

# Puzzling out the proton radius puzzle

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THE LOW-ENERGY FRONTIER  
OF THE STANDARD MODEL

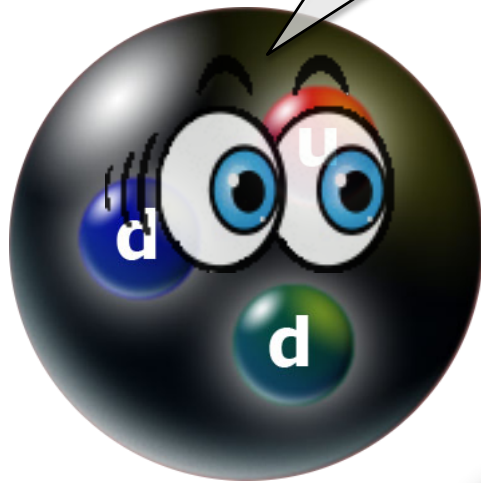


A1

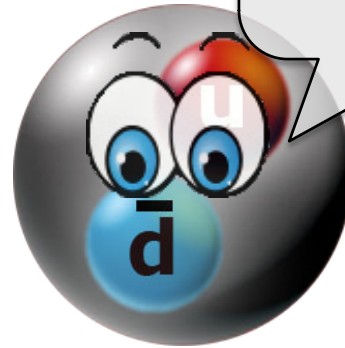


M E S O N  
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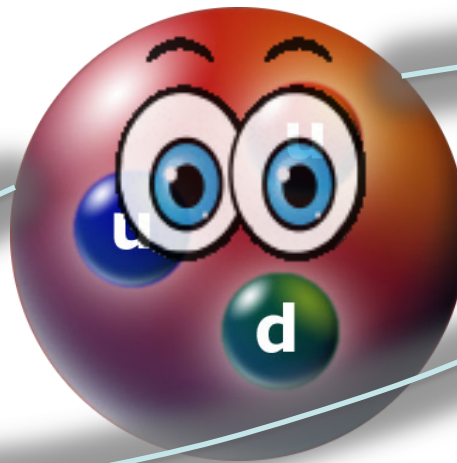
And what is he doing on a Meson conference ?!



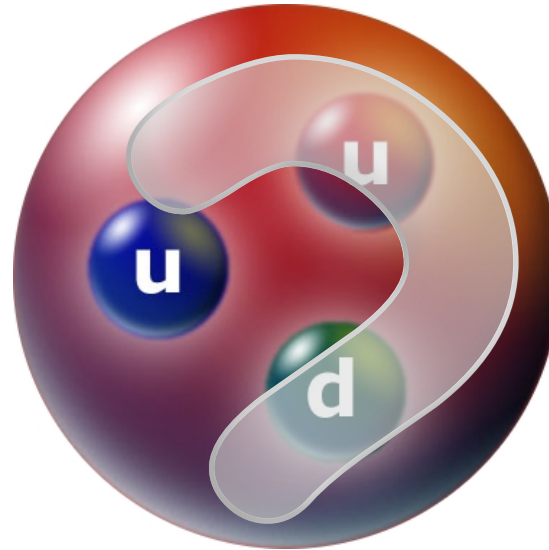
Probably bragging about his extra quark and causing all sorts of problems!



It puzzles me, but he dragged me into it as well!



# What is the size of the proton?



1963

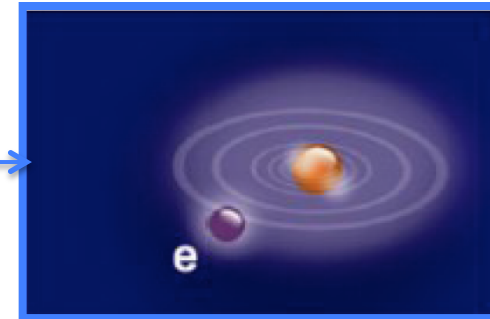
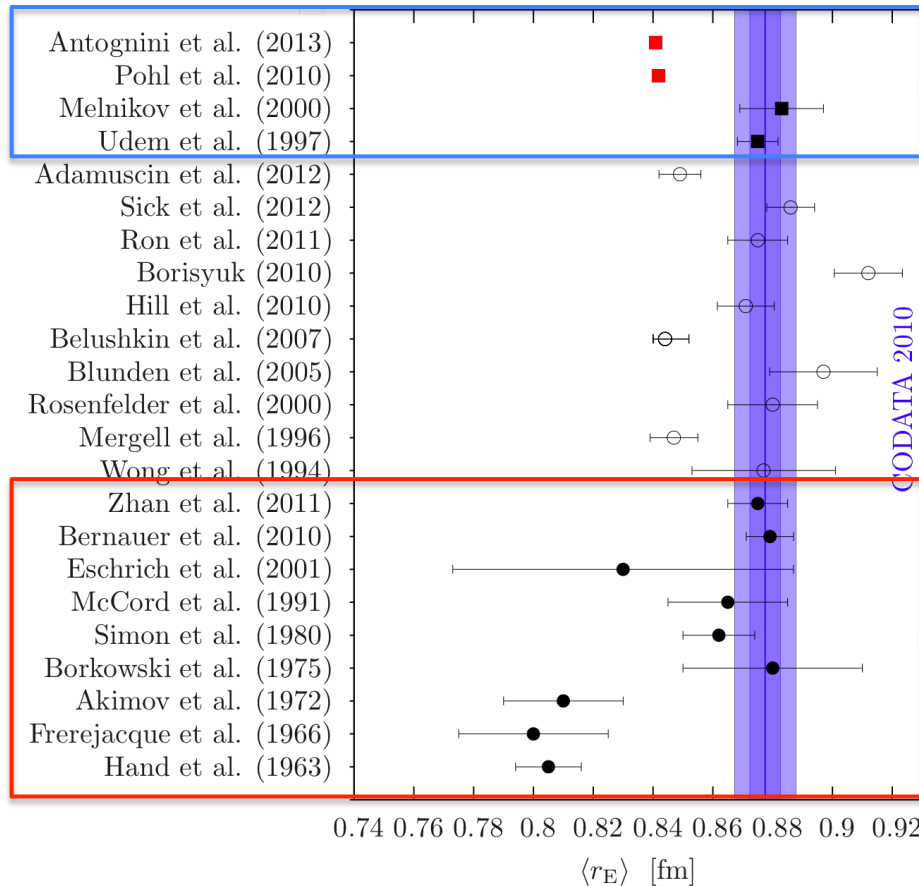


2014

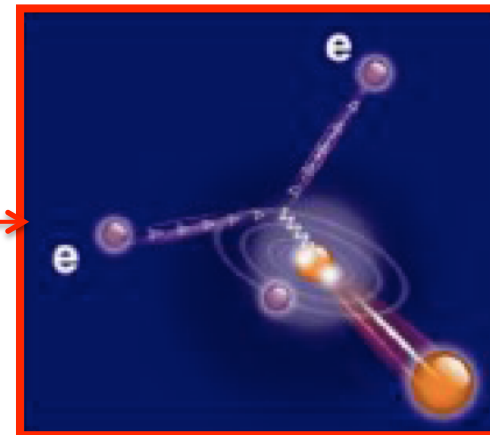


After 50 year of research is the size of the proton still not understood to a desirable accuracy!

# The proton radius puzzle



Atomic spectroscopy



V. Sulkosky

Scattering experiments

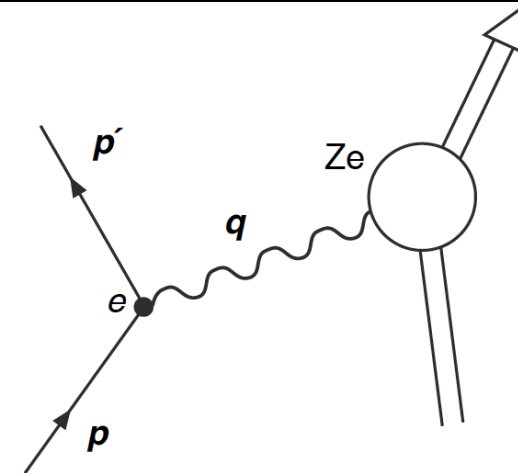
- Many different measurements done through the years.
- New  $\mu$ -p Lamb shift measurement,  $7\sigma$  away.
- Further investigations necessary.

# Elastic Cross-Section measurement

- Radius can be obtained by measuring cross section of  $H(e, e')p$ :

$$\frac{d\sigma}{d\Omega} = \left( \frac{d\sigma}{d\Omega} \right)_{Mott} \frac{1}{1 + \tau} \left[ G_E^2(Q^2) + \frac{\tau}{\epsilon} G_M^2(Q^2) \right]$$

$$\epsilon = \left[ 1 + 2(1 + \tau) \tan^2 \frac{\vartheta_e}{2} \right]^{-1} \quad \tau = \frac{Q^2}{4m_p^2},$$

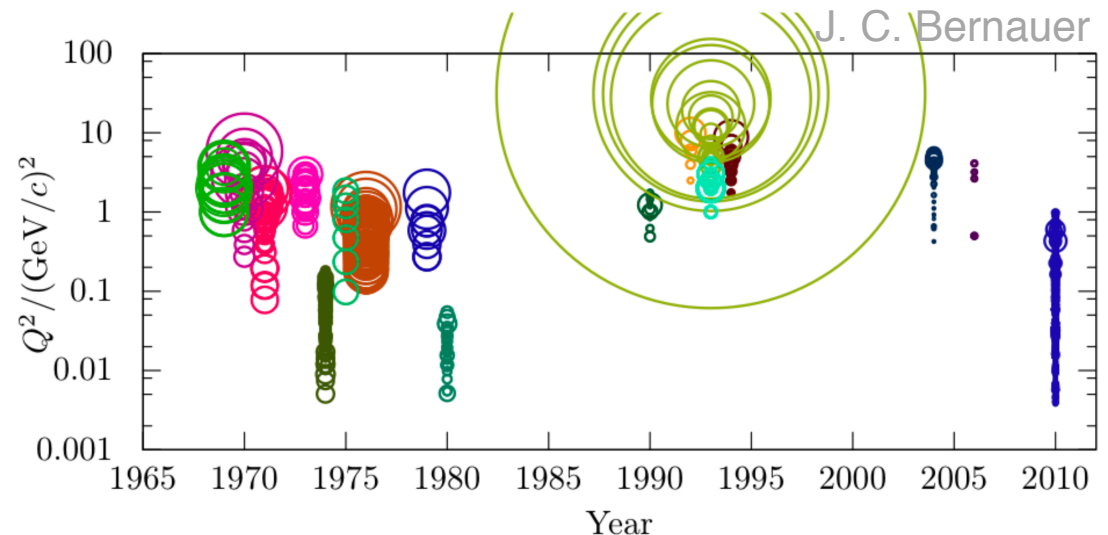


- Extraction of FF via Rosenbluth Separation (separation at constant  $Q^2$ ):

$$G_E(Q^2) \approx G^{Dipole}(Q^2) = \left( 1 + \frac{Q^2}{0.71} \right)^{-2}$$

- Best estimate for radius:

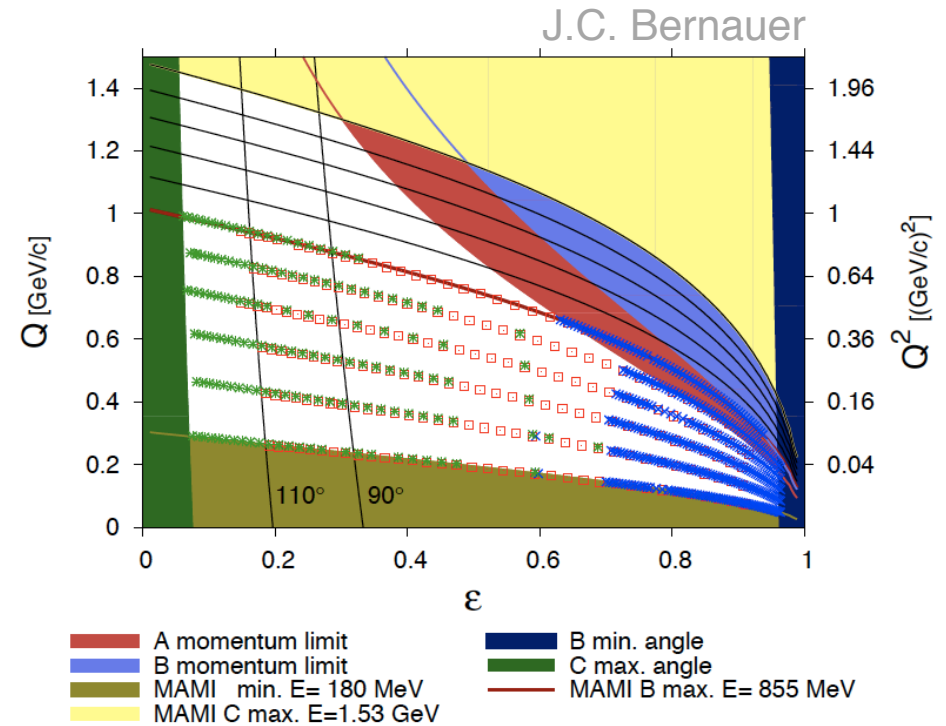
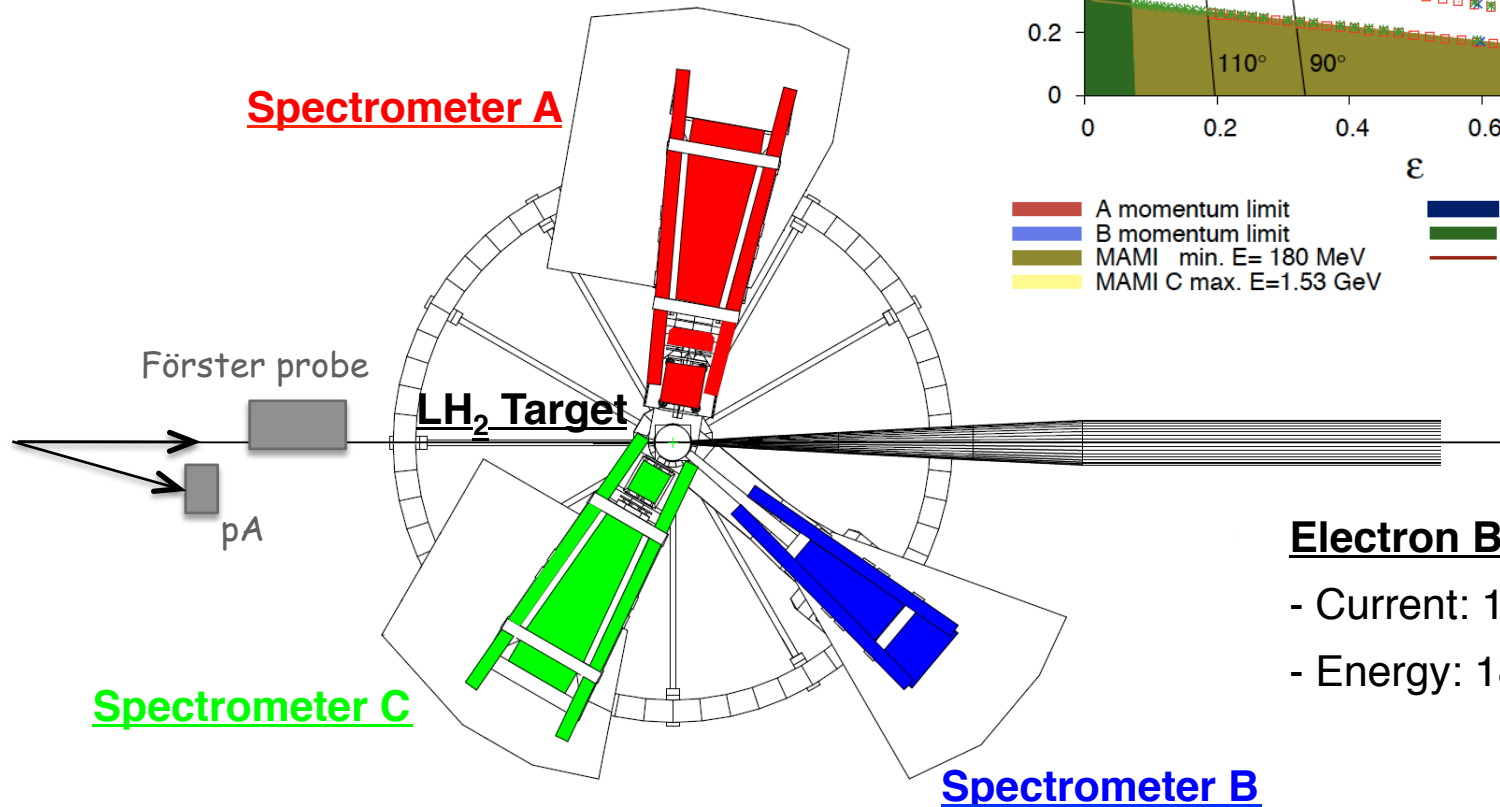
$$\langle r_E^2 \rangle = -6\hbar^2 \left. \frac{d}{dQ^2} G_E(Q^2) \right|_{Q^2=0}$$



- |             |             |            |         |          |
|-------------|-------------|------------|---------|----------|
| ○ Andivahis | ○ Borkowski | ○ Janssens | ○ Rock  | ○ Walker |
| ○ Bartel    | ○ Bosted    | ○ Litt     | ○ Sill  |          |
| ○ Berger    | ○ Christy   | ○ Price    | ○ Simon |          |
| ○ Bernauer  | ○ Goitein   | ○ Qattan   | ○ Stein |          |

# The MAMI experiment

- $H(e,e')p$  cross-section measurement.
- About **1400** measured cross-section points.
- Data for  $0.004 \leq Q^2 \leq 1 (\text{GeV}/c)^2$ .
- Statistical precision better than 0.2%.



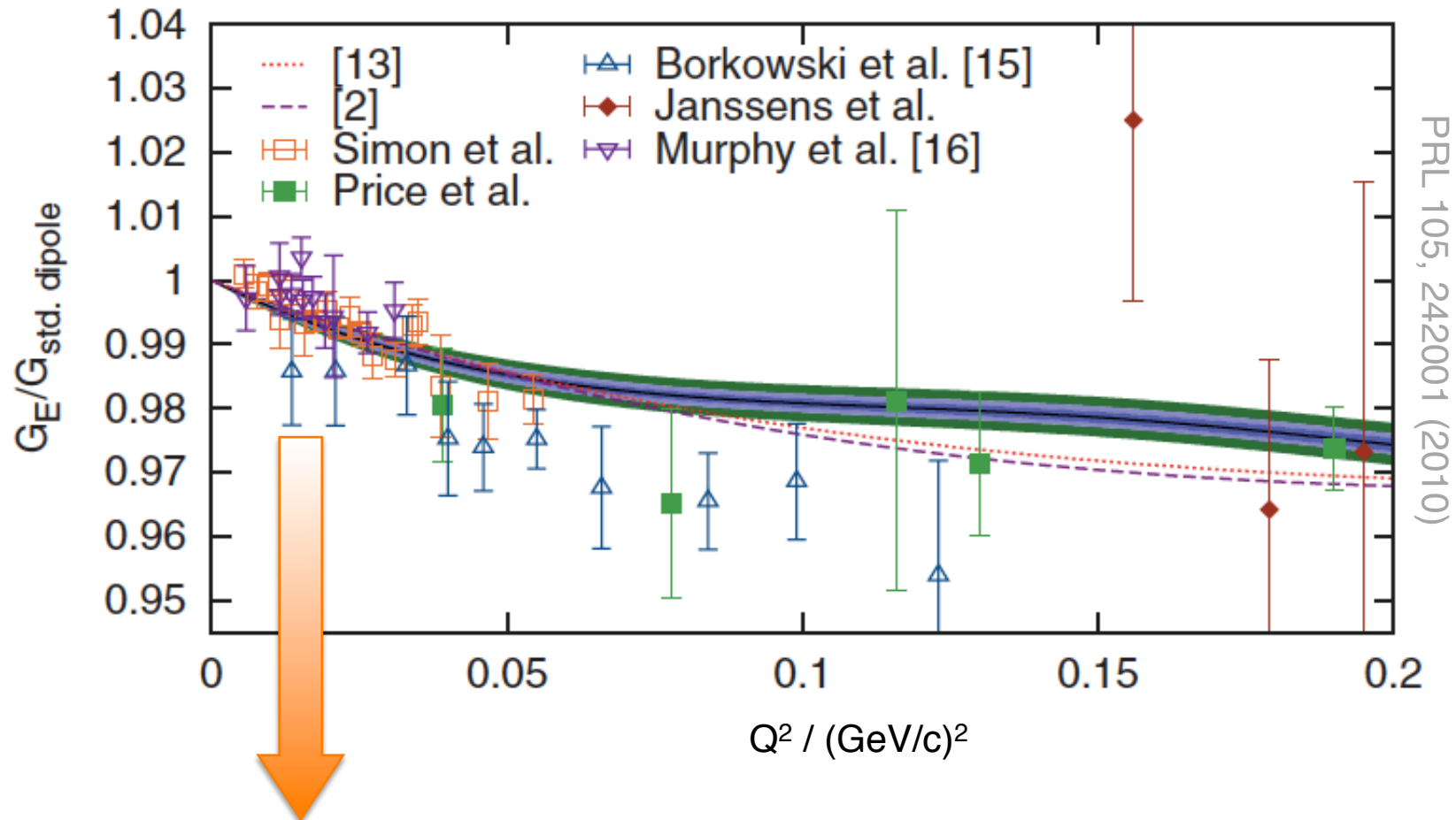
## Electron Beam:

- Current: 1 nA – 10  $\mu$ A
- Energy: 180 – 855 MeV

# The best cross-section measurement

- Direct fit of  $G_E$ ,  $G_M$  models to the data for all  $Q^2$  and  $\vartheta$ :

$$\chi^2/(1400) \approx 1.14$$



PRL 105, 242001 (2010)

$$\sqrt{\langle r_E^2 \rangle} = 0.879 \pm 0.005_{\text{stat}} \pm 0.004_{\text{syst}} \pm 0.002_{\text{mod}} \pm 0.004_{\text{group}} \text{ fm}$$

# Hydrogen spectroscopy

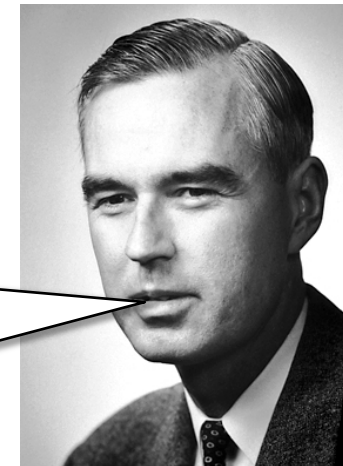
- Spectroscopy of Hydrogen states represents a stringent test of QED.
- Tests require two input parameters:  $R_\infty$  and  $r_p$ .

Determine parameters with other measurements and use them to test QED.

Trust QED and use it to determine the values of two free parameters.

- An important success of the QED is the prediction and measurement of the **Lamb shift (1947)**:

There is small difference in energy between energy levels  $2S_{1/2}$  and  $2P_{1/2}$  due to QED vacuum fluctuations.





# Lamb shift in Hydrogen

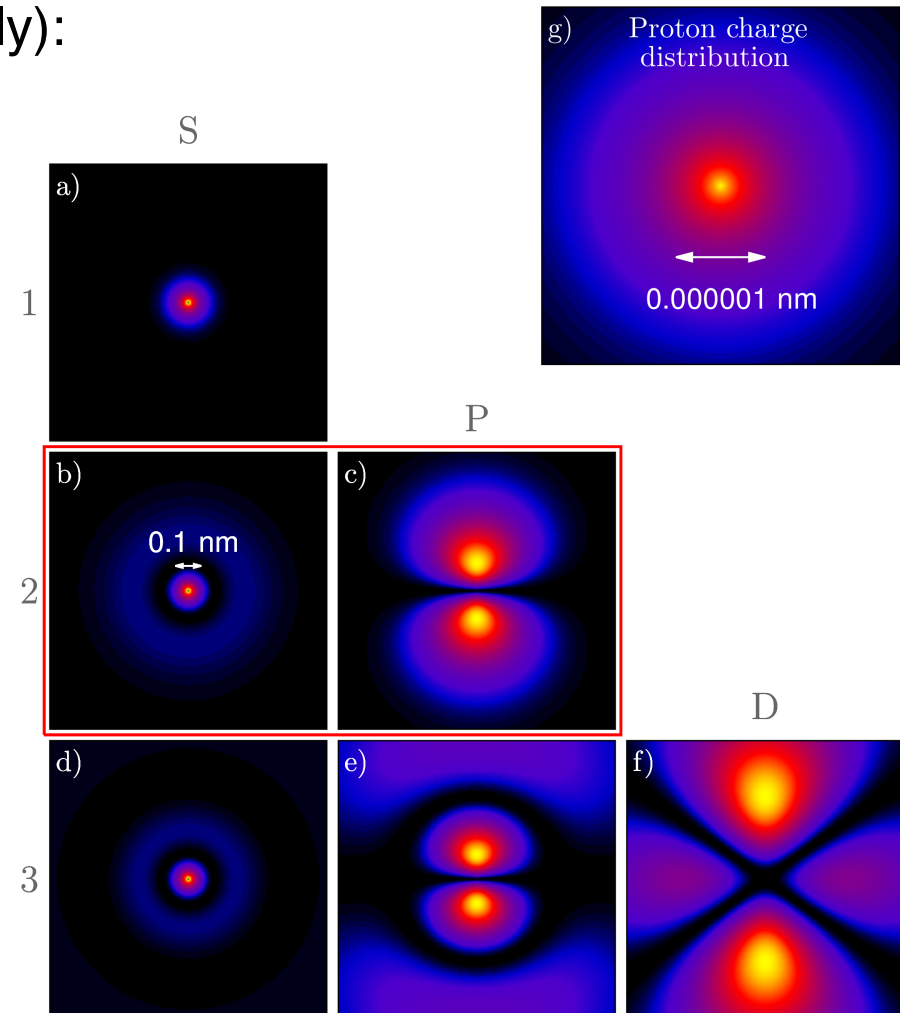
- Change in level energy (approximately):

$$\Delta E_{Lamb}^{nl} \propto |\psi_{nl}(0)|^2$$

$$E(nS) \cong -\frac{R_\infty}{n^2} + \frac{\Delta E_{Lamb}^{1S}}{n^3}$$

$$\Delta E_{Lamb}^{1S} \cong (8.172 + 1.56 r_p^2) \text{ MHz}$$

- Significant effect in S-states and only tiny change in P-states.
- The center of the hydrogen atom is not empty. **Proton is here!**

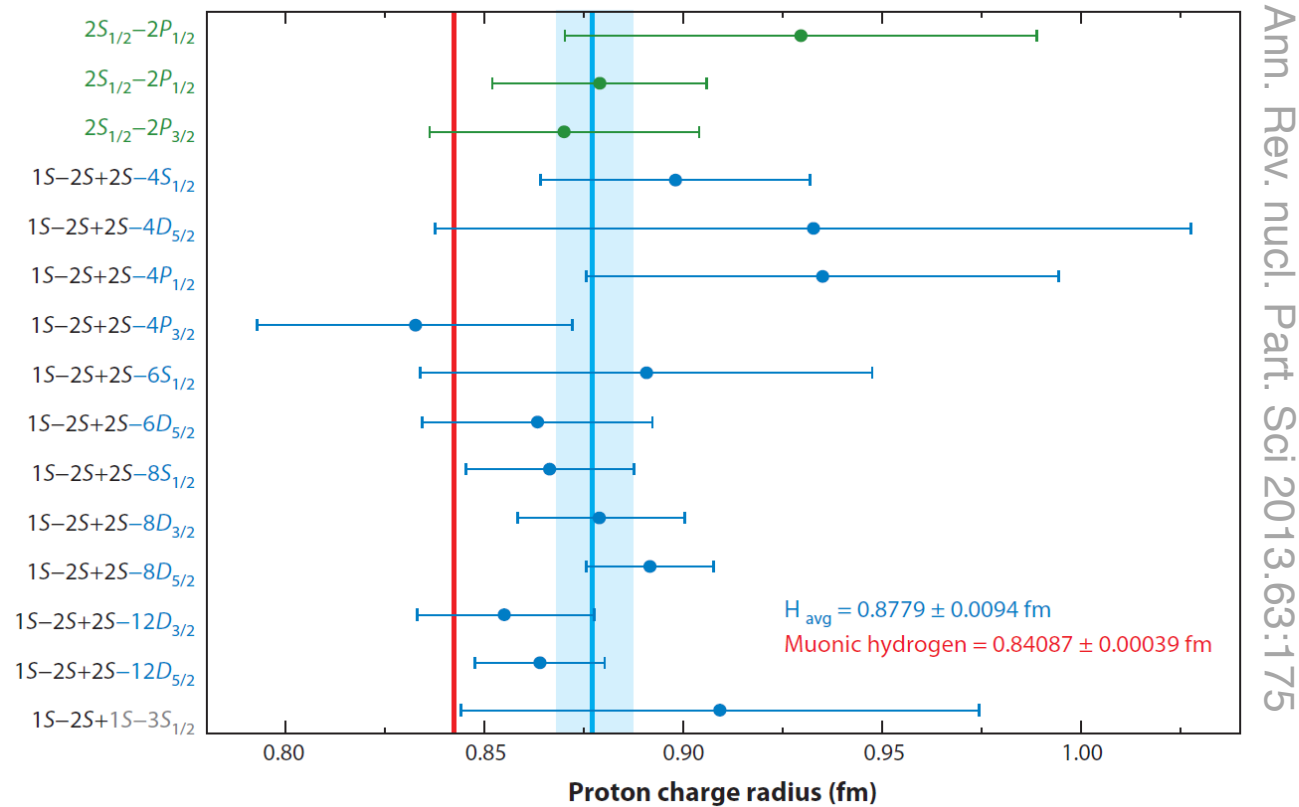


Electron probability densities for different states in eH

- Different **n-dependence** of the two terms allows the determination of  $R_\infty$  and  $r_p$  from at least two different measurements.

# Hydrogen measurement

- Many different level transitions have been measured.

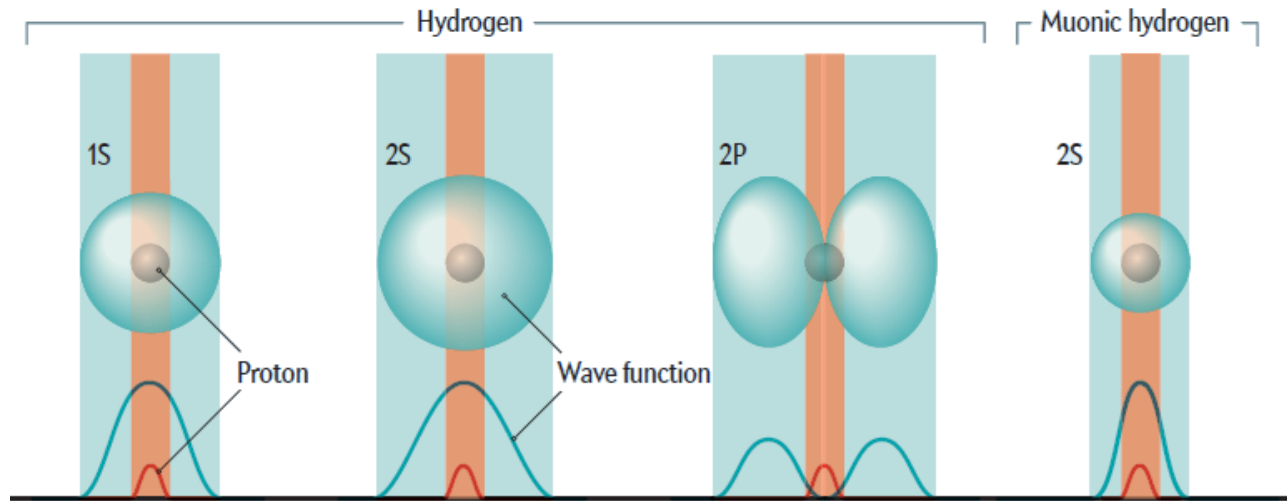


- These results together with scattering data form the new CODATA value.

$$\sqrt{\langle r_E^2 \rangle} = 0.8775 \pm 0.0051 \text{ fm}$$

# $\mu\text{P}$ -Lamb shift measurement

- Allows better determination of proton charge radius.
- Due to larger mass muon much closer to the nucleus, resulting in a more **pronounced Lamb shift effect**.



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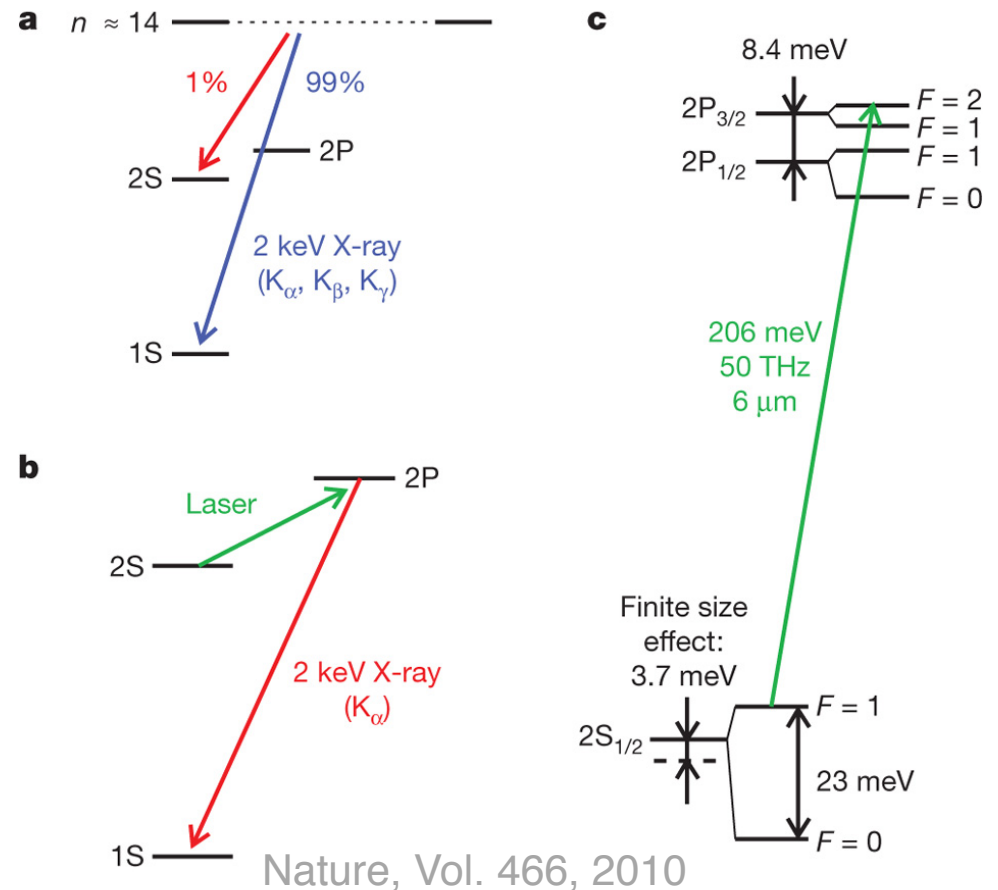
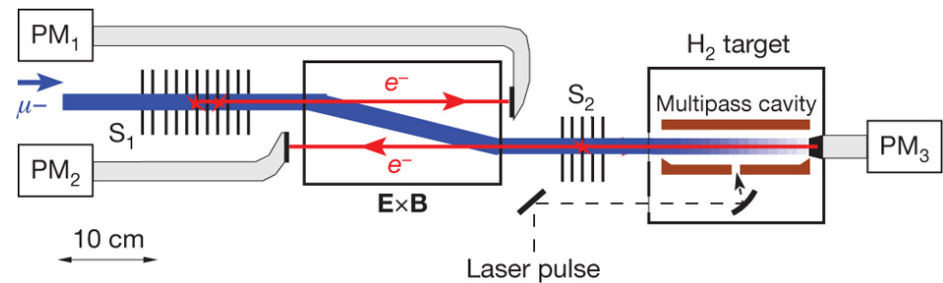
- The largest signal is given by the  $2S_{1/2}^{F=1}$  and  $2P_{3/2}^{F=2}$  transition.
- The QED calculation, considering relativistic, radiative, recoil, proton structure corrections, fine, hyperfine splitting, predict:

$$\Delta E = 209.9779(49) - 5.2262 r_p^2 + 0.0347 r_p^3 \text{ meV}$$

- Finite size of the proton contributes 1.8% of the energy difference.

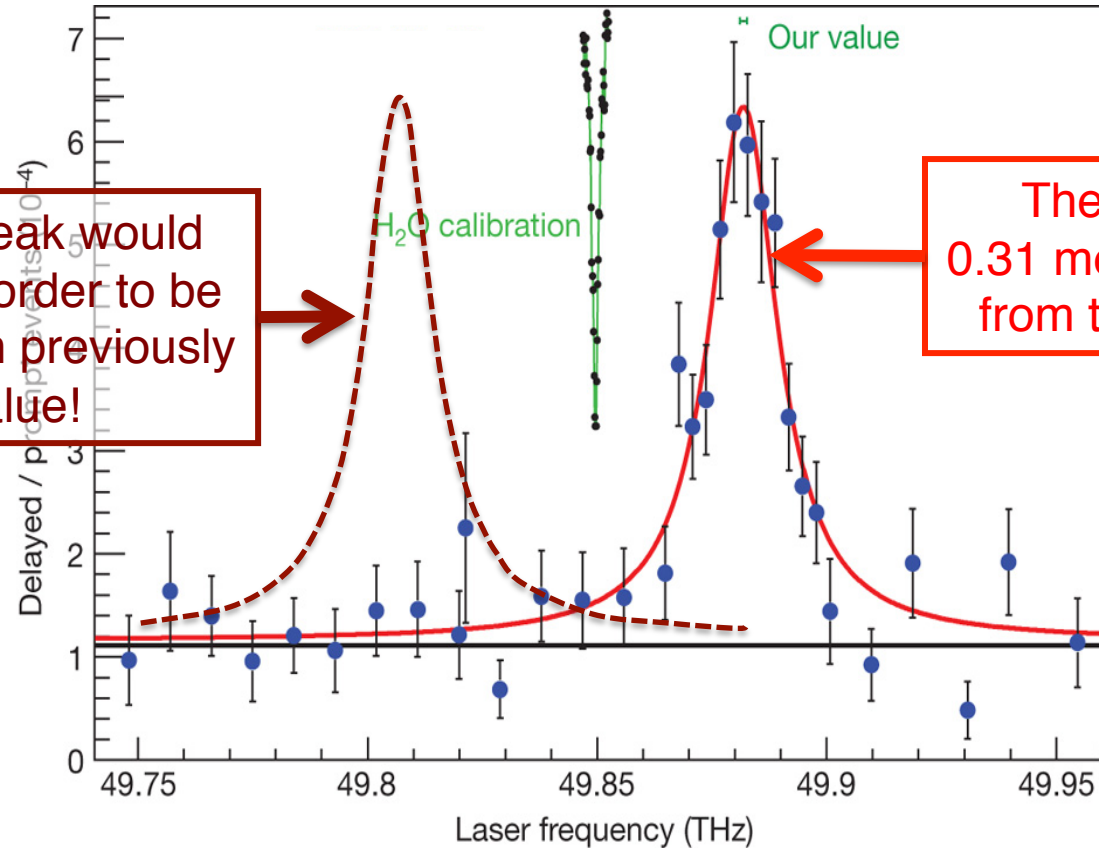
# $\mu$ P-Lamb shift measurement

- First such measurement done at the  $\pi$ E5 beam line of the PSI.
- The  $\mu$ s are stopped in  $H_2$  target where the excited  $\mu$ H is formed.
- Majority de-excites to 1S state.
- Emitted X-ray peak used for normalization of the data to the number of  $\mu$ H.
- 1% populates the 2S state.
- Tunable pulsed laser induces the  $2S \rightarrow 2P$  transitions.
- 2P states de-excite instantly to 1S, emitting 1.9 keV X-rays.
- The whole resonance peak recorded by changing the laser frequency.



# $\mu$ P-Lamb shift measurement #2

Nature, Vol. 466, 2010



Where the peak would have to be in order to be consistent with previously best value!

The measured peak 0.31 meV (0.15% relatively) from the expected value.

The mean position of the peak:

$$f_{2S-2P} = 49881.88(76) \text{ GHz}$$

$$\Delta E = 206.2949(32) \text{ meV}$$



The resulting radius:

$$r_p = 0.84184(36)(56) \text{ fm}$$

# Possible explanations ?!

## - Errors in the measurements:

Spectroscopic and scattering data reexamined.  
No problem found.

## - Coulomb and $2\gamma$ effects incomplete:

Effect is negligible at  $Q^2 \leq 1 (\text{GeV}/c)^2$ .

## - Radiative corrections in the eH Scattering:

Well under control. Simulation precisely describes the tail of the elastic peak tail.

## - Problems with $\mu$ -H theory:

- \* Unexplained proton structure effects.
- \* Clandestine problem with one loop vacuum polarization term.
- \* Fundamental problems with QED.

## - Effects of three body physics:

Contribution of molecular ions?  $p\mu e^-$ ,  $pp\mu^-$  are unstable.

## - Physics beyond standard model?

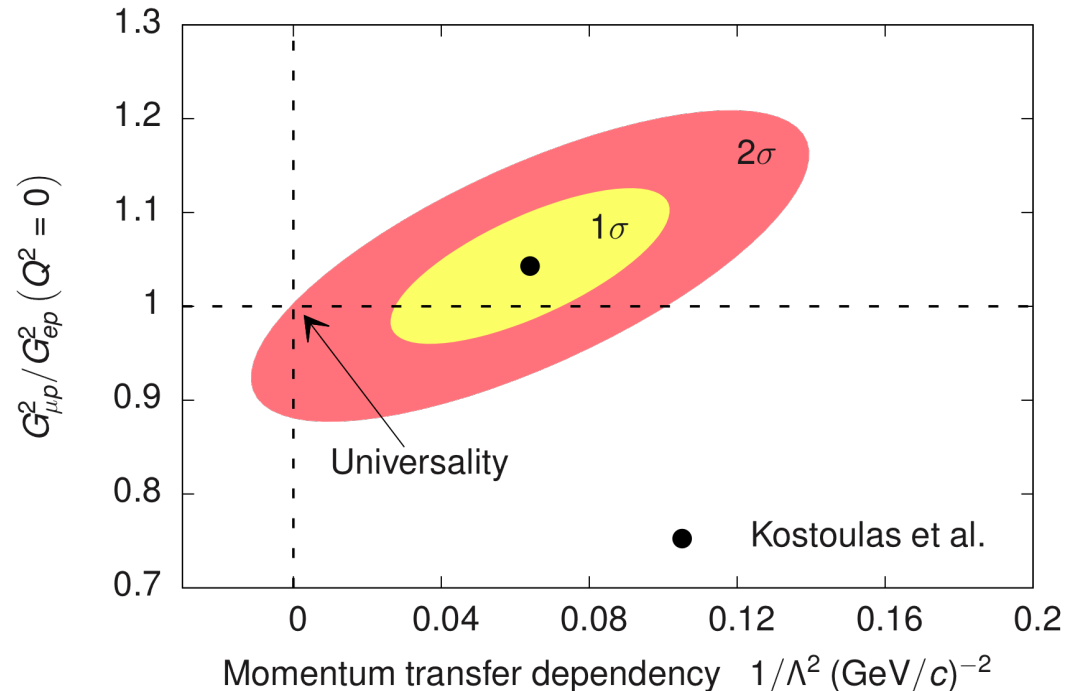


# Physics beyond the Standard model

- Puzzle could be explained by **breaking the e- $\mu$  universality**.

- New interaction could also explain the  $(g-2)_\mu$  puzzle.

- The universality tested, but constrains loose enough for such explanations.



- Various new interactions proposed.

Constraints on new forces limit the possibilities.

- **Most interesting candidate:** A new U(1) gauge boson mediating the interaction between dark matter and the Standard model particles.

- See talk of Harald Merkel (Monday).

**Extensive experimental efforts trying to solve the puzzle.**

### **Upcoming measurements:**

- **Scattering experiments** (ISR, MUSE, Prad)

-  **$\mu$ -d Lamb shift measurement:**

Proton radius extraction via isotope shift.

- **Spectroscopy of electronic Hydrogen:**

Improve eH Lamb shift results. More precise measurement of  $R_\infty$ .

- **Spectroscopy of exotic atoms:**

Measurement of leptonic states  $e^+e^-$  and  $\mu^+\mu^-$  provides strict tests of QED.

-  **$\mu$ - $^3\text{He}$  and  $\mu$ - $^4\text{He}$  Lamb shift measurement:**

Interesting for the comparison with the scattering data.

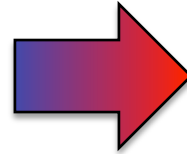




# New elastic Cross-Section measurement

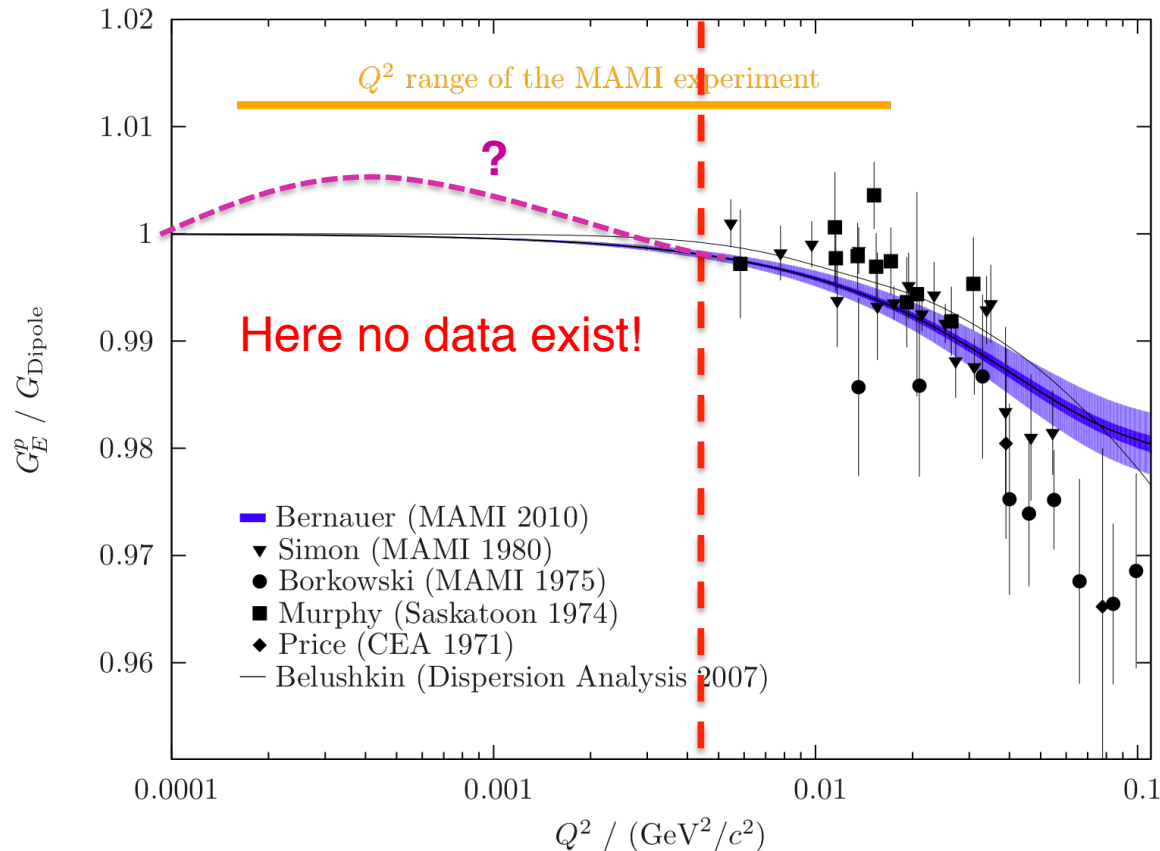
Elastic cross section for H(e,e')p:

$$\frac{d\sigma}{d\Omega} = \left( \frac{d\sigma}{d\Omega} \right)_{Mott} \frac{1}{1 + \tau} \left[ G_E^2(Q^2) + \frac{\tau}{\varepsilon} G_M^2(Q^2) \right]$$



Best estimate for radius:

$$\langle r_E^2 \rangle = -6\hbar^2 \left. \frac{d}{dQ^2} G_E(Q^2) \right|_{Q^2=0}$$



Determination of proton radius depends on the slope of FF ( $Q^2 \rightarrow 0$ ).  
**No data at lowest  $Q^2$ .**

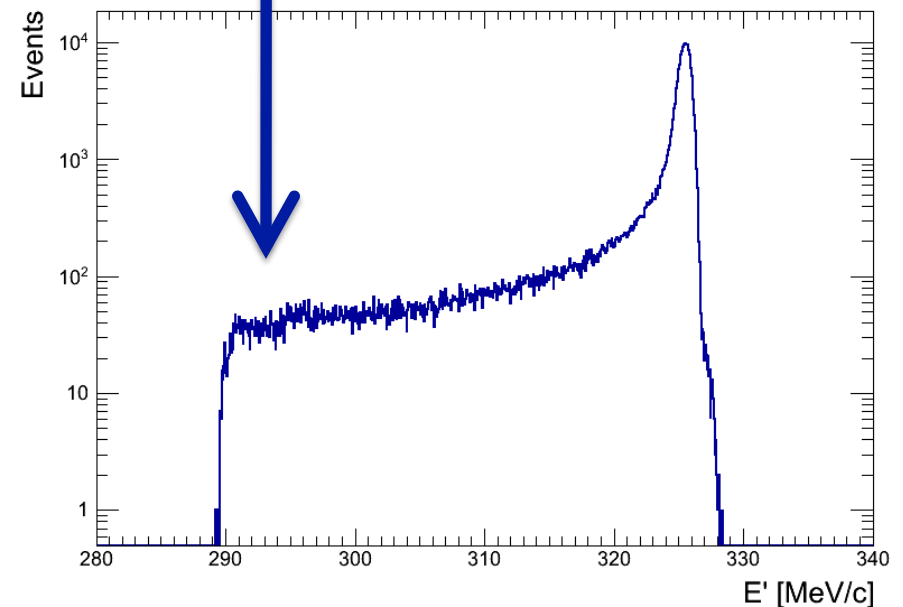
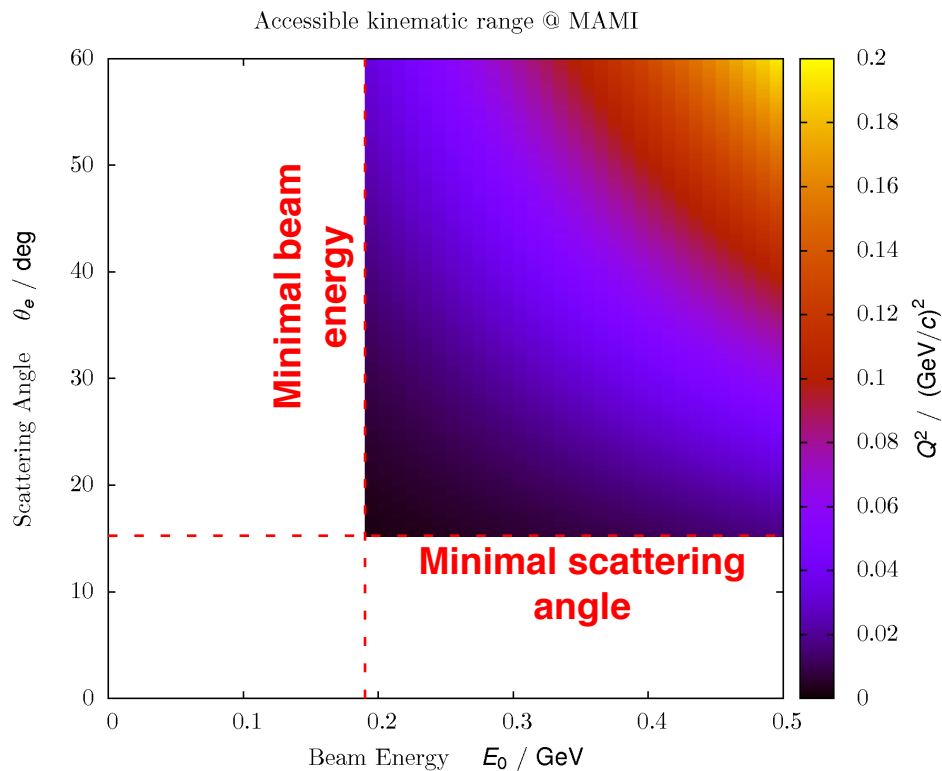
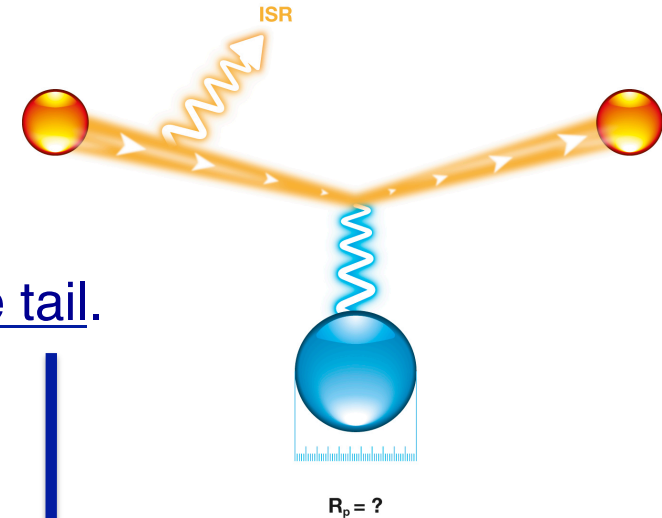


For precise radius determination new measurements at even **lower  $Q^2$  are needed.**

# ISR Experiment at MAMI

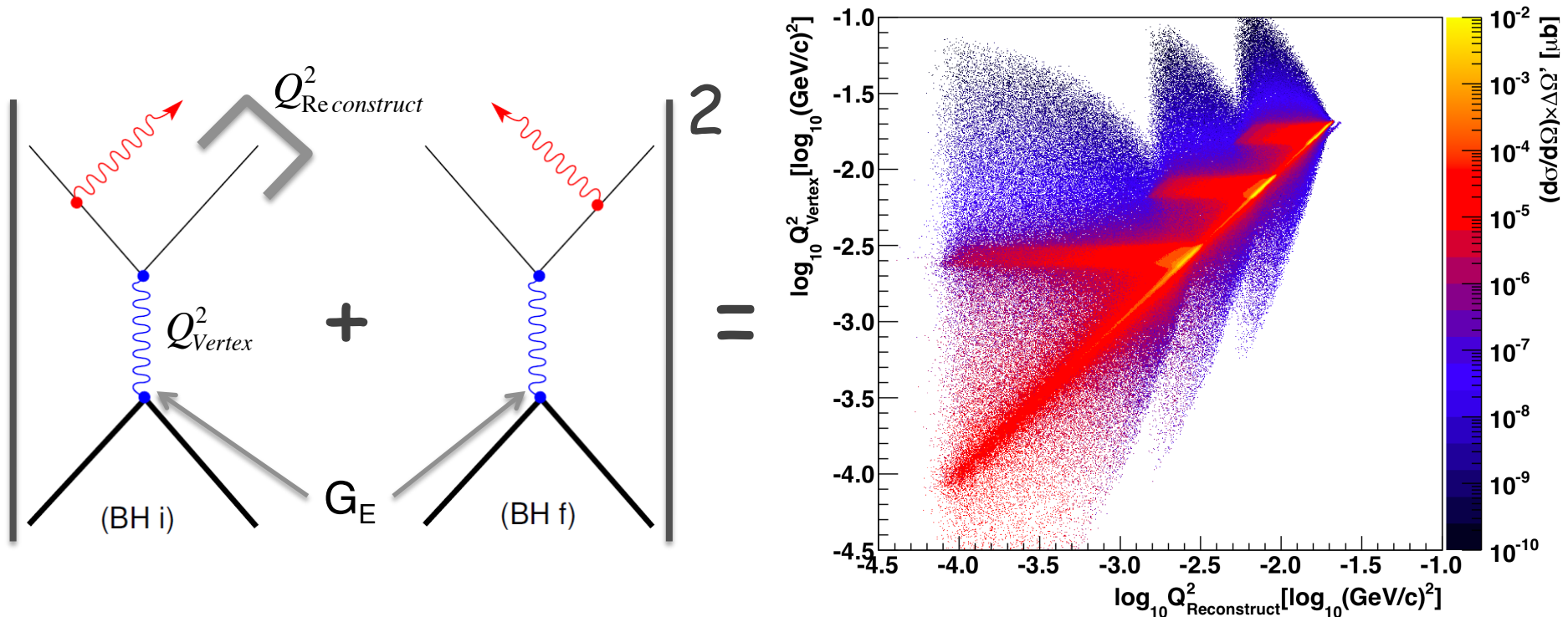
- Lowest  $Q^2$  where the elastic cross-section can be measured is constrained by the limitations of experimental apparatus.

- Way around: Use information from the radiative tail.



# Initial state radiation

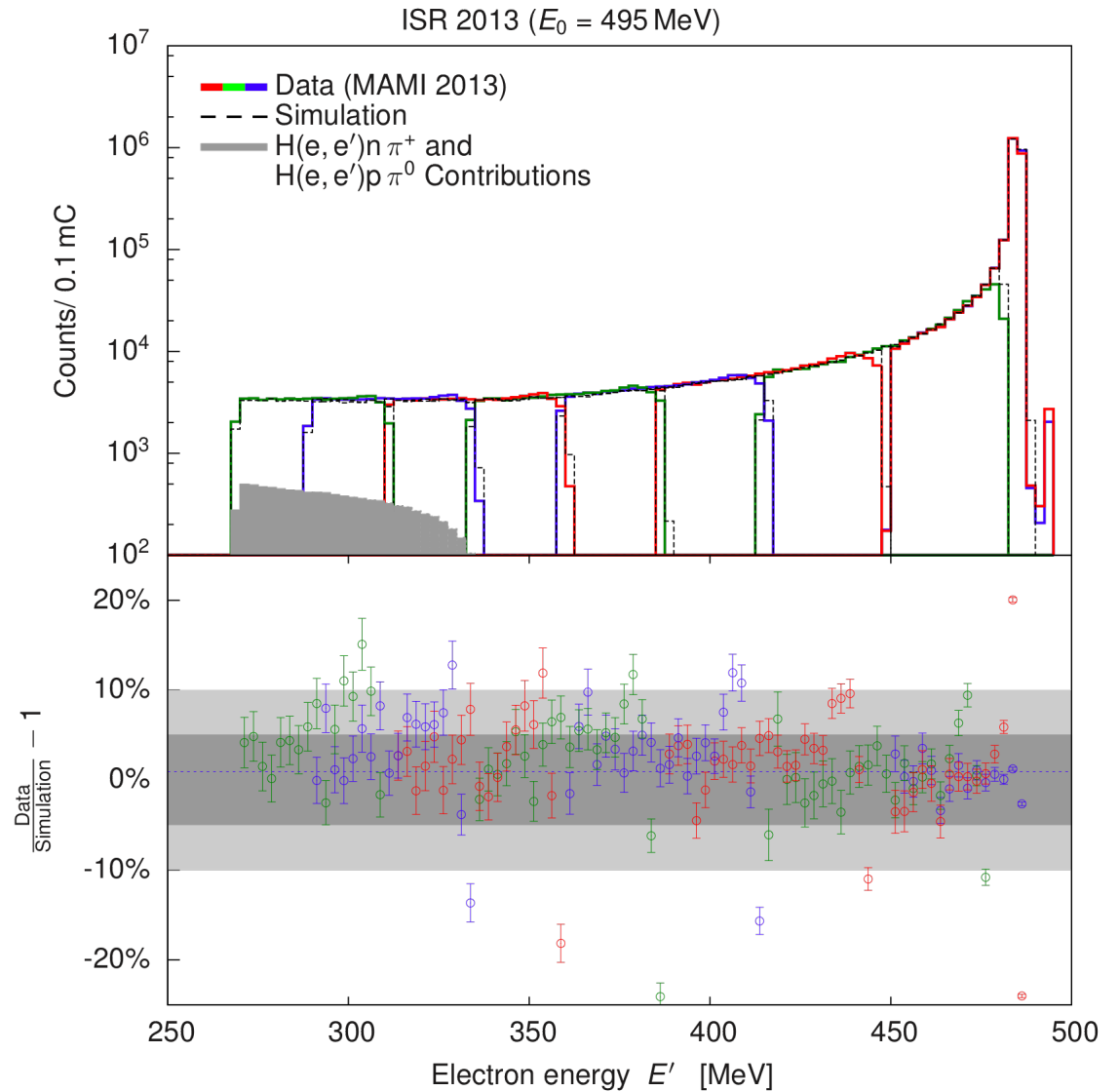
- Radiative tail dominated by coherent sum of two Bethe-Heitler diagrams.



- In data ISR can not be distinguished from FSR.
- **Combining data with the simulation, ISR information can be reached.**
- Idea behind new MAMI experiment to extract  $G_e^p$  at  $Q^2 \sim 10^{-4} (\text{GeV}/c)^2$
- Redundancy measurements at higher  $Q^2$  for testing this approach in a region, where FFs are well known.

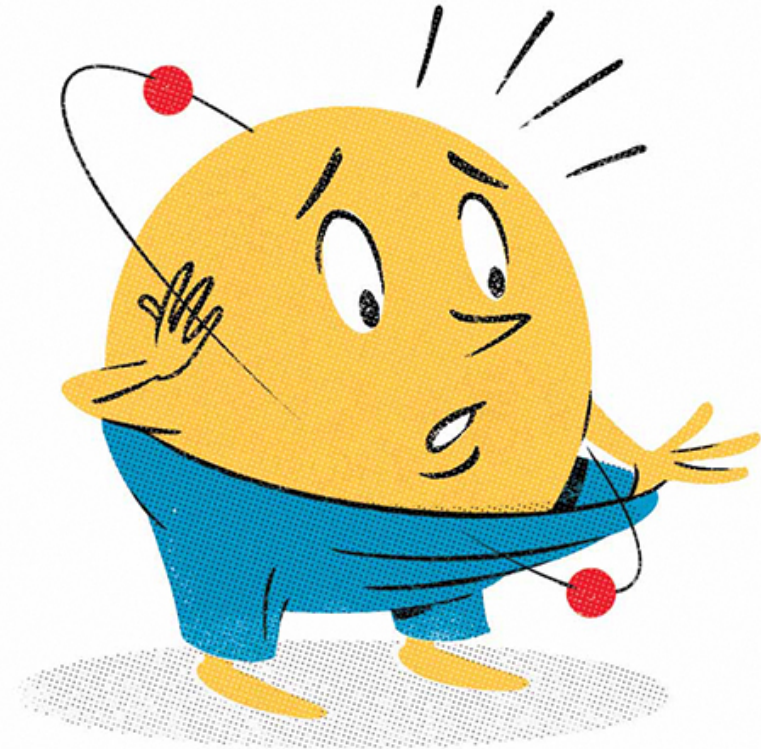
# First Results

- Experiment done in August 2013.
- First findings of online analysis.
- Pion production processes contribute  $\sim 10\%$  at smallest momenta.
- Visible effects of finite resolution. (wall contributions still present)
- **Agreement between data and simulation justifies use of Simul++.**
- Full offline analysis underway.
- The FFs will be determined by a  $\chi^2$ -minimization.



# Conclusions

- **Proton radius puzzle** is a persisting open question of nuclear physics.
- The 4% difference in radii or 0.15% difference in the transition energy **remains unexplained**.
- Indication of a new interaction beyond standard model?
- Fundamental problem with QED?
- Continuous theoretical efforts to find the missing piece of the puzzle.
- New experiments are scheduled, examining different aspects of the problem.



Thank you!

THINK LIKE A

**PROTON**

*and stay positive*