ )*



- (background for  $\rho^0$  resonance)



A similar bremsstrahlung processes were discussed in  $pp$  and/or  $p\bar{p}$  collisions at high energies

*A. Cisek, P. L., W. Schäfer and A. Szczurek, Phys. Rev. D83 (2011) 114004 ( $pp \rightarrow pp\pi^0$ ),*

*P. L. and A. Szczurek, Phys. Rev. D87 (2013) 074037 ( $pp \rightarrow pp\omega$ ), Phys. Rev. D87 (2013) 114004 ( $pp \rightarrow ppy$ )*