

Eta Meson Production in Proton-Deuteron Collisions

**MESON 2014: 13th International Workshop on Meson
Production, Properties and Interaction**

29th May - 3rd June 2014



Why η -Meson Production Close to Threshold?

- Attractive S-wave ηN interaction

R.S. Bhalerao and L.C. Liu, Phys. Rev. Lett. 54 (1985) 685

- Possible formation of η -nucleus bound states

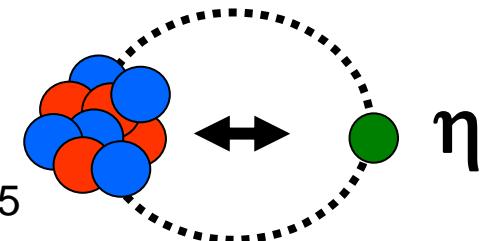
Q. Haider and L.C. Liu, Phys. Lett. B172 (1986) 257

C. Wilkin, Phys. Rev. C47 (1993) 938

- Broad η -mesic nuclei program at COSY

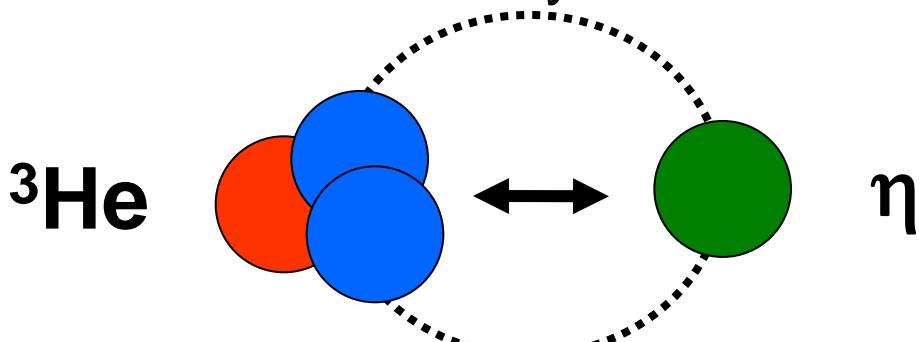
- $A>4$: GEM ($\eta^7\text{Be}$)
- $\eta^4\text{He}$: ANKE, GEM, WASA-at-COSY
- $\eta^3\text{He}$: ANKE, COSY11, GEM, WASA-at-COSY
- ηd : ANKE

- New data from proton-deuteron collisions

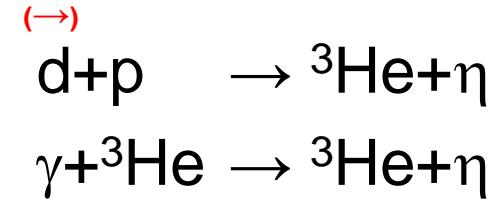


Why η -Meson Production Close to Threshold?

- Do bound meson-nucleus systems exist?

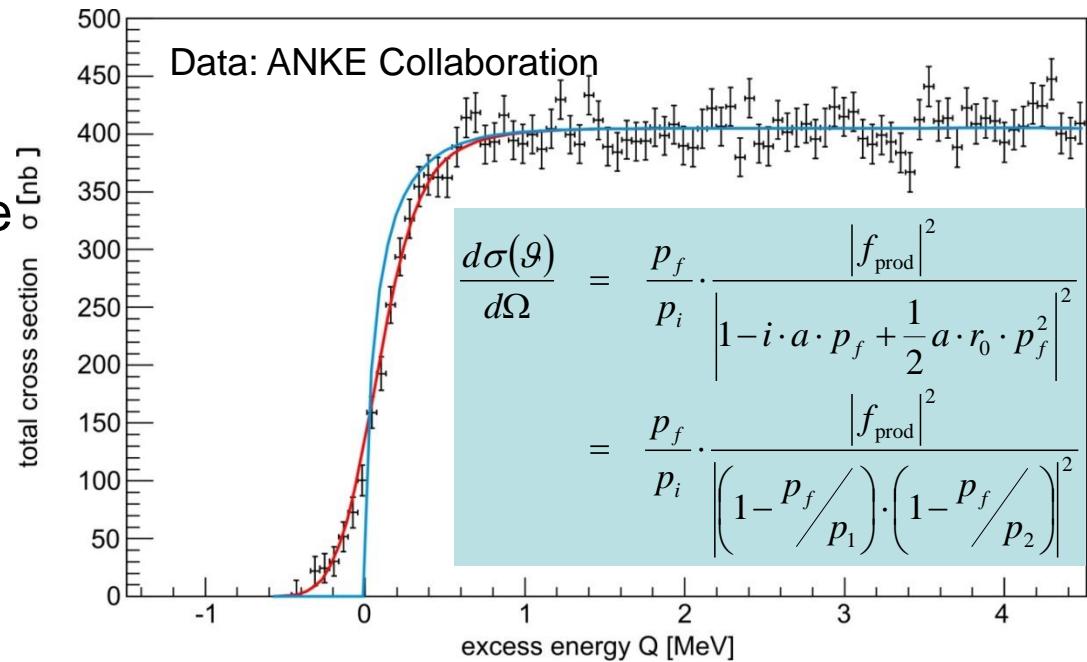


- Experimental access e.g. via
- Excitation function close to threshold \rightarrow FSI
- Polarized beam \rightarrow Test of FSI hypothesis, role of spins



Results for the Reaction $d+p \rightarrow {}^3\text{He}+\eta$

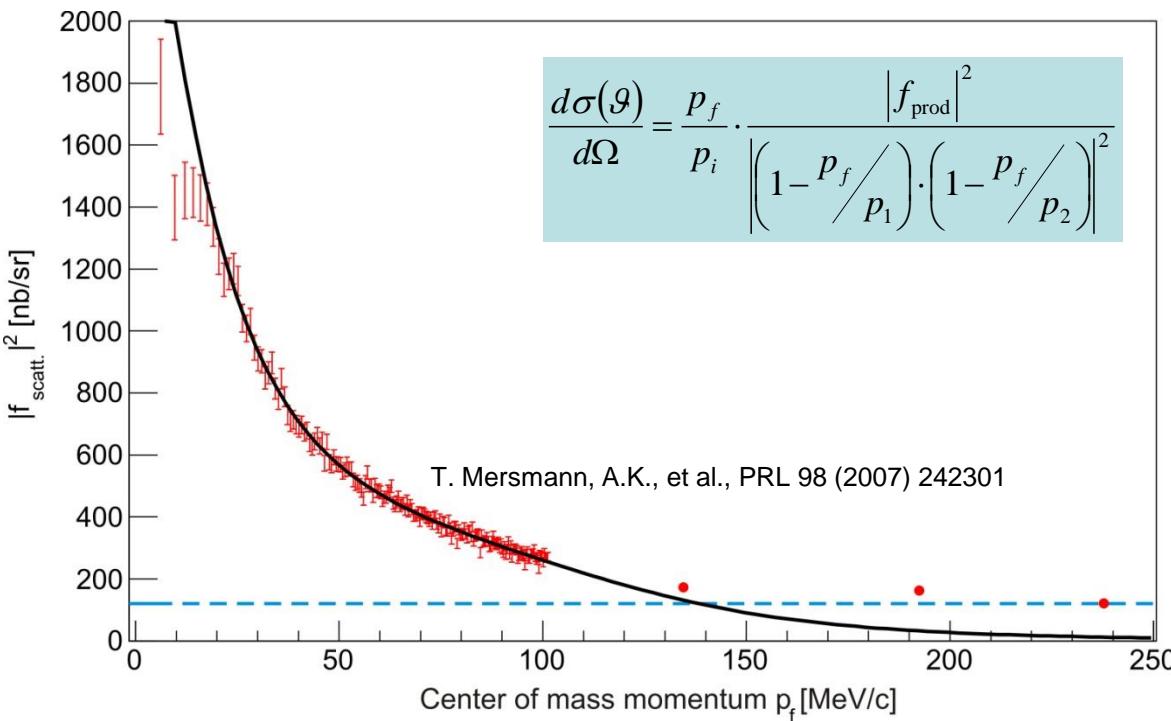
- A good candidate for a bound state is the $\eta^3\text{He}$ -system
 - High precision data from ANKE and COSY-11
 - Observation of **strong FSI**
 - Strong indication for a pole at $|Q_0| \approx 0.37 \text{ MeV}$
 - Further evidence for pole hypothesis by **angular dependence** of $d\sigma/d\Omega$



T. Mersmann et al. , Phys. Rev. Lett. 98 (2007) 242301

The $d+p \rightarrow {}^3\text{He}+\eta$ Scattering Amplitude

Extracted scattering amplitude ($Q > 0$ MeV)

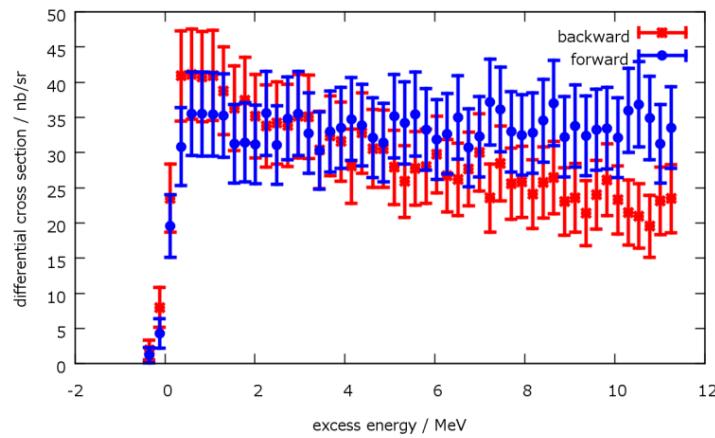
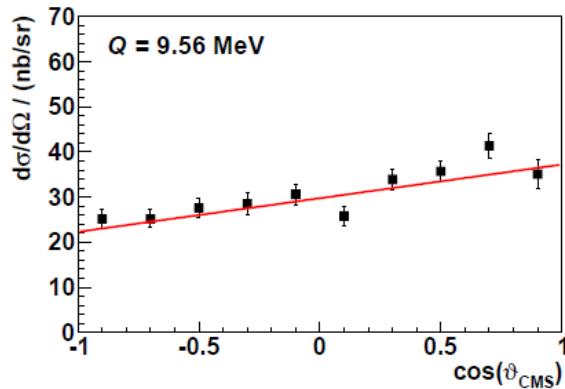


- Scattering amplitude decreases rapidly with increasing final state momentum p_f
- Scattering amplitude almost constant at high energies

→ strong FSI in $\eta {}^3\text{He}$ system

Consideration of Higher Partial Waves: *P*-Waves

- Close to threshold: $d\sigma/d\Omega(\theta) = \text{const.}$ → **s-wave**
- $Q > \sim 4 \text{ MeV}$: Contributions $\sim \cos(\theta)$ visible → **p-wave**



- Asymmetry in the angular distribution (η -meson):
Slope at $\cos(\theta)=0$:

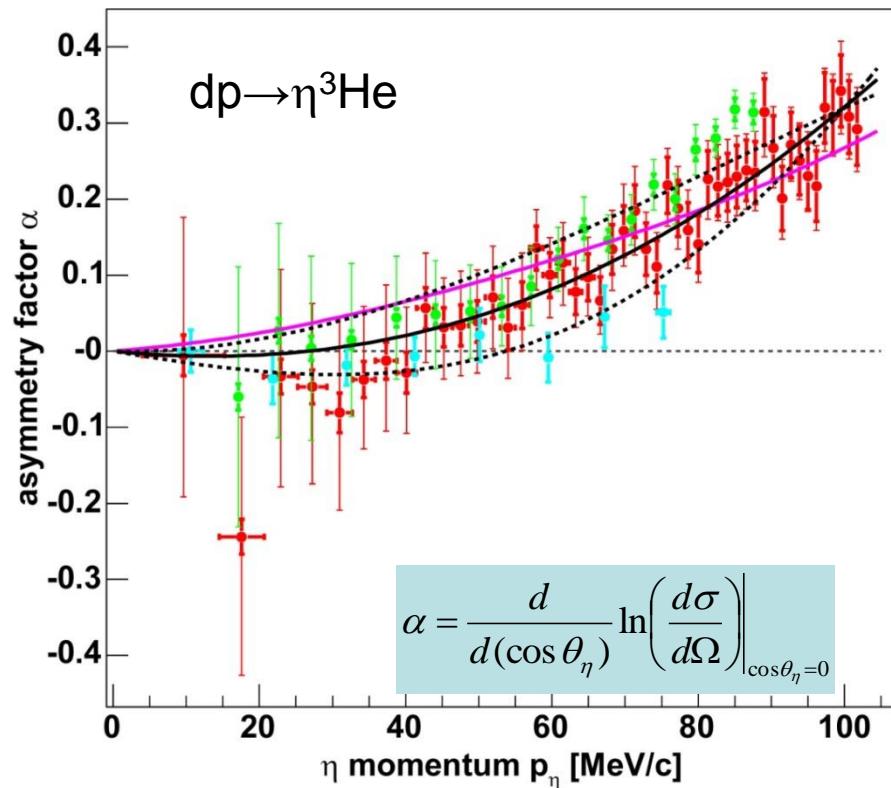
$$\alpha = \frac{d}{d(\cos \theta_\eta)} \ln \left(\frac{d\sigma}{d\Omega} \right) \Big|_{\cos \theta_\eta = 0}$$

$$\left(\frac{d\sigma}{d\Omega} \right)_{CM} = \frac{\sigma_{tot}}{4\pi} \cdot (1 + \alpha \cdot \cos \theta_{CM})$$

Consideration of Higher Partial Waves: *P*-Waves

- Slope might arises from the interference between the *s*- and *p*-waves in the $\eta^3\text{He}$ system
- Indication of a **strong phase variation** of the *s*-wave at low *Q*
- Data (σ_{total} and $d\sigma/d\Omega$) can be described well by assumption of a **pole close to threshold**

$$\left(\frac{d\sigma}{d\Omega}\right)_{CM} = \frac{\sigma_{tot}}{4\pi} \cdot (1 + \alpha \cdot \cos \theta_{CM})$$



T. Mersmann et al., Phys. Rev. Lett. 98 (2007) 242301

C. Wilkin et al., Phys. Rev. B 649 (2007) 92

Consideration of Higher Partial Waves: *P*-Waves

- Assumption: Only *s*- and *p*-waves

Production operator:

C. Wilkin et al., PLB 654 (2007) 92

$$\hat{f} = A \vec{\varepsilon} \cdot \hat{p}_p + iB(\vec{\varepsilon} \times \vec{\sigma}) \cdot \hat{p}_p + C \vec{\varepsilon} \cdot \vec{p}_\eta + iD(\vec{\varepsilon} \times \vec{\sigma}) \cdot \vec{p}_\eta$$

A, B : s-wave amplitudes

C, D : *p*-wave amplitudes

ε : polarisation vector of the deuteron

$$\frac{d\sigma}{d\Omega} = \frac{p_\eta}{p_p} \overline{|f|^2} = \frac{p_\eta}{3p_p} I$$

$$I = |A|^2 + 2|B|^2 + p_\eta^2 |C|^2 + 2p_\eta^2 |D|^2 + 2p_\eta \operatorname{Re}(A * C + 2B * D) \cos \theta_\eta$$

Consideration of Higher Partial Waves: *P*-Waves

- Resulting asymmetry factor:

$$\alpha = 2p_\eta \frac{\operatorname{Re}(A * C + 2B * D)}{|A|^2 + 2|B|^2 + p_\eta^2 |C|^2 + 2p_\eta^2 |D|^2}$$

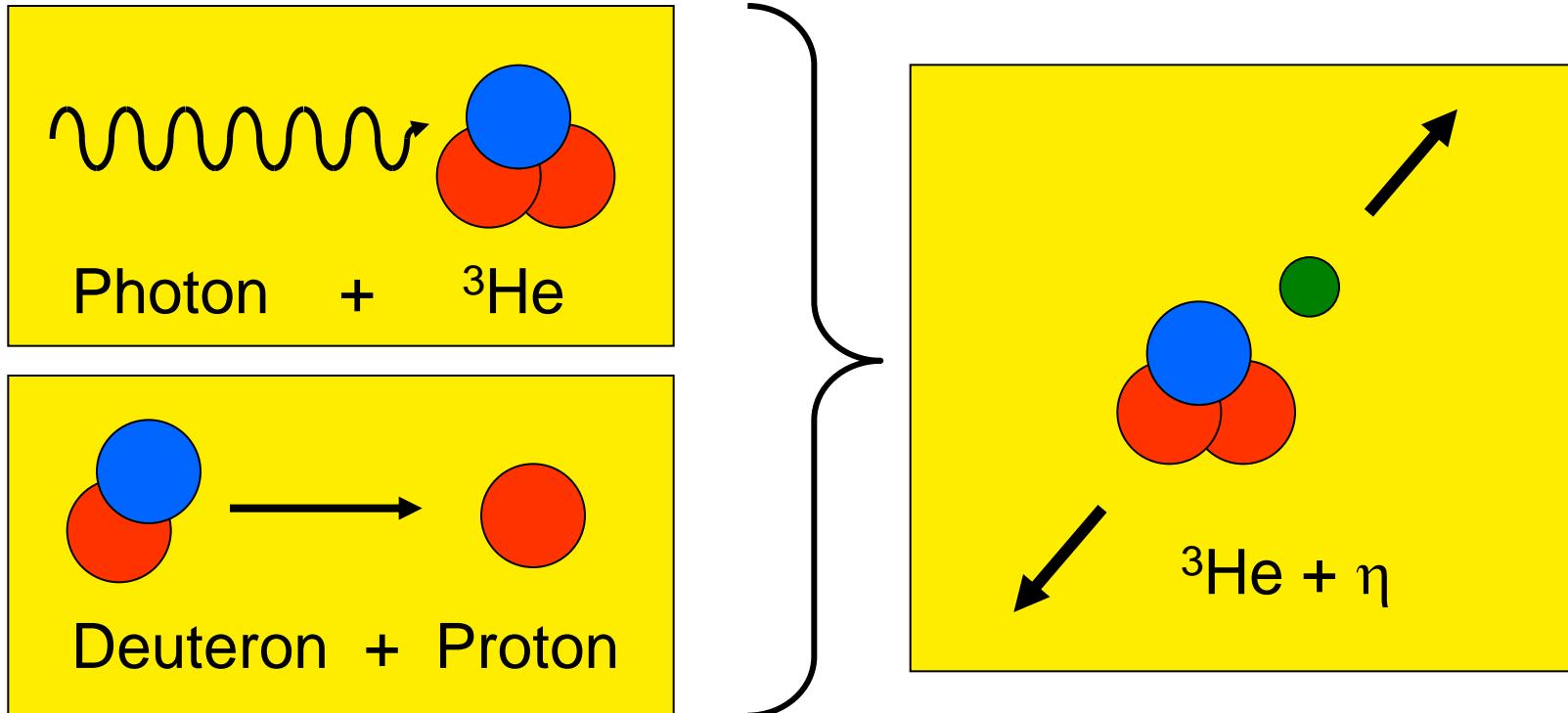
Assumption:

- Same *s*-wave amplitudes: $A = B = f_s$
energy dependence due to FSI
- Same *p*-wave amplitudes: $C = D = \text{const.}$

$$\sigma = 4\pi \frac{p_\eta}{p_p} \left[|f_s|^2 + p_\eta^2 |C|^2 \right]$$

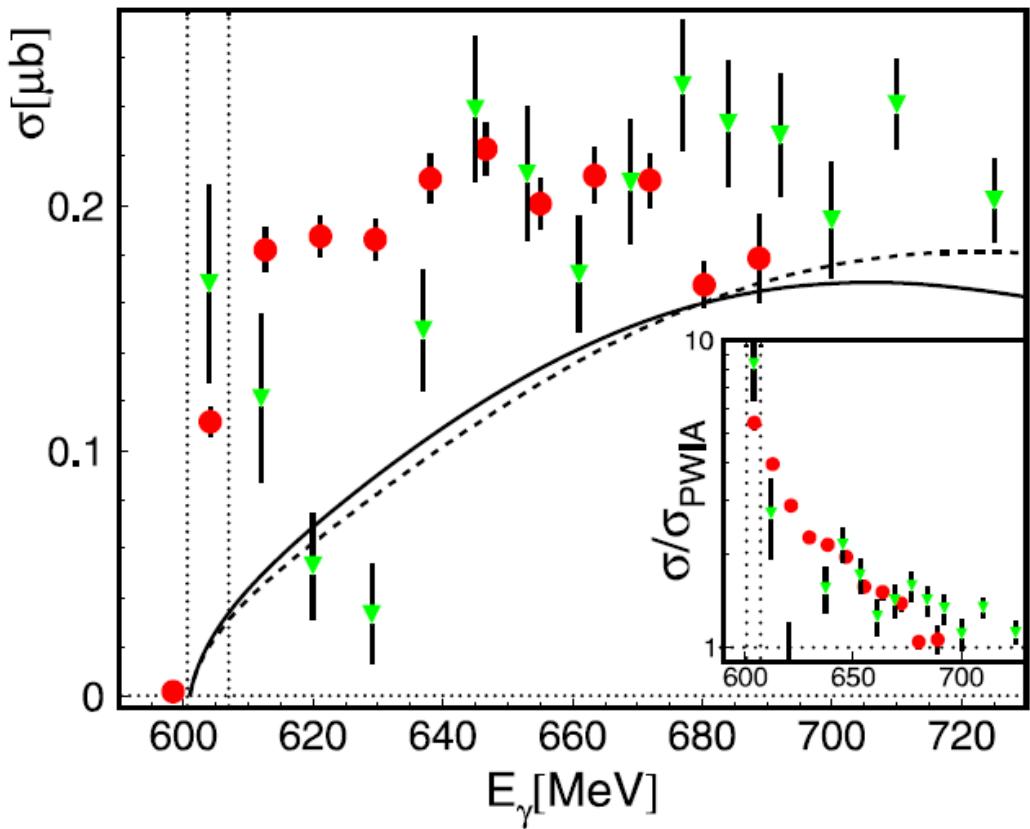
$$\alpha = 2p_\eta \frac{\operatorname{Re}(f_s^* C)}{|f_s|^2 + p_\eta^2 |C|^2}$$

Compare: dp- and $\gamma^3\text{He}$ -Scattering



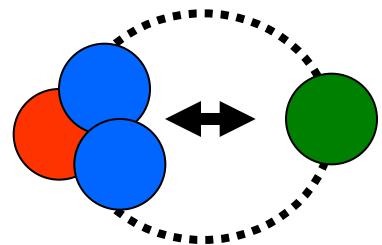
- Different initial states and production mechanism, but same final state

Compare: dp- and $\gamma^3\text{He}$ -Scattering

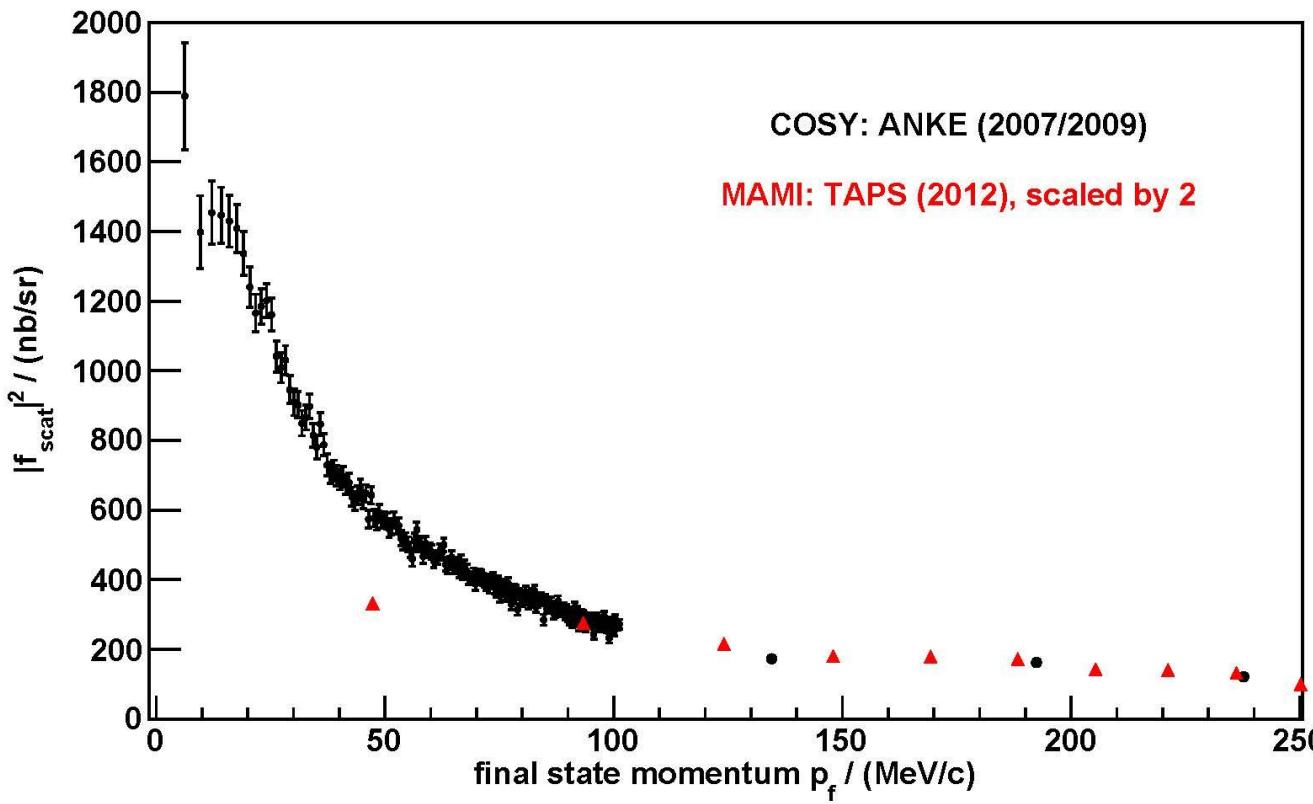


F. Pheron et al., PLB 709 (2012) 21-27

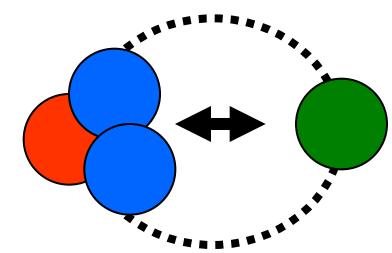
- Scattering amplitudes show similar energy dependence
- Strong hint for a strong FSI between He-nuclei and η -mesons



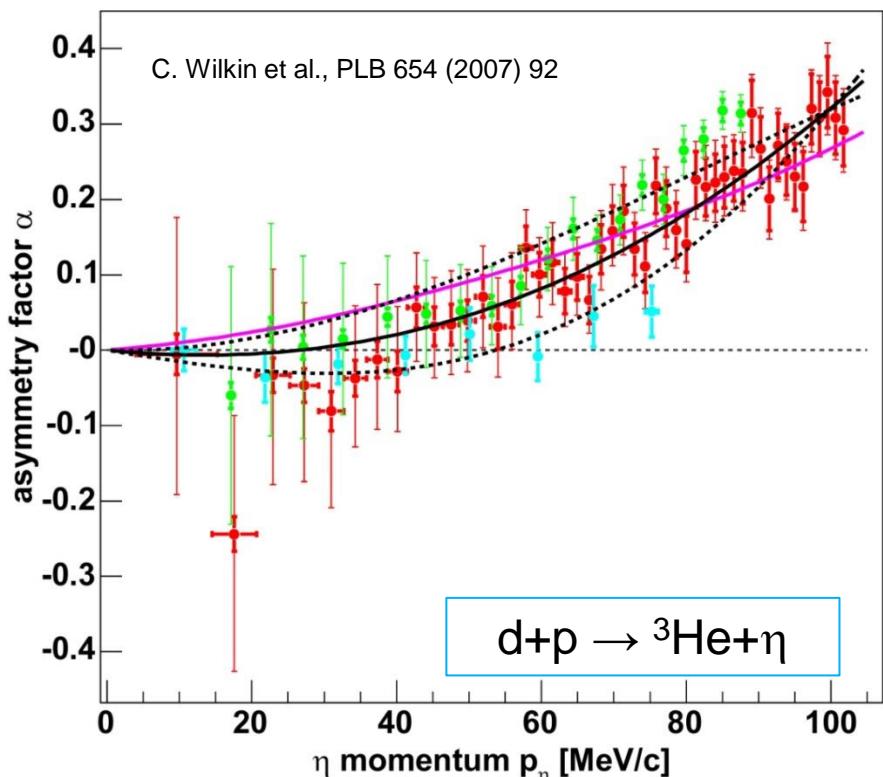
Compare: dp- and $\gamma^3\text{He}$ -Scattering



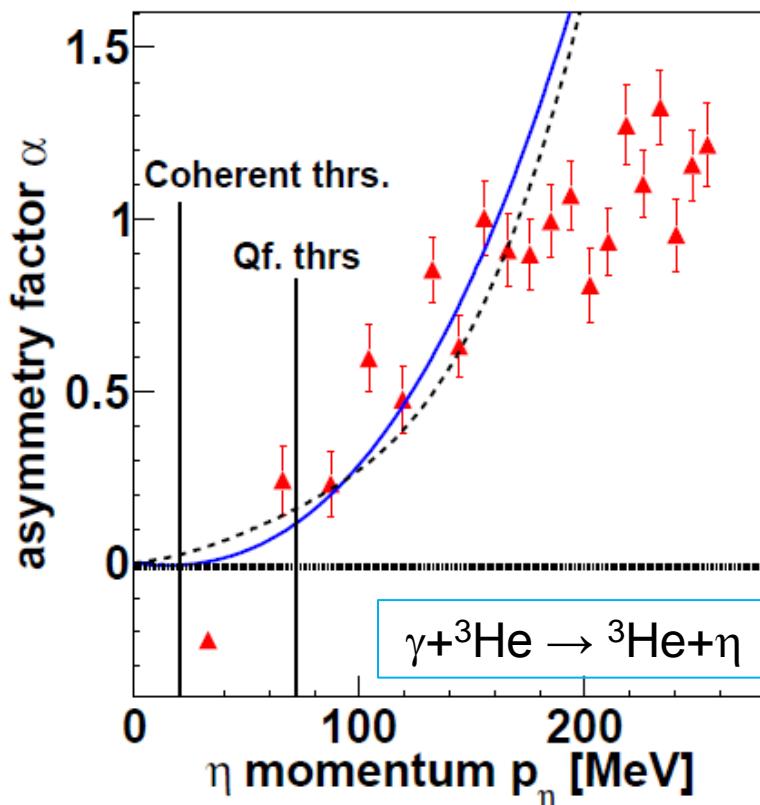
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Compare: dp- and $\gamma^3\text{He}$ -Scattering



$$\alpha = \frac{d}{d(\cos \theta_\eta)} \ln \left(\frac{d\sigma}{d\Omega} \right) \Big|_{\cos \theta_\eta=0} \quad \left(\frac{d\sigma}{d\Omega} \right)_{CM} = \frac{\sigma_{tot}}{4\pi} \cdot (1 + \alpha \cdot \cos \theta_{CM})$$



F. Pheron, PhD thesis, University Basel, 2012

Need of Further Data

- Excitation function(s) and differential cross sections for the $\eta - {}^3\text{He}$ final state are compatible with the presence of a pole close to threshold
- Further input is needed to investigate e.g. the role of the spin of the entrance channel
- Very close to threshold the $d + p \rightarrow {}^3\text{He} + \eta$ reaction is dominated by an **s-wave ${}^3\text{He} + \eta$ system**
- ANKE:
 - Studies with tensor polarised deuterons
 - $\vec{d}p \rightarrow {}^3\text{He} + \eta$
 - Possible spins: $S_{dp} = 1/2$ or $3/2$

Polarized Measurements

Production amplitude for $d\bar{p} \rightarrow {}^3\text{He} + \eta (\pi^0)$:

$$f_B = \bar{u}_\tau \vec{p}_p \cdot (A \vec{\varepsilon}_d + iB \vec{\varepsilon}_d \times \vec{\sigma}) u_p$$

Determination of the energy dependence of the **amplitudes A and B** by measurement of:

$$\frac{d\sigma}{d\Omega} = \frac{1}{3} \frac{p_\eta}{p_p} \left[|A|^2 + 2|B|^2 \right]$$

$$T_{20} = \sqrt{2} \left[\frac{|B|^2 - |A|^2}{|A|^2 + 2|B|^2} \right]$$

$$|A|^2 = \frac{p_p}{p_\eta} (1 - \sqrt{2} T_{20}) \frac{d\sigma}{d\Omega}$$

$$|B|^2 = \frac{p_p}{p_\eta} (1 + \frac{1}{\sqrt{2}} T_{20}) \frac{d\sigma}{d\Omega}$$

$$T_{20} = \frac{2 \cdot \sqrt{2}}{p_{zz}} \cdot \frac{d\sigma_0/d\Omega(\vartheta) - d\sigma_\uparrow/d\Omega(\vartheta)}{d\sigma_0/d\Omega(\vartheta)} \quad \vartheta = 0^\circ \text{ or } 180^\circ$$

see:
 C. Kerboul et al.,
 Phys. Lett. B 181, 28 (1986)

Polarized Measurements

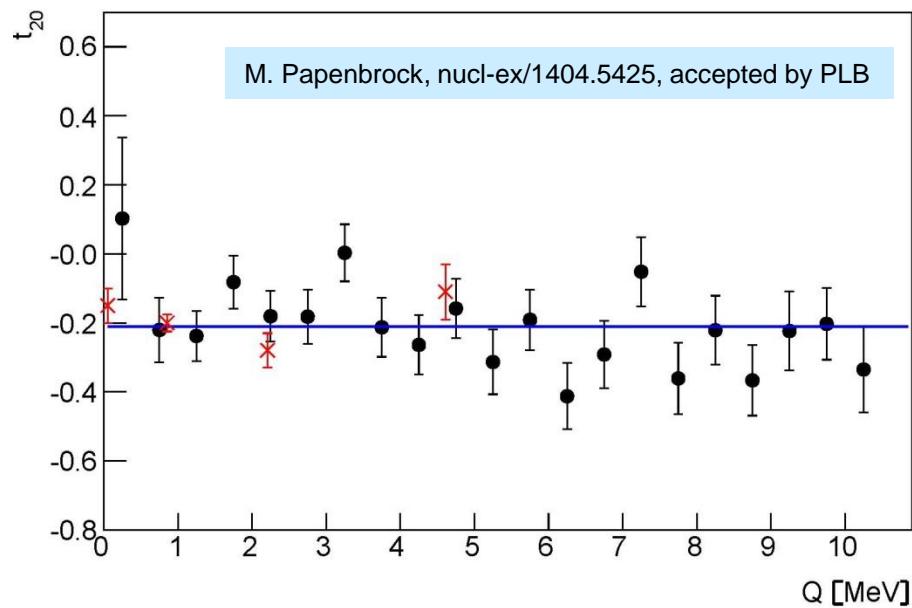
Assumption for $\vec{d}p \rightarrow {}^3\text{He} + \eta$:

- Negligible effect of ISI
- Energy dependence of $|f|^2$ only given by FSI
 - Shape of excitation function independent of spins
 - Same energy dependence of amplitudes $|A|^2$ and $|B|^2$

$$\begin{aligned}|A|^2 &= |A_0|^2 \cdot FSI(p_\eta) \\|B|^2 &= |B_0|^2 \cdot FSI(p_\eta)\end{aligned}\Rightarrow T_{20} = \sqrt{2} \left[\frac{|B_0|^2 - |A_0|^2}{|A_0|^2 + 2|B_0|^2} \right] \cdot \frac{FSI(p_\eta)}{FSI(p_\eta)} = \text{const.}$$

- Measure T_{20} as function of the excess energy

Recent results from ANKE: $d+p \rightarrow {}^3\text{He}+\eta$

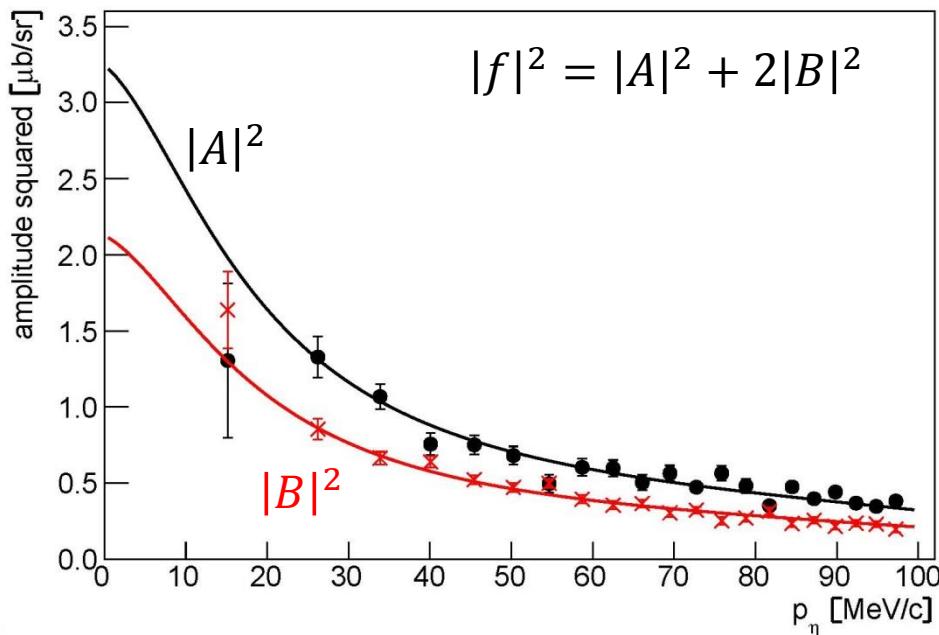


- Data close to threshold consistent with $T_{20}=\text{const.}$
$$T_{20} = -0.21 \pm 0.02 \pm 0.05$$
- $|T_{20}| \ll 1 \rightarrow |A|^2/|B|^2 = O(1)$
- S-Wave amplitudes $|A|^2$ and $|B|^2$ are of similar size



Recent Results: $d+p \rightarrow {}^3\text{He}+\eta$

- Energy dependence of $|f|^2$ known from „old“ unpolarized measurements
 $\rightarrow |A|^2(p_f)$ and $|B|^2(p_f)$ can be calculated



$$\frac{d\sigma}{d\Omega} = \frac{1}{3} \frac{p_\eta}{p_p} \left[|A|^2 + 2|B|^2 \right]$$

$$|A|^2 = \frac{p_p}{p_\eta} (1 - \sqrt{2} T_{20}) \frac{d\sigma}{d\Omega}$$

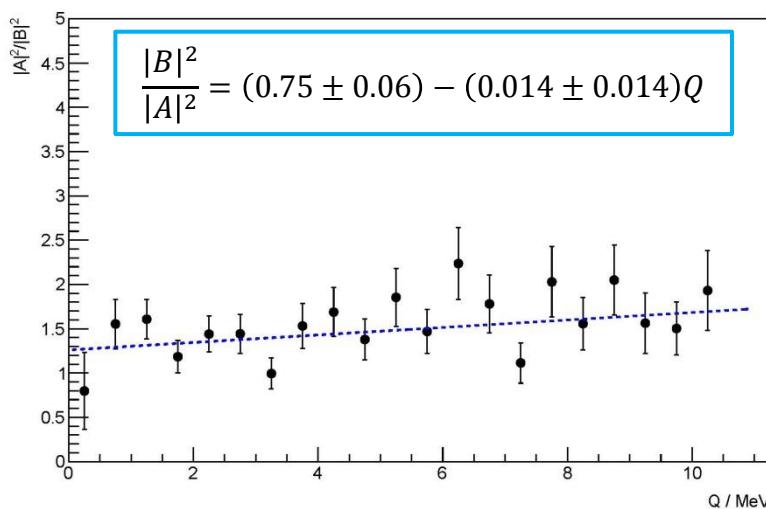
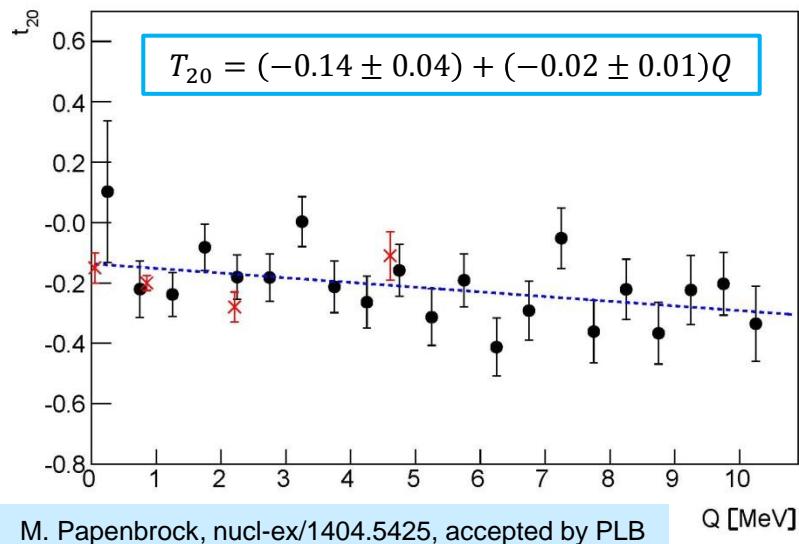
$$|B|^2 = \frac{p_p}{p_\eta} \left(1 + \frac{1}{\sqrt{2}} T_{20} \right) \frac{d\sigma}{d\Omega}$$

M. Papenbrock, nucl-ex/1404.5425, accepted by PLB



Recent Results: $d+p \rightarrow {}^3\text{He}+\eta$

- Allow for a linear energy dependence of T_{20} and $|A|^2/|B|^2$:

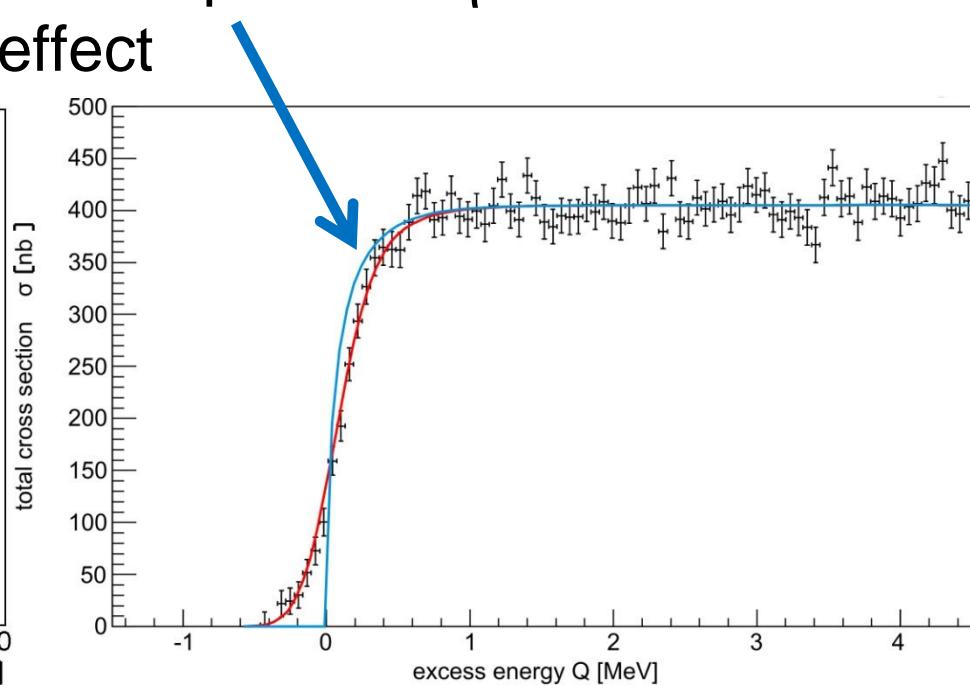
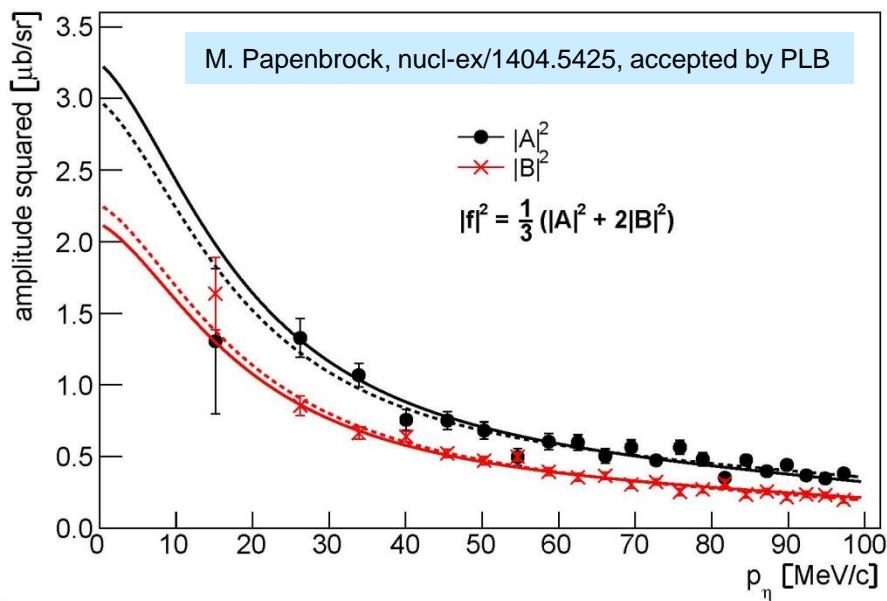


→ Possible energy variation of $|A|^2(p_f)$ and $|B|^2(p_f)$ on the scale of $0.75/0.014$ MeV ≈ 50 MeV



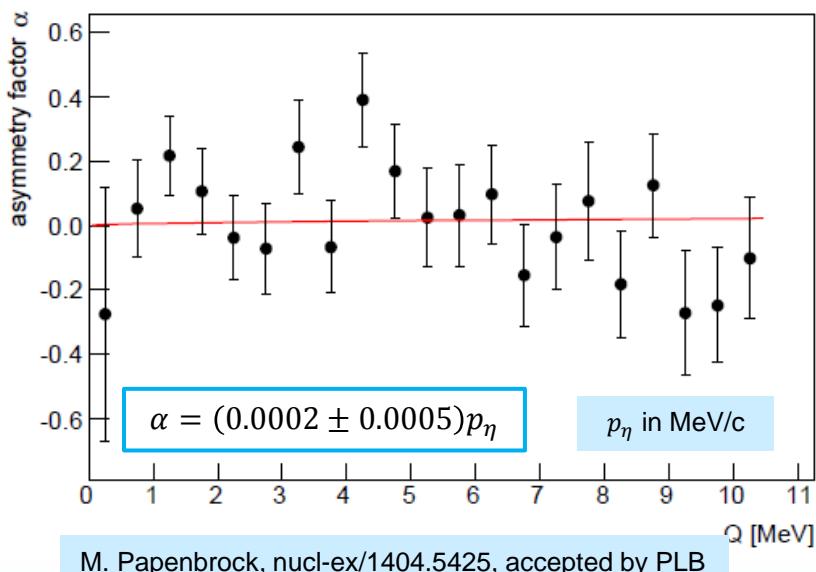
Recent Results: $d+p \rightarrow {}^3\text{He}+\eta$

- No significant different energy dependence of $|A|^2$ and $|B|^2$
- Remarkable excitation function of $d+p \rightarrow {}^3\text{He}+\eta$ still an indication for very strong FSI effect



Angular Dependence of T_{20}

- Asymmetry parameter: $\alpha = \frac{dT_{20}}{d \cos \vartheta} \Big|_{\cos \vartheta = 0}$
 - sensitive to interferences between even and odd η partial waves
 - odd function of p_η with $\alpha(Q=0)=0$



- No sign for any $s-p$ interference here

But:

- Unpolarized data show already at $Q = 4$ MeV a non-isotropy $d\sigma/d\Omega$

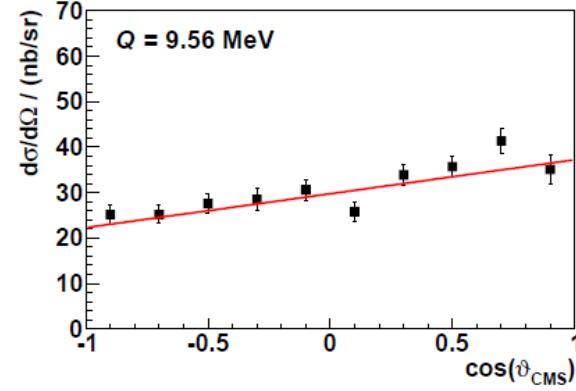
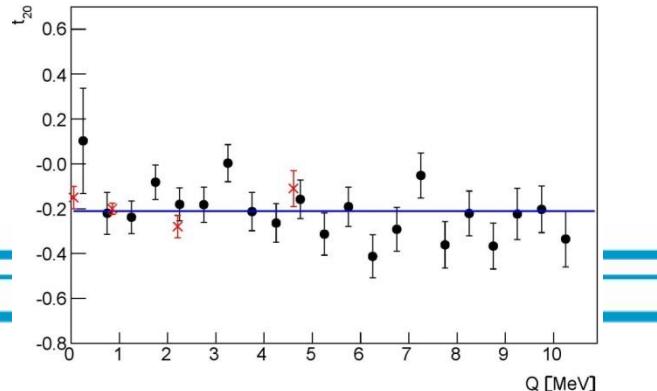
Ansatz for Structure of Amplitudes A and B

$$A = A_0 \left[FSI(p_\eta) + \alpha p_\eta \cos \vartheta + \beta p_\eta^2 (3 \cos^2 \vartheta - 1)/2 \right]$$

$$B = B_0 \left[FSI(p_\eta) + \alpha p_\eta \cos \vartheta + \beta p_\eta^2 (3 \cos^2 \vartheta - 1)/2 \right]$$

M. Papenbrock, nucl-ex/1404.5425, accepted by PLB

- FSI term influences only the s-wave term
- A proportional to $B \rightarrow T_{20}$ independent of p_η and ϑ
- Ansatz allows for observed non-isotropy of $d\sigma/d\Omega$ at higher excess energies

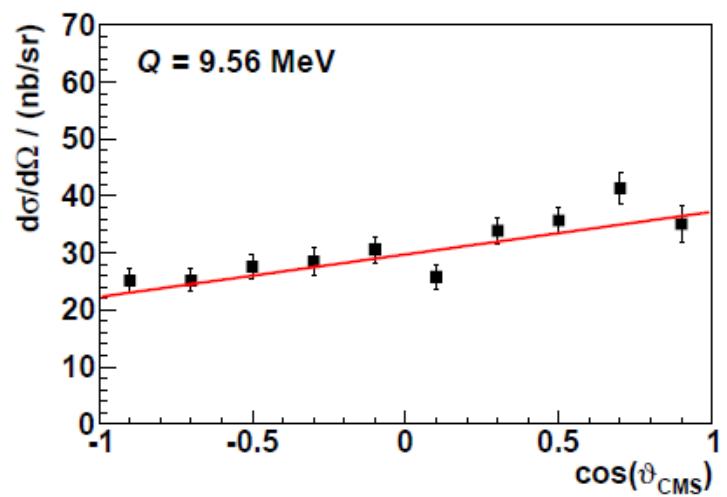


Ansatz for Structure of Amplitudes A and B

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$$B = B_0 \left[FSI(p_\eta) + \alpha p_\eta \cos \vartheta + \beta p_\eta^2 (3 \cos^2 \vartheta - 1)/2 \right]$$

- Unpolarized data show linearity in $d\sigma/d\Omega$ for $Q > 4$ MeV
- Can be explained by cancellation of **interference between s and d waves** and the **square of p waves**

→ Important new information on $|f|^2$



T. Mersmann et al., PRL 98 (2007) 242301

The Reaction $d+p \rightarrow {}^3\text{He}+\eta$ at Higher Q-Values

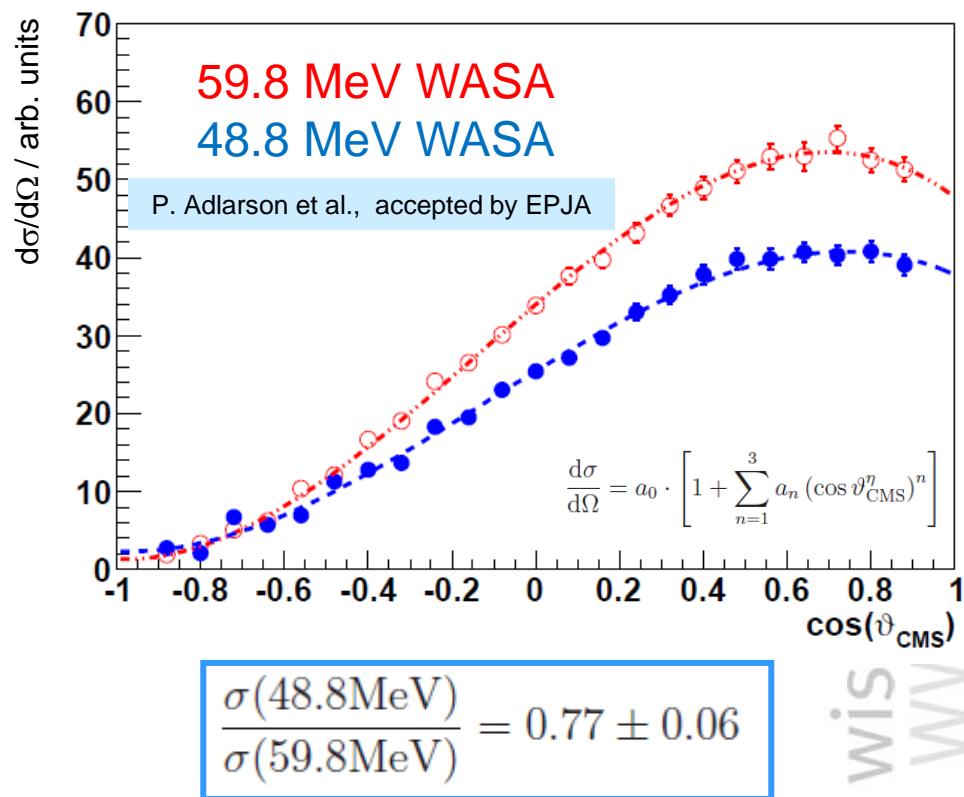
- Good understanding of the production mechanism is important for an even better investigation of the FSI effects at threshold and/or of possible bound states
- Threshold data are not sufficient for solid investigations
 - FSI effects dominate very close to threshold
→ data at higher excess energies (>10 MeV) important
- New differential cross section data from WASA-at-COSY recently published (**$Q = 48.8$ MeV & 59.8 MeV**)

Recent Results from WASA-at-COSY

- Angular distributions show strong anisotropy
- Precise determination of total cross section ratio

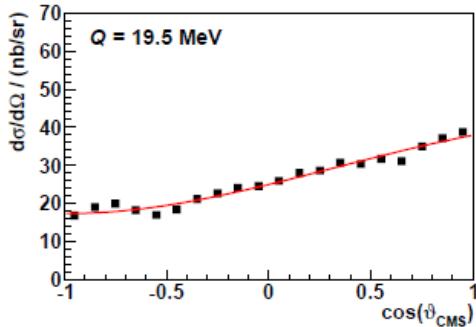
But

- Theoretical models (e.g. two-step process) completely fail to explain total & differential cross sections

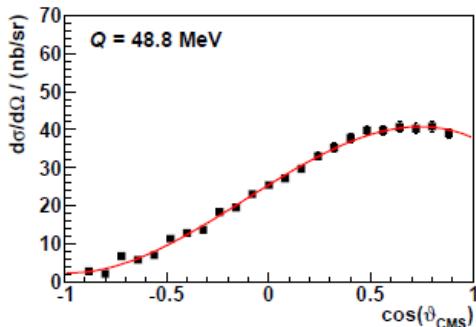


Development of Angular Distributions

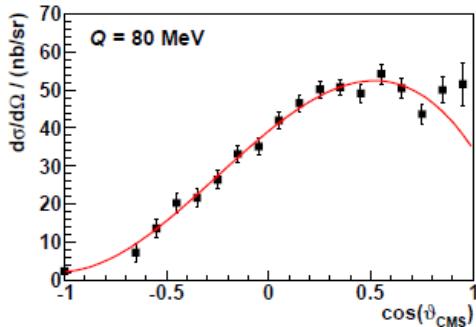
ANKE



WASA-at-
COSY



WASA-
Promice



WASA-
Promice

WASA-at-
COSY

WASA-
Promice

Predictions from a Two-Step Model

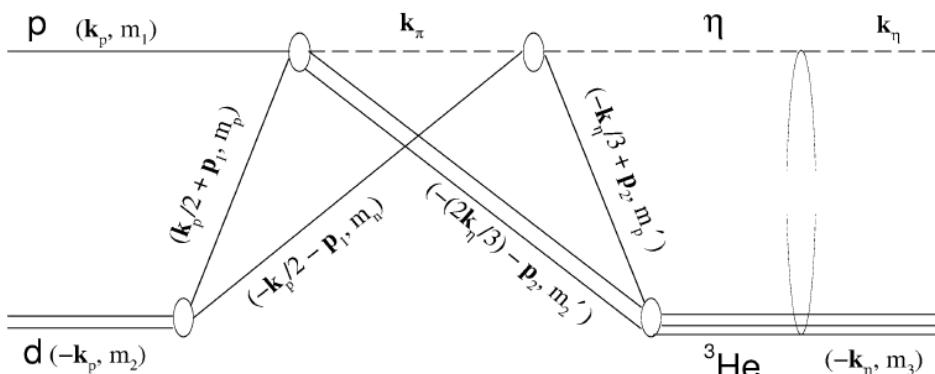
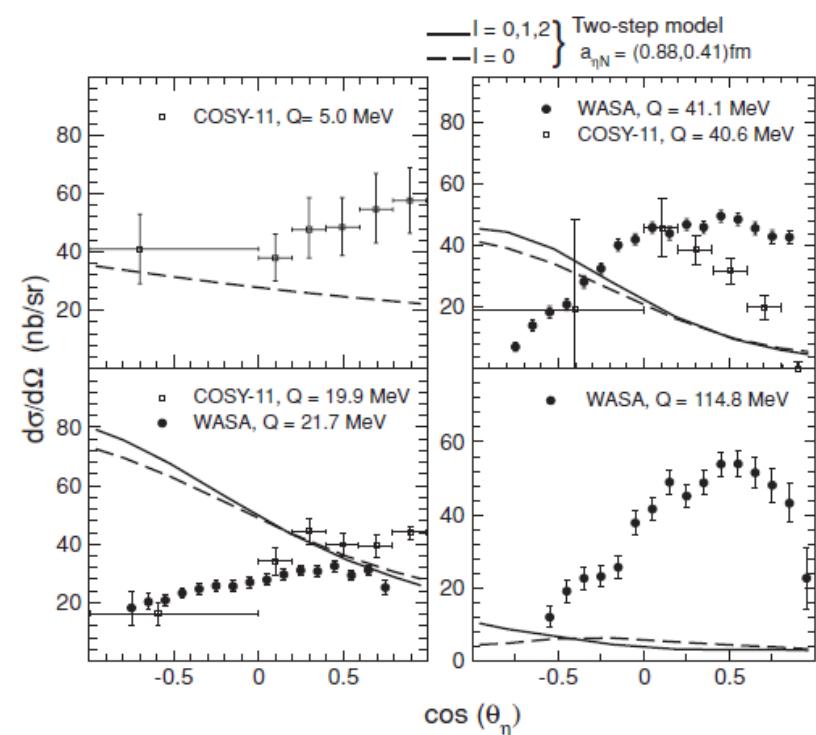
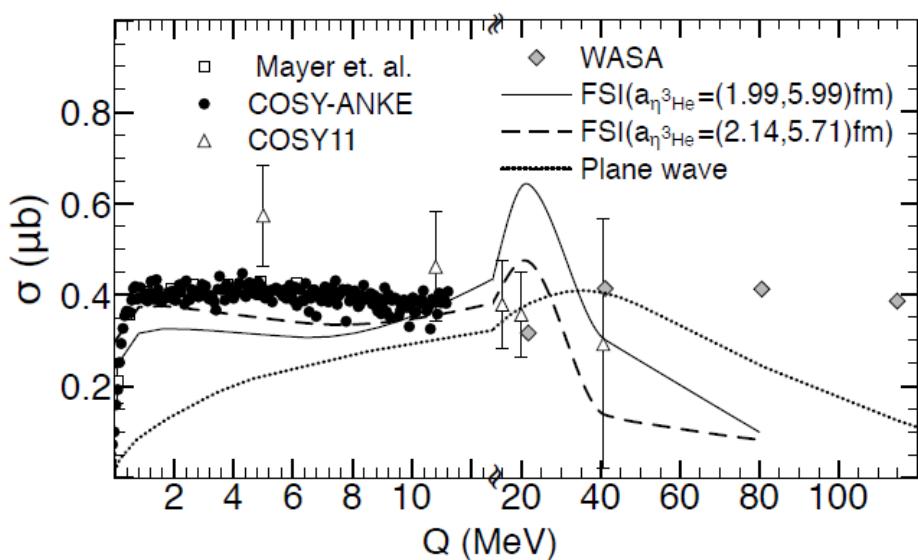


Fig. 1. Diagram of η production in the $pd \rightarrow ^3\text{He} \eta$ reaction with a two step process. The ellipse indicates the final state interaction of ^3He and η .

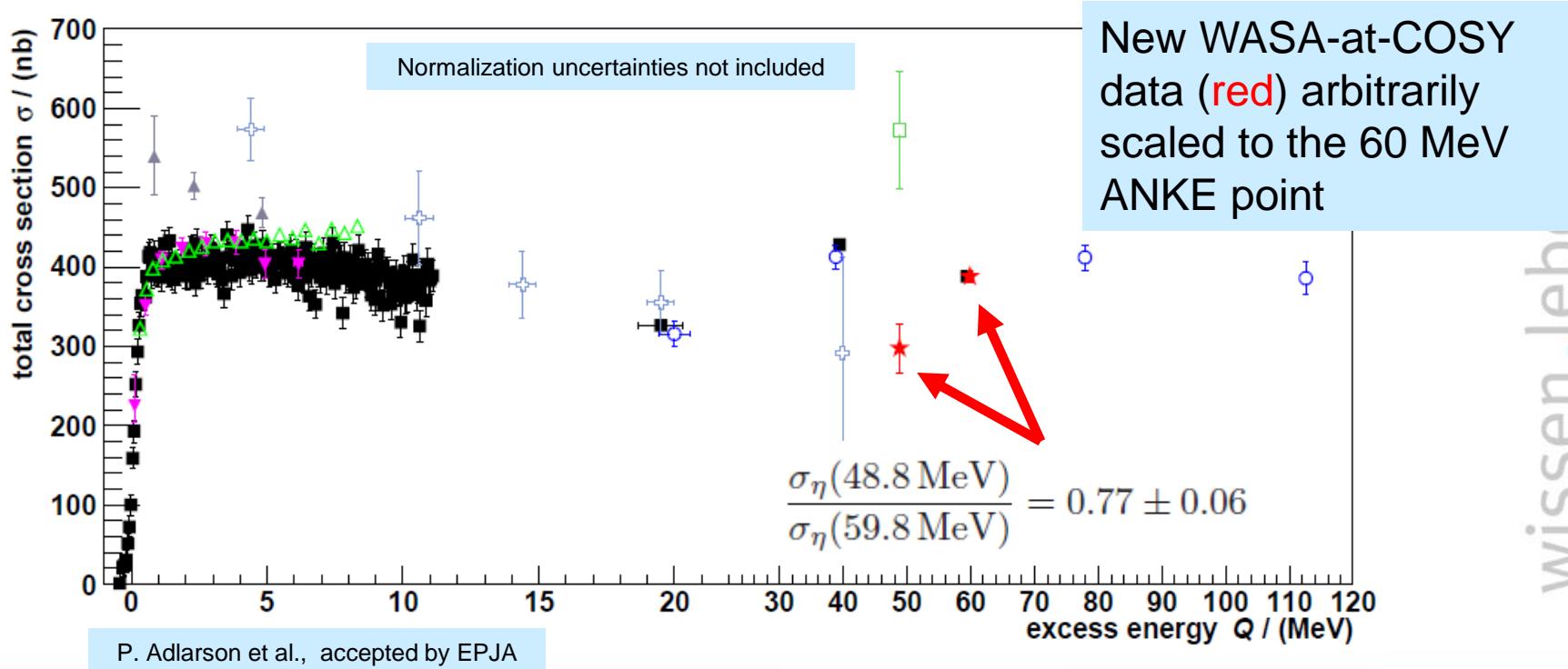


KP Khemchandani , Phys. Rev. C 76 (2007) 069801

K.P. Khemchandani, N.G. Kelkar, B.K Jain,
NPA 708 (2002) 312-324

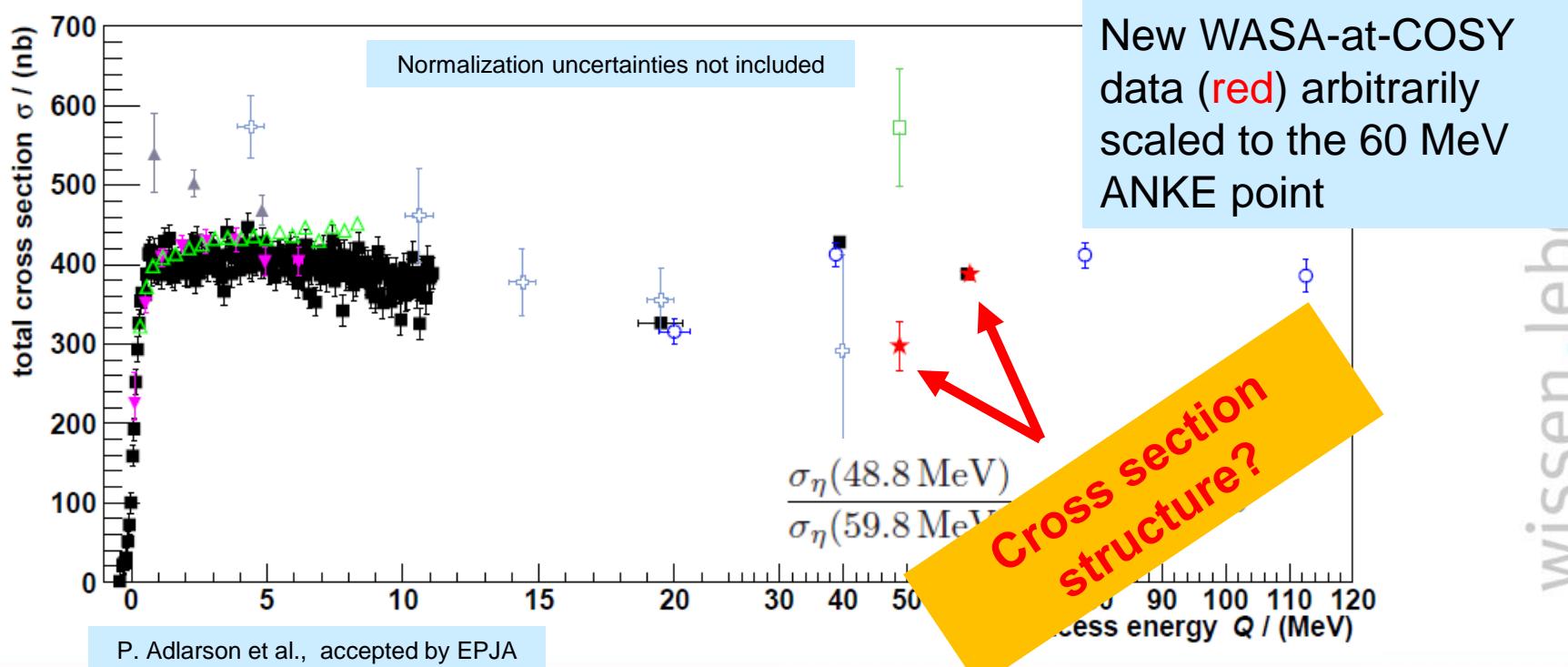
The Reaction $d+p \rightarrow {}^3\text{He}+\eta$ at Higher Q-Values

- Recent data might indicate a cross section variation at higher excess energies, i.e. at 20 MeV...60 MeV



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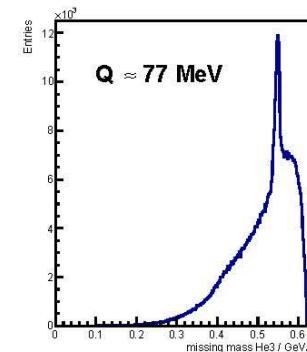
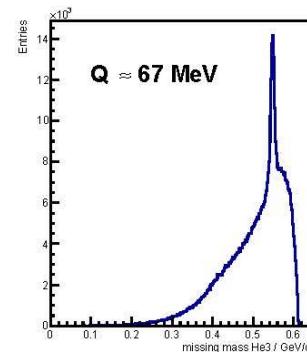
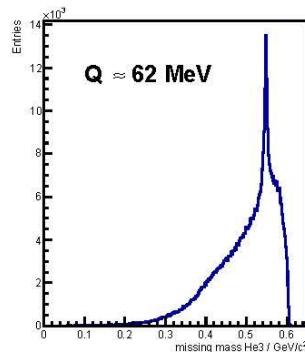
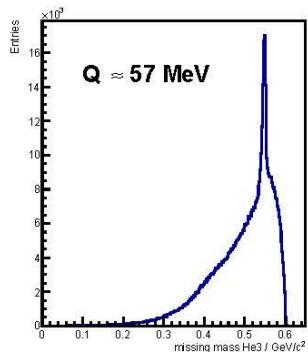
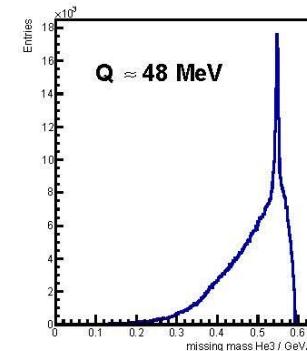
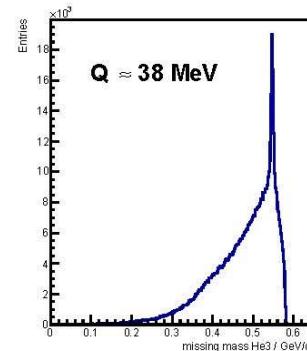
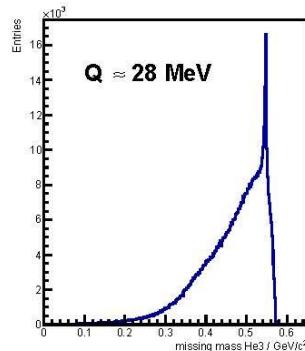
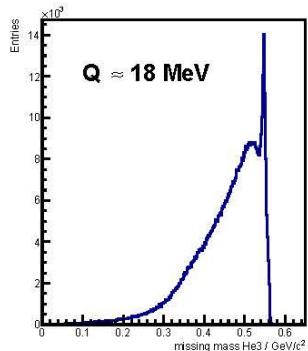


The Reaction $d+p \rightarrow {}^3\text{He}+\eta$ at Higher Q-Values

- Current data base for $Q > 20$ MeV not sufficient for solid investigations → new data needed
- Very recently new high statistics data have been recorded at WASA-at-COSY at 15 Q-values, i.e. in the interval $Q = 14$ MeV – 88 MeV
- Precise total and differential cross sections can be expected for the future (>100 kevents per energy!)
- Solid data base for further investigations on
 - Production processes
 - Possible cross section structures

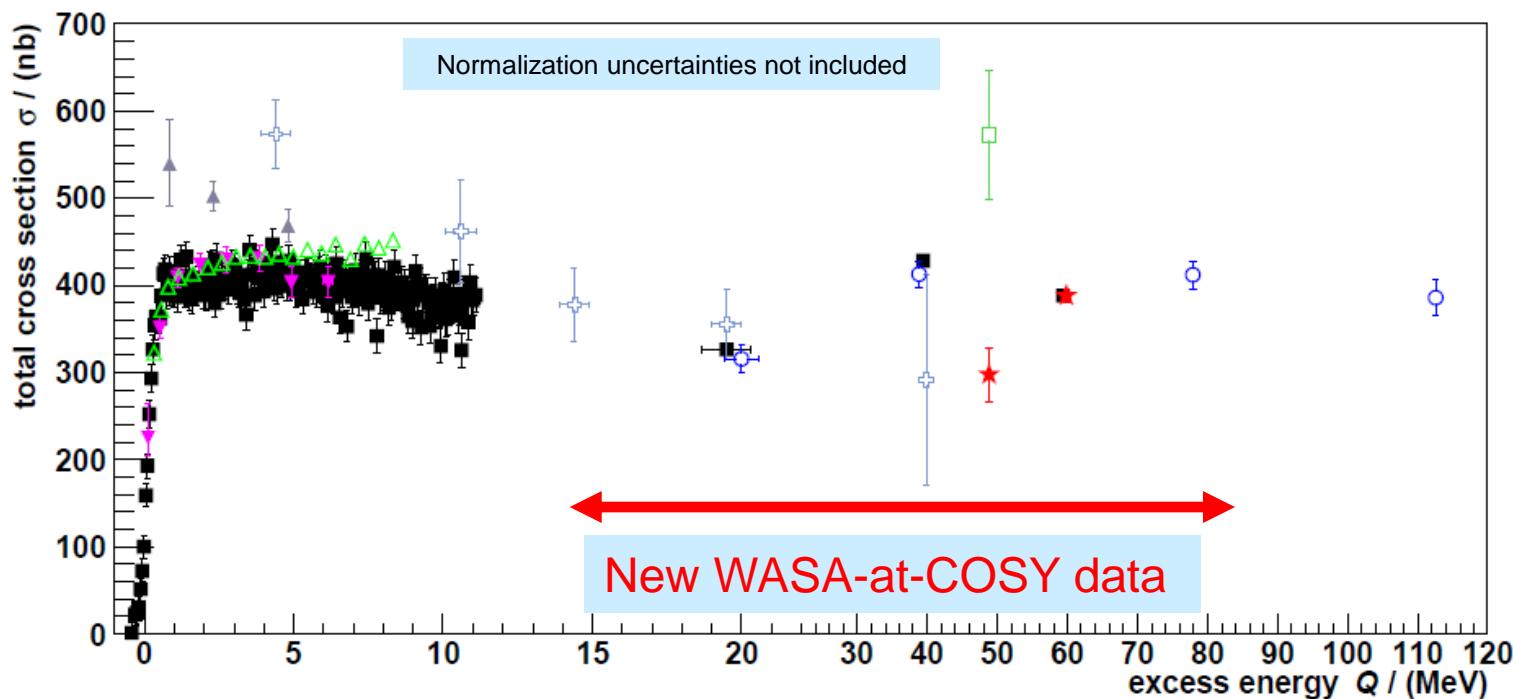
WASA-at-COSY Beam Time: May 2014

„Online spectra“ from supercycle 2: 8 energies



Nils Hüsken, private communication

The Reaction $d+p \rightarrow {}^3\text{He}+\eta$ at Higher Q-Values



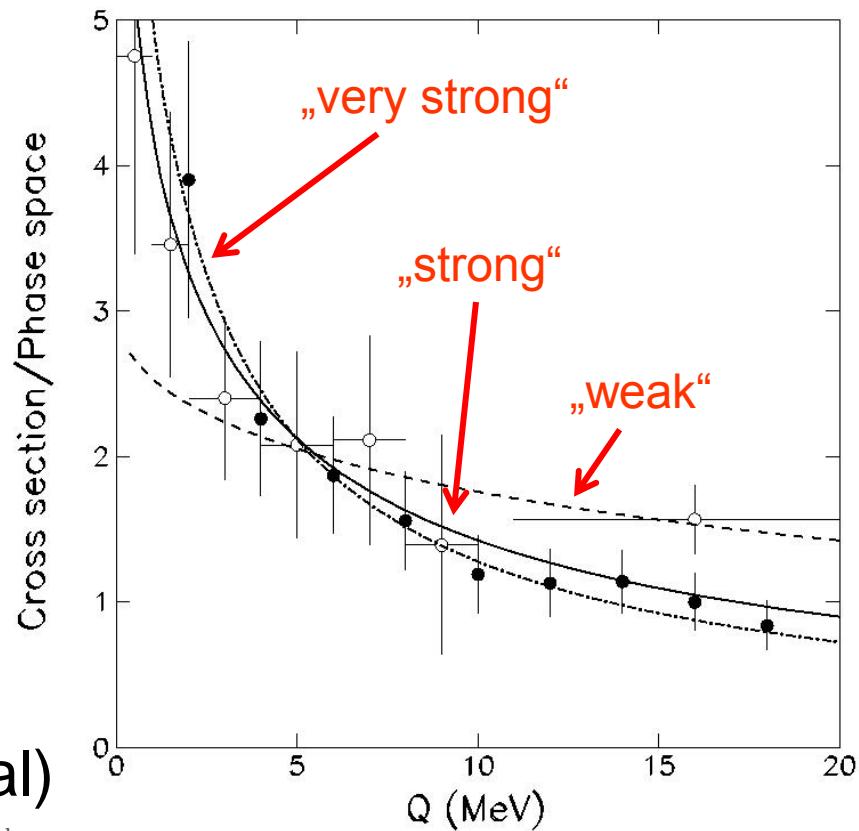
P. Adlarson et al., accepted by EPJA

Outlook: $p\bar{d} \rightarrow p_{sp}\bar{d}\eta$

- Threshold enhancement
 $\sigma/PS \leftrightarrow FSI$ calculations
- Filled symbols: $p\bar{d} \rightarrow p\bar{d}\eta$ taken
 below $NN \rightarrow NN\eta$ threshold
 → far from quasi-free (controversial)

TABLE II. Results of the AGS and three different approximate calculations of $A_{\eta d}$ with $\alpha = 3.316 \text{ fm}^{-1}$.

Ref.	ηN input	Exact $A_{\eta d}$ (fm)		Approximate $A_{\eta d}$ (fm)	
		$a_{\eta N}$ (fm)	AGS	MST I [8]	MST II [8]
[20]	$0.25+i0.16$	$0.73+i0.56$		0.66+i0.71	0.66+i0.58
[2]	$0.27+i0.22$	$0.71+i0.84$		0.57+i0.97	0.64+i0.81
[21]	$0.291+i0.360$	$0.38+i1.36$		0.17+i1.35	0.42+i1.25
[3]	$0.30+i0.30$	$0.61+i1.22$		0.39+i1.28	0.58+i1.11
[21]	$0.430+i0.394$	$0.50+i2.07$		0.14+i1.91	0.65+i1.73
[2]	$0.44+i0.30$	$1.15+i1.89$		0.63+i1.93	1.01+i1.50
[20]	$0.46+i0.29$	$1.31+i1.99$		0.72+i2.04	1.11+i1.54
[22]	$0.476+i0.279$	$1.49+i2.06$		0.81+i2.15	1.22+i1.56
[23]	$0.51+i0.21$	$2.37+i1.77$		1.48+i2.31	1.65+i1.39
[3]	$0.55+i0.30$	$1.64+i2.99$		0.61+i2.73	1.40+i1.98
[21]	$0.579+i0.399$	$0.34+i3.31$		-0.13+i2.64	0.93+i2.41
[24]	$0.62+i0.30$	$1.80+i4.30$		0.36+i3.36	1.65+i2.41
[22]	$0.876+i0.274$	$-8.81+i4.30$		-2.76+i4.24	2.42+i5.55
[22]	$0.888+i0.274$	$-8.63+i3.49$		-2.90+i4.12	2.37+i5.79
[25]	$0.98+i0.37$	$-4.69+i1.59$		-2.75+i2.77	-0.06+i6.20



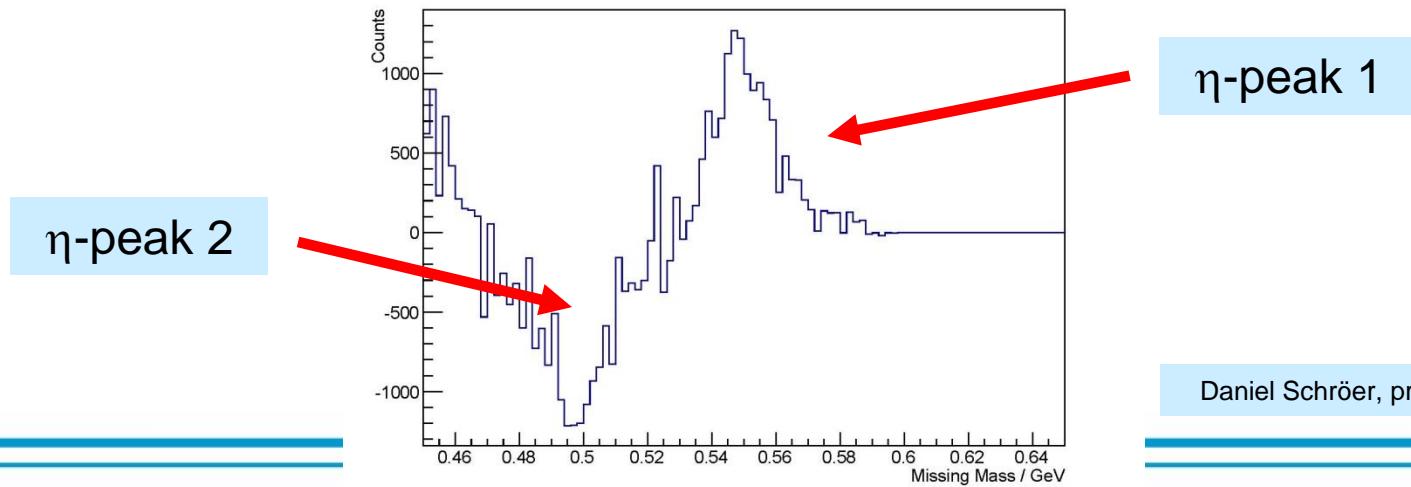
$$|f(p_f)|^2 = \frac{S}{|1 - i \cdot a_{d\eta} \cdot p_f|^2}$$

Outlook: $p\bar{d} \rightarrow p_{sp} d\eta$

- New data from ANKE/COSY are expected to allow for
 - a scattering length $|a_{d\eta}|$ determination with a precision of ~5%
 - the determination of angular distributions

in the excess energy range $Q = 0 \dots 100$ MeV

- First signals: Subtraction from two data sets obtained at different beam momenta, but analyzed assuming the same beam momentum



Daniel Schröer, private communication

Summary

- New data on η meson production in pd-collisions give important information on η -nucleus systems
- Results from measurements with polarized beams
 - support the strong ${}^3\text{He} + \eta$ FSI interpretation
 - show no spin-dependent contributions on a scale of $\sim\text{MeV}$ above threshold
 - give new insight into the structure of the relevant production amplitudes
- Data at higher excess energies might indicate an unexpected cross section structure
- New data have been recorded recently and will allow for more detailed experimental and theoretical investigations

Thank you very much....





$$J^G(J^{PC}) = 0^+(0^{-+})$$

We have omitted some results that have been superseded by later experiments. The omitted results may be found in our 1988 edition Physics Letters **B204** (1988).

η MASS

Recent measurements resolve the obvious inconsistency in previous η mass measurements in favor of the higher value first reported by NA48 (LAI 02). We use only precise measurements consistent with this higher mass value for our η mass average.

VALUE (MeV)	EVTS	DOCUMENT ID	TECN	COMMENT
547.862±0.018 OUR AVERAGE				
547.873±0.005±0.027	1M	GOSLAWSKI	12	SPEC $d p \rightarrow {}^3\text{He} \eta$
547.874±0.007±0.029		AMBROSINO	07B	KLOE $e^+ e^- \rightarrow \phi \rightarrow \eta \gamma$
547.785±0.017±0.057	16k	MILLER	07	CLEO $\psi(2S) \rightarrow J/\psi \eta$
547.843±0.030±0.041	1134	LAI	02	NA48 $\eta \rightarrow 3\pi^0$
• • • We do not use the following data for averages, fits, limits, etc. • • •				
547.311±0.028±0.032		¹ ABDEL-BARY	05	SPEC $d p \rightarrow {}^3\text{He} \eta$
547.12 ± 0.06 ± 0.25		KRUSCHE	95D	SPEC $\gamma p \rightarrow \eta p$, threshold
547.30 ± 0.15		PLOUIN	92	SPEC $d p \rightarrow {}^3\text{He} \eta$
547.45 ± 0.25		DUANE	74	SPEC $\pi^- p \rightarrow n$ neutrals
548.2 ± 0.65		FOSTER	65C	HBC
549.0 ± 0.7	148	FOELSCHE	64	HBC
548.0 ± 1.0	91	ALFF-...	62	HBC
549.0 ± 1.2	53	BASTIEN	62	HBC

¹ ABDEL-BARY 05 disagrees significantly with recent measurements of similar or better precision. See comment in the header.

The COSY-Accelerator at Jülich



COSY (Cooler Synchrotron)

Energy range

- 0.045 – 2.8 GeV (p)
- 0.023 – 2.3 GeV (d)
(momentum 3.7 GeV/c)

Beam cooling

- Electron cooling
- Stochastic cooling

Polarisation

- p, d beams & targets

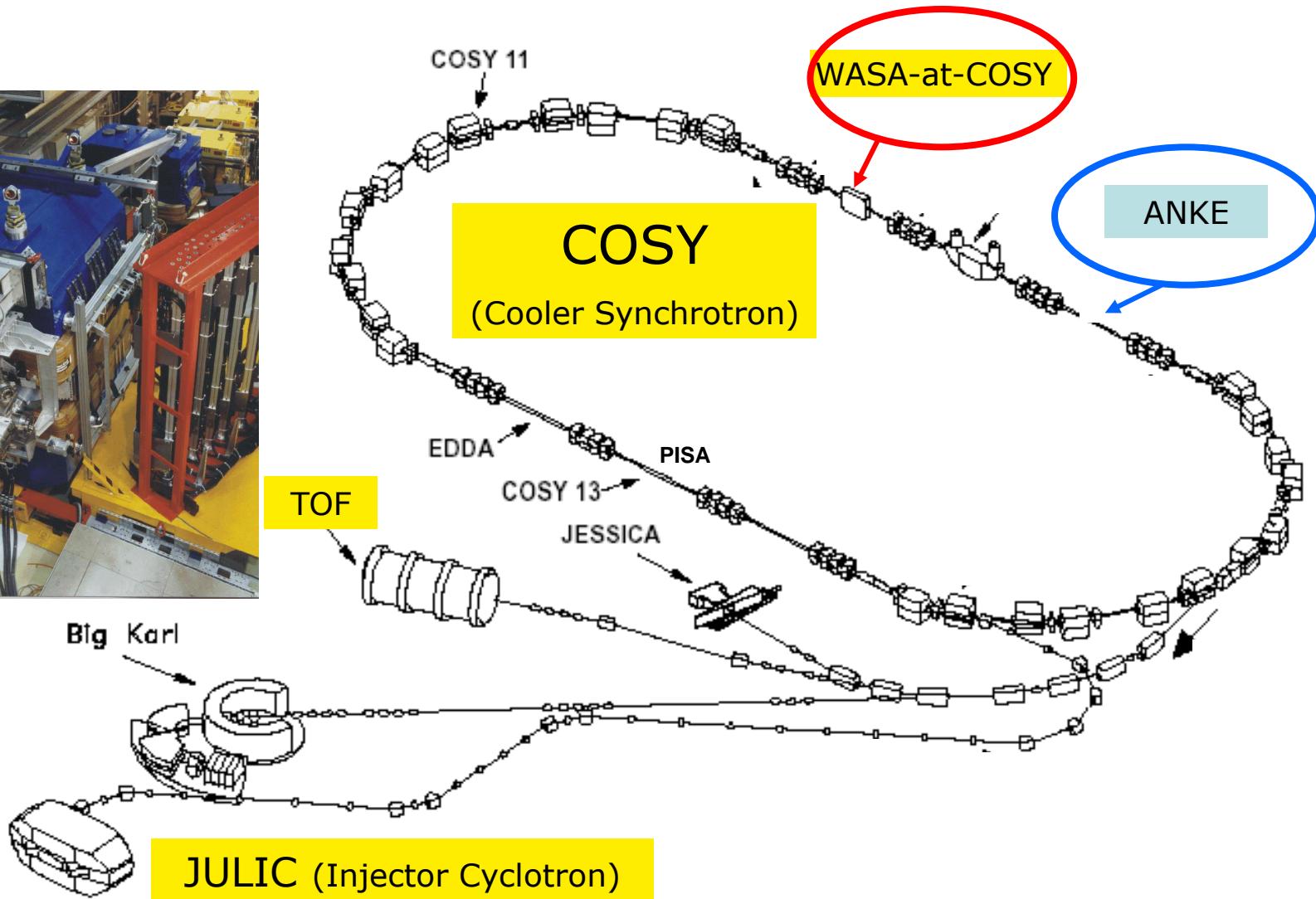
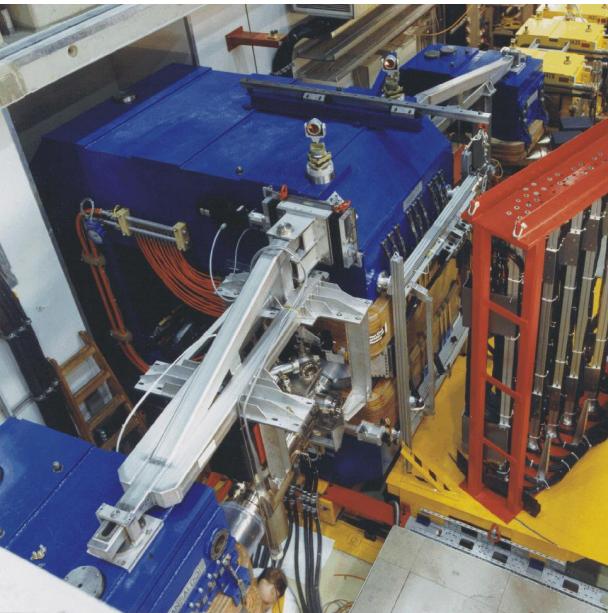
Beams

- internal, external

Experiments, Detectors

- ANKE, TOF, WASA, ...

The Experiments ANKE and WASA-at-COSY



Scattering Theory and Final State Interaction

- The scattering length can deliver informationen about possible bound states
- Conditions for bound $\eta^3\text{He}$ state:
 - Existence of a pole in the complex p_f plane

$$f_s = \frac{f_{\text{prod}}}{1 - i \cdot a \cdot p_f + \frac{1}{2} a \cdot r \cdot p_f^2}$$

$$a \equiv a_r + ia_i$$

$$r \equiv r_r + ir_i$$

- As well as

$$a_r < 0, \quad a_i > 0, \quad R = \frac{|a_i|}{|a_r|} < 1$$

η - ${}^3\text{He}$ Scattering Length

Fit to data delivers information about the complex η - ${}^3\text{He}$ scattering length:

$$\left(\frac{d\sigma(\vartheta)}{d\Omega} \right) \cdot \frac{p_i}{p_f} = |f_{\text{scat}}|^2 = |f_{\text{prod}} \cdot FSI|^2 = |f_{\text{prod}}|^2 \cdot |FSI|^2$$



Result:

$$a = [\pm (10.7 \pm 0.8^{+0.1}_{-0.5}) + i(1.5 \pm 2.6^{+1.0}_{-0.9})] \text{ fm}$$

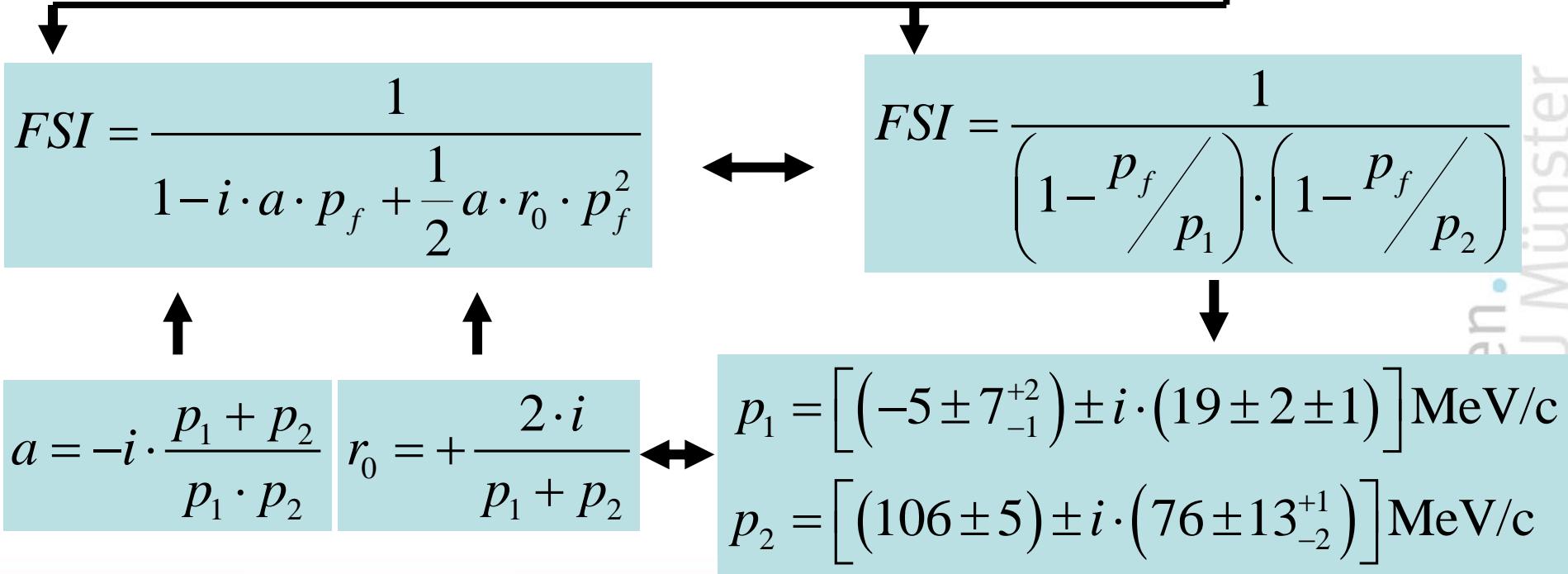
$$FSI = \frac{1}{1 - i \cdot a \cdot p_f + \frac{1}{2} a \cdot r_0 \cdot p_f^2}$$

Notice: Determination of $|a_r|$!

T. Mersmann, A.K., et al., PRL 98 (2007) 242301

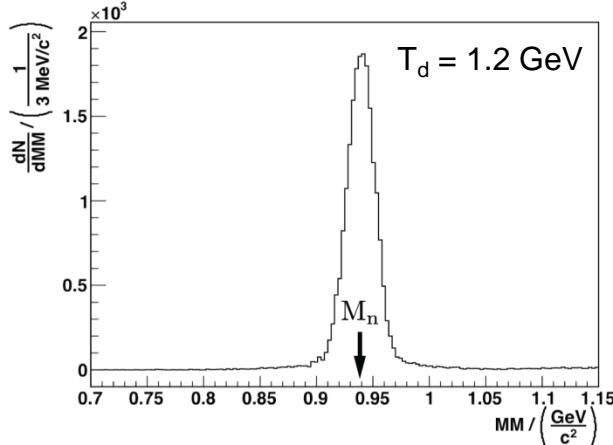
η - ${}^3\text{He}$ -Interaction: Determination of Pol's

$$\left(\frac{d\sigma(\vartheta)}{d\Omega} \right) \cdot \frac{p_i}{p_f} = |f_{\text{scatt}}|^2 = |f_{\text{prod}} \cdot FSI|^2 = |f_{\text{prod}}|^2 \cdot |FSI|^2$$



The Reaction $d+p \rightarrow {}^3\text{He}+\eta$ at ANKE

- Alternating injection of unpolarized and tensor polarized deuterons in COSY
- Ramped COSY beam: $Q = -5 \text{ MeV} \dots +10 \text{ MeV}$ (300 s)
- Full geometrical acceptance of ANKE for $d+p \rightarrow {}^3\text{He}+\eta$
- Determination of p_{zz} by, e.g., $d+p \rightarrow (\text{pp})+n$ (analyzing powers known)



$$\frac{d\sigma_\uparrow}{dt}(q, \varphi) / \frac{d\sigma_0}{dt}(q, \varphi) =$$

$$1 + \sqrt{3} p_z i t_{11}(\vartheta) \cos(\varphi) - \frac{1}{2\sqrt{2}} p_{zz} t_{20}(\vartheta)$$

$$- \frac{\sqrt{3}}{2} p_{zz} t_{22}(\vartheta) \cos(2\varphi)$$

Tensor Polarizations

- Three different polarizations used for the experiment

1.) Nominal: $p_{zz} = -1, p_z = +1/3$
Measured: $p_{zz} = -0.635 \pm 0.087$

2.) Nominal: $p_{zz} = +1, p_z = -1$
Measured: $p_{zz} = 0.529 \pm 0.077$

3.) Nominal: $p_{zz} = +1, p_z = +1$
Measured: $p_{zz} = 0.217 \pm 0.082$