

# TOPICS in LOW-ENERGY QCD with STRANGE QUARKS



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- **Symmetry breaking** patterns in **low-energy QCD: chiral SU(3) effective field theory**
- **Antikaon-nucleon** interactions and news on  $\Lambda(1405)$
- $K^-$  **d scattering length** and **kaonic deuterium**
- $\bar{K}NN$  **systems** and search for **quasi-bound state**
- **Hyperon-nucleon interactions** with **strangeness**  
News from **ChEFT** and **Lattice QCD**
- **Strangeness** in **dense baryonic matter**  
New **constraints** from **neutron stars**

## BASIC ISSUES

- **Strange quarks** are intermediate between “**light**” and “**heavy**”:
  - ▶ Interplay between **spontaneous** and **explicit chiral symmetry breaking** in low-energy QCD
- Testing ground: high-precision **antikaon-nucleon** threshold physics
  - ▶ **Attractive** low-energy  $\bar{K}N$  interaction
- Nature and structure of  $\Lambda(1405)$  ( $B = 1$ ,  $S = -1$ ,  $J^P = 1/2^-$ )
  - ▶ **Three-quark** valence structure vs. “**molecular**” meson-baryon state ?
- Quest for quasi-bound **antikaon-NN** system(s) ?
- Role of **strangeness** in dense baryonic matter
  - ▶ **Kaon condensation** ?  
**Strange quark matter, hyperons in neutron stars** ?



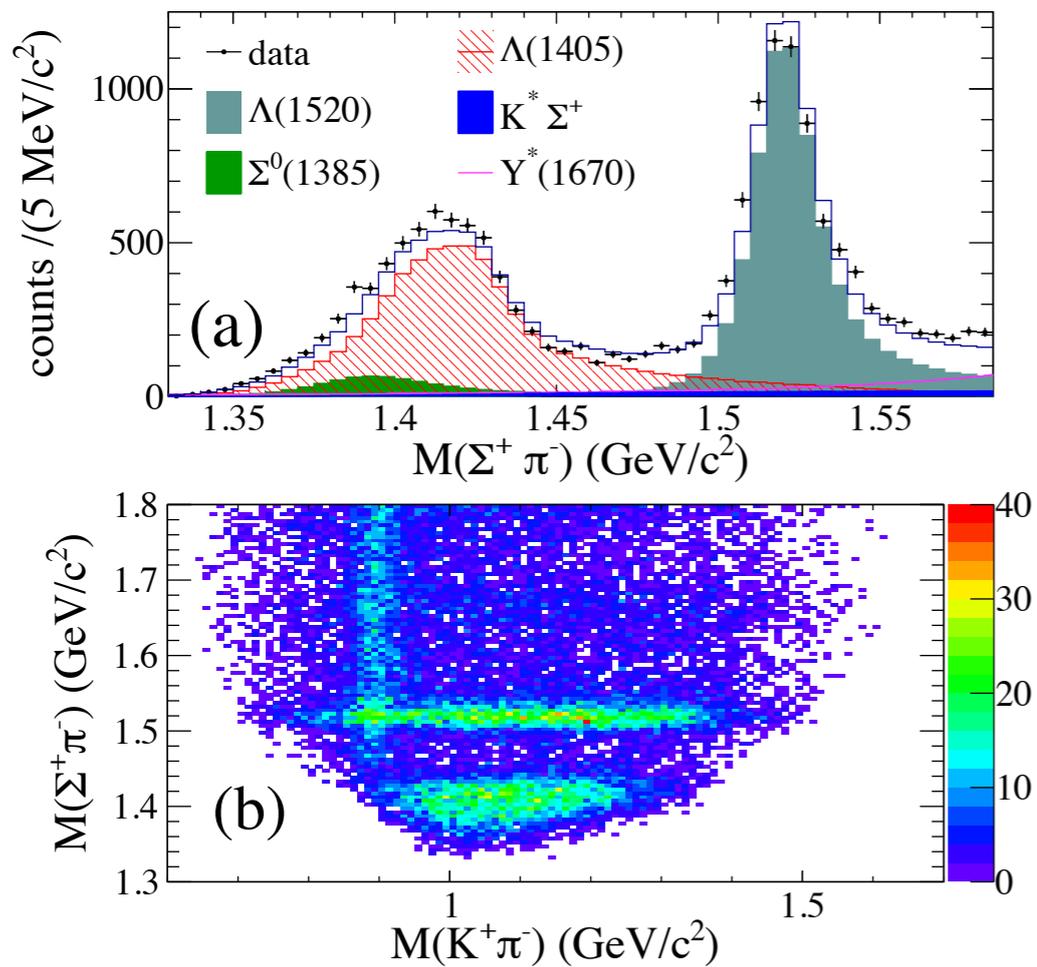
*PART I:*

**$\bar{K}N$  and  $\bar{K}NN$   
Interactions**



# $\Lambda(1405)$ : RECENT NEWS

- $\gamma p \rightarrow K^+ \pi^- \Sigma^+$  @ CLAS / JLab



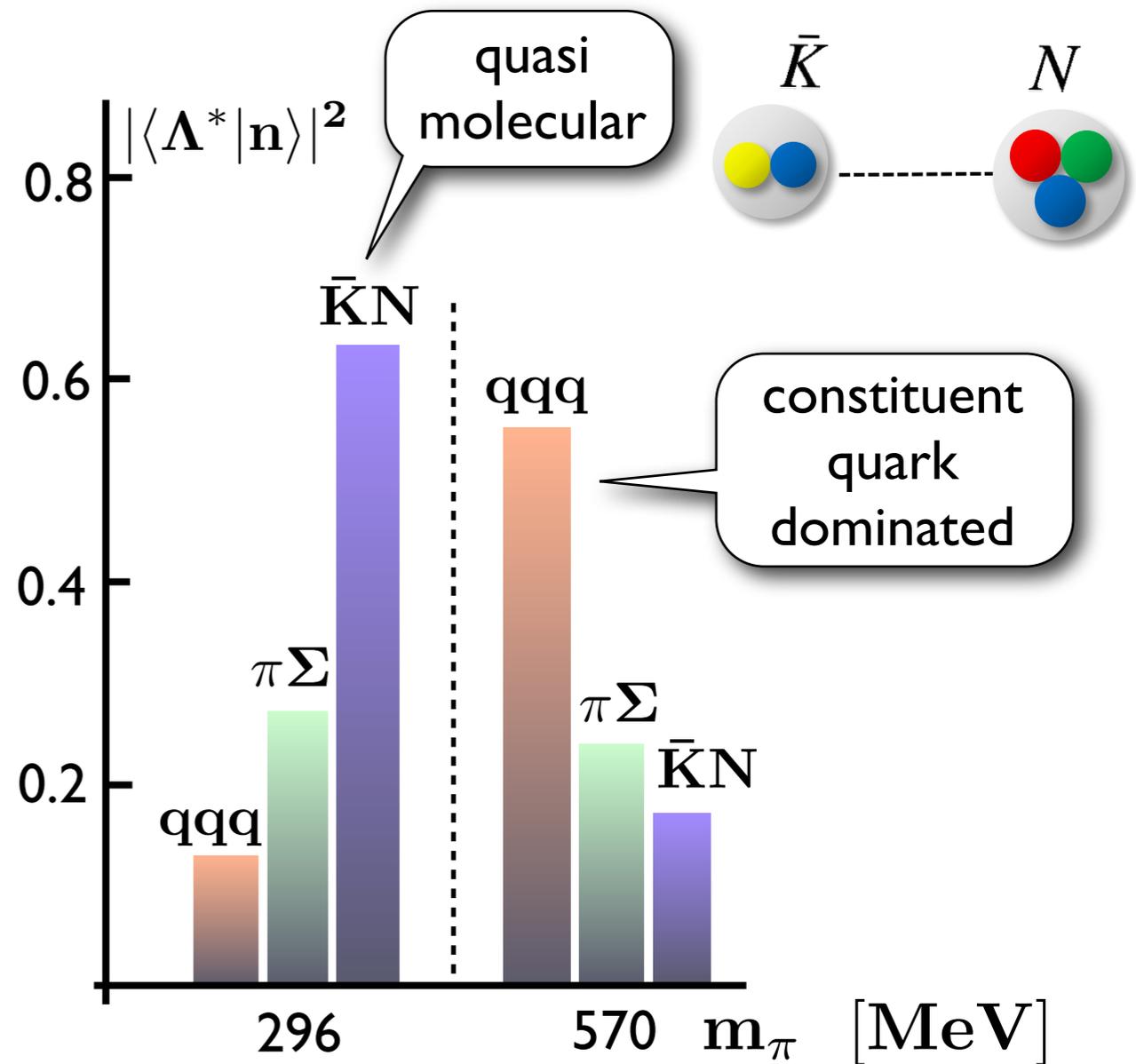
- Detailed analysis of  $\Sigma^+ \pi^-$  distribution and  $\Sigma^+$  polarization confirms

$$J^P = \frac{1}{2}^- \text{ of } \Lambda(1405)$$

K. Moriya et al. (CLAS collaboration)  
Phys. Rev. Lett. 112 (2014) 068103

- Structure of  $\Lambda(1405)$  from Lattice QCD

$$|\Lambda^*\rangle = a|uds\rangle + b|(udu)(\bar{u}s)\rangle + \dots$$



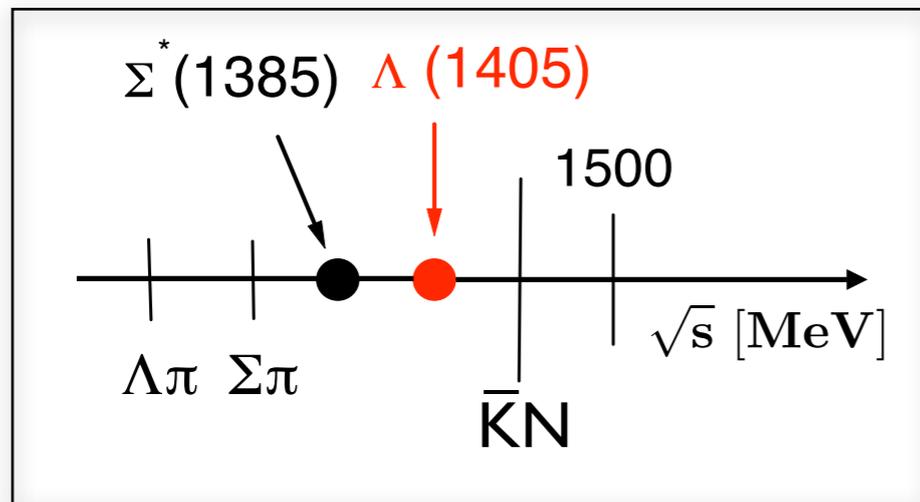
- Quasimolecular  $\bar{K}N$  structure of  $\Lambda(1405)$

J.M.M. Hall et al. (Adelaide group)  
(2014)

# Low-Energy $\bar{K} N$ Interactions

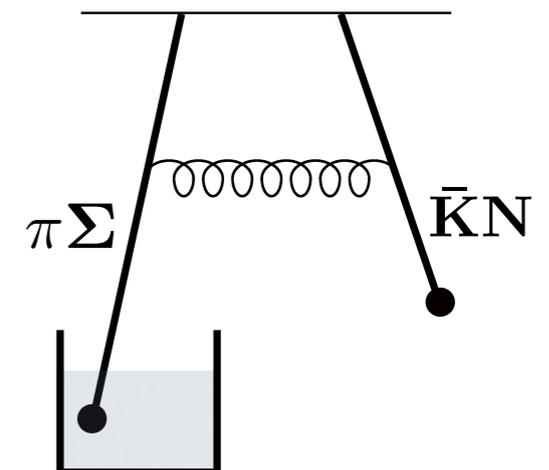
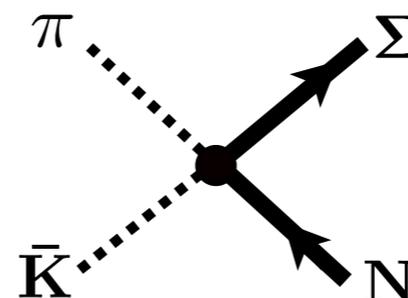
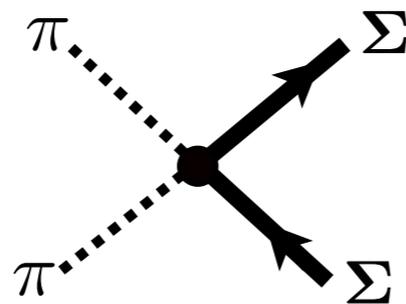
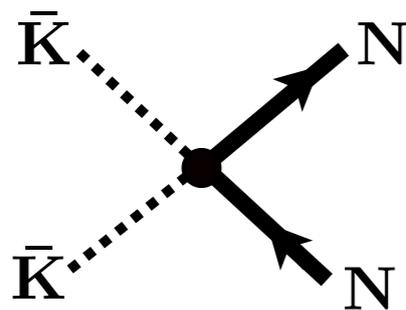
- Framework: **Chiral SU(3) Effective Field Theory** ... but :
- Chiral Perturbation Theory **NOT** applicable:  
 $\Lambda(1405)$  resonance 27 MeV below  $\bar{K}^- p$  threshold

N. Kaiser, P. Siegel, W.W. (1995)  
 E. Oset, A. Ramos (1998)



Non-perturbative  
**Coupled Channels**  
 approach based on  
**Chiral SU(3) Dynamics**

- Leading s-wave  $l = 0$  meson-baryon interactions (Tomozawa-Weinberg)



**channel coupling**

**Recent Review:**

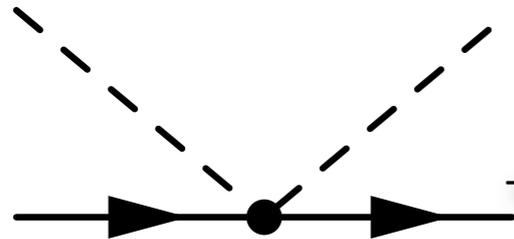
T. Hyodo, D. Jido

Prog. Part. Nucl. Phys. 67 (2012) 55

# CHIRAL SU(3) EFFECTIVE FIELD THEORY

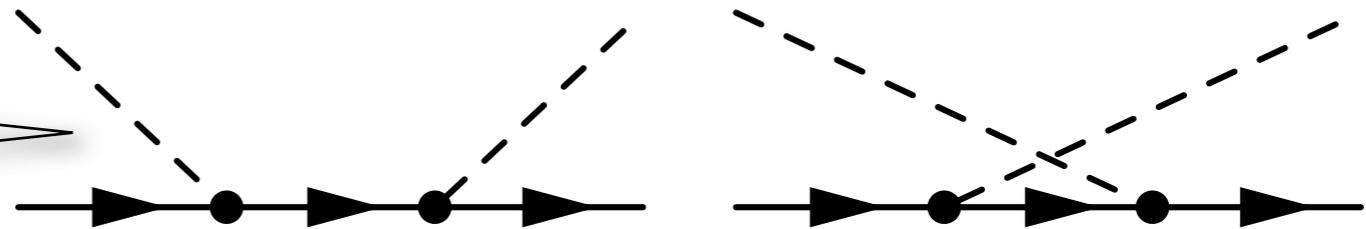
## COUPLED CHANNELS DYNAMICS:

- NLO hierarchy of driving terms -



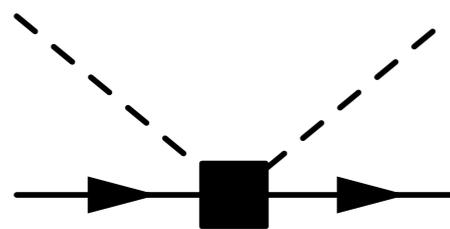
leading order (**W**einberg-**T**omozawa) terms  
**input:** physical pion and kaon decay constants

direct and crossed **B**orn terms  
**input:** axial vector constants  
 D and F from hyperon beta decays



$$g_A = D + F = 1.26$$

$$\mathcal{L}_1^{MB} = \text{Tr} \left( \frac{D}{2} (\bar{B} \gamma^\mu \gamma_5 \{u_\mu, B\}) + \frac{F}{2} (\bar{B} \gamma^\mu \gamma_5 [u_\mu, B]) \right)$$



next-to-leading order (**NLO**)  $\mathcal{O}(p^2)$   
**input:** several low-energy constants

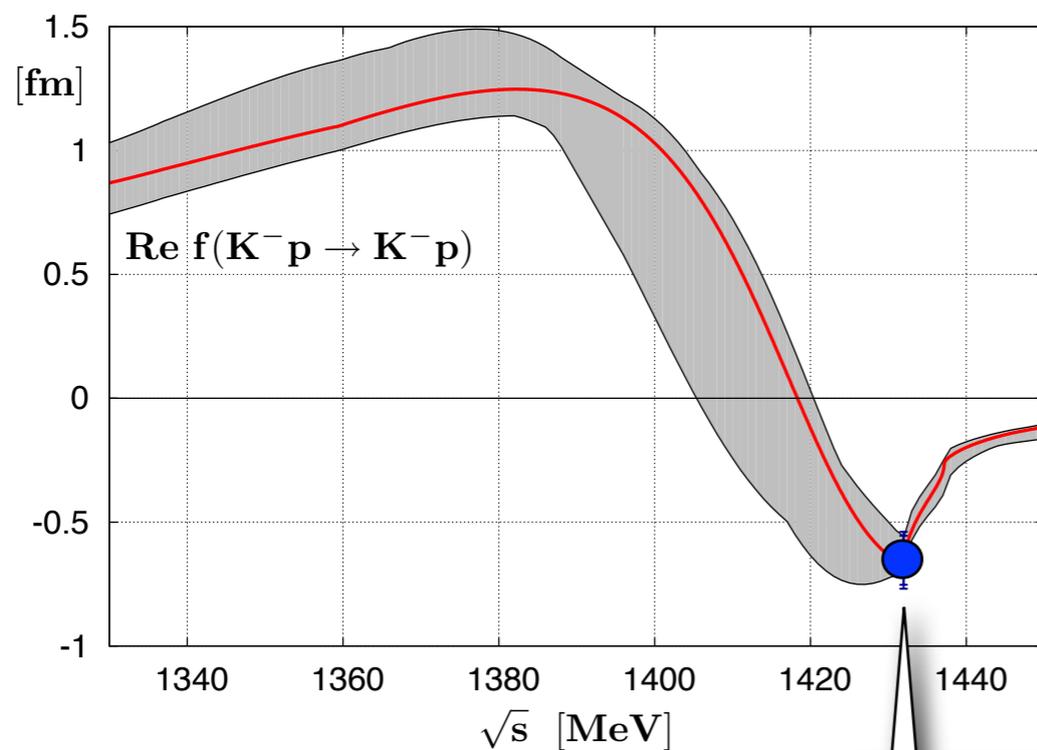
$$\begin{aligned} \mathcal{L}_2^{MB} = & b_D \text{Tr}(\bar{B} \{\chi_+, B\}) + b_F \text{Tr}(\bar{B} [\chi_+, B]) + b_0 \text{Tr}(\bar{B} B) \text{Tr}(\chi_+) \\ & + d_1 \text{Tr}(\bar{B} \{u^\mu, [u_\mu, B]\}) + d_2 \text{Tr}(\bar{B} [u^\mu, [u_\mu, B]]) \\ & + d_3 \text{Tr}(\bar{B} u_\mu) \text{Tr}(u^\mu B) + d_4 \text{Tr}(\bar{B} B) \text{Tr}(u^\mu u_\mu), \end{aligned}$$

# $K^-p$ SCATTERING AMPLITUDE from CHIRAL SU(3) COUPLED CHANNELS DYNAMICS

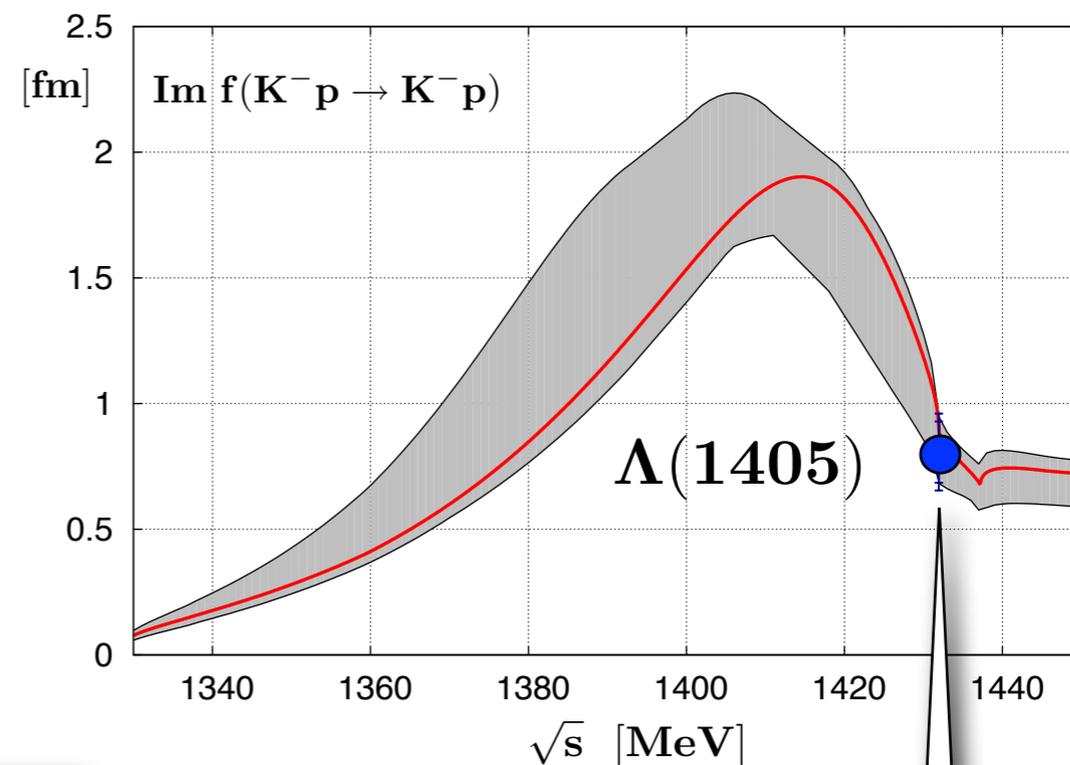
$$f(K^-p) = \frac{1}{2} [f_{\bar{K}N}(I=0) + f_{\bar{K}N}(I=1)]$$

Y. Ikeda, T. Hyodo, W. W.  
PLB 706 (2011) 63  
NPA881 (2012) 98

$\Lambda(1405)$ :  $\bar{K}N$  ( $I=0$ ) **quasibound state** embedded in the  $\pi\Sigma$  continuum



Re  $a(K^-p)$



Im  $a(K^-p)$

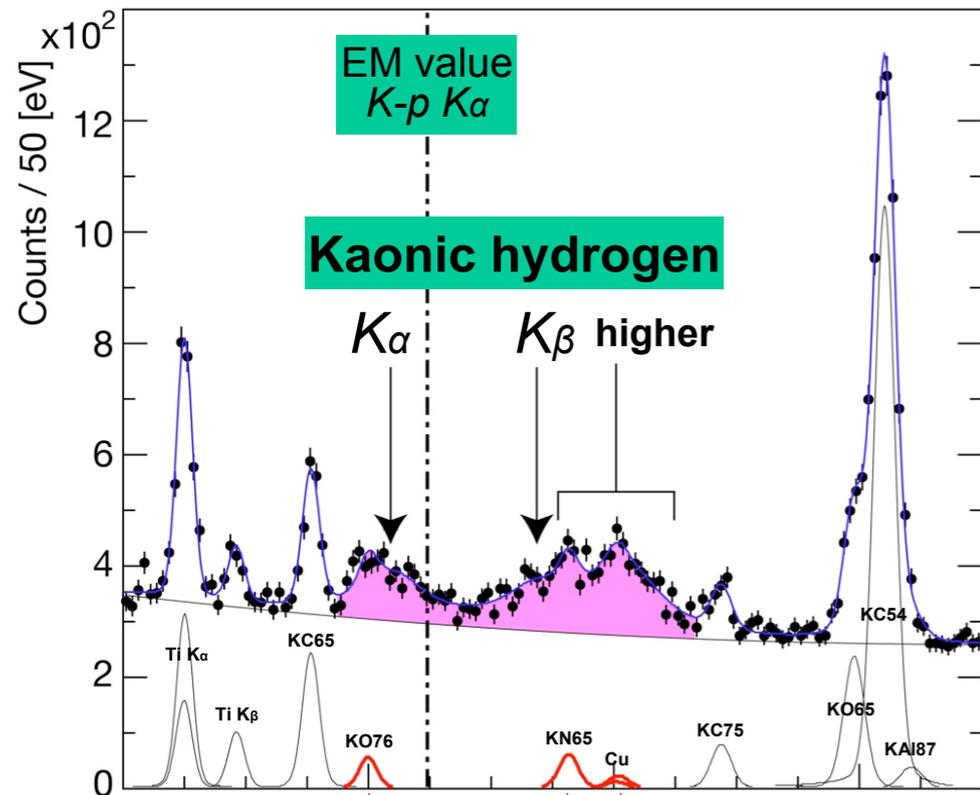
- Complex scattering length (including Coulomb corrections)

$$\text{Re } a(K^-p) = -0.65 \pm 0.10 \text{ fm}$$

$$\text{Im } a(K^-p) = 0.81 \pm 0.15 \text{ fm}$$

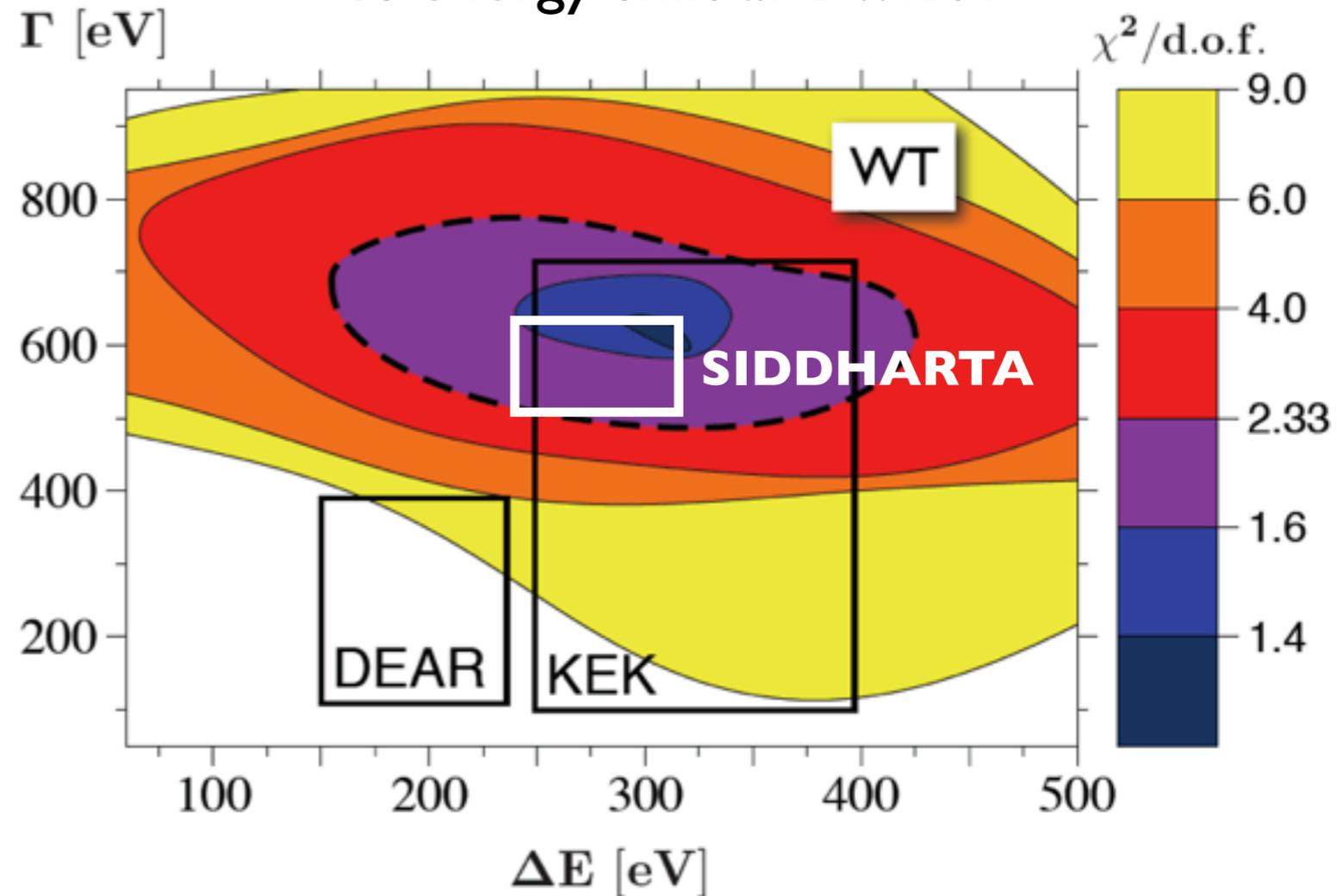
# CONSTRAINTS from SIDDHARTA

- **Kaonic hydrogen**  
precision data



M. Bazzi et al. (SIDDHARTA)  
Phys. Lett. B 704 (2011) 113

- **Strong interaction**  
Is energy shift and width



$$\Delta E = 283 \pm 36 (stat) \pm 6 (syst) \text{ eV}$$

$$\Gamma = 541 \pm 89 (stat) \pm 22 (syst) \text{ eV}$$

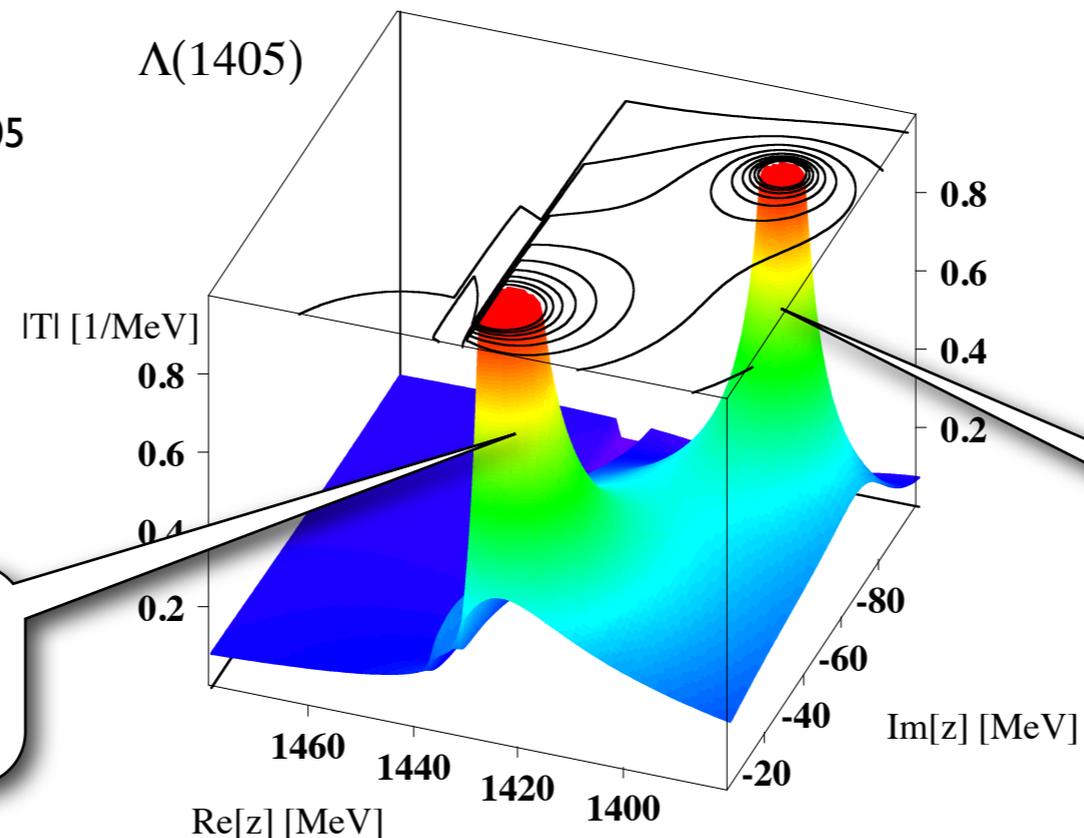
# The TWO POLES scenario

- Characteristic feature of **Chiral SU(3) Dynamics**  
**Energy dependent** driving interactions

D. Jido et al.  
Nucl. Phys. A723 (2003) 205

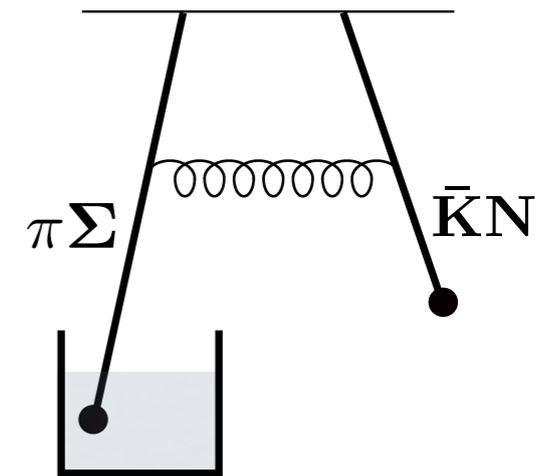
T. Hyodo, W.W.  
Phys. Rev. C 77 (2008) 03524

T. Hyodo, D. Jido  
Prog. Part. Nucl. Phys. 67 (2012) 55



dominantly  
 $\bar{K}N$

dominantly  
 $\pi\Sigma$



- Pole positions from **chiral SU(3) coupled-channels calculation** with **SIDDHARTA** threshold constraints:

$$E_1 = 1424 \pm 15 \text{ MeV} \quad E_2 = 1381 \pm 15 \text{ MeV}$$

$$\Gamma_1 = 52 \pm 10 \text{ MeV} \quad \Gamma_2 = 162 \pm 15 \text{ MeV}$$

Y. Ikeda, T. Hyodo, W.W.:  
Nucl. Phys. A 881 (2012) 98

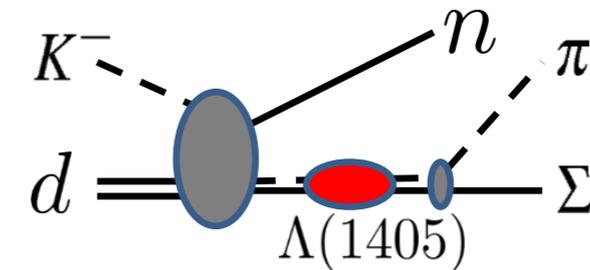
- Note: phenomenological potential approach is qualitatively different:  
energy-**independent** interaction, **single**  $\Lambda(1405)$  pole

# Scenarios: TWO-POLES ENERGY-DEPENDENT vs. SINGLE-POLE ENERGY-INDEPENDENT

- Three-body coupled channels (Faddeev) calculations

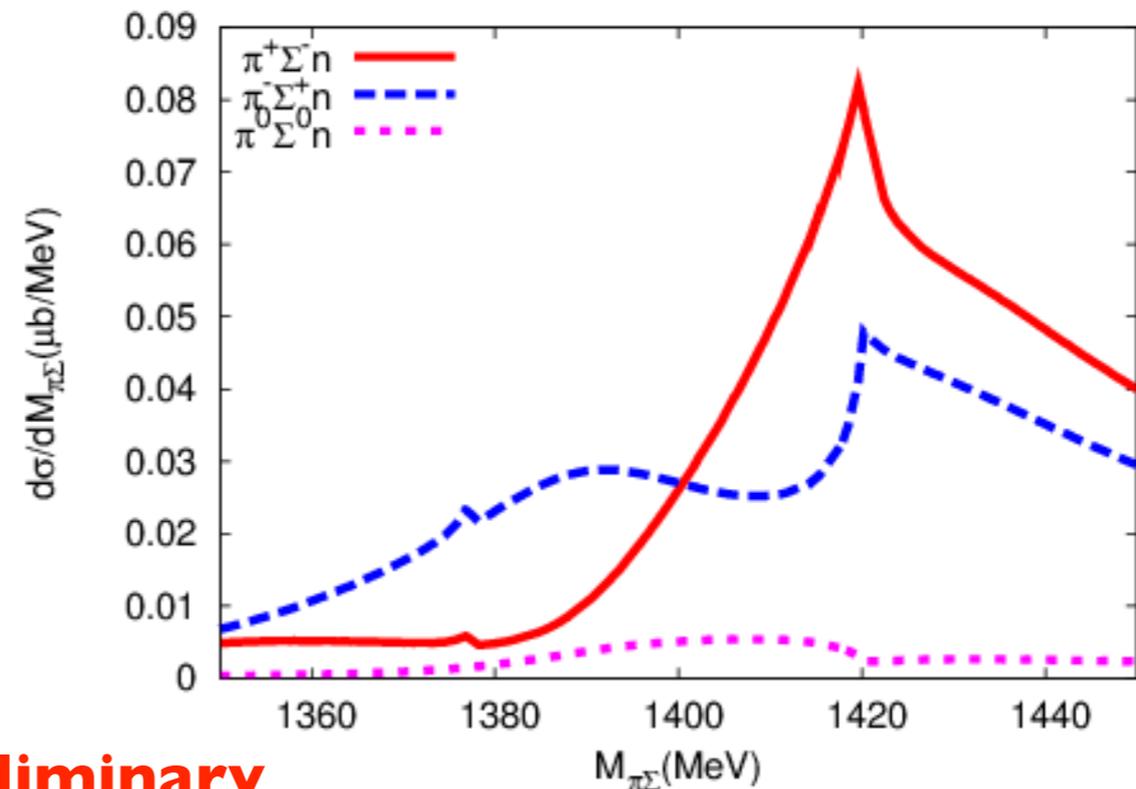
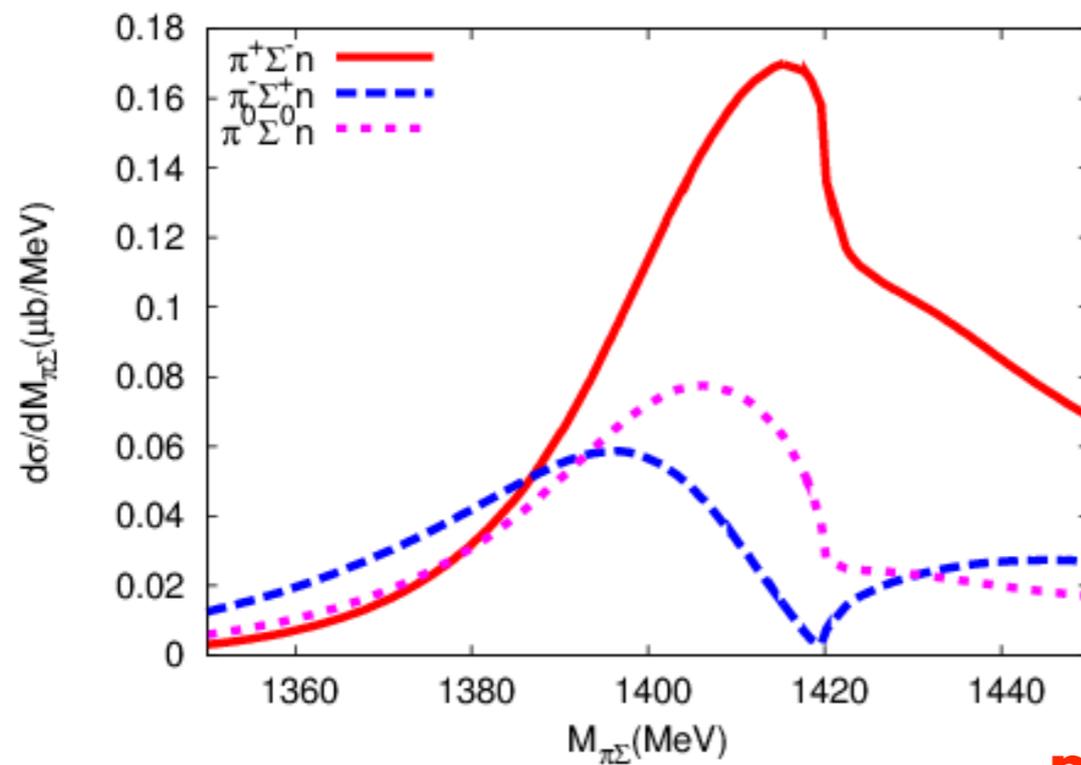
$\pi\Sigma$  invariant mass distribution

$$p_{\bar{K}}^{lab} = 700\text{MeV}$$



E-dep. (two-pole, 1420)

E-indep. (one-pole, 1405)



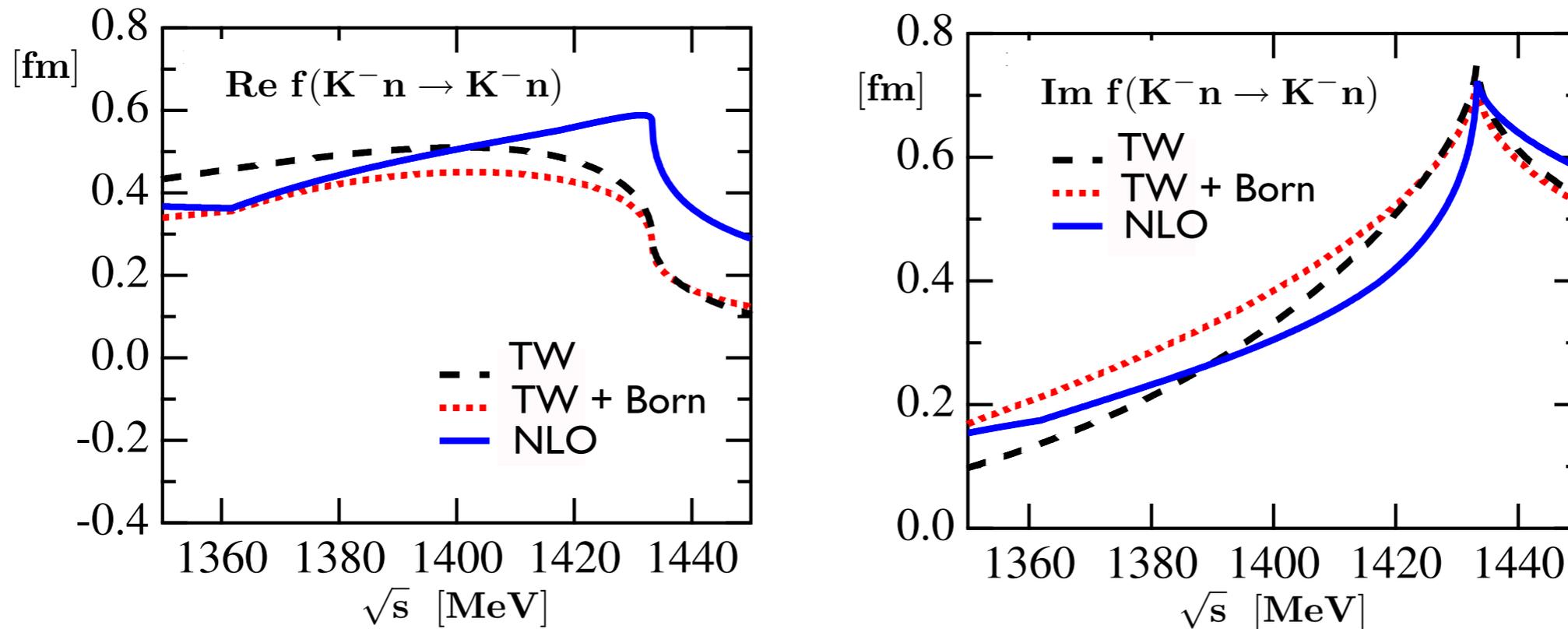
**preliminary**

Shota Ohnishi, Y. Ikeda, T. Hyodo, E. Hiyama, W.W. (2014)

# CHIRAL SU(3) COUPLED CHANNELS DYNAMICS

- Predicted **antikaon-neutron** amplitudes at and below threshold

Y. Ikeda, T. Hyodo, W. Weise : Phys. Lett. B 706 (2011) 63 , Nucl. Phys. A 881 (2012) 98



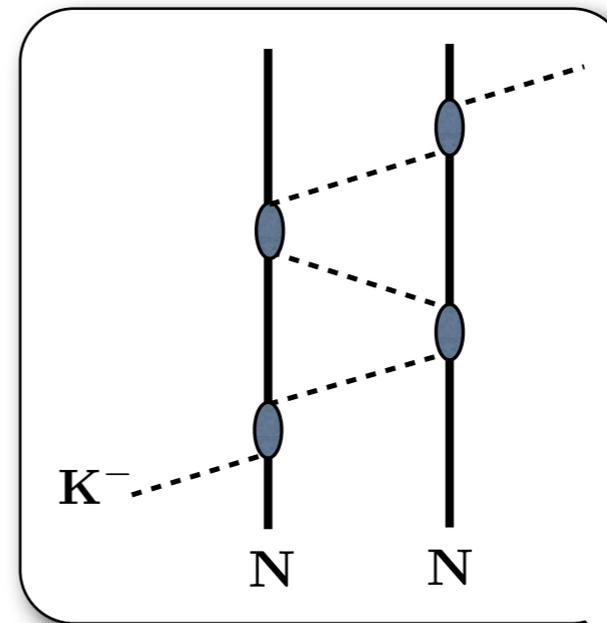
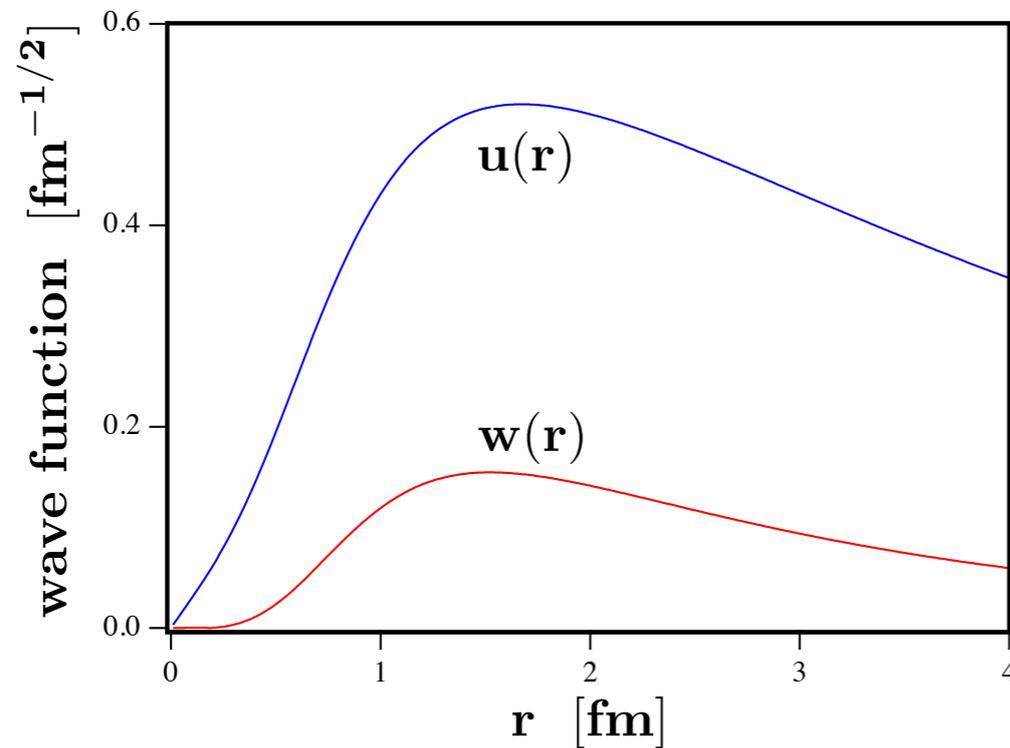
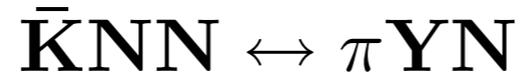
$$a(K^- n) = 0.57_{-0.21}^{+0.04} + i 0.72_{-0.41}^{+0.26} \text{ fm}$$

- Needed:** accurate constraints from **antikaon-deuteron** threshold measurements
  - ▶ **complete** information for both isospin  $I = 0$  and  $I = 1$   $\bar{K}N$  channels
  - ▶ plus potentially important information about **K-NN absorption**

# ANTIKAON - DEUTERON THRESHOLD PHYSICS

## $K^-d$ SCATTERING LENGTH and KAONIC DEUTERIUM

- Three-body calculation using Chiral SU(3) Coupled Channels approach



- Importance of charge exchange:  
 $K^-pn \leftrightarrow \bar{K}^0nn$

S.S. Kamalov, E. Oset, A. Ramos  
Nucl. Phys. A 690 (2001) 494

$$a(K^-d) = \left(1 + \frac{m_K}{M_d}\right)^{-1} \int_0^\infty dr [u^2(r) + w^2(r)] A(r)$$

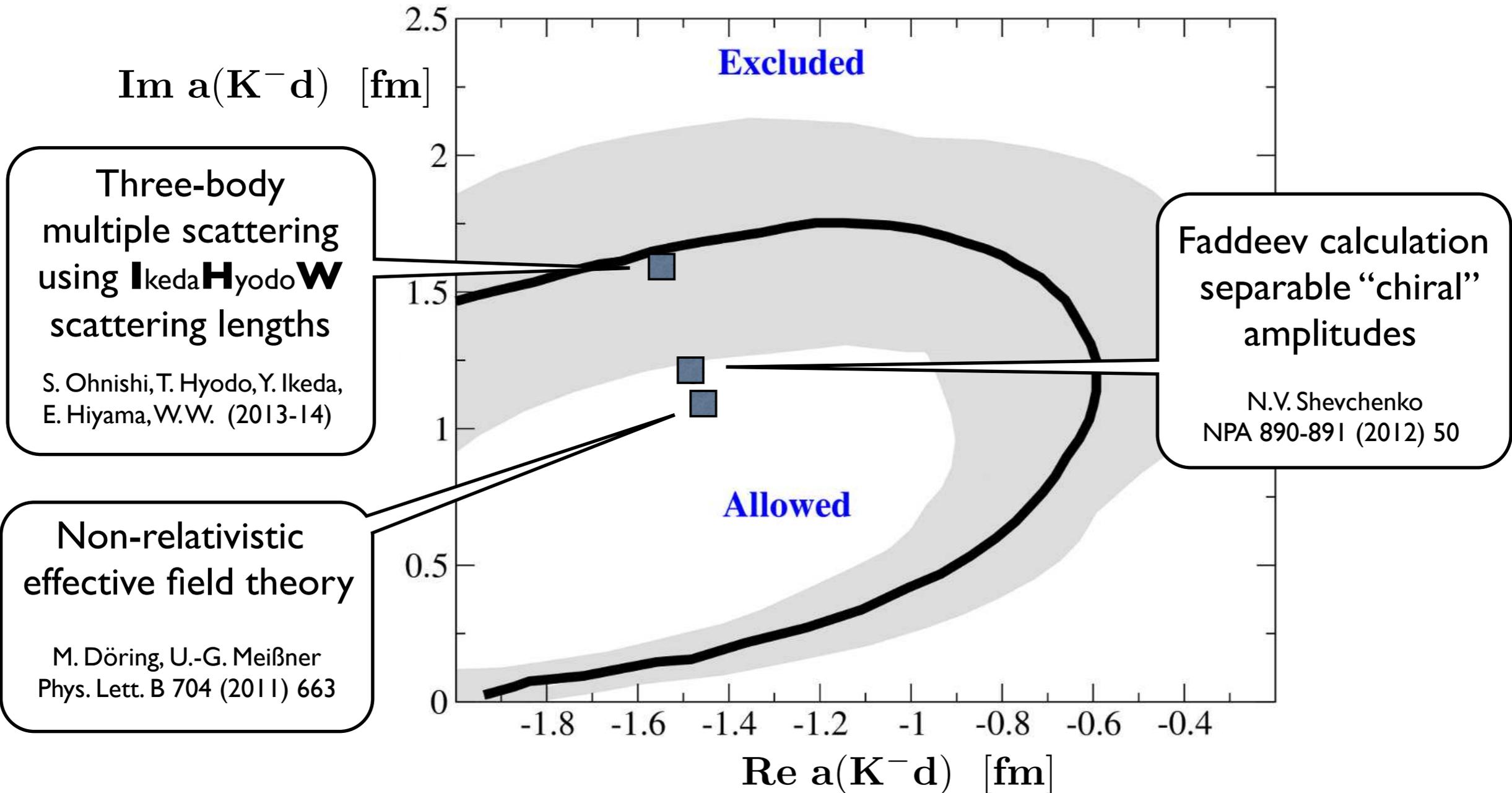
- Recent result constrained by SIDDHARTA  $K^-p$  input:

$$a(K^-d) = (-1.55 + i 1.66) \text{ fm} \quad (\pm 10\%)$$

S. Ohnishi, Y. Ikeda, T. Hyodo,  
E. Hiyama, W.W. (2014)

# ANTIKAON - DEUTERON SCATTERING LENGTH

- Recent calculations using SIDDHARTA - constrained input



- Sources of (10 - 20 %) uncertainties:

- ▶ “Fixed scatterer” approximation
- ▶  $\text{K}^- \text{n}$  amplitude
- ▶  $\text{K}^- \text{d} \rightarrow \text{YN}$  absorption

A. Gal, Int. J. Mod. Phys. A 22 (2007) 226

# KAONIC DEUTERIUM

## STRONG INTERACTION ENERGY SHIFT & WIDTH

- **Exp. Proposals:** SIDDHARTA-2 and J-PARC
- **Theory:** using  $K^-d$  scattering length based on 3-body Chiral SU(3) dynamics

Complex potential

$$U = -\frac{2\pi}{\mu} A_{KNN} \rho_d$$

$K^-NN$   
3-body amplitude

deuteron density  
distribution

Energy shift and width (1s)

$$\Delta E - \frac{i}{2}\Gamma = \frac{\langle \Phi | U | \Psi \rangle}{\langle \Phi | \Psi \rangle}$$

kaonic deuterium  
Coulomb wavefunction

kaonic deuterium  
Coulomb + **strong**  
wavefunction

$$\Delta E = (958 \pm 50) \text{ eV} \quad \Gamma = (906 \pm 70) \text{ eV}$$

S. Ohnishi, T. Hyodo, Y. Ikeda,  
E. Hiyama, W.W. (2014)

including finite-size Coulomb, vacuum polarization and binding corrections

- Comparison with improved Deser formula:

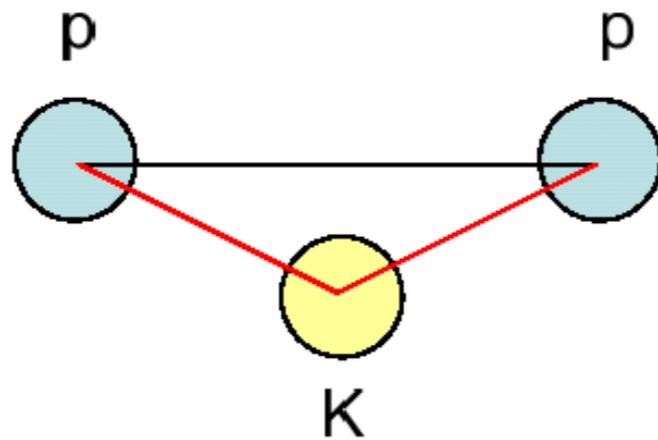
U.-G. Meißner, U. Raha, A. Rusetsky  
Eur. Phys. J. C 35 (2004) 349

$$\Delta E - \frac{i}{2}\Gamma = -\frac{2\mu^2 \alpha^3 a(K^-d)}{1 - 2\mu\alpha(1 - \ln \alpha) a(K^-d)}$$

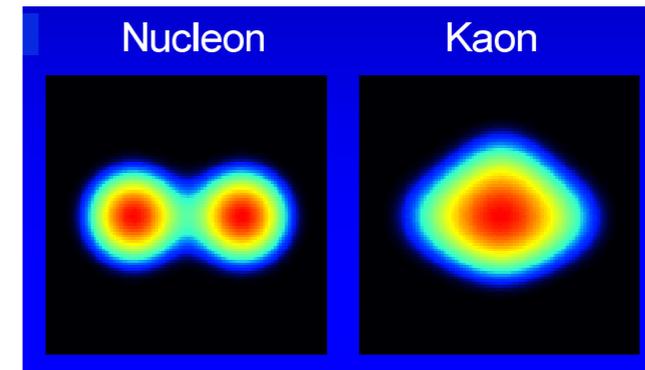
$$\left(\Delta E, \frac{\Gamma}{2}\right) = (870, 593) \text{ eV}$$



# UPDATE on QUASIBOUND $K^-pp$



**3-Body (Faddeev) calculations**



**Variational calculations**

- ... now consistently using amplitudes from **Chiral SU(3) coupled-channels** dynamics including **energy dependence** in subthreshold extrapolations
- Calculated **binding energy** and **width** (in MeV) of the  $K^-pp$  system

**modest binding**  
**large width**

	[1]	[2]	[3]
B	16	17–23	9–16
$\Gamma$	41	40–70	34–46

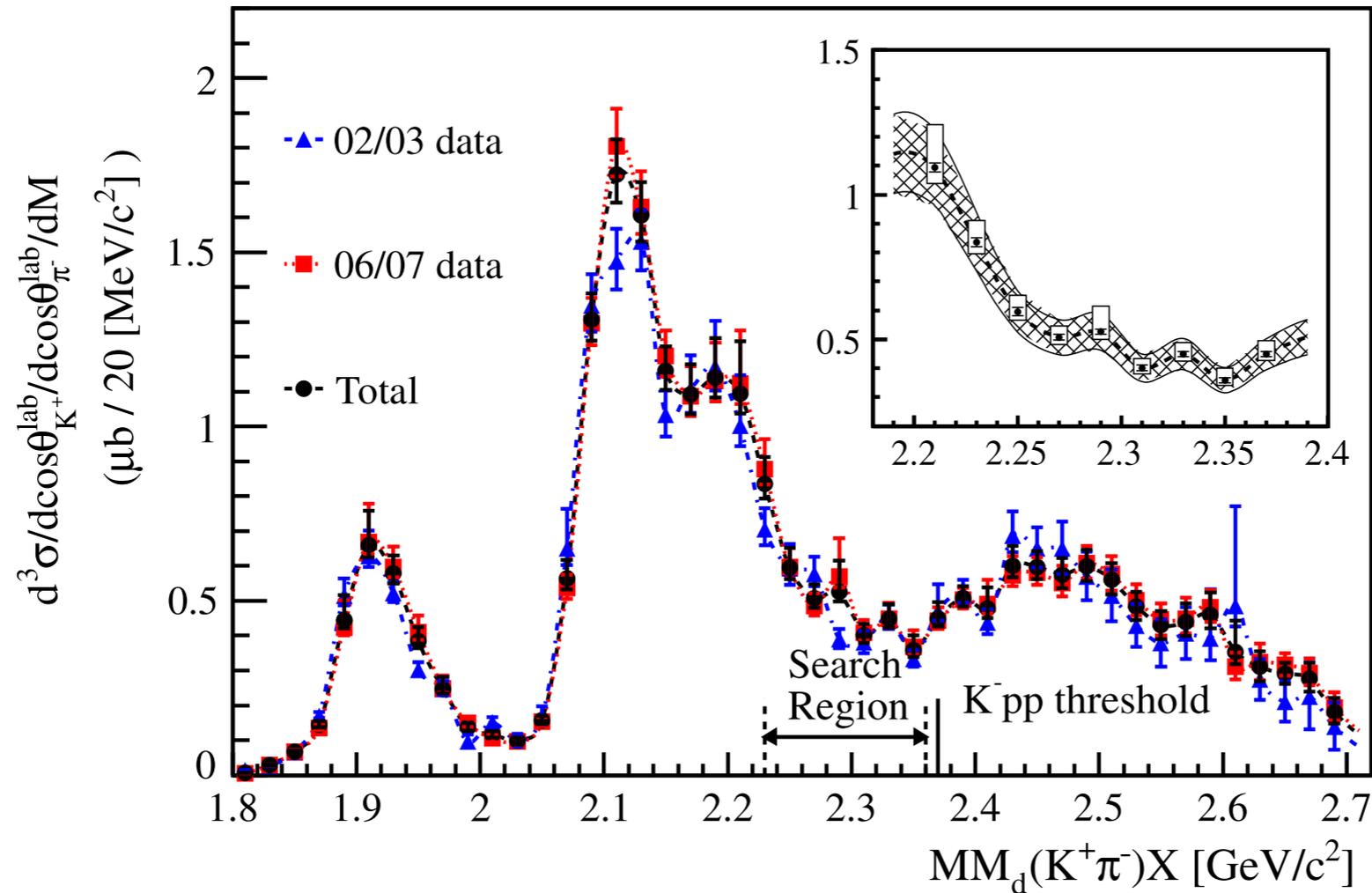
remarkable  
degree of  
consistency

- [1] Variational (hyperspherical harmonics): N. Barnea, A. Gal, E.Z. Livets ; Phys. Lett. B 712 (2012) 132
- [2] Variational (Gaussian trial wave functions): A. Doté, T. Hyodo, W.W.; Phys. Rev. C 79 (2009) 014003
- [3] Faddeev: Y. Ikeda, H. Kamano, T. Sato ; Prog. Theor. Phys. 124 (2010) 533

# New Searches for QUASIBOUND $K^-pp$

## - part I -

●  $\gamma d \rightarrow K^+ \pi^- X$  at LEPS / SPRING-8

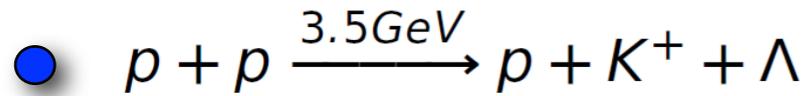


A.O.Tokiyasu et al.  
(LEPS collaboration)  
Phys. Lett. B 728 (2014) 616

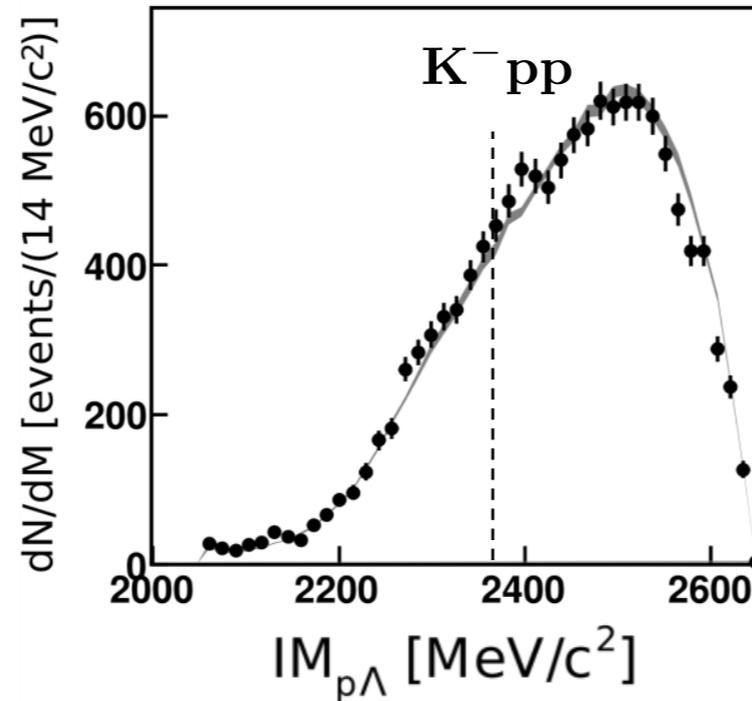
- **No significant signal** found in the search region of interest
- **Upper limits** (0.1 - 0.7  $\mu\text{b}$ ) estimated for differential cross section of quasibound state production

# New Searches for QUASIBOUND $K^-pp$

## - part II -

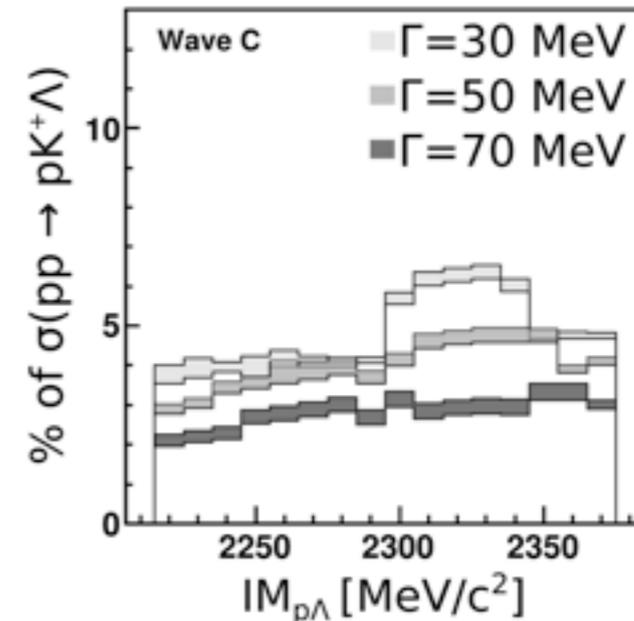
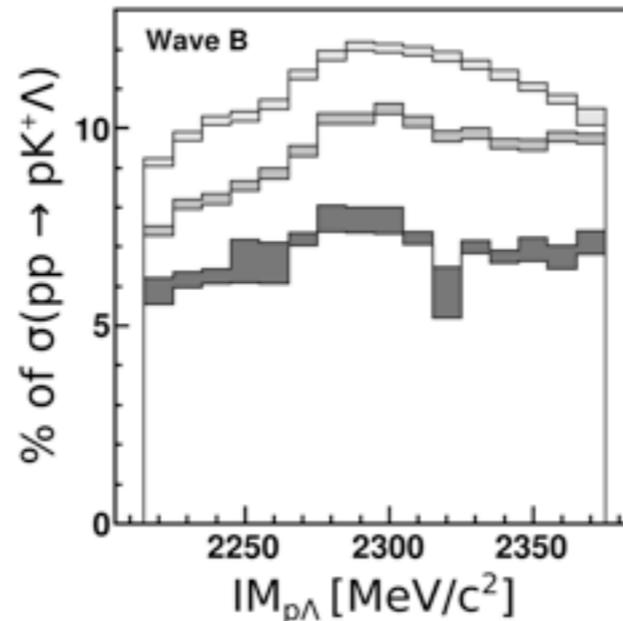
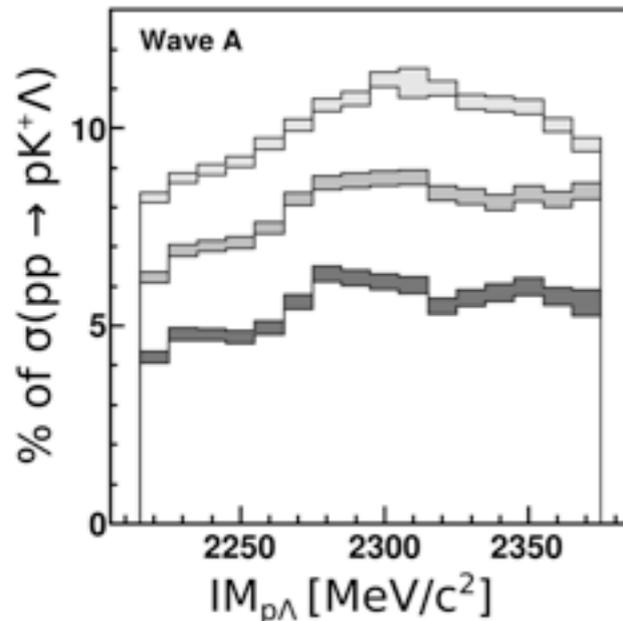


E. Epple et al.  
(HADES collaboration)



Systematic  
**partial  
wave  
analysis**  
using series of  
 $N^*$  resonances

● **No significant signal** found in the search region of interest



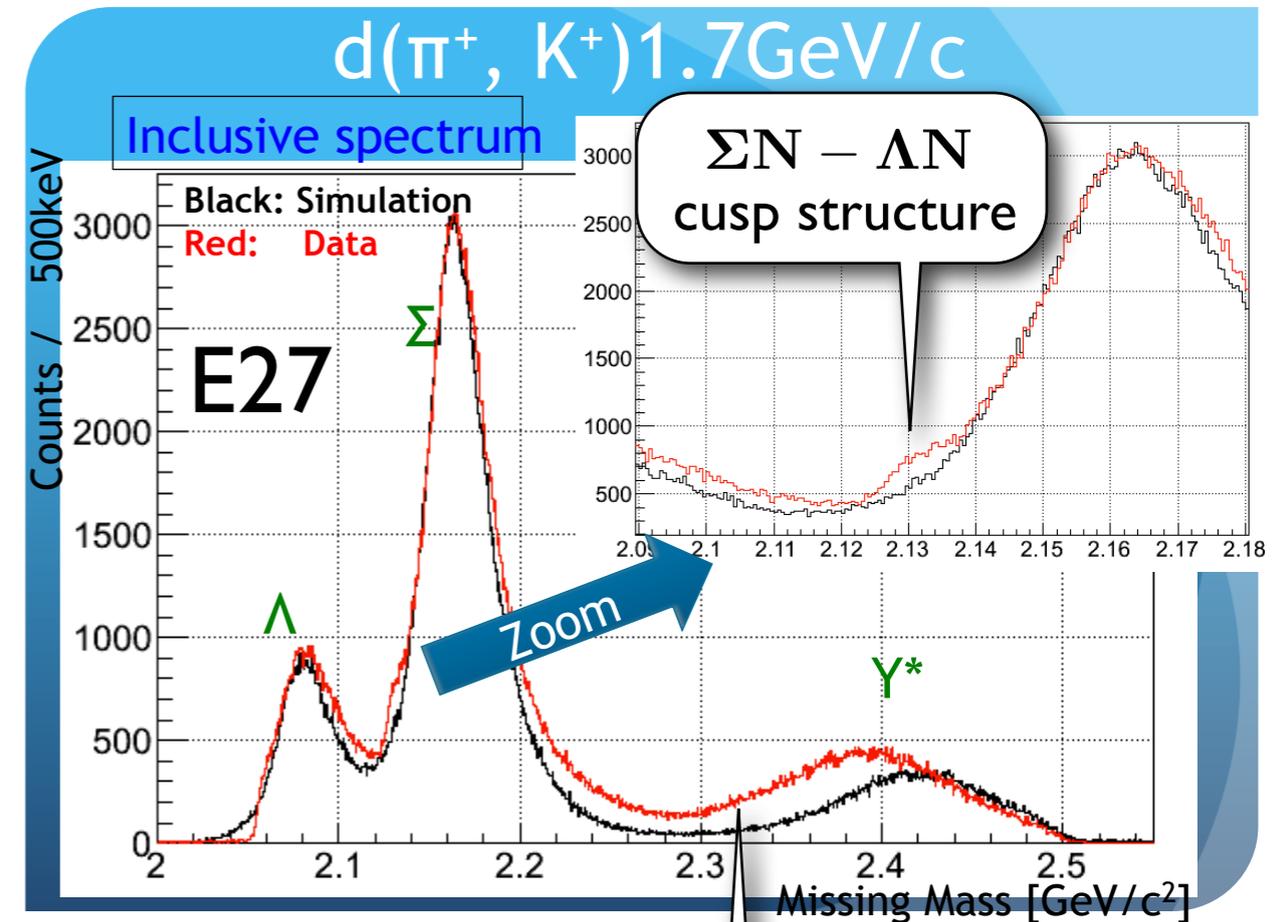
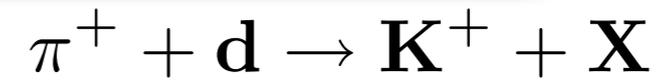
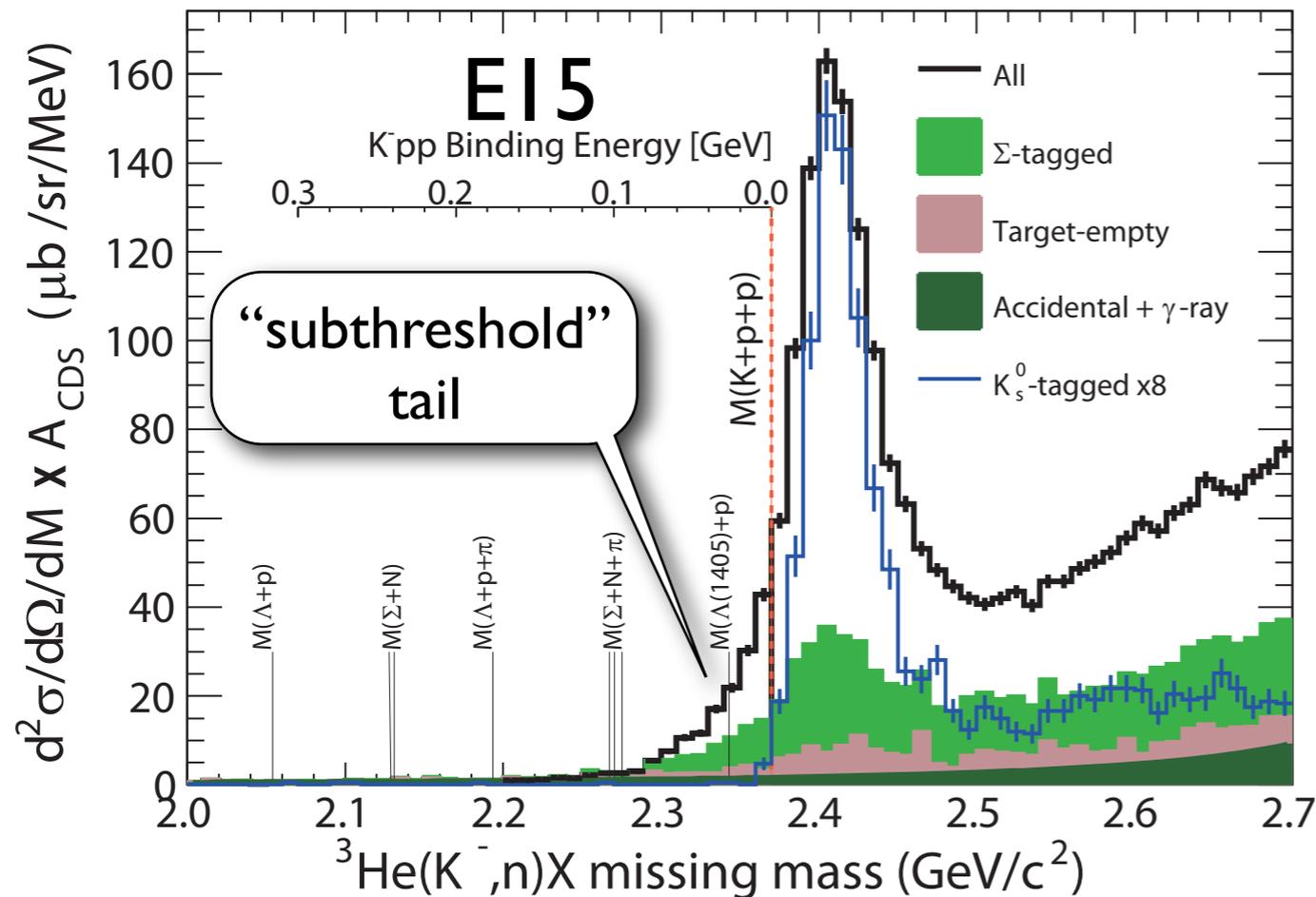
● **Upper limit** for cross section of  $pp \rightarrow K^+ \text{ "K}^-pp\text{ "}$  quasibound state production



# New Searches for QUASIBOUND $K^-pp$

- part III -

● **Experiments at J-PARC**  
(in progress)



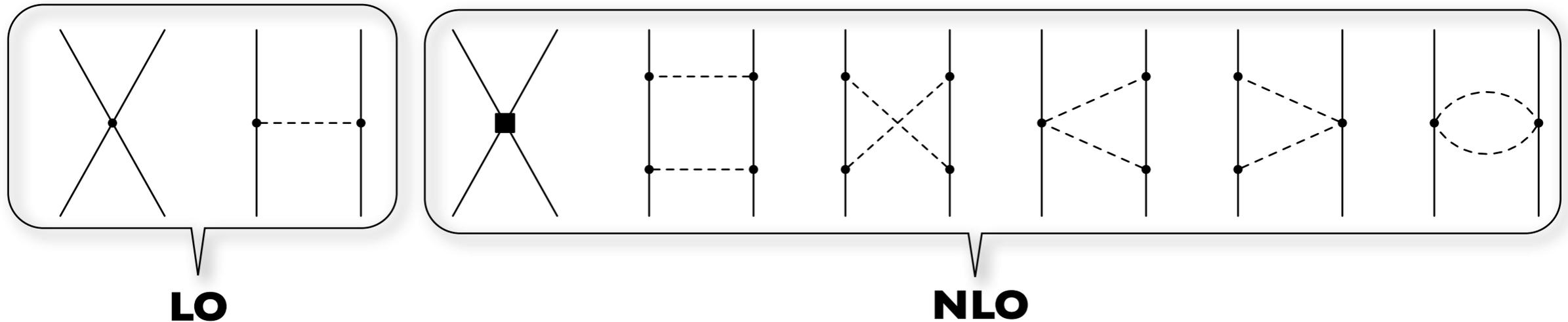
▶ presentation by Tomo Nagae

*PART II:*

**Hyperon-Nucleon Interactions  
and  
Strangeness in Dense Matter**

# Chiral SU(3) Effective Field Theory and Hyperon-Nucleon Interactions

J. Haidenbauer, S. Petschauer, N. Kaiser, U.-G. Meißner, A. Nogga, W.W.: Nucl. Phys. A 915 (2013) 24



- Interaction terms involving baryon and pseudoscalar meson octets ...

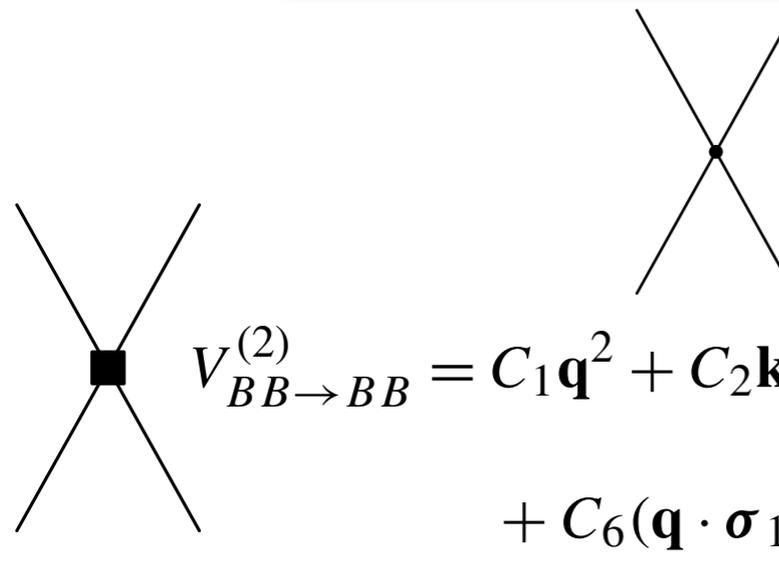
$$P = \begin{pmatrix} \frac{\pi^0}{\sqrt{2}} + \frac{\eta}{\sqrt{6}} & \pi^+ & K^+ \\ \pi^- & -\frac{\pi^0}{\sqrt{2}} + \frac{\eta}{\sqrt{6}} & K^0 \\ K^- & \bar{K}^0 & -\frac{2\eta}{\sqrt{6}} \end{pmatrix} \quad B = \begin{pmatrix} \frac{\Sigma^0}{\sqrt{2}} + \frac{\Lambda}{\sqrt{6}} & \Sigma^+ & p \\ \Sigma^- & -\frac{\Sigma^0}{\sqrt{2}} + \frac{\Lambda}{\sqrt{6}} & n \\ -\Xi^- & \Xi^0 & -\frac{2\Lambda}{\sqrt{6}} \end{pmatrix}$$

$$\mathcal{L}_1 = -\frac{\sqrt{2}}{2f_0} \text{tr}(D\bar{B}\gamma^\mu\gamma_5\{\partial_\mu P, B\} + F\bar{B}\gamma^\mu\gamma_5[\partial_\mu P, B])$$

$$\mathcal{L}_2 = \frac{1}{4f_0^2} \text{tr}(i\bar{B}\gamma^\mu[[P, \partial_\mu P], B])$$

- ...generate Nambu-Goldstone boson exchange processes

# Hyperon - Nucleon Interaction (contact terms)



$$V_{BB \rightarrow BB}^{(0)} = C_S + C_T \boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2$$

$$V_{BB \rightarrow BB}^{(2)} = C_1 \mathbf{q}^2 + C_2 \mathbf{k}^2 + (C_3 \mathbf{q}^2 + C_4 \mathbf{k}^2) \boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2 + \frac{i}{2} C_5 (\boldsymbol{\sigma}_1 + \boldsymbol{\sigma}_2) \cdot (\mathbf{q} \times \mathbf{k})$$

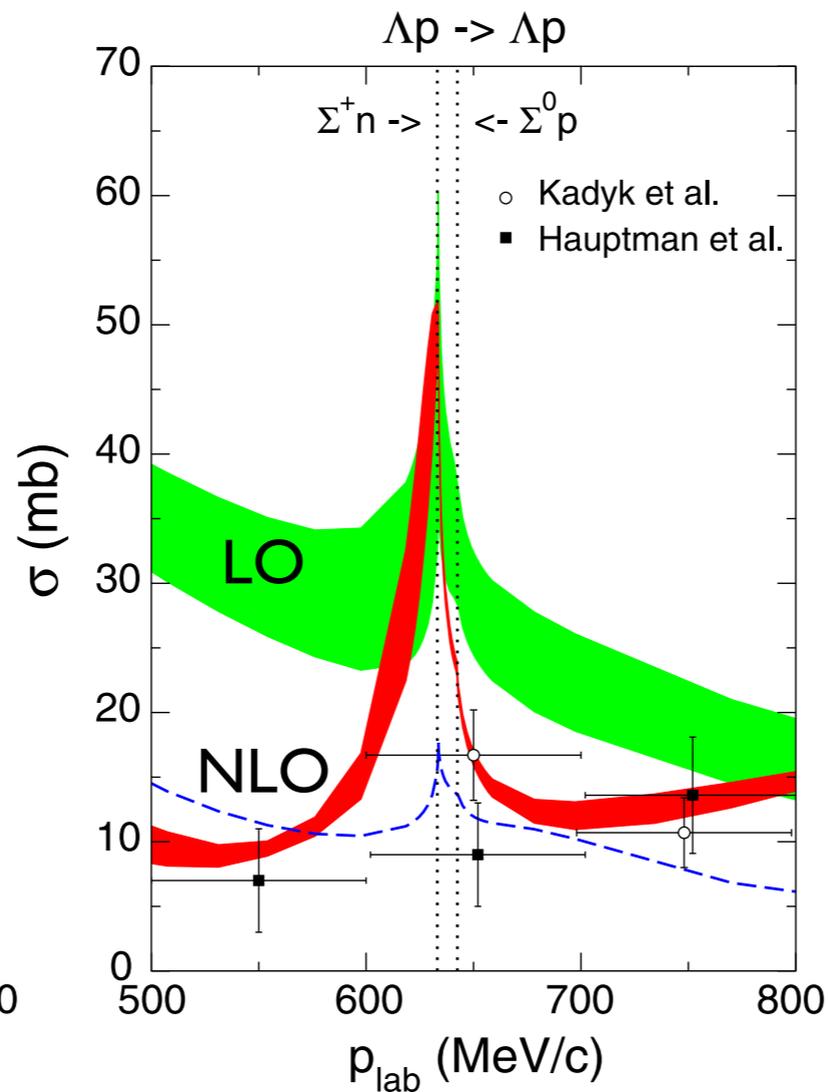
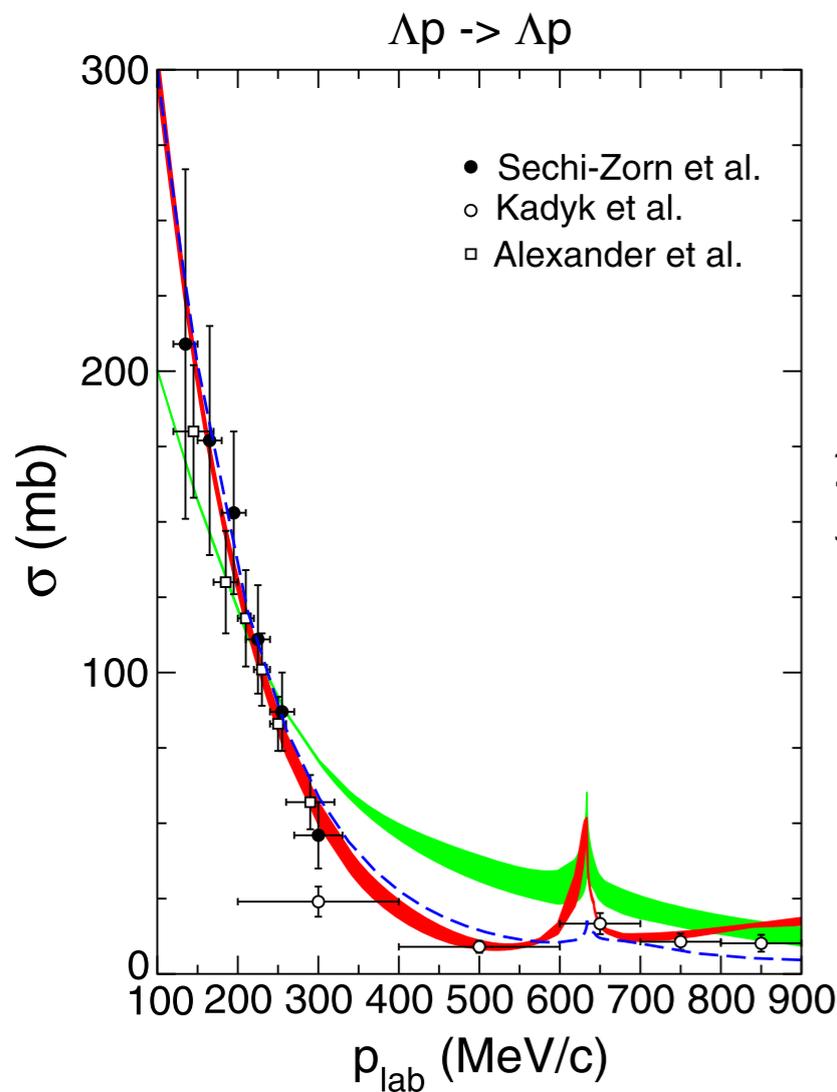
$$+ C_6 (\mathbf{q} \cdot \boldsymbol{\sigma}_1) (\mathbf{q} \cdot \boldsymbol{\sigma}_2) + C_7 (\mathbf{k} \cdot \boldsymbol{\sigma}_1) (\mathbf{k} \cdot \boldsymbol{\sigma}_2) + \frac{i}{2} C_8 (\boldsymbol{\sigma}_1 - \boldsymbol{\sigma}_2) \cdot (\mathbf{q} \times \mathbf{k})$$

see also:  
S. Petschauer, N. Kaiser  
Nucl. Phys. A 916 (2013) 1-29

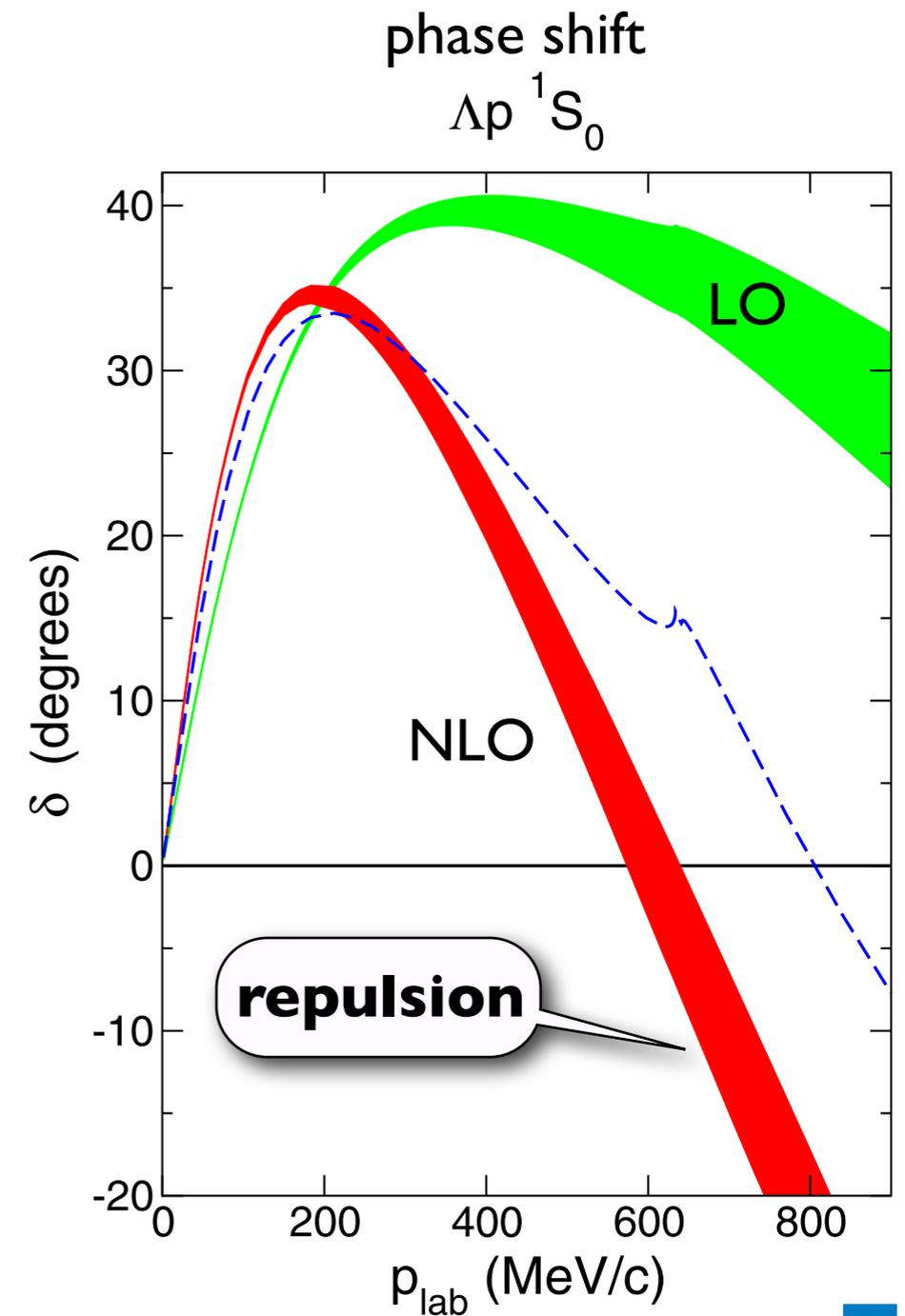
SU(3) relations for the various contact potentials in the isospin basis.  $C_\xi^{27}$  etc. refers to the corresponding irreducible SU(3) representation for a particular partial wave  $\xi$ . The actual potential still needs to be multiplied by pertinent powers of the momenta  $p$  and  $p'$ .

	Channel	I	$V(\xi)$		
			$\xi = {}^1S_0, {}^3P_0, {}^3P_1, {}^3P_2$	$\xi = {}^3S_1, {}^3S_1-{}^3D_1, {}^1P_1$	$\xi = {}^1P_1-{}^3P_1$
$S = 0$	$NN \rightarrow NN$	0	–	$C_\xi^{10^*}$	–
	$NN \rightarrow NN$	1	$C_\xi^{27}$	–	–
$S = -1$	$\Lambda N \rightarrow \Lambda N$	$\frac{1}{2}$	$\frac{1}{10} (9C_\xi^{27} + C_\xi^{8_s})$	$\frac{1}{2} (C_\xi^{8_a} + C_\xi^{10^*})$	$\frac{-1}{\sqrt{20}} C_\xi^{8_s 8_a}$
	$\Lambda N \rightarrow \Sigma N$	$\frac{1}{2}$	$\frac{3}{10} (-C_\xi^{27} + C_\xi^{8_s})$	$\frac{1}{2} (-C_\xi^{8_a} + C_\xi^{10^*})$	$\frac{-3}{\sqrt{20}} C_\xi^{8_s 8_a}$
	$\Sigma N \rightarrow \Lambda N$				$\frac{1}{\sqrt{20}} C_\xi^{8_s 8_a}$
	$\Sigma N \rightarrow \Sigma N$	$\frac{1}{2}$	$\frac{1}{10} (C_\xi^{27} + 9C_\xi^{8_s})$	$\frac{1}{2} (C_\xi^{8_a} + C_\xi^{10^*})$	$\frac{3}{\sqrt{20}} C_\xi^{8_s 8_a}$
	$\Sigma N \rightarrow \Sigma N$	$\frac{3}{2}$	$C_\xi^{27}$	$C_\xi^{10}$	–

# Hyperon - Nucleon Interaction (contd.)



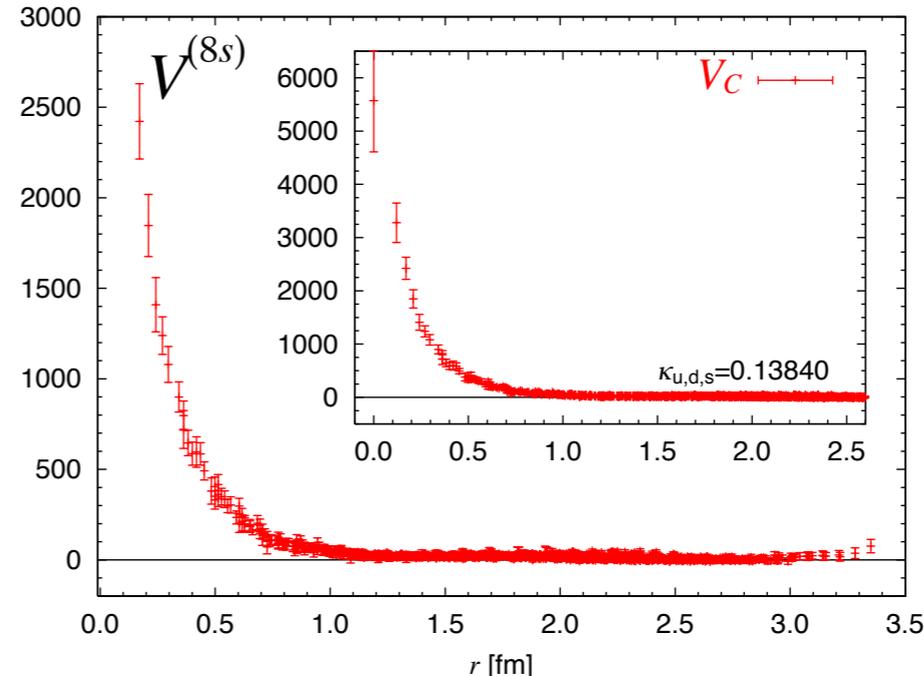
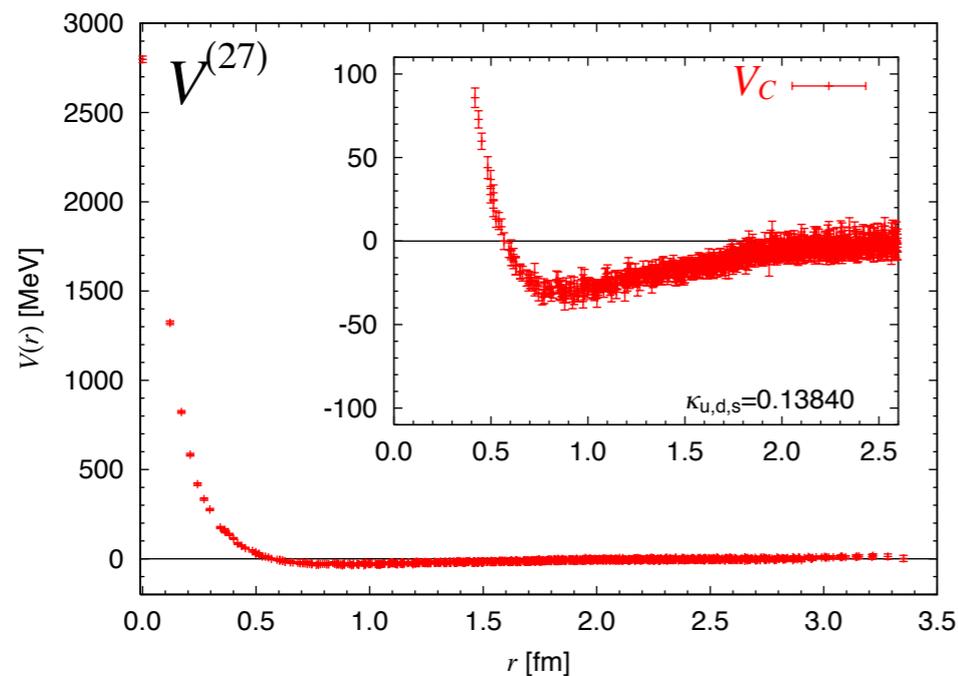
J. Haidenbauer, S. Petschauer, N. Kaiser,  
 U.-G. Meißner, A. Nogga, W.W.  
 Nucl. Phys. A 915 (2013) 24



● note:  
**moderate attraction** at low momenta  
**strong repulsion** at higher momenta

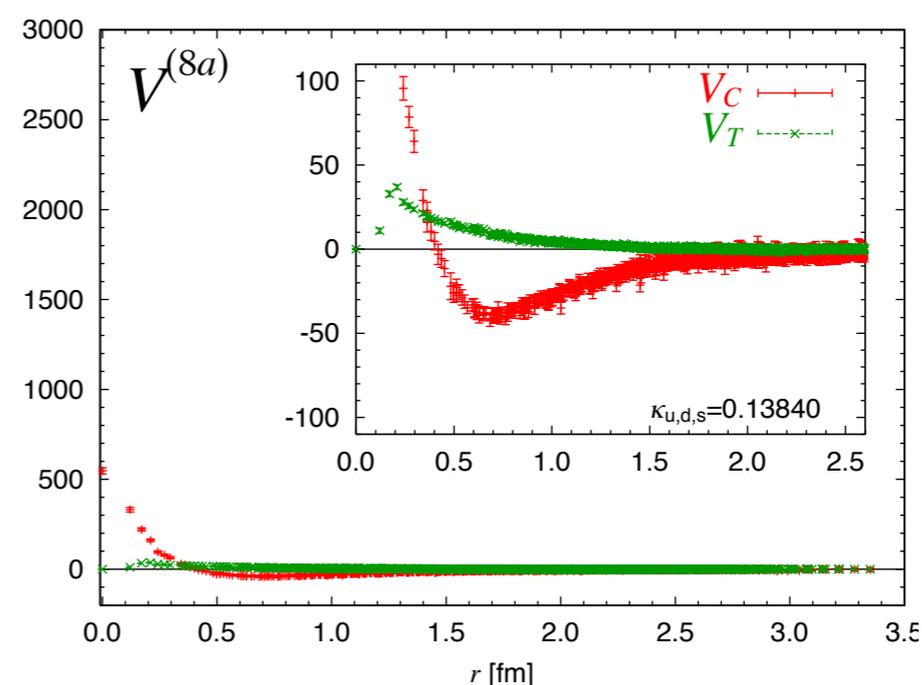
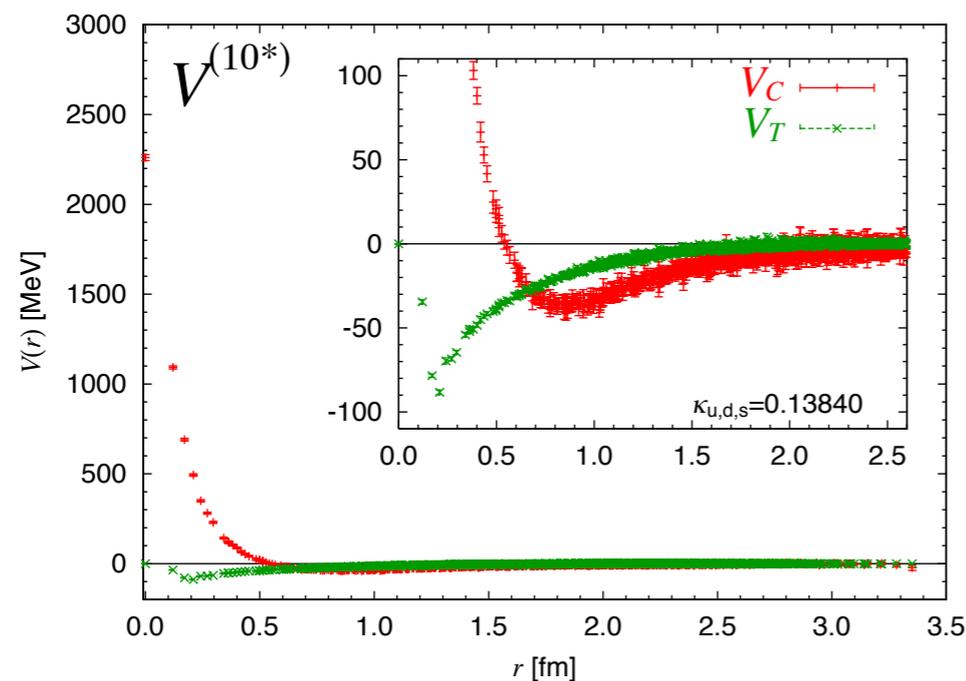
# Hyperon - Nucleon Interactions from Lattice QCD

$$\Lambda N(^1S_0) = \frac{9}{10} [27] + \frac{1}{10} [8_s]$$



$m_{ps} = 0.47 \text{ GeV}$

$$\Lambda N(^3S_1) = \frac{1}{2} [10^*] + \frac{1}{2} [8_a]$$



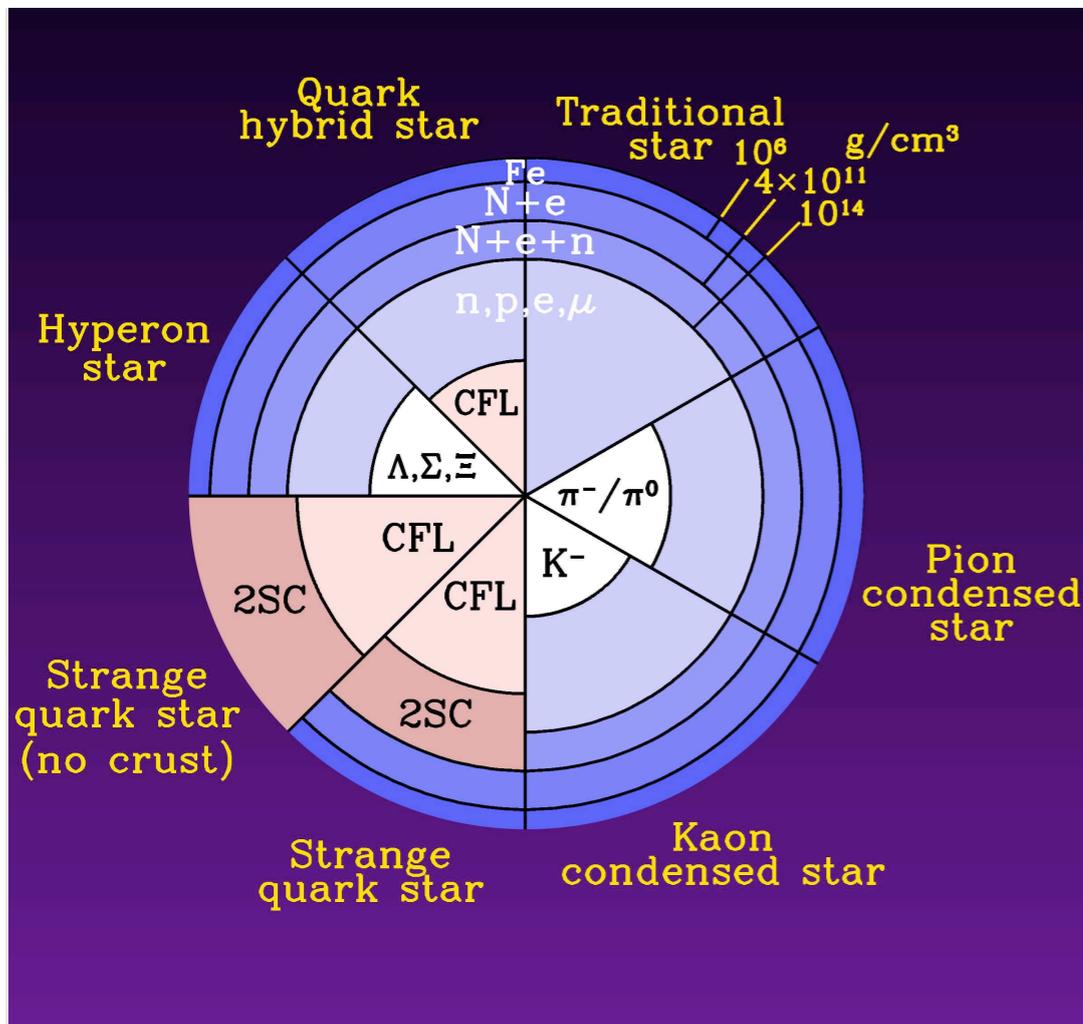
T. Inoue et al.  
(HAL QCD)  
PTP 124 (2010) 591  
Nucl. Phys.  
A881 (2012) 28



# NEUTRON STARS and the EQUATION OF STATE of DENSE BARYONIC MATTER

J. Lattimer, M. Prakash: *Astrophys. J.* 550 (2001) 426  
*Phys. Reports* 442 (2007) 109

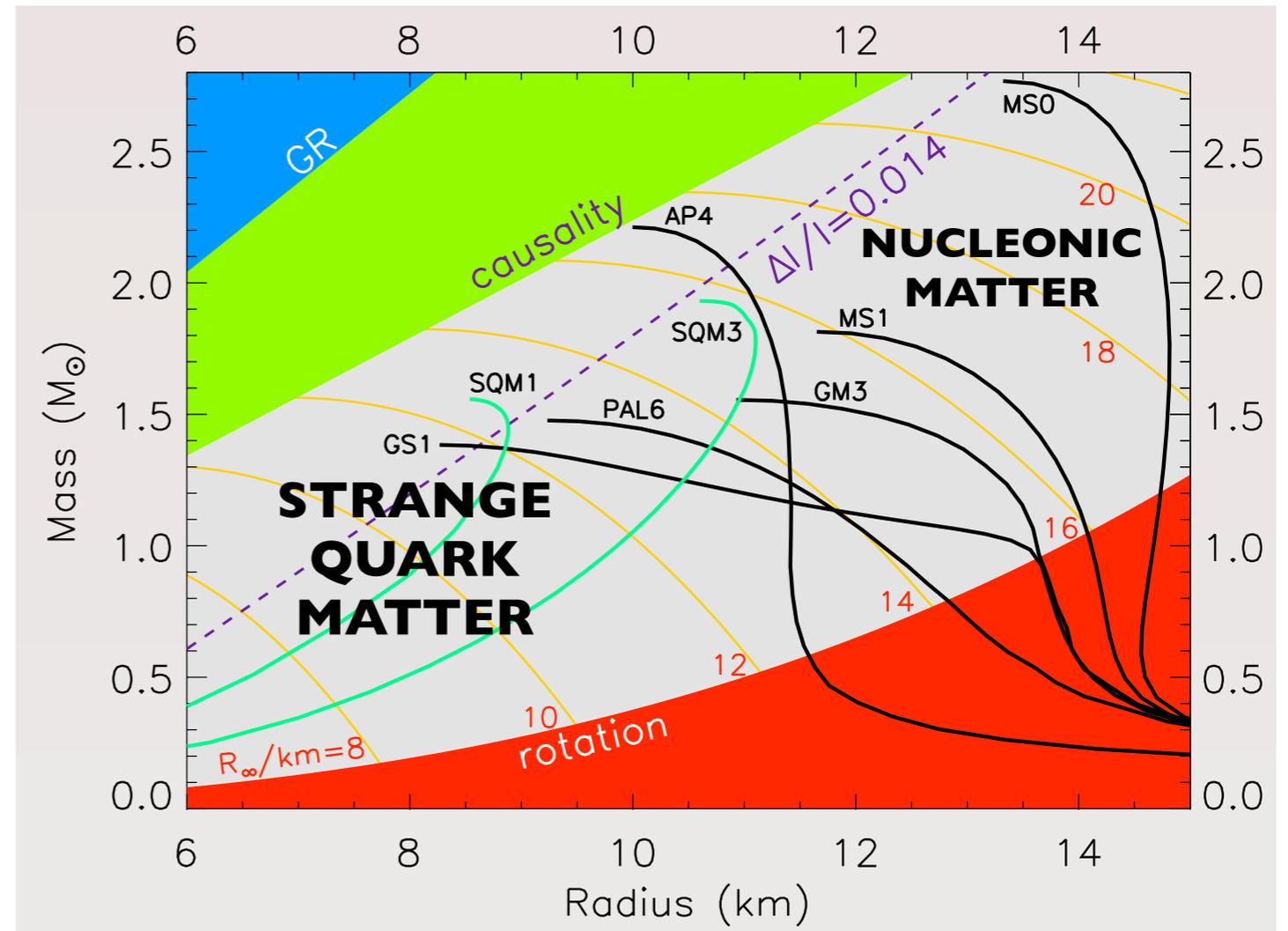
## ● Mass-Radius Relation



## Neutron Star Scenarios Tolman-Oppenheimer-Volkov Equations

$$\frac{dP}{dr} = -\frac{G}{c^2} \frac{(M + 4\pi Pr^3)(\mathcal{E} + P)}{r(r - GM/c^2)}$$

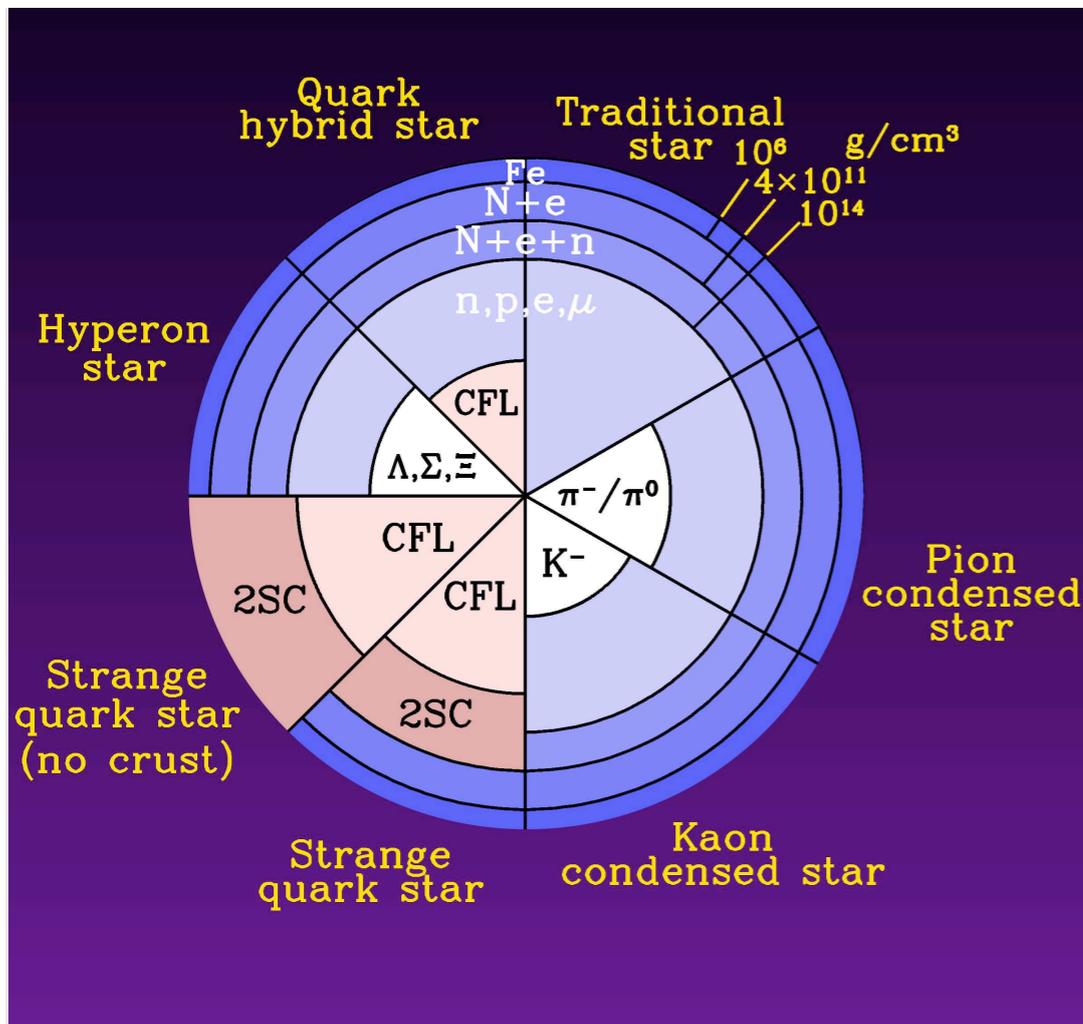
$$\frac{dM}{dr} = 4\pi r^2 \frac{\mathcal{E}}{c^2}$$



# NEUTRON STARS and the EQUATION OF STATE of DENSE BARYONIC MATTER

J. Lattimer, M. Prakash: *Astrophys. J.* 550 (2001) 426  
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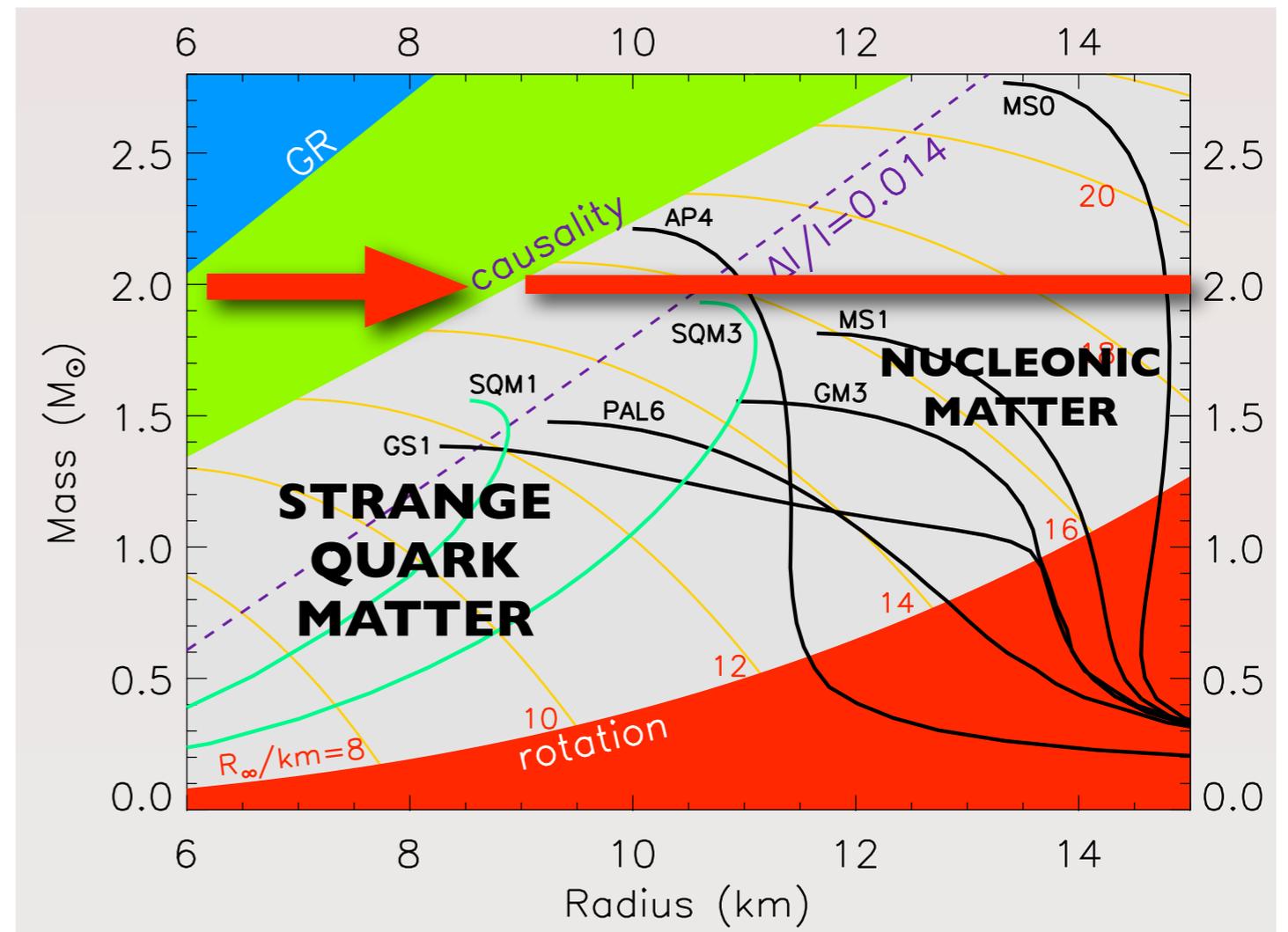
## ● Mass-Radius Relation



## Neutron Star Scenarios Tolman-Oppenheimer-Volkov Equations

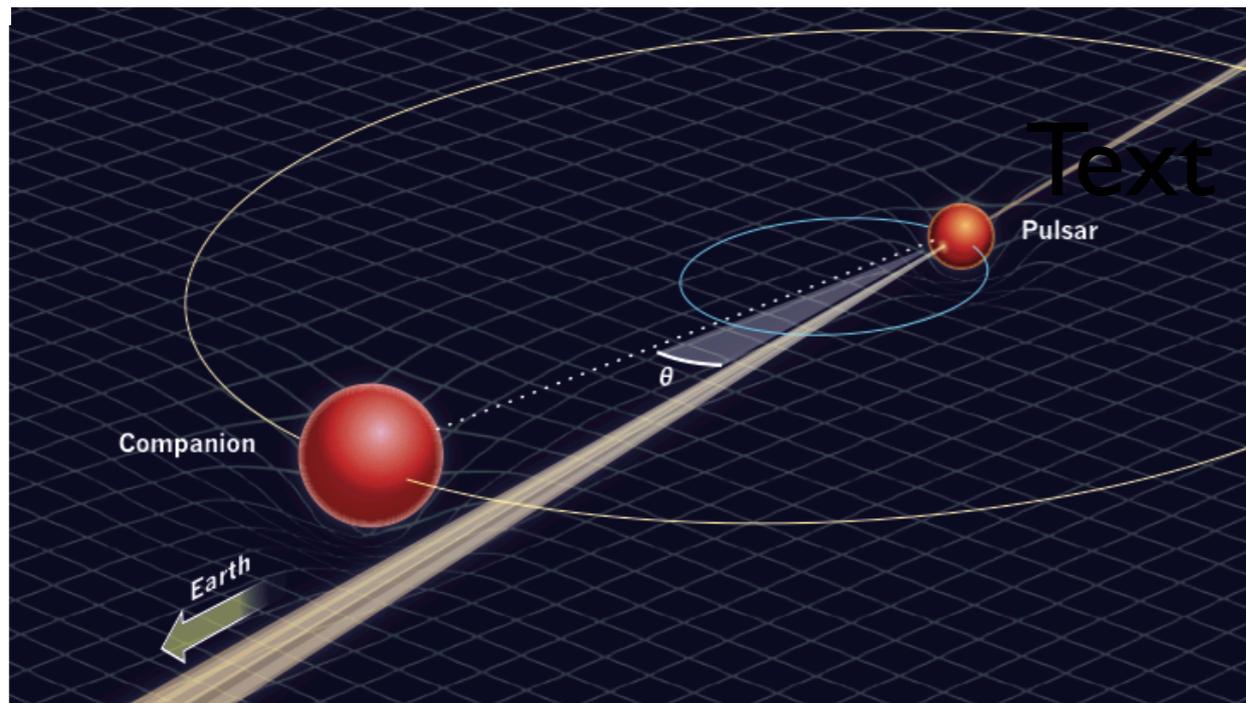
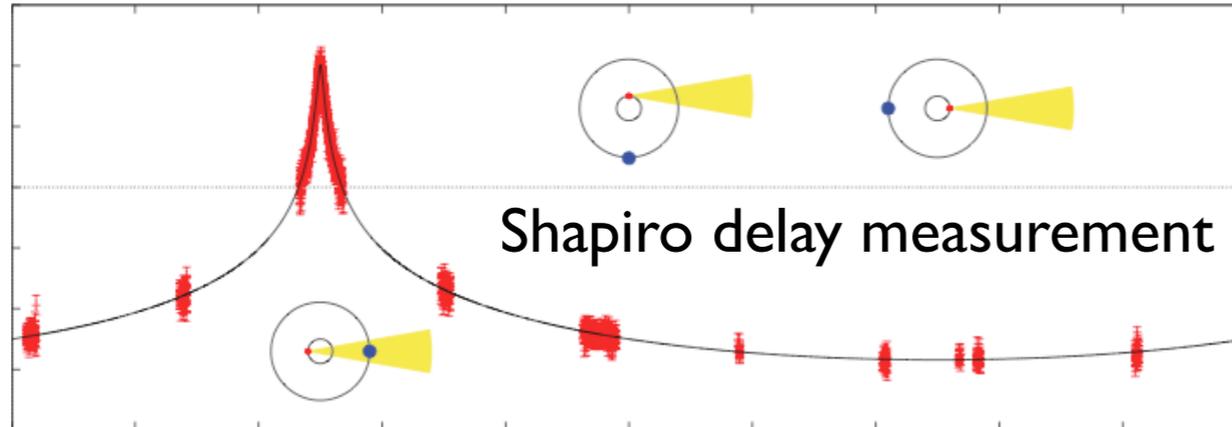
$$\frac{dP}{dr} = -\frac{G}{c^2} \frac{(M + 4\pi Pr^3)(\mathcal{E} + P)}{r(r - GM/c^2)}$$

$$\frac{dM}{dr} = 4\pi r^2 \frac{\mathcal{E}}{c^2}$$



# New constraints from NEUTRON STARS

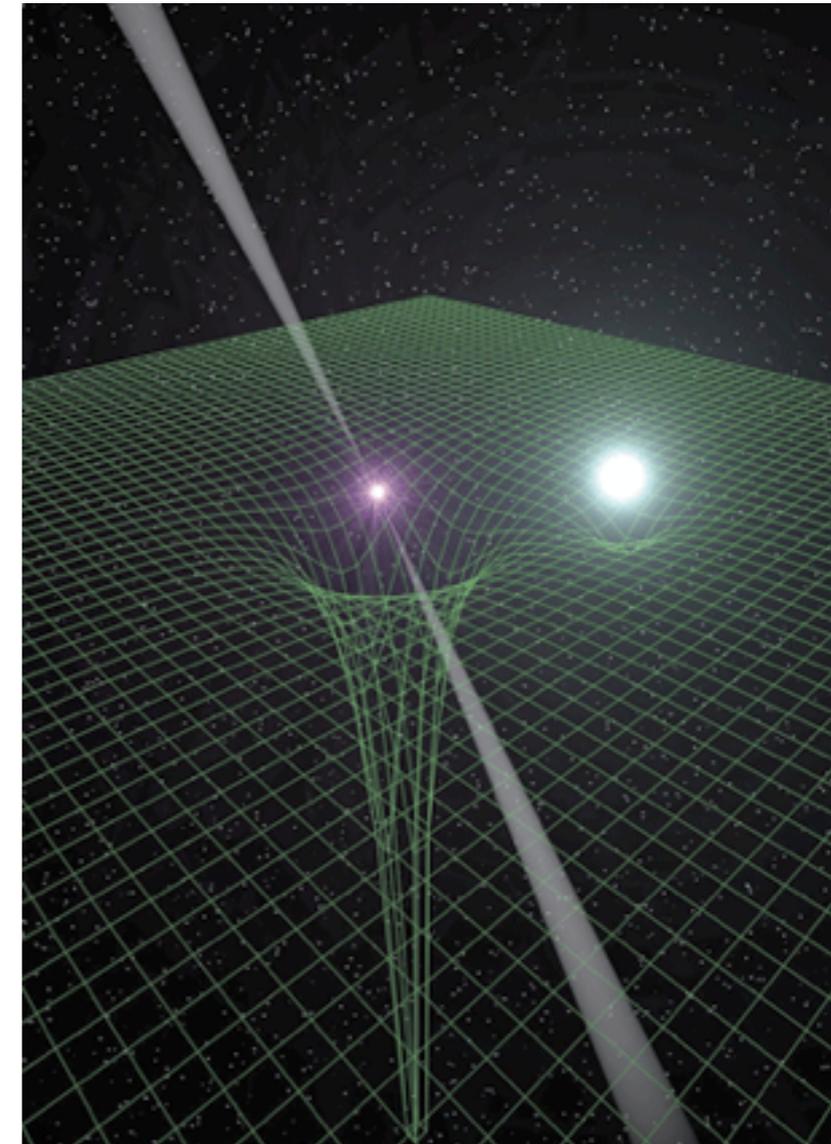
P.B. Demorest et al.  
Nature 467 (2010) 1081



PSR J1614+2230

$$M = 1.97 \pm 0.04 M_{\odot}$$

J. Antoniadis et al.  
Science 340 (2013) 6131



PSR J0348+0432

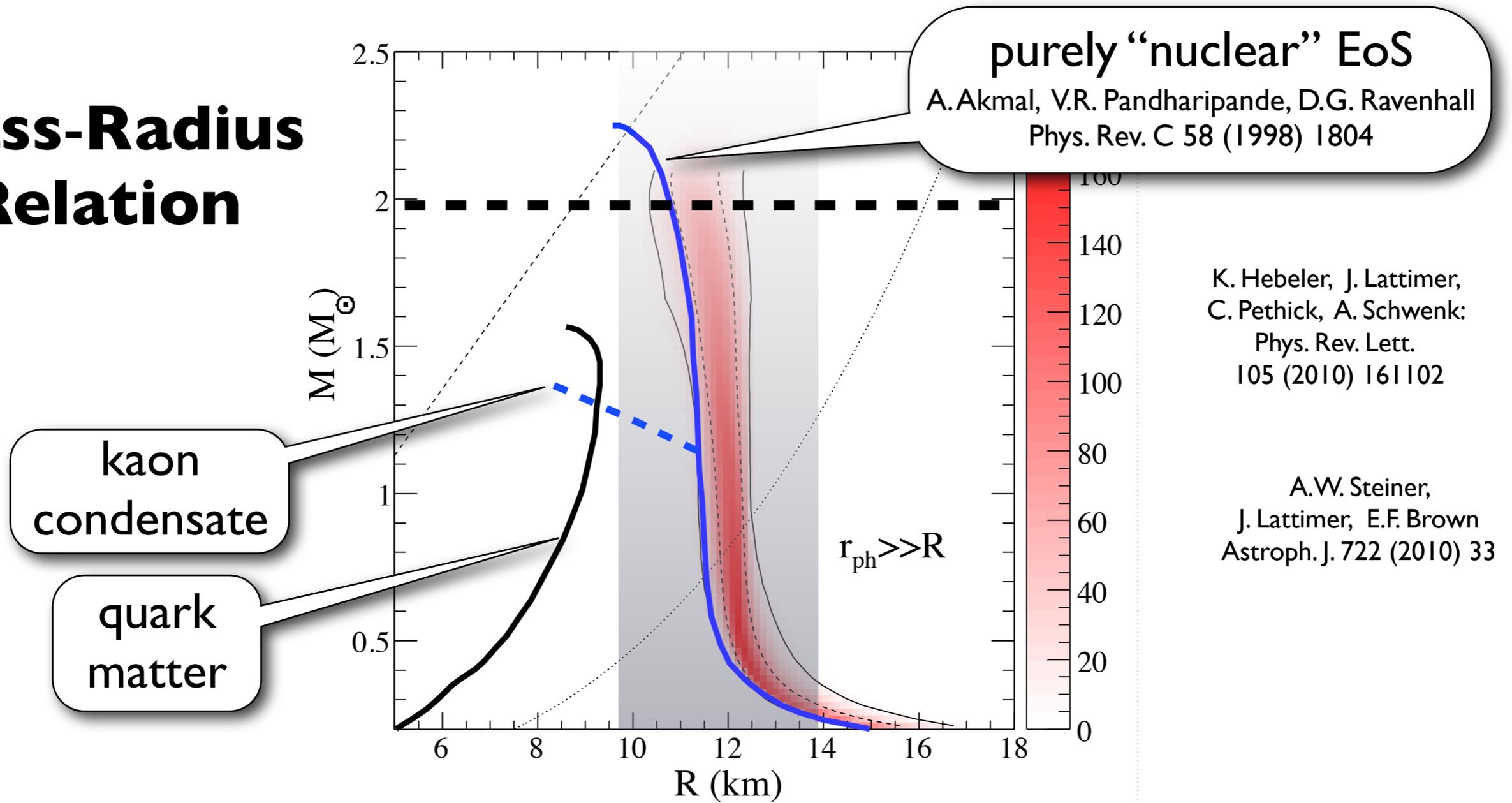
$$M = 2.01 \pm 0.04 M_{\odot}$$

# News from NEUTRON STARS

- Constraints from **neutron star observables**

F. Özel, D. Psaltis: Phys. Rev. D80 (2009) 103003  
 F. Özel, G. Baym, T. Güver: Phys. Rev. D82 (2010) 101301

## Mass-Radius Relation

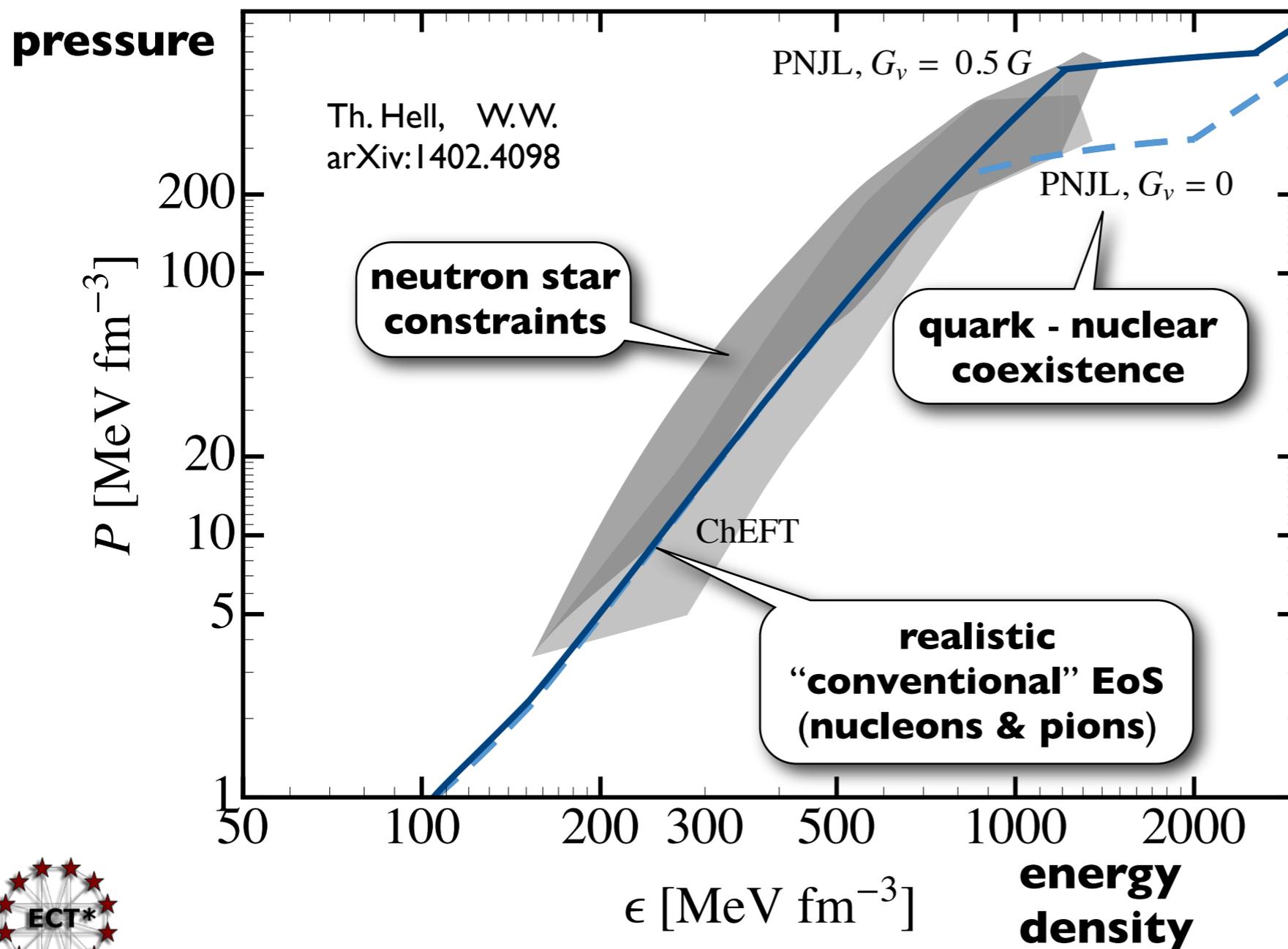


- “**Exotic**” equations of state ruled out ?

# NEUTRON STAR MATTER

## Equation of State

- In-medium **Chiral Effective Field Theory** up to 3 loops (reproducing thermodynamics of normal nuclear matter)
- 3-flavor PNJL (chiral quark) model at high densities (incl. **strange** quarks)



- beta equilibrium  
 $n \leftrightarrow p + e, \mu$
- charge conservation
- coexistence region:  
**Gibbs conditions**

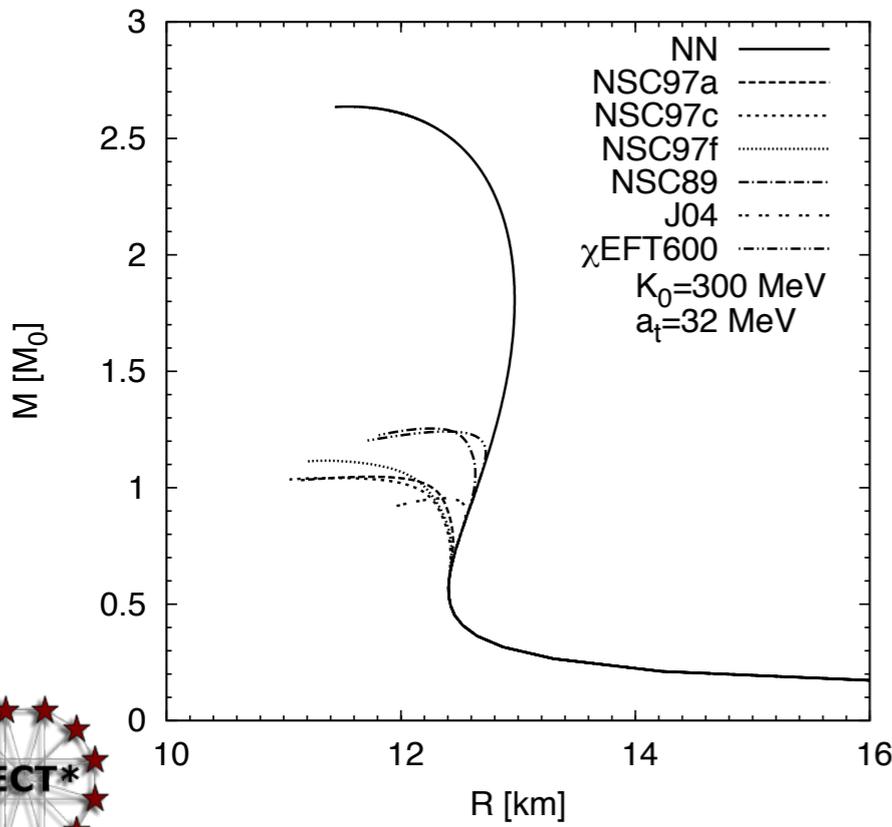
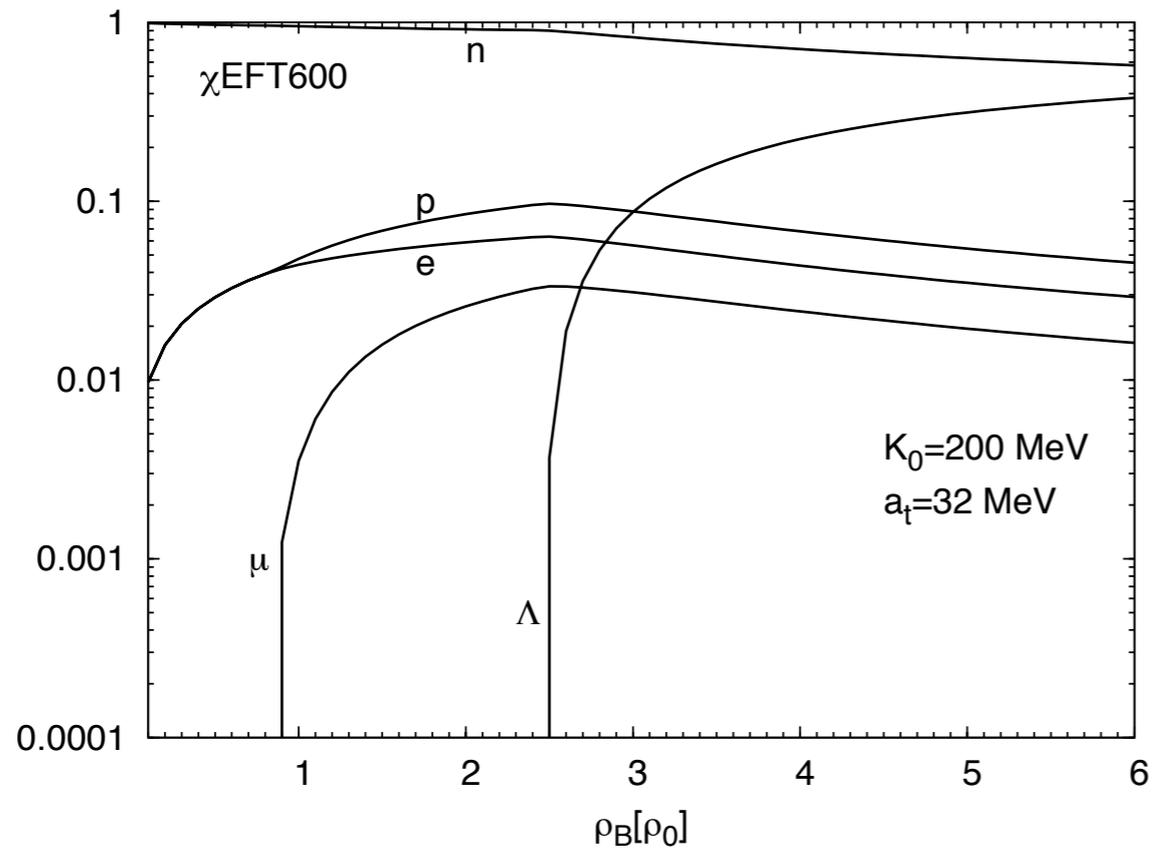
● **quark-nuclear** coexistence occurs (if at all) at baryon densities  $\rho > 5 \rho_0$

see also:

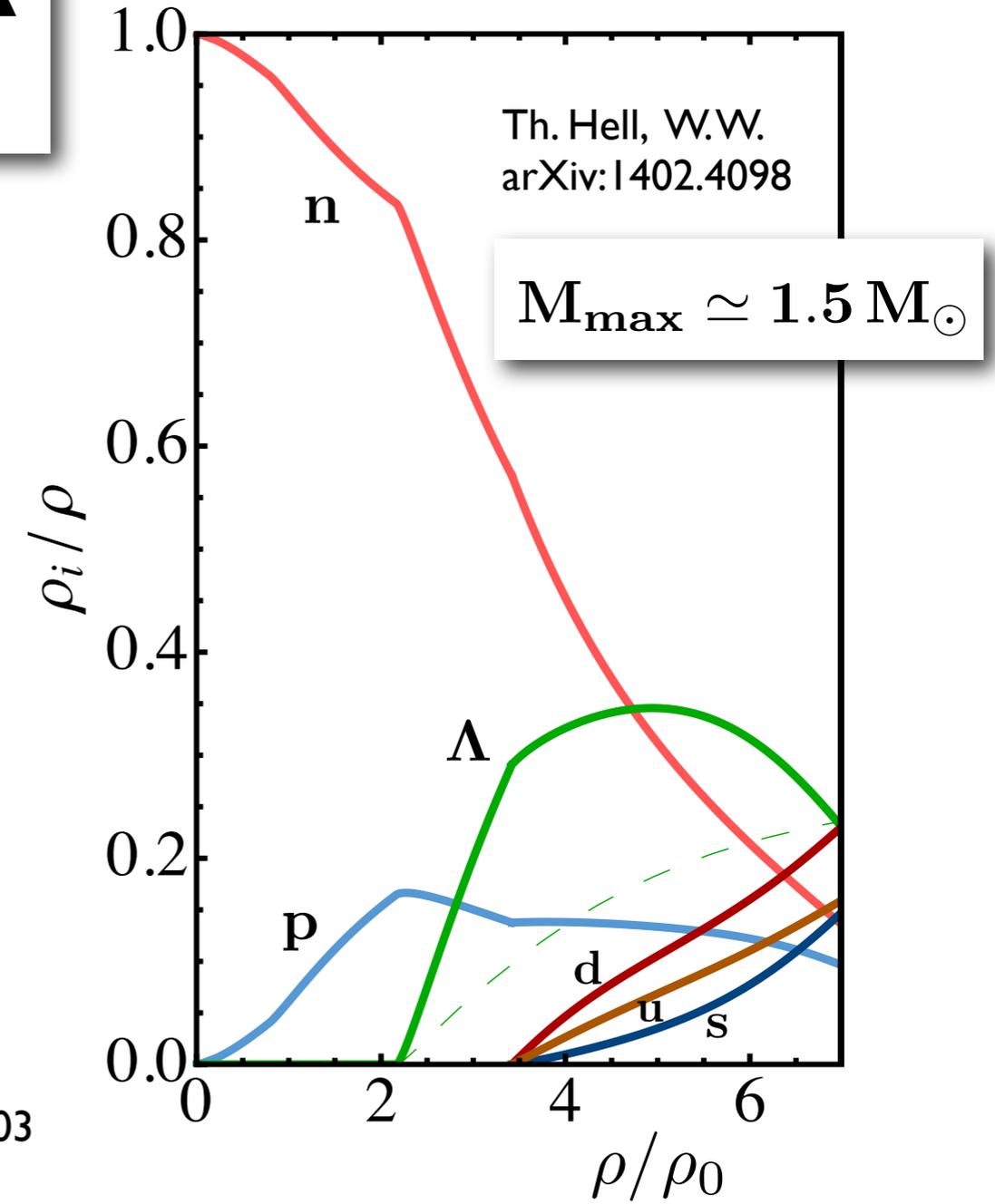
K. Masuda, T. Hatsuda, T. Takatsuka  
PTEP (2013) 7, 073D01



# NEUTRON STAR MATTER including HYPERONS



H. Djapo,  
 B.-J. Schaefer,  
 J. Wambach  
 Phys. Rev. C81 (2010) 035803

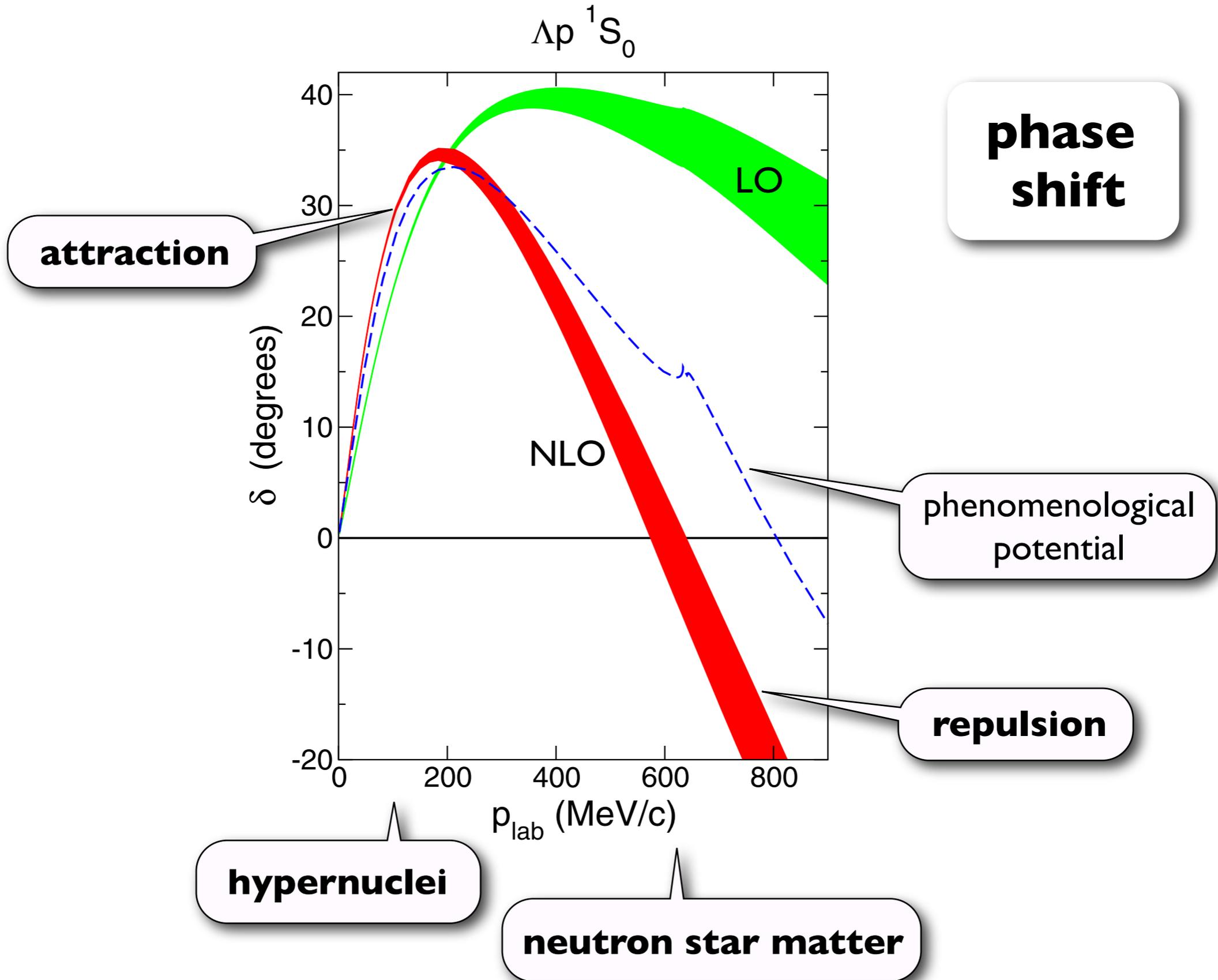


with inclusion of hyperons:  
**EoS too soft** to support 2 solar mass star  
 unless strong short-range **repulsion** in  
 YN and / or YNN interactions



recall:

# Chiral SU(3) Effective Field Theory and Hyperon-Nucleon Interactions



# SUMMARY

- **Chiral SU(3) Effective Field Theory**
  - ▶ realization of **low-energy QCD** with **strange quarks**
  - ▶ well-defined framework  
both for **antikaon-** and **hyperon-**nuclear systems
- Active communication between **theory** and **experiment**
  - ▶ **progress** in understanding the  $\Lambda(1405)$
  - ▶  $\bar{K}NN$  **threshold** and **subthreshold** physics:  
**focused** experimental programmes
- Role of **strangeness** in **dense matter**
  - ▶ new constraints from **two-solar-mass neutron stars**:  
**stiff** equation-of-state
  - ▶ consequences for hyperon-nuclear two- and three-body interactions:  
quest for strong short-distance **repulsion**

