# Inclusive production of $J/\psi$ and $\psi'$ mesons at the LHC

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> **Abstract.** We discuss the prompt production of  $J/\psi$  mesons in proton-proton collisions at the LHC within a NRQCD  $k_t$ -factorization approach using Kimber-Martin-Ryskin (KMR) unintegrated gluon distributions (UGDF). We include both direct color-singlet production  $(gg \rightarrow J/\psi g)$  as well as a feed-down from  $\chi_c \rightarrow J/\psi\gamma$  and  $\psi' \rightarrow J/\psiX$ . The production of the decaying mesons ( $\chi_c$  or  $\psi'$ ) is also calculated within NRQCD  $k_t$ factorization. The corresponding matrix elements for  $gg \rightarrow J/\psi$ ,  $gg \rightarrow \psi'$  and  $gg \rightarrow \chi_c$ include parameters of the nonrelativistic spatial wave functions of quarkonia at r = 0, which are taken from potential models from the literature. We get the ratio of the corresponding of the cross sections for  $\chi_c(2)$ -to- $\chi_c(1)$  much closer to experimental data than obtained in recent analyses. Differential distributions in rapidity of  $J/\psi$  and  $\psi'$  are calculated and compared to experimental data of the ALICE and LHCb collaborations. We discuss possible onset of gluon saturation effects at forward/backward rapidities. One can describe the experimental data for  $J/\psi$  production within model uncertainties with color-singlet component only. Therefore our theoretical results leave only a relatively small room for the color-octet contributions.

## 1 Introduction

For a long time there are discrepancies among authors about the production mechanism of  $J/\psi$  quarkonia in proton-proton and proton-antiproton collisions. Some authors think that the cross section is dominated by the color-octet contribution. Some authors believe that the color-singlet contribution dominates. The color-octet contribution cannot be calculated from first principle and is rather fitted to the experimental data. Different fits from the literature give different magnitudes of the color-octet contributions. Therefore we concentrate on the color-singlet contribution. In the present paper we wish to calculate the color-singlet contribution as well as possible in the NRQCD  $k_t$ -factorization and see how much room is left for the more difficult color-octet contribution. In the present approach we concentrate rather on small transverse momenta of  $J/\psi$  or  $\psi'$  relevant for ALICE and LHCb data [1– 5]. We expect that color-singlet contributions may dominate in this region of the phase space. Finally  $\psi'$  quarkonium also has a sizable branching fraction into  $J/\psi X$  [6]. Fortunately this contribution is much smaller than the direct one as will be discussed in [8]. It was considered recently in an almost identical approach in [9].

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**Figure 1.** The leading-order diagram for prompt  $J/\psi(\psi')$  meson production in the  $k_t$ -factorization approach.

# **2** Inclusive production of $J/\psi$ and $\psi'$ mesons in the NRQCD $k_t$ -factorization approach

The main color-singlet mechanism for the production of  $J/\psi$  and  $\psi'$  mesons is shown in Fig.1 (left panel). We restrict ourselves to the gluon-gluon fusion mechanism. In the NLO the differential cross section in the  $k_t$ -factorization can be written as:

$$\frac{d\sigma(pp \to J/\psi gX)}{dy_{J/\psi} dy_g d^2 p_{J/\psi,t} d^2 p_{g,t}} = \frac{1}{16\pi^2 \hat{s}^2} \int \frac{d^2 q_{1t}}{\pi} \frac{d^2 q_{2t}}{\pi} \overline{|\mathcal{M}_{g^*g^* \to J/\psi g}^{off-shell}|^2} \times \delta^2 \left(\vec{q}_{1t} + \vec{q}_{2t} - \vec{p}_{H,t} - \vec{p}_{g,t}\right) \mathcal{F}_g(x_1, q_{1t}^2, \mu_F^2) \mathcal{F}_g(x_2, q_{2t}^2, \mu_F^2) .$$
(1)

We calculate the dominant color-single  $gg \rightarrow J/\psi g$  contribution taking into account transverse momenta of initial gluons. The corresponding matrix element squared for the  $gg \rightarrow J/\psi g$  is

$$\left|\mathcal{M}_{gg \to J/\psi g}\right|^2 \propto \alpha_s^3 |R(0)|^2 \,. \tag{2}$$

The matrix element is taken from [10]. In our calculation we choose the scale of the running coupling constant as:

$$\alpha_s^3 \to \alpha_s(\mu_1^2)\alpha_s(\mu_2^2)\alpha_s(\mu_3^2) , \qquad (3)$$

where  $\mu_1^2 = max(q_{1t}^2, m_t^2), \mu_2^2 = max(q_{2t}^2, m_t^2)$  and  $\mu_3^2 = m_t^2$ , where here  $m_t$  is the  $J/\psi$  transverse mass. The factorization scale in the calculation was taken as  $\mu_F^2 = (m_t^2 + p_{t,g}^2)/2$ .

Similarly we calculate the P-wave  $\chi_c$  meson production. Here the lowest-order subprocess  $gg \rightarrow \chi_c$  is allowed by positive C-parity of  $\chi_c$  mesons.

In the  $k_t$ -factorization approach the leading-order cross section for the  $\chi_c$  meson production can be written as:

$$\sigma_{pp \to \chi_c} = \int dy d^2 p_t d^2 q_t \frac{1}{sx_1 x_2} \frac{1}{m_{t_{\chi_c}}^2} \overline{|\mathcal{M}_{g^*g^* \to \chi_c}|^2} \mathcal{F}_g(x_1, q_{1t}^2, \mu_F^2) \mathcal{F}_g(x_2, q_{2t}^2, \mu_F^2) / 4 , \qquad (4)$$

which can also be used to calculate rapidity and transverse momentum distributions of the  $\chi_c$  mesons. In the last equation  $\mathcal{F}_g$  are unintegrated gluon distributions and  $\sigma_{gg \to \chi_c}$  is  $gg \to \chi_c$  (off-shell) cross section. The situation is illustrated diagrammatically in Fig.1 (right panel).



**Figure 2.** Rapidity distribution of  $\psi'$  meson with KMR (left plots) and mixed UGDFs (KS and KMR, right plots). The ALICE data [4] are shown for comparison.

The matrix element squared for the  $gg \rightarrow \chi_c$  subprocess is

$$\left|\mathcal{M}_{gg \to \chi_c}\right|^2 \propto \alpha_s^2 |R'(0)|^2 \,. \tag{5}$$

We used the matrix element taken from the Kniehl, Vasin and Saleev paper [7].

For this subprocess the best choice for running coupling constant is:

$$\alpha_s^2 \to \alpha_s(\mu_1^2)\alpha_s(\mu_2^2) , \qquad (6)$$

where  $\mu_1^2 = max(q_{1t}^2, m_t^2)$  and  $\mu_2^2 = max(q_{2t}^2, m_t^2)$ . Above  $m_t$  is transverse mass of the  $\chi_c$  meson. The factorization scale for the  $\chi_c$  meson production is fixed as  $\mu_F^2 = m_t^2$ .

### 3 Results

In Fig.2 we show differential cross section in rapidity for  $\psi'$  production at 7 TeV. Our results are compared with ALICE experimental data [4]. In the left panel we present results for Kimber-Martin-Ryskin (KMR) UGDF and in the right panel for mixed Kimber-Martin-Ryskin (KMR) and Kutak-Stasto (KS) UGDFs. Because KMR alone overshoot experimental data for rapidity distribution the best solution is to take the KMR distribution for large x and KS for small x. For  $\psi'$  meson we have to include only the direct diagram so it's easy to compare our result with experimental data.

For  $J/\psi$  meson we have to include both diagrams. Below we present results for these two subprocesses. In Fig.3 we show rapidity distribution for direct  $J/\psi$  meson production. We present results for three different values of energy: W = 2.76 TeV (left), W = 7 TeV (middle) and W = 13 TeV (right). Our results are compared with ALICE and LHCb experimental data [1–5].

In Fig.4 we present results for three different values of energy: W = 2.76 TeV (left), W = 7 TeV (middle) and W = 13 TeV (right) panel. The dotted lines are for  $\chi_{c1}$  meson contribution, the dotdashed lines are for  $\chi_{c2}$  meson contributions and the solid lines are sum of these two components. The presented here results are calculated with mixed UGDFs (KMR and KS).

#### 4 Conclusion

We have calculated the color-singlet contribution in the NRQCD  $k_t$ -factorization and compared our results with ALICE and LHCb data. Our results in rapidity are almost consistent or even exceed



**Figure 3.** Rapidity distribution of  $J/\psi$  meson with KMR (upper plots) and mixed UGDFs (Kutak-Stasto and KMR). The ALICE and LHCb data points [1–5] are shown for comparison.



**Figure 4.** Rapidity distribution of  $\chi_c$  meson with mixed UGDFs (Kutak-Stasto and KMR). The ALICE and LHCb data points [1–5] for  $J/\psi$  are shown for comparison.

experimental data. Cross section strongly depends on UGDF and we think the best solution is to use mixed UGDFs (KMR-KS). In our approach only small room is left for color-octet contribution.

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