

In-medium \bar{K} mesons

from atoms to strange dibaryons

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- $\bar{K}N - \pi Y$ chiral dynamics and its consequences
- \bar{K} nuclear clusters; **strange dibaryons**
- \bar{K} -nucleus potentials from K^- atoms
- **No** \bar{K} condensation on earth

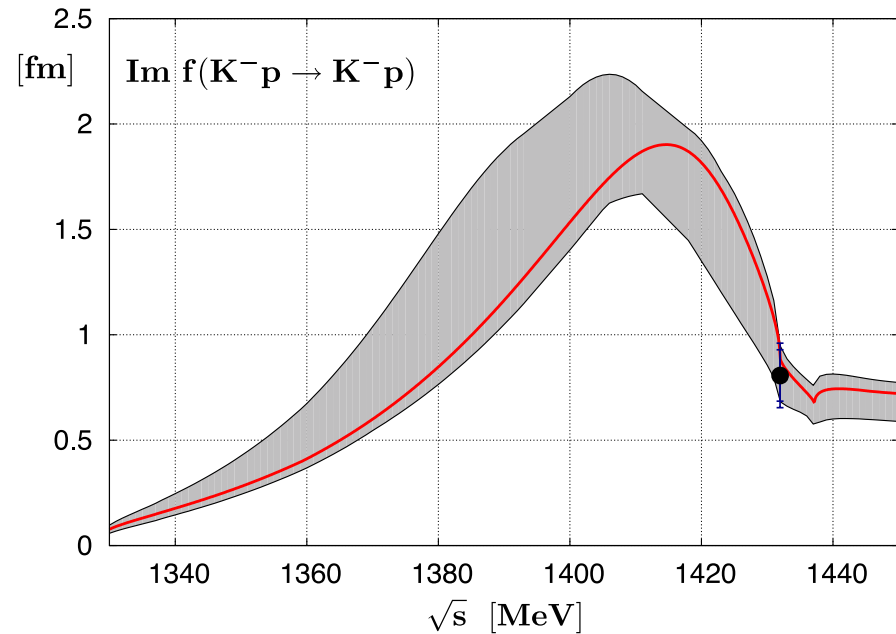
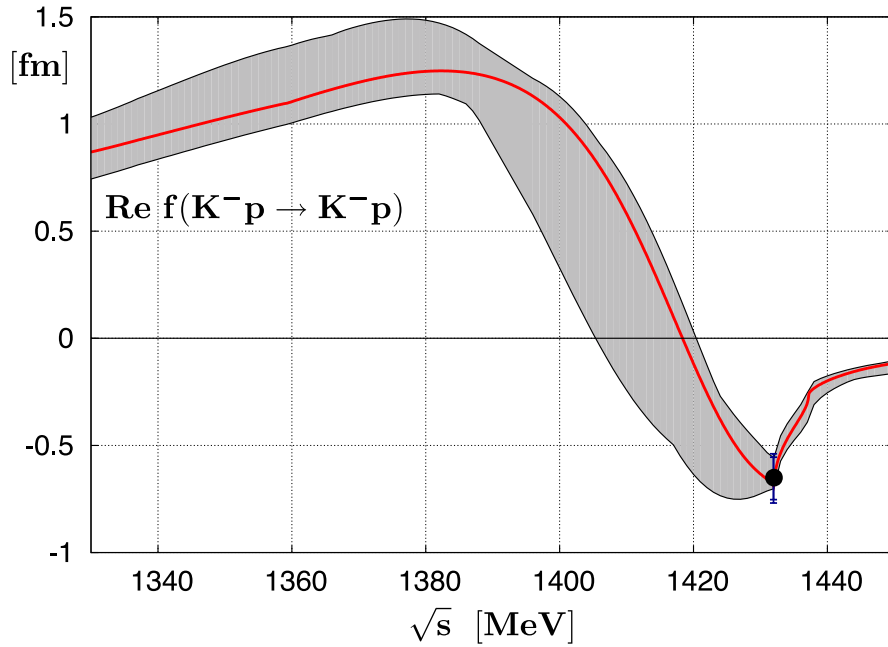
SNP: NPA 881 (2012), HYP12: NPA 914 (2013)

A.Gal, E.Friedman, N.Barnea, A.Cieplý, D.Gazda, J.Mareš

Acta Physica Polonica B 45 (2014) 673-687

$\bar{K}N - \pi Y$ Chiral Dynamics

K^-p scattering amplitude from NLO chiral SU(3) dynamics

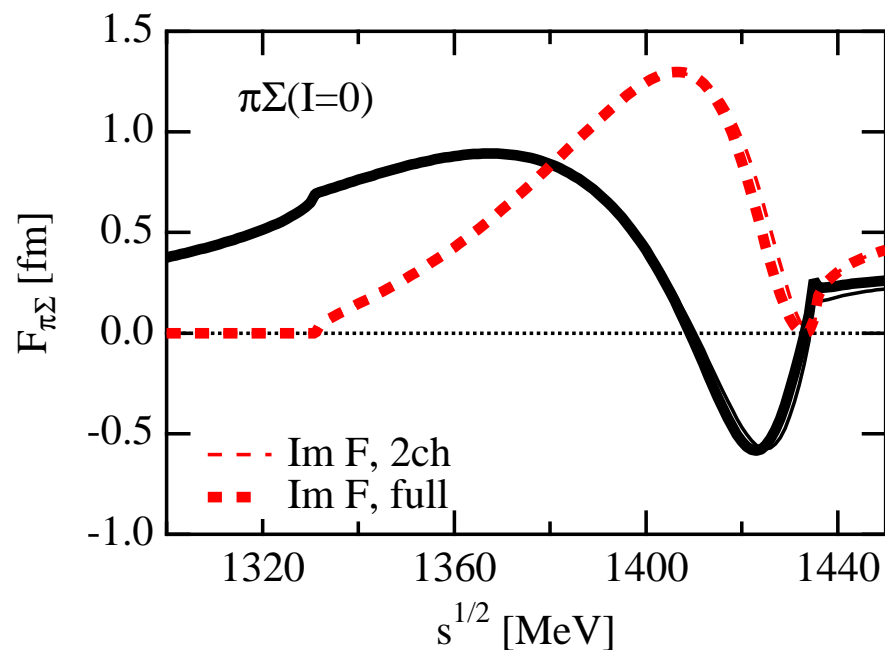
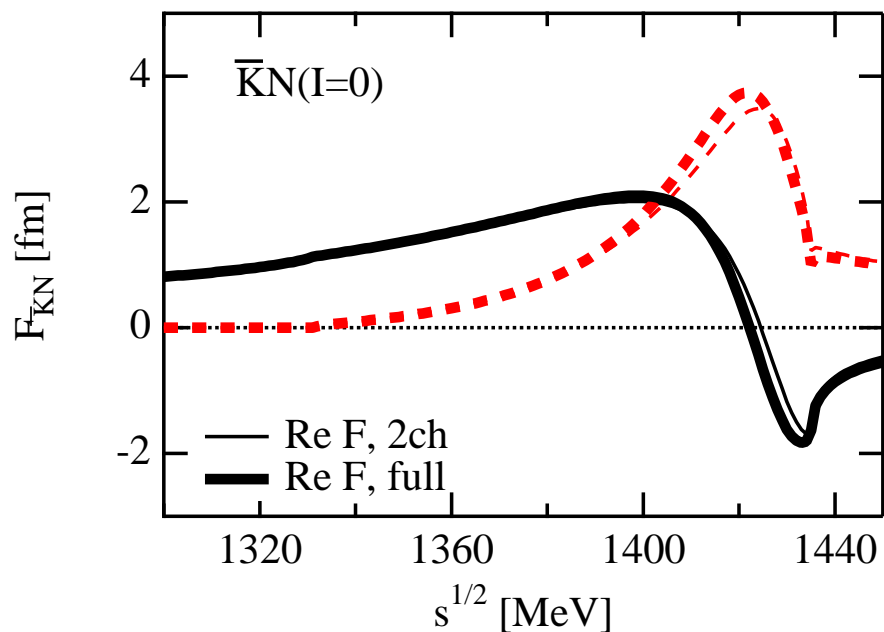


Y. Ikeda, T. Hyodo, W. Weise (IHW), PLB **706** (2011) 63; NPA **881** (2012) 98

Threshold amplitude constrained by SIDDHARTA exp.

**Strong subthreshold K^-p attraction; $\Lambda(1405)$ physics;
consequences for kaonic atoms & nuclear clusters**

$K^-NN \rightarrow YN$ absorption not accounted for by this model.



T. Hyodo, W. Weise, PRC 77 (2008) 035204 *I* = 0 coupled-channel amplitudes

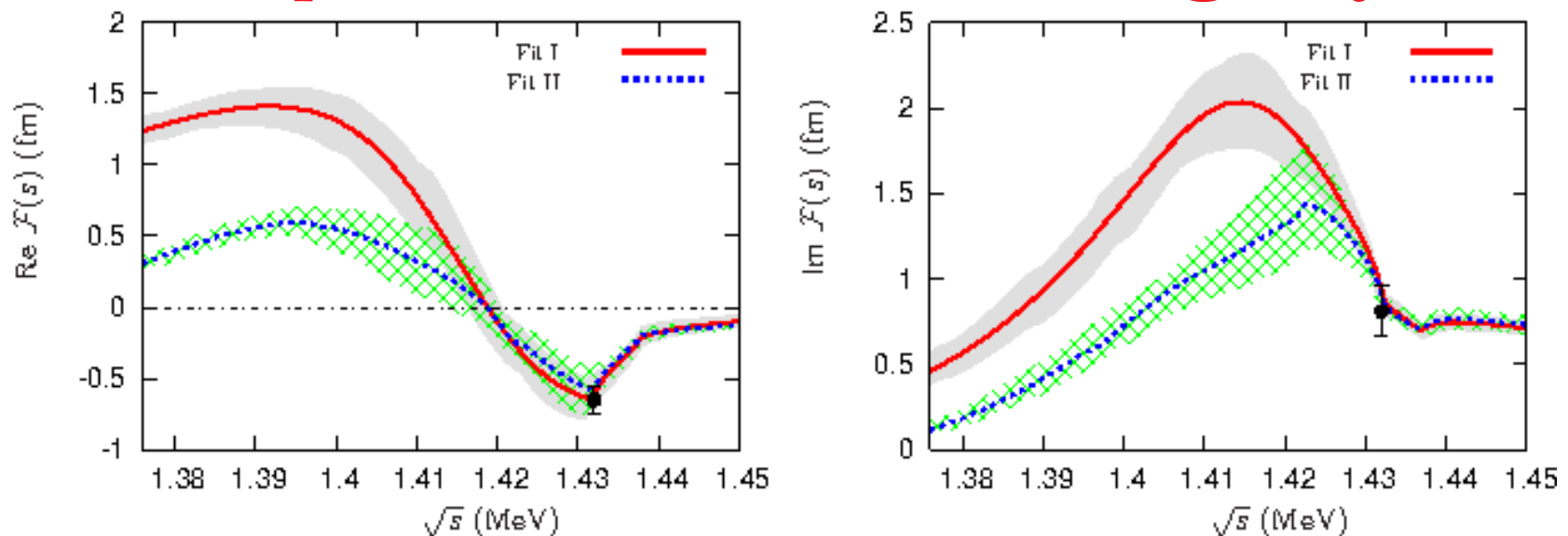
Location of ‘resonances’: $\bar{K}N \approx 1420$ MeV, $\pi\Sigma \approx 1405$ MeV

$\bar{K}N$ pole relatively narrow, and stable to fit variations.

$\pi\Sigma$ pole broader, unstable, and affects subthreshold.

IHW (2012): $z_{\bar{K}N} = 1424 - i26$ MeV, $z_{\pi\Sigma} = 1381 - i81$ MeV

K^-p subthreshold ambiguity



Two NLO chiral-model fits by Guo-Oller, PRC 87 (2013) 035202

- **Fit I: meson-independent** $f = 125.7 \pm 1.1$ MeV.
- **Fit II: physical values for f_π , f_K , f_η .**
Will create problems when confronted with K^- -atom data.
- **Amplitudes constrained at threshold by SIDDHARTA.**
 $\bar{K}N$ pole robust, $\pi\Sigma$ pole correlated with fit.

\bar{K} nuclear few-body systems

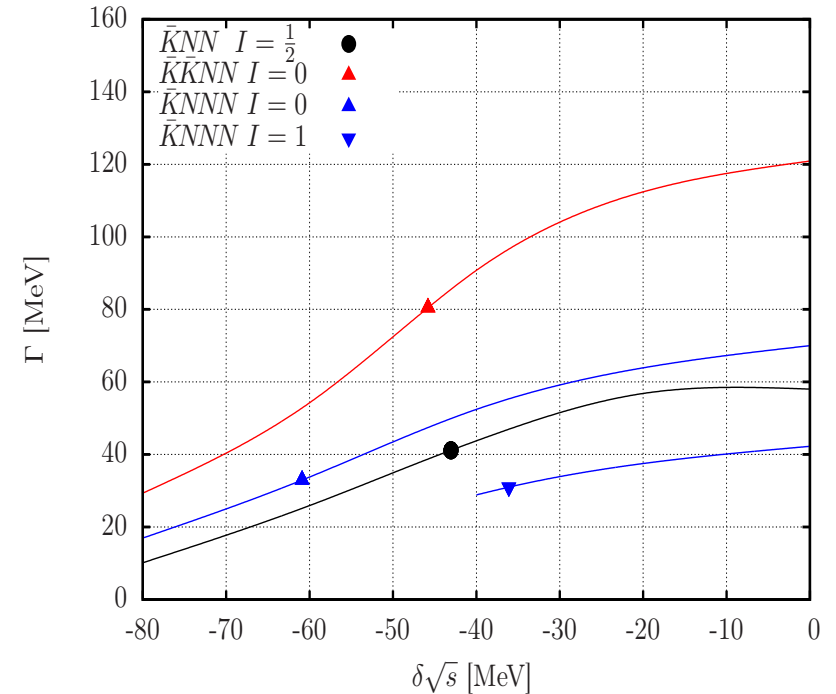
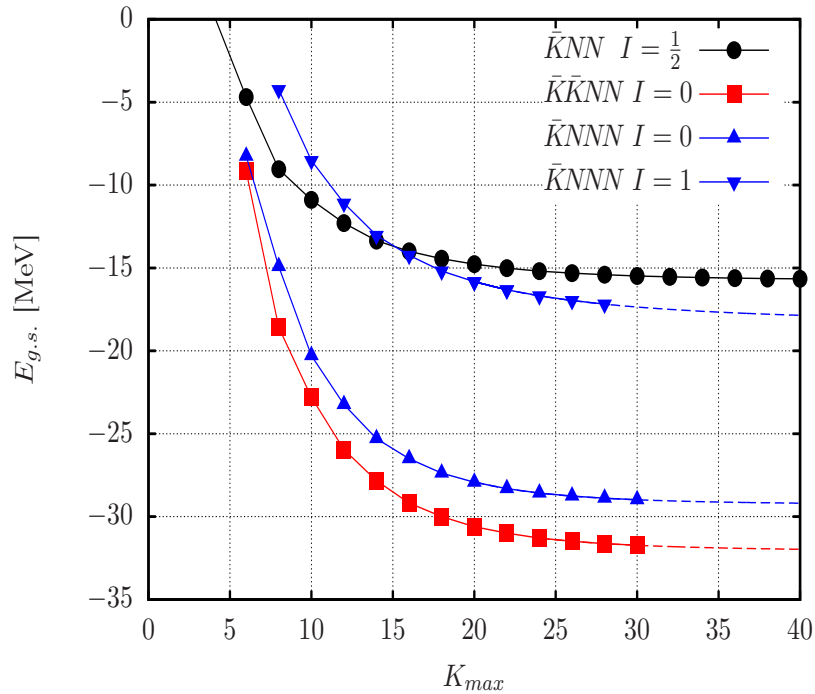
Energy dependence in \bar{K} nuclear few-body systems

- $\Lambda(1405)$ induces strong energy dependence of the scattering amplitudes $f_{\bar{K}N}(\sqrt{s})$ and the underlying effective single-channel input potentials $v_{\bar{K}N}(\sqrt{s})$.
- $s = (\sqrt{s_{\text{th}}} - B_K - B_N)^2 - (\vec{p}_K + \vec{p}_N)^2 \leq s_{\text{th}}$
- Expanding nonrelativistically near $\sqrt{s_{\text{th}}} \equiv m_K + m_N$:

$$\delta\sqrt{s} = -\frac{B}{A} - \frac{A-1}{A}B_K - \xi_N \frac{A-1}{A} \langle T_{N:N} \rangle - \xi_K \left(\frac{A-1}{A}\right)^2 \langle T_K \rangle,$$

$$\delta\sqrt{s} \equiv \sqrt{s} - \sqrt{s_{\text{th}}}, \quad B_K = -E_K, \quad \xi_{N(K)} \equiv \frac{m_{N(K)}}{(m_N + m_K)}.$$
- **Self-consistency:** output \sqrt{s} from solving the Schroedinger equation identical with input \sqrt{s} .

3- & 4-body B & Γ calculated self-consistently



N. Barnea, A. Gal, E.Z. Liverts, PLB **712** (2012)

- Variational calculation in hyperspherical basis controlled by K_{max}
- $\bar{K}N$ energy dependence [Hyodo–Weise, PRC 77 (2008) 035204]
restrains B & Γ by treating $\delta\sqrt{s}_{\bar{K}N}$ self-consistently
- $B(4\text{-body})$ small w.r.t. non-chiral estimates of over 100 MeV

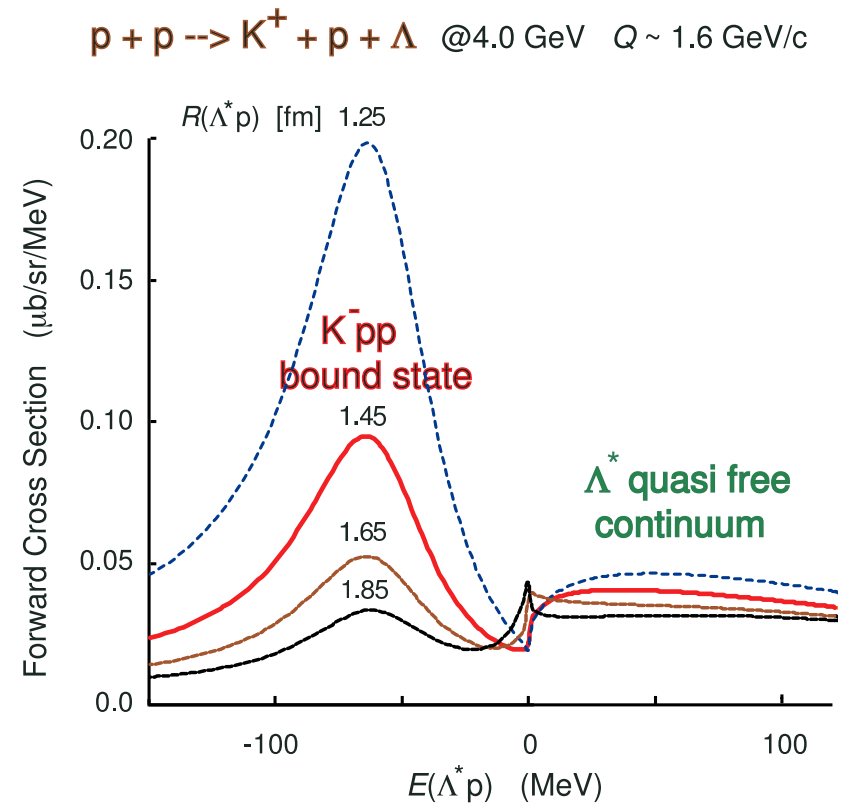
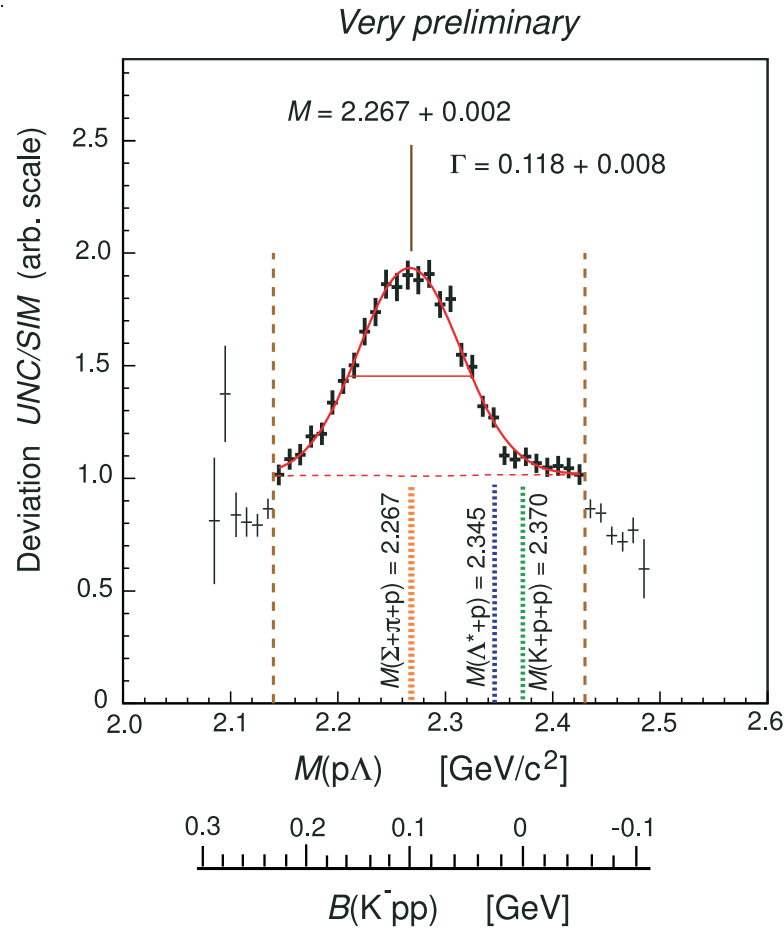
- $\bar{K}NN$: is there an excited $I = 1/2$ quasibound state ($\bar{K}d$, dominantly $I_{NN} = 0$) on top of “ K^-pp ” g.s. ?
- Barnea, Gal & Liverts do not find such a bound state below the Λ^*N threshold at $B = 11.4$ MeV.
- Bayar & Oset [NPA **881** (2012) 127]: **YES**, bound by about 9 MeV, from a peak in $|T_{\bar{K}NN}|^2$ calculated in a fixed-scatterer approximation to Faddeev equations.
- Shevchenko [NPA **890-1** (2012) 50]: **UNLIKELY**, judging from the K^-d scattering length and effective range deduced from a $\bar{K}NN$ Faddeev calculation.
- Shevchenko & Revai [PRC, arXiv:1402.3935]: **NO**, searching for poles in a $\bar{K}NN$ Faddeev calculation.

K^-pp calculated binding energies & widths

(MeV)	chiral, energy dep. calculations				non-chiral, static calculations			
	var. [1]	var. [2]	Fad. [3]	Fad. [4]	var. [5]	Fad. [6]	Fad. [7]	var. [8]
B	16	17–23	9–16	32	48	50–70	60–95	40–80
Γ	41	40–70	34–46	49	61	90–110	45–80	40–85

Robust binding & large widths; chiral models give weak binding

1. N. Barnea, A. Gal, E.Z. Liverts, PLB **712** (2012)
2. A. Doté, T. Hyodo, W. Weise, NPA **804** (2008) 197, PRC **79** (2009) 014003
3. Y. Ikeda, H. Kamano, T. Sato, PTP **124** (2010) 533
4. J Revai, N.V. Shevchenko, arXiv:1403.0757
5. T. Yamazaki, Y. Akaishi, PLB **535** (2002) 70
6. N.V. Shevchenko, A. Gal, J. Mareš, PRL **98** (2007) 082301
7. Y. Ikeda, T. Sato, PRC **76** (2007) 035203, PRC **79** (2009) 035201
8. S. Wycech, A.M. Green, PRC **79** (2009) 014001 (including p waves)



Yamazaki et al. PRL 104 (2010) 132502, DISTO data reanalysis at 2.85 GeV

Broad K^-pp structure in $pp \rightarrow \Lambda p K^+$ at $\pi N \Sigma$ threshold

Forthcoming experiments: $pp \rightarrow (K^-pp) + K^+$ at GSI

$K^-^3He \rightarrow (K^-pp) + n$ (E15) & $\pi^+d \rightarrow (K^-pp) + K^+$ (E27) at J-PARC

from $\Lambda(1405)N$ to $\Sigma(1385)N$

- $\Lambda(1405)N$ is in a way a doorway to the quasibound $I = 1/2, J^P = 0^- \bar{K}NN$ dibaryon. Lower $S = -1$ components are $\pi\Lambda N$ and $\pi\Sigma N$, the lowest of which is $\pi\Lambda N$, but it cannot support any strongly attractive meson-baryon s -wave interaction.
- The $\pi\Lambda N$ system can benefit from strong meson-baryon p -wave interactions fitted to the $\Delta(1232) \rightarrow \pi N$ and $\Sigma(1385) \rightarrow \pi\Lambda$ form factors. Maximize isospin and angular momentum couplings by full alignment: $I = 3/2, J^P = 2^+$. In particular, ΛN is in 3S_1 . This is a **Pion Assisted Dibaryon**, see **Gal & Garcilazo, PRD 78 (2008) 014013**.

- Add the $\pi\Sigma N$ channel [PRC **81** (2010) 055205, and finalized in NPA **897** (2013) 167].

A $\pi\Lambda N$ resonance about 10–20 MeV below the $\pi\Sigma N$ threshold is found by solving coupled-channel Faddeev equations. Results are **sensitive** to the pion-baryon p -wave form factors.

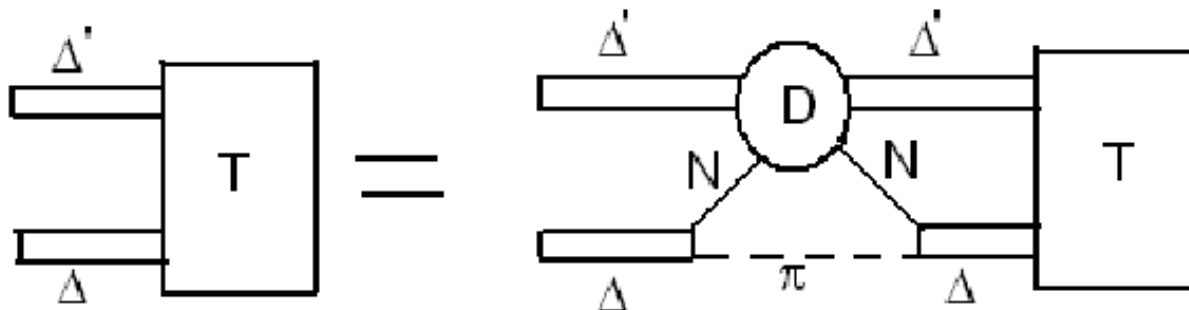
- This resonance is a pion assisted quasibound dibaryon, suggesting doorway states of the type $\Sigma(1385)N$ and $\Delta(1232)Y$, the lower of which is $\Sigma(1385)N$ with $I = 3/2$ and 5S_2 , $J^P = 2^+$. These are different labels from the $I = 1/2$ and 1S_0 , $J^P = 0^-$ for $\Lambda(1405)N$ viewed as a doorway to K^-pp .

- Adding a $\bar{K}NN$ channel does not help, because the leading 3S_1 NN configuration is Pauli forbidden.
- Search for this \mathcal{Y} dibaryon **at GSI & J-PARC** in:
 $p + p \rightarrow \mathcal{Y}^{++} + K^0, \quad \mathcal{Y}^{++} \rightarrow \Sigma^+ + p,$
 or $\pi^+ + d \rightarrow \mathcal{Y}^{++} + K^0, \quad \mathcal{Y}^{++} \rightarrow \Sigma^+ + p.$
- A (π^+, K^+) reaction as in E27 would lead to YN decay states similar to those anticipated in searches of K^-pp . **Another possibility at J-PARC or GSI is:**
 $\pi^- + d \rightarrow \mathcal{Y}^- + K^+, \quad \mathcal{Y}^- \rightarrow \Sigma^- + n.$
- **Nonstrange \mathcal{D}_{IS} pion assisted dibaryons**
 πNN : $\mathcal{D}_{12}(\mathbf{2150})$ & $\mathcal{D}_{21}(?)$;
 $\pi N\Delta$: $\mathcal{D}_{03}(\mathbf{2370})$ & $\mathcal{D}_{30}(?)$

Pion-assisted $\mathcal{D}_{03}(2370)$ $\Delta\Delta$ dibaryon

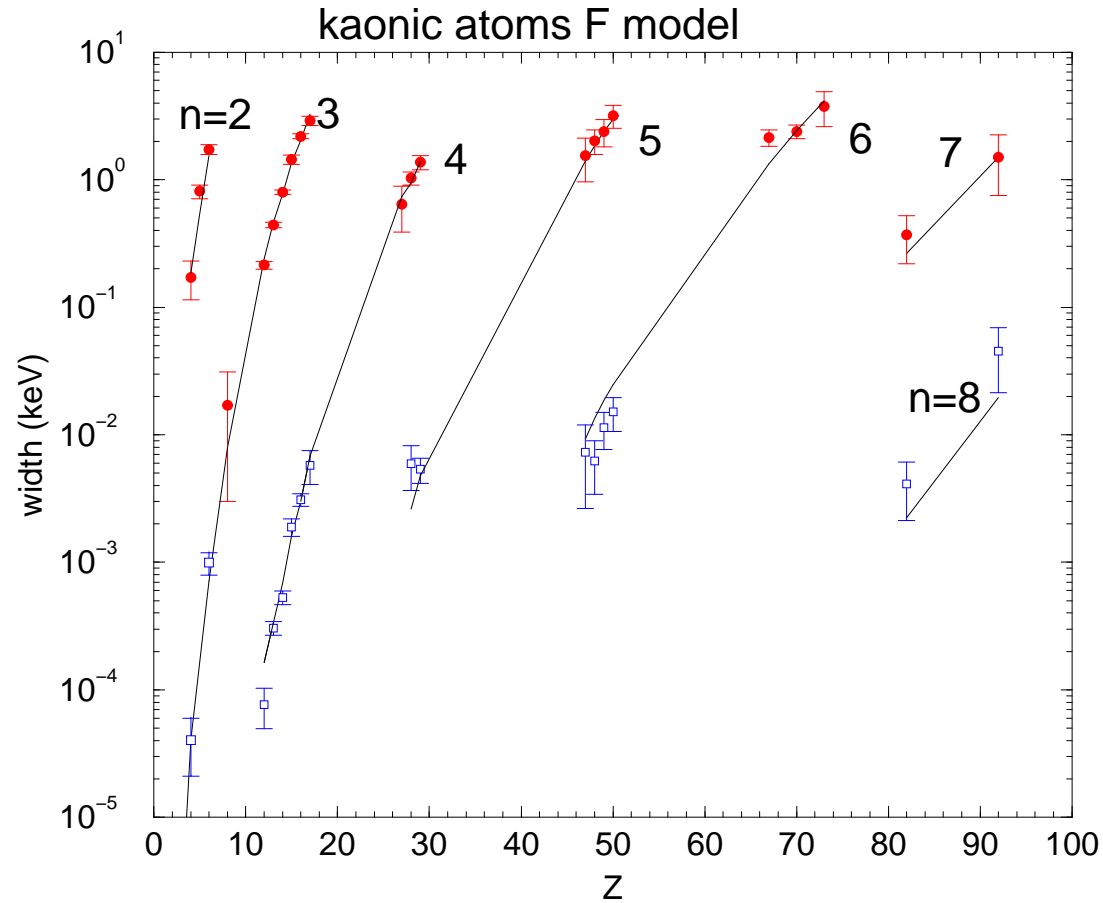
Gal-Garcilazo, PRL 111 (2013) 172301, NPA (2014)

- Approximate $\pi\pi NN$ problem by $\pi N\Delta'$ problem.
- Separable pair interactions: πN Δ -isobar form factor by fitting $\delta(P_{33})$; $N\Delta'$ $\mathcal{D}_{12}(2150)$ -isobar form factor by fitting $NN(^1D_2)$ scattering.
- 3-body S -matrix pole equation reduces to effective $\Delta\Delta'$ diagram:



- P_{33} form factors of size 0.9 & 1.3 fm:
 $M = 2363 \pm 20$, $\Gamma = 65 \pm 17$ MeV,
in good agreement with WASA@COSY
(Clement's & Workman's talks here).
- Although bound w.r.t. $\Delta\Delta$, $\mathcal{D}_{03}(2370)$ is
resonating w.r.t. the $\pi - \mathcal{D}_{12}(2150)$ threshold.
The subsequent decay $\mathcal{D}_{12}(2150) \rightarrow \pi d$ is seen
in the πd Dalitz plot projection.
- NN -decoupled dibaryon resonances \mathcal{D}_{21} & \mathcal{D}_{30}
predicted 10–30 MeV higher, respectively;
see also Bashkanov-Brodsky-Clement
“Novel 6q Hidden-Color Dibaryons in QCD”
PLB 727 (2013) 438 (Bashkanov's poster here).

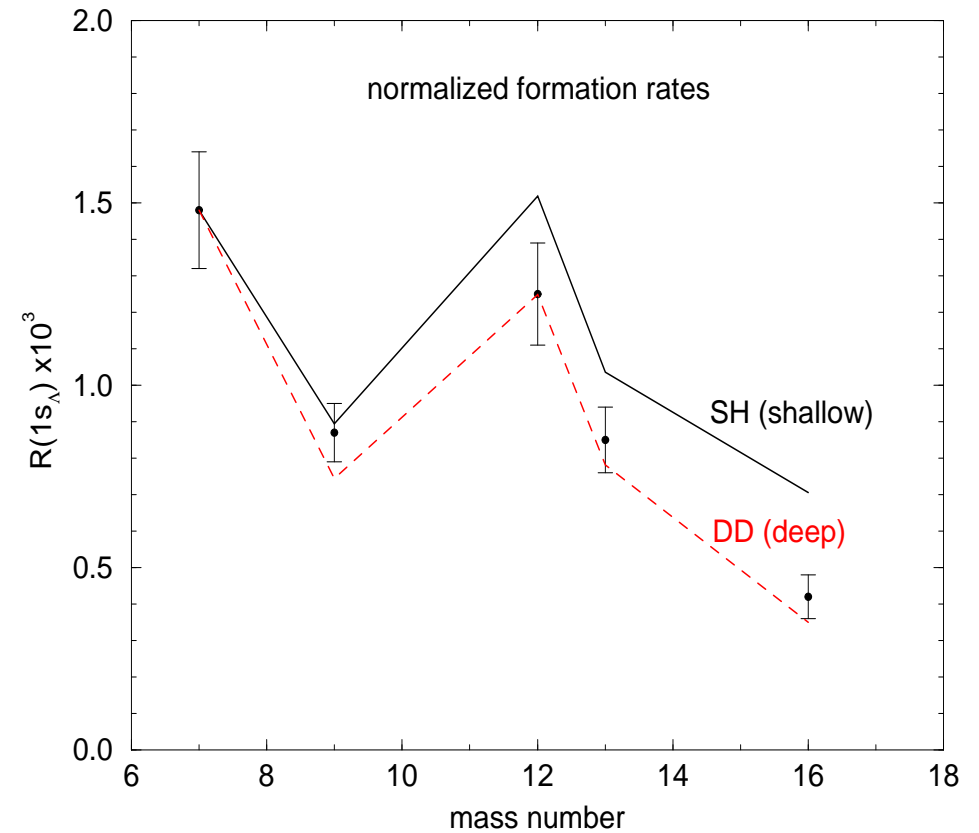
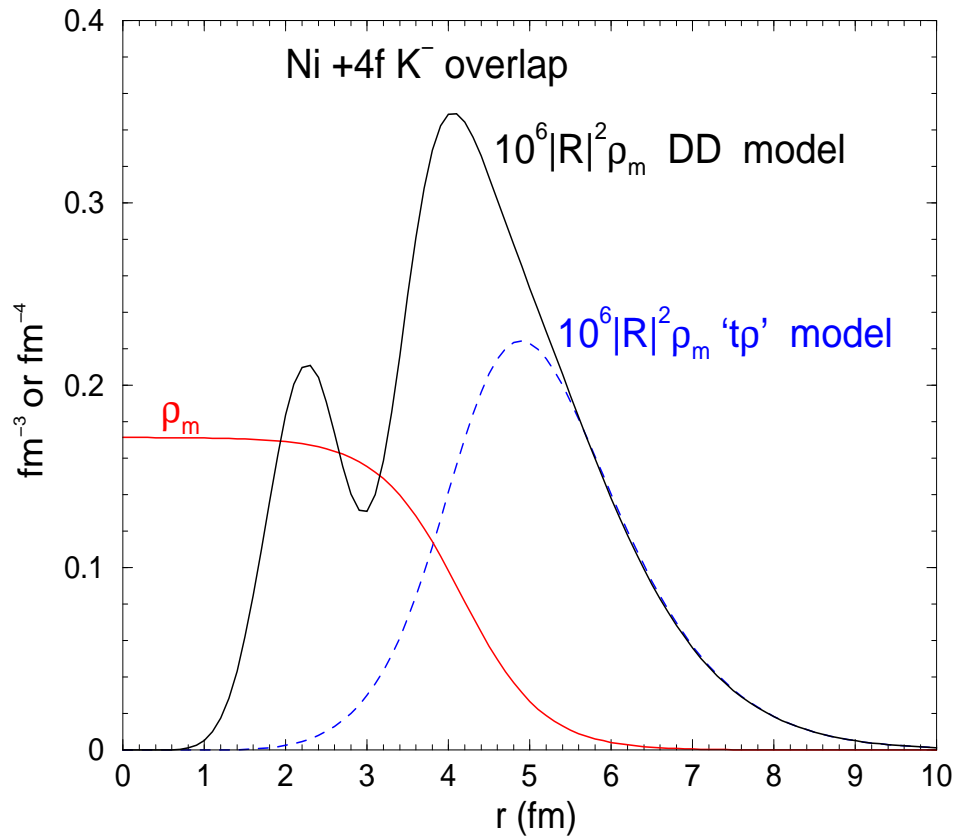
What do K^- atoms tell us?



K_{atom}^- widths across the periodic table in model F (deep pot.)

Lowest χ^2 phenom. model, $\chi^2 = 84$ per 65 data points,

J. Mareš, E. Friedman, A. Gal, NPA 770 (2006) 84.



Left: K^- -Ni 4f atomic wavefunction overlap with nuclear density for deep potential, revealing a nuclear $\ell = 3$ quasibound state.

Right: FINUDA $1s_\Lambda$ formation rates in K^-_{stop} capture in nuclei [Cieplý-Friedman-Gal-Krejčířík, PLB 698 (2011) 226].

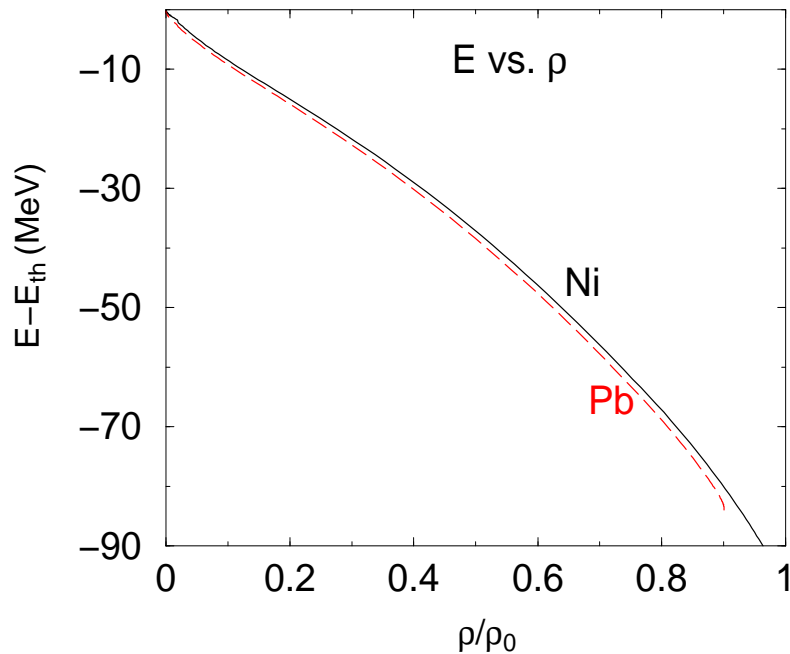
Deep K^- nuclear potential is favored.

Self-consistency requirement imposed in recent K^- atom calculations

[Cieplý-Friedman-Gal-Gazda-Mareš, PLB 702 (2011) 402]:

$$\sqrt{s_{K^-N}} \rightarrow E_{\text{th}} - B_N - B_K - \xi_N \frac{p_N^2}{2m_N} - \xi_K \frac{p_K^2}{2m_K}$$

$$\xi_{N(K)} = \frac{m_{N(K)}}{(m_N + m_K)} \quad \frac{p_K^2}{2m_K} \sim -V_{K^-} \approx 100 \text{ MeV}$$

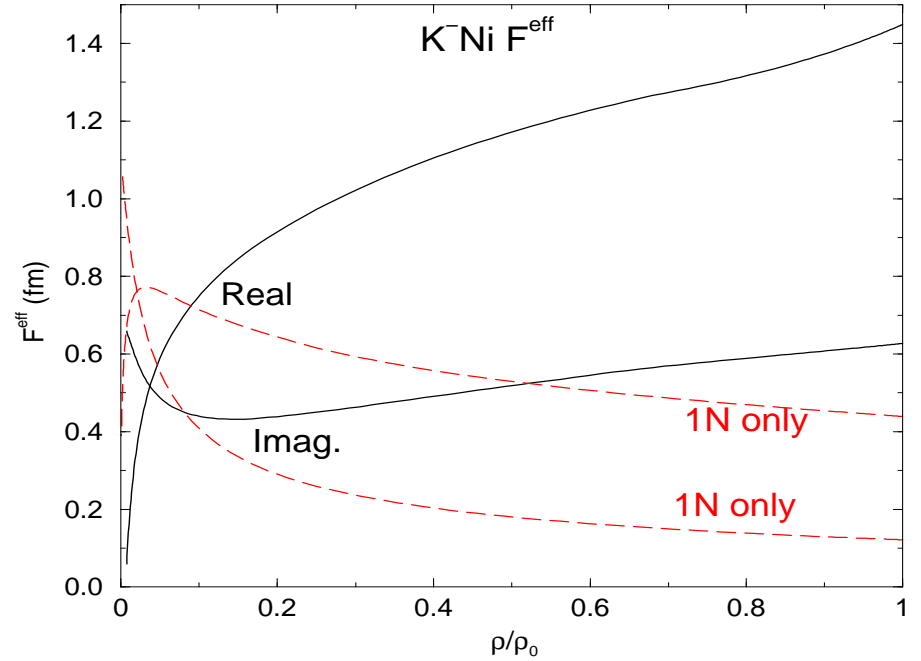
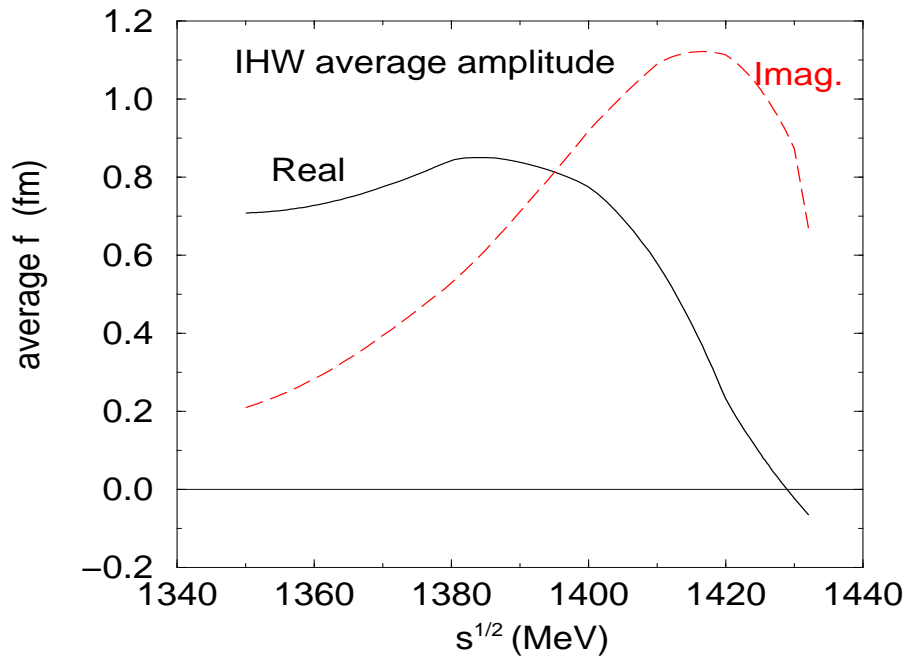


K^- is not at rest!

Friedman-Gal, NPA 899 (2013) 60

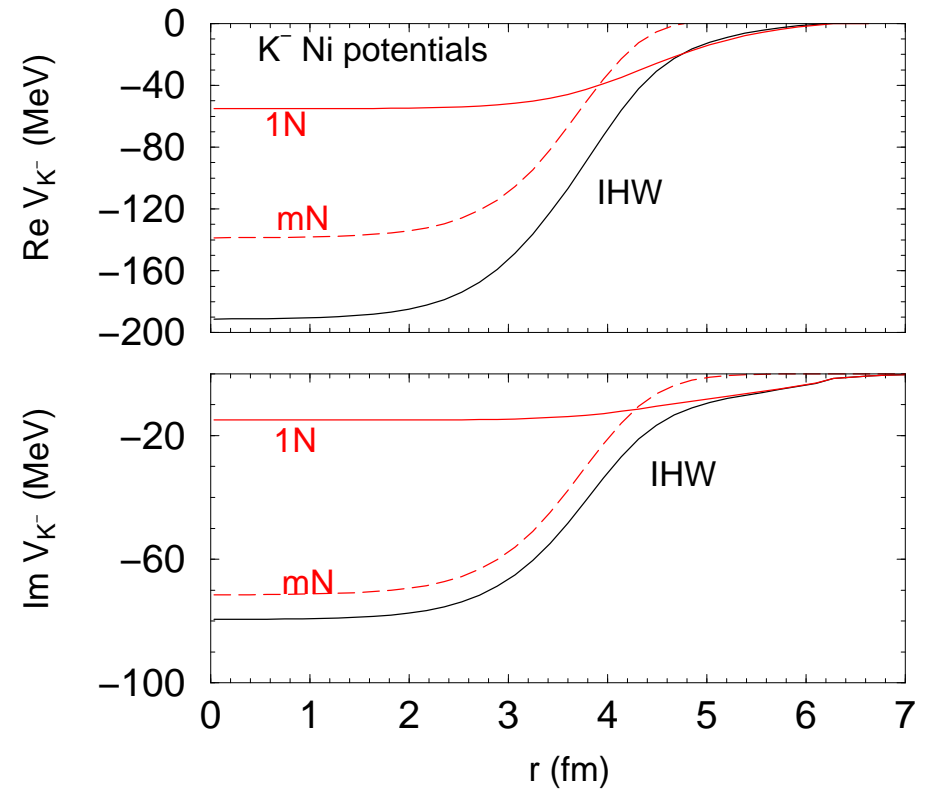
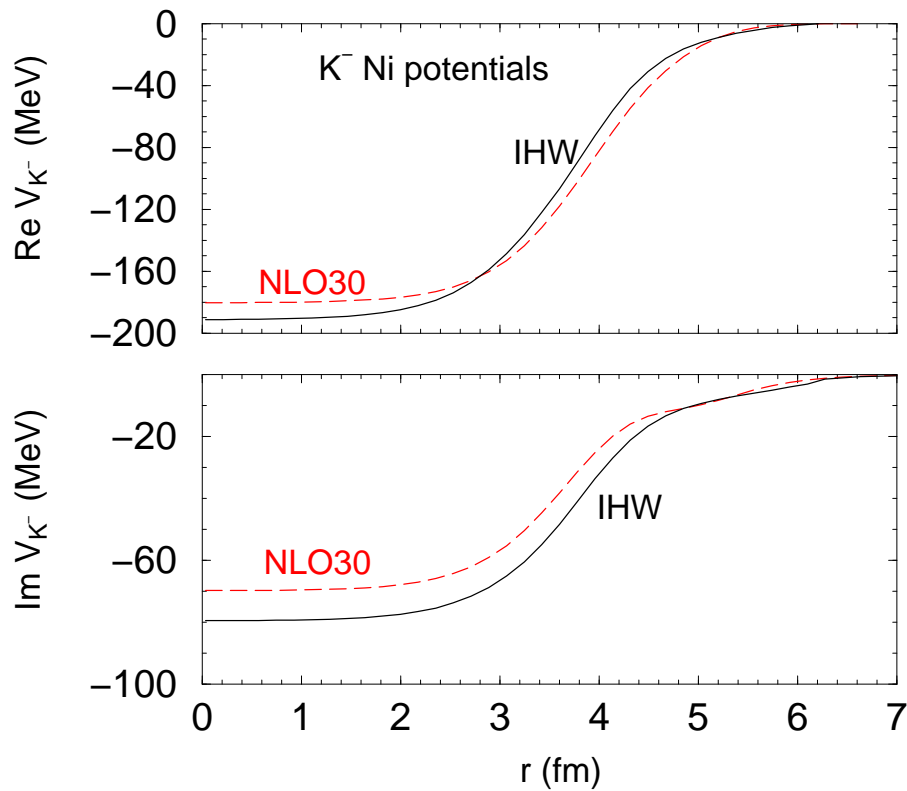
K^-N subthreshold energy *vs* nuclear density in K^- atoms.

A dominant in-medium effect



Left: IHW free-space input f_{K-N} Right: atomic-fit output $\mathcal{F}_{\text{tot}}^{\text{eff}}$

- Subthreshold energy shift is applied self consistently to in-medium $1N$ amplitude plus $(2+\dots)N$ phenomenological amplitude.
- Multiple-scattering inclusion of in-medium correlations.
- K^- -atom best-fit: $\chi^2/N_{\text{data}} = 118/65$ [Friedman-Gal, NPA 899 (2013) 60].



Kaonic-atom best-fit V_{K^-} for Ni & its non-additive breakdown into in-medium **1N** and phenomenological **m(any)N** contributions. **Upper level sensitive to 1N & lower level to mN terms.**

NLO30: A. Cieply, J. Smejkal, NPA **881** (2012) 115 (in-medium).

IHW: Y. Ikeda, T. Hyodo, W. Weise, NPA **881** (2012) 98.

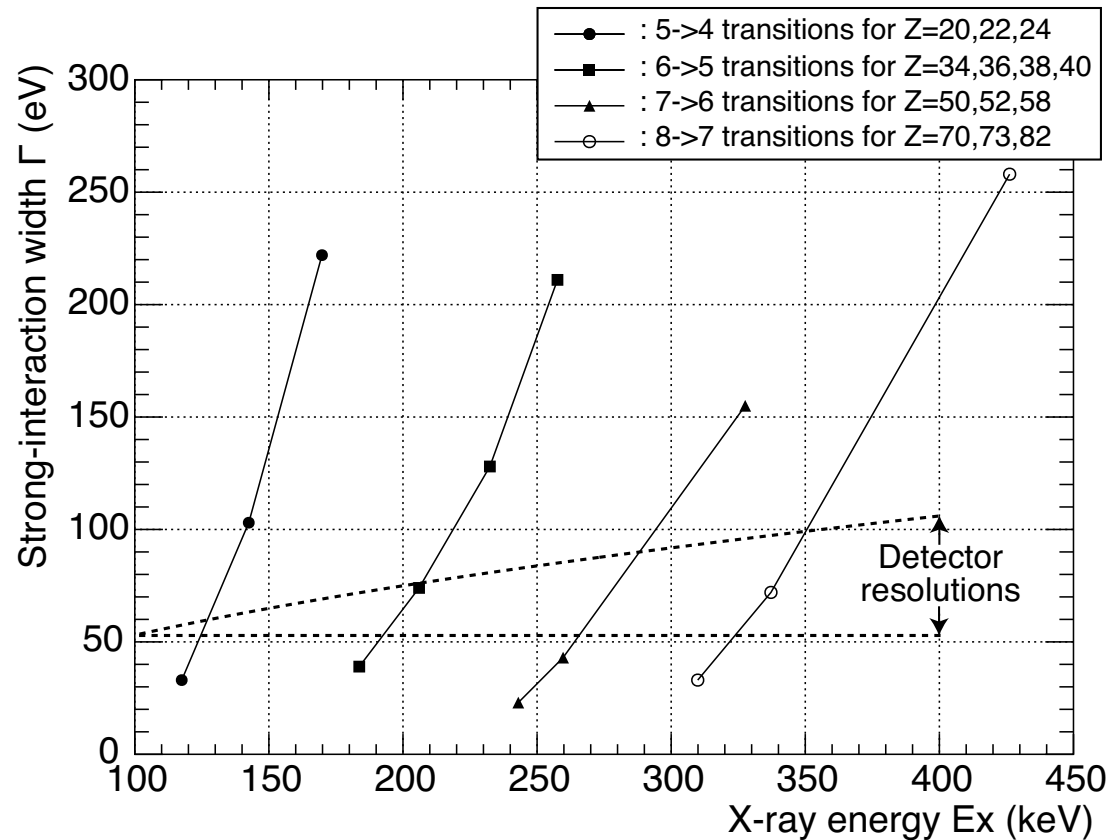
Full and reduced data set fits [$b(\rho_0)$ in fm]

N	shallow potential			deep potential		
	χ^2	Re $b(\rho_0)$	Im $b(\rho_0)$	χ^2	Re $b(\rho_0)$	Im $b(\rho_0)$
65	130	0.62 ± 0.05	0.93 ± 0.04	84	1.44 ± 0.03	0.59 ± 0.03
15	44	0.78 ± 0.13	0.92 ± 0.11	26	1.47 ± 0.05	0.55 ± 0.06

Reduced sets, C(2p) Si(3d) Ni(4f) Sn(5g) Pb(7i),
with upper-level yield & lower-level width & shift,
preserve features obtained from fits to full data.

Need more accurate measurements in a few atoms.

[E. Friedman, in MESON 2010, IJMPA 26 (2011) 468]

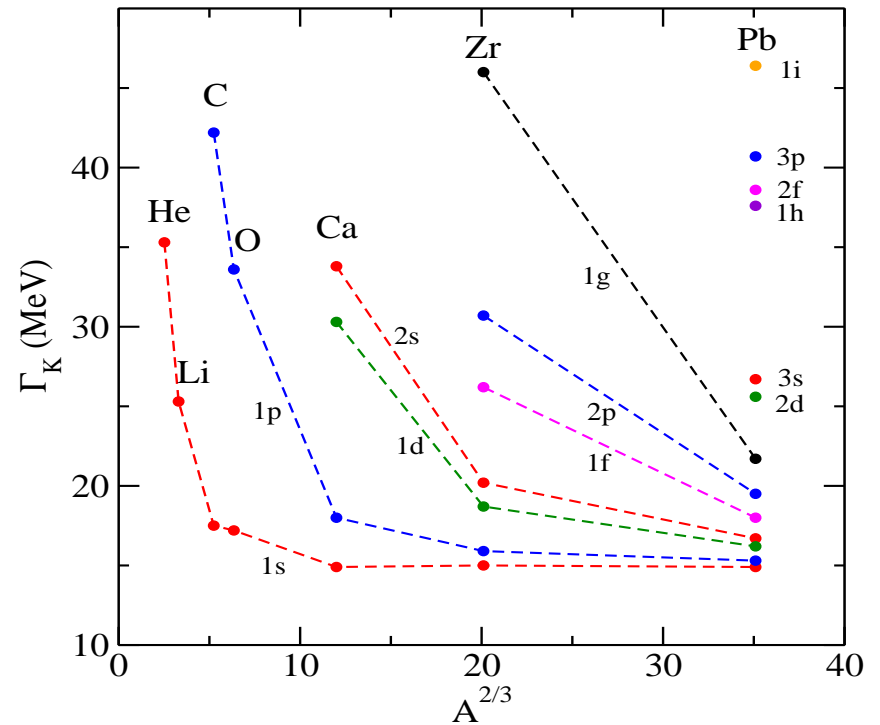
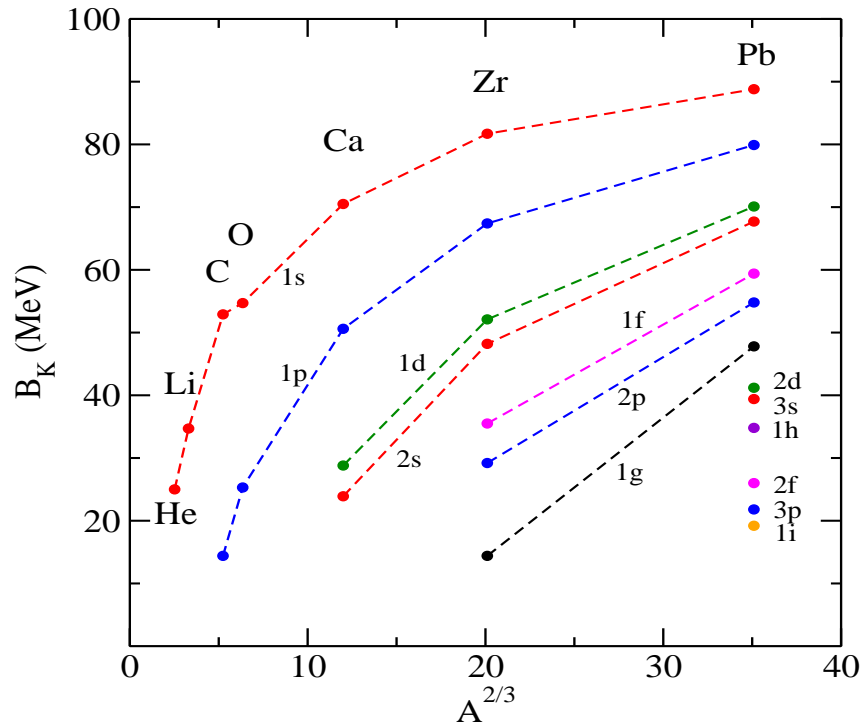


Feasibility of upper-level width measurements, on top of lower-level, vs. detector resolution for superconducting microcalorimeter detectors, normalized at 53 eV width for 100 keV x-ray.

E. Friedman, S. Okada, NPA 915 (2013) 170.

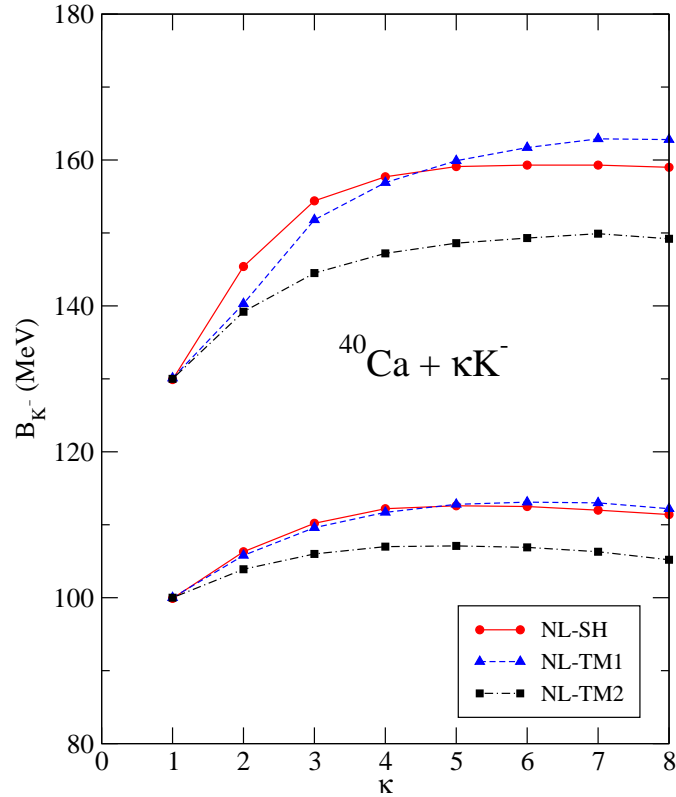
\overline{K} condensation on earth?

RMF quasibound spectra calculated self-consistently (NLO30 '+ SE')



D. Gazda, J. Mareš, NPA 881 (2012) 159

- NLO30 is a chirally motivated coupled channel separable model with in-medium versions [A. Cieplý, J. Smejkal, NPA 881 (2012) 115]
- Γ_K due only to $K^-N \rightarrow \pi Y$ (no $K^-NN \rightarrow YN$) decay modes
- Self consistency: deep K^- levels are narrower than shallow ones

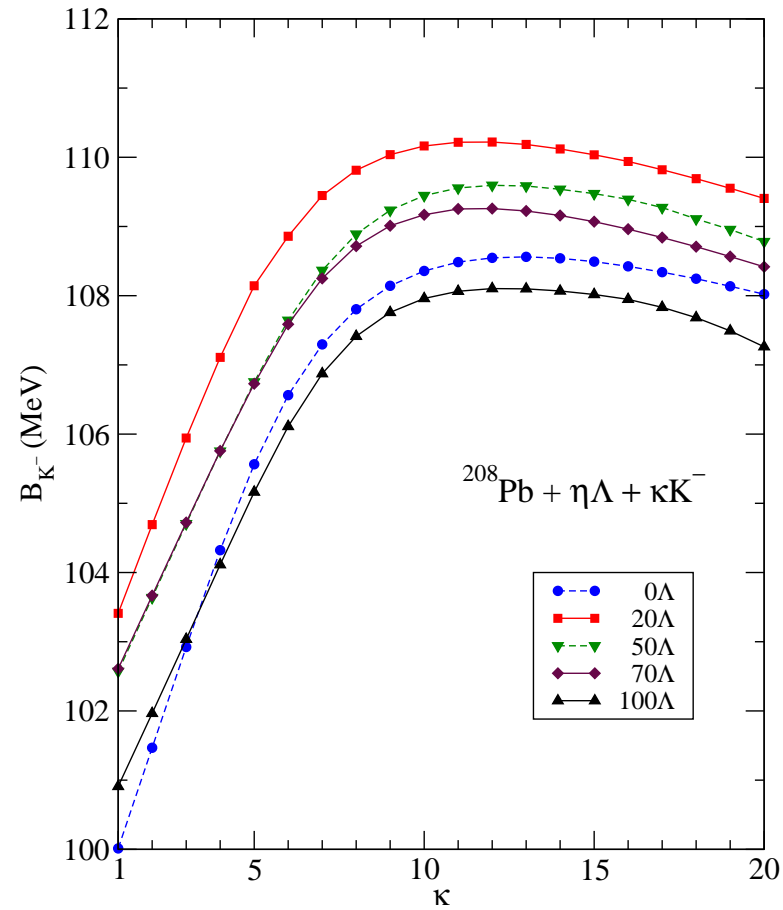


D. Gazda, E. Friedman, A. Gal, J. Mareš, PRC 77 (2008) 045206

Saturation of $B_{\bar{K}}(\kappa)$ in RMF for multi- K^- ^{40}Ca nuclei.

Vector-meson repulsion among \bar{K} mesons.

$B_{\bar{K}}(\kappa \rightarrow \infty) \ll (m_K + M_N - M_\Lambda) \approx 320 \text{ MeV}$.



D. Gazda, E. Friedman, A. Gal, J. Mareš, Phys. Rev C 80 (2009) 035205

Saturation of $B_{\bar{K}}(\kappa)$ in RMF for $^{208}\text{Pb} + \eta\Lambda + \kappa K^-$.

\bar{K} mesons do not replace hyperons in stable self-bound strange matter.

Summary

- Large widths, $\Gamma_{\bar{K}} > 50$ MeV, expected for single- \bar{K} quasibound nuclear states. Focus on light systems. K^-pp searches are underway in GSI and J-PARC.
- **Look for $(I = \frac{3}{2}, J^P = 2^+)$ $YN\pi$ dibaryon.**
- Major issues: (i) how deep is \bar{K} nuclear spectrum?
(ii) how big is $\Gamma(\bar{K}NN \rightarrow YN)$ w.r.t. $\Gamma(\bar{K}N \rightarrow \pi Y)$?
**Do K^-d atom (SIDDHARTA-II at DAΦNE)
& selective K^- atom measurements (JPARC?)**
- $B_{\bar{K}}$ saturates in multi- \bar{K} nuclei and hypernuclei.
 \bar{K} condensation is unlikely in self-bound matter.
- **Thanks to my collaborators N. Barnea,
A. Cieplý, E. Friedman, D. Gazda, J. Mareš**