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## The $Y(4260)$ and $Y(4360)$ enhancements within coupled-channels

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## Introduction

Ideas about dynamical poles:

scalar mesons

Boglione, Penington, PRD **65**, 114010 (2002)

van Beveren, Rijken, Metzger, Dullemond, Rupp, Ribeiro, ZPC **30**, 615 (1986)

van Beveren, Rupp, IJTPGTNO **11**, 179 (2006) [arXiv:hep-ph/0605317]

open-charm axial mesons

van Beveren, Rupp, PRL **91**, 012003 (2003)

charmonium scalar

Gamermann, Oset, Strottman, and Vacas, PRD **76**, 074016 (2007)

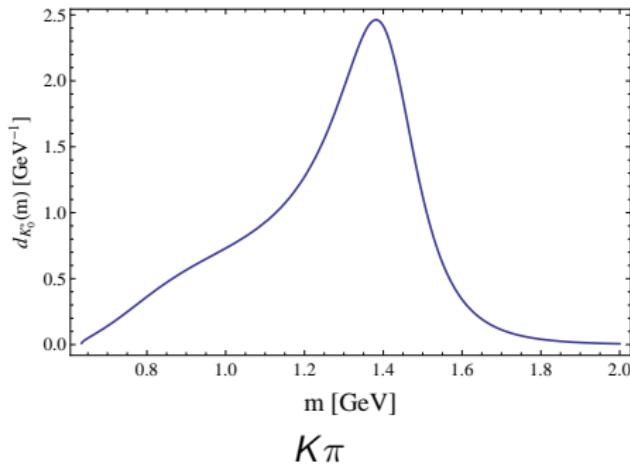
Within similar models to the one we present here

$a_0(980)$

Wolkanowski, Giacosa, Rischke, PRD **93**, 014002 (2016)

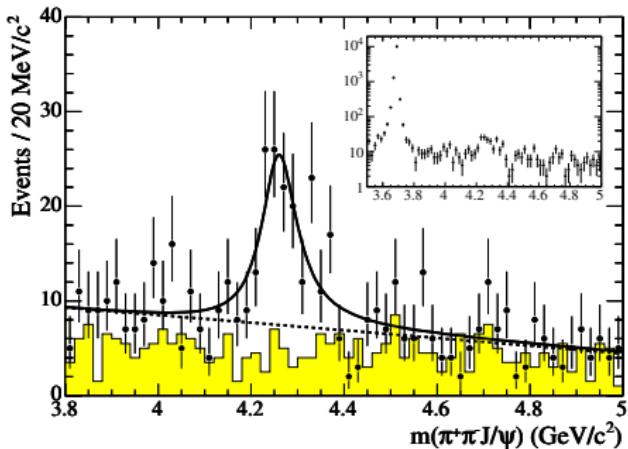
$K_0^*(800)$

Wolkanowski, Sołtysiak, Giacosa, NPB **909**, 418 (2016)



## Concerning the $Y(4260)$

A signal that has 1st been detected in

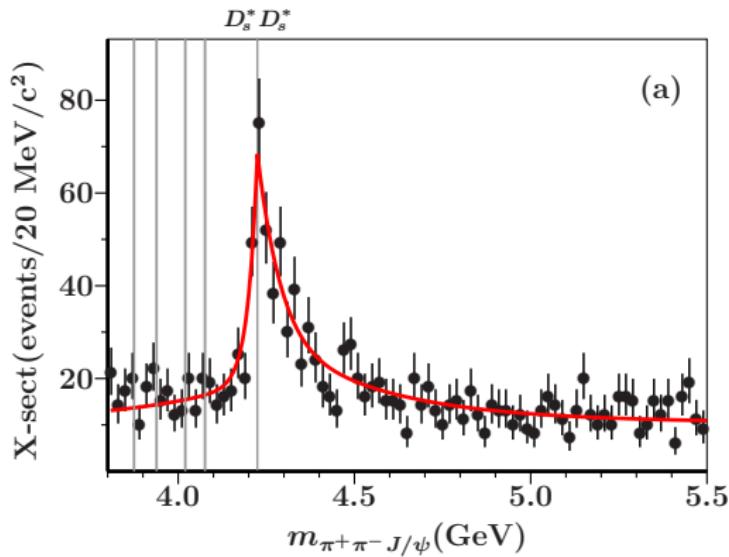


PRL95,142001 (2005) BABAR,  $e^+e^- \rightarrow J/\psi\pi^+\pi^-$ .

$M \sim 4.26 \text{ GeV}$ ,  $\Gamma = 50 - 90 \text{ MeV}$

yet showing no decays to any of the open OZI-allowed decay channels!

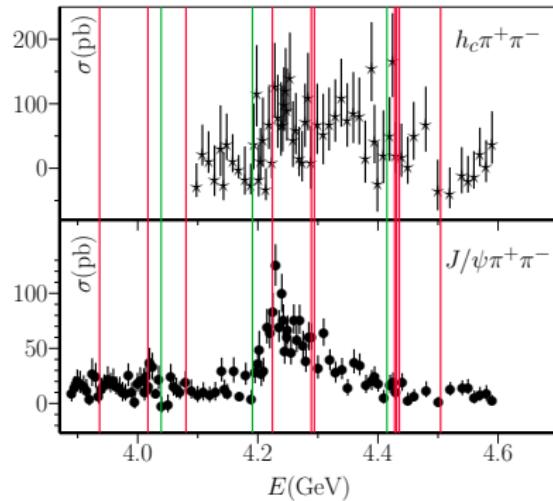
There is the idea that such enhancement might not be a true resonance



van Beveren, Rupp, PRL **105**, 102001 (2010)

van Beveren, Rupp, PRD **79**, 111501(R) (2009)

$D_s D_s$ ,  $D^* D^*$ ,  $D_s D_s^*$ ,  $D_s^* D_s^*$ ,  $DD_1$ ,  $D^* D_1$ ,  $D_s D_{1s}$



$\psi(4040)$ ,  $\psi(4160)$ ,  $\psi(4415)$

Data: BESIII PRL118,092001(2017); PRL118,092002(2017)

## Recent ideas about the $Y(4260)$ and the $Y(4390)$

- Possible identification of  $Y$  states with  $\psi$  states through coupling to decay channels in a “molecular” manner
- Interference between  $\psi(4160)$  and  $\psi(4415)$  states

Lu, Anwar, Zou, PRD **96**, 114022 (2017)

Chen, Liu, Matsuki, EPJC **78**, 136 (2018)

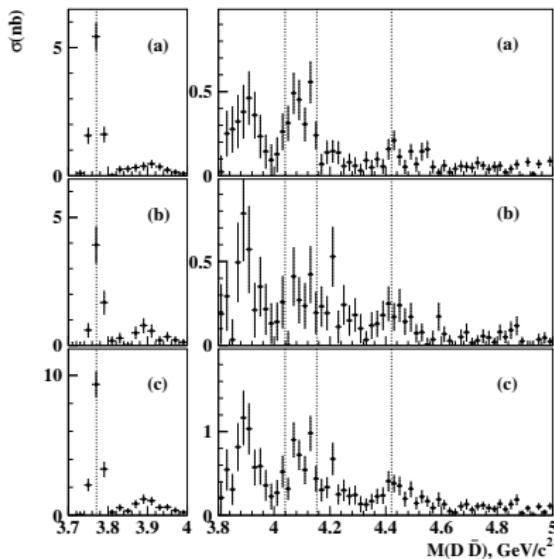
Zhang, Zhang, PRD **96**, 054008 (2017)

He, Chen, EPJC **77**, 398 (2017)

Wang, CPC **41**, 083103 (2017)

On the other hand, the determination of the  $\psi$  masses is not always easy to disentangle...

$$\psi(3770), \psi(4040), \psi(4160), \psi(4415)$$



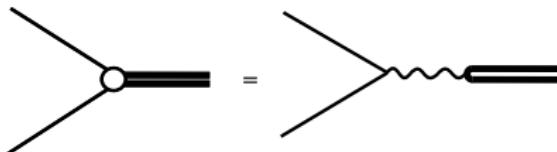
BELLE, PRD**77**,011103(R)(2008)  $e^+e^- \rightarrow D\bar{D}$

## An effective Lagrangian model

production experiment → interaction region → final hadrons



annihilation and production vertex



meson-meson loops  $\Leftrightarrow$  coupled-channels



## The case of the $\psi(3770)$ with $D^0\bar{D}^0$ and $D^+D^-$ loops

S. Coito, F. Giacosa, arXiv:1712.00969

a Lagrangian density for a  $V \rightarrow PP$

$$\mathcal{L}_{\psi D_i \bar{D}_i} = ig_{\psi D \bar{D}} \psi_\mu \sum_i^2 \left( \partial^\mu D_i \bar{D}_i - \partial^\mu \bar{D}_i D_i \right)$$

Vertex decay width and amplitude

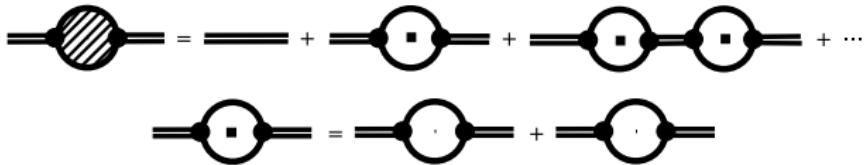
$$\Gamma_{\psi \rightarrow D_i \bar{D}_i}(s) = \frac{k_i(s, m_{D_i})}{8\pi s} |\mathcal{M}_{\psi \rightarrow D_i \bar{D}_i}|^2$$

$$|\mathcal{M}_{\psi \rightarrow D_i \bar{D}_i}|^2 = g_{\psi D \bar{D}}^2 \frac{4}{3} k_i^2(s, m_{D_i}) f_\Lambda^2(s)$$

Form-factor

$$f_\Lambda(\mathbf{q}_i) = e^{-\mathbf{q}_i^2/\Lambda^2}$$

Building a propagator



$$G_{\mu\nu}(p) = \frac{1}{p^2 - m_\psi^2 + i\varepsilon} \left( -g_{\mu\nu} + \frac{p_\mu p_\nu}{m_\psi^2} \right)$$

$$\Delta_{\mu\nu}(p) = G_{\mu\nu}(p) + G_{\mu\mu'}(p)\Pi_{\mu'\nu'}(p)G_{\nu'\nu}(p) + \dots ,$$

$$\Pi_{\mu\nu}(p) = g_{\psi D\bar{D}}^2 \sum_i \Pi_{i\mu\nu}(p, m_{D_i})$$

$$\Pi(s) = \frac{1}{3} \left( -g^{\mu\nu} + \frac{p^\mu p^\nu}{p^2} \right) \Pi_{\mu\nu}(p) = g_{\psi D\bar{D}}^2 \sum_i \Pi_i(s, m_{D_i})$$

$$\Delta(s) = \frac{1}{s - m_\psi^2 + \Pi(s)}$$

For N channels

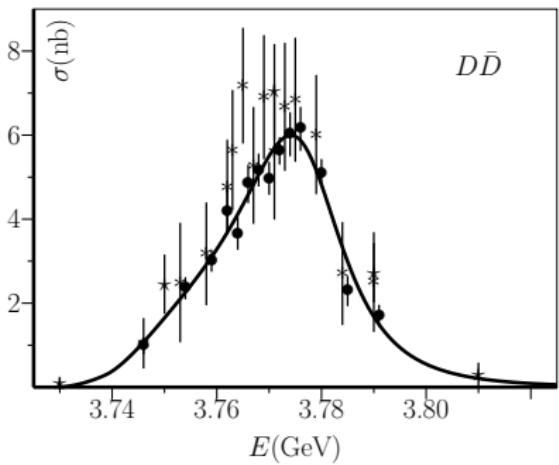
$$\Pi(s) = \sum_j^N \left( \Omega_j(s) + i\sqrt{s}\Gamma_j(s) \right), \quad \Omega, \Gamma \in \Re,$$

$$\Omega_j(s, m_1, m_2) = \frac{PP}{\pi} \int_{s_{th}}^{\infty} \frac{\sqrt{s}\Gamma_j(s', m_1, m_2)}{s' - s} \, ds'$$

The unitarized spectral function is given by

$$\begin{aligned} d_\psi(E) &= -\frac{2E}{\pi} \operatorname{Im} \Delta(E) \\ &= \frac{2E^2}{\pi} \frac{\sum_j \Gamma_j(E^2)}{[E^2 - m_\psi^2 + \operatorname{Re} \Pi(E^2)]^2 + [\operatorname{Im} \Pi(E^2)]^2} \end{aligned}$$

## The $\psi(3770)$ cross section



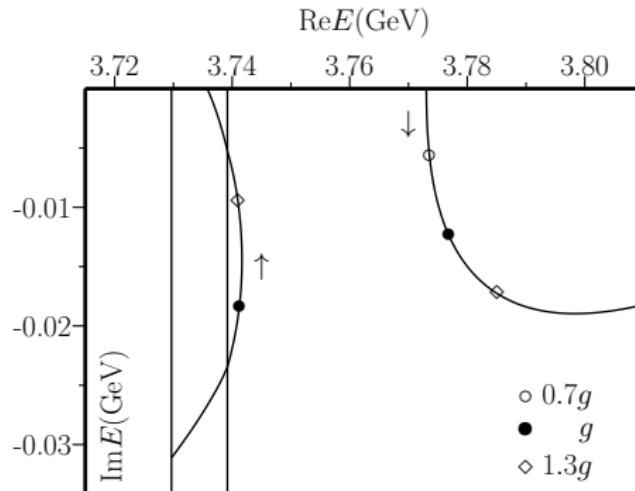
Data: BES PLB **668**,263 (2008); BES PRL **97**,121801 (2006)

Fit parameters:  $m_\psi$ :  $3773.05 \pm 0.95$  MeV

$\Lambda$ :  $272.55 \pm 1.17$  MeV

$\chi^2/d.o.f$  - 0.86

## Pole trajectories

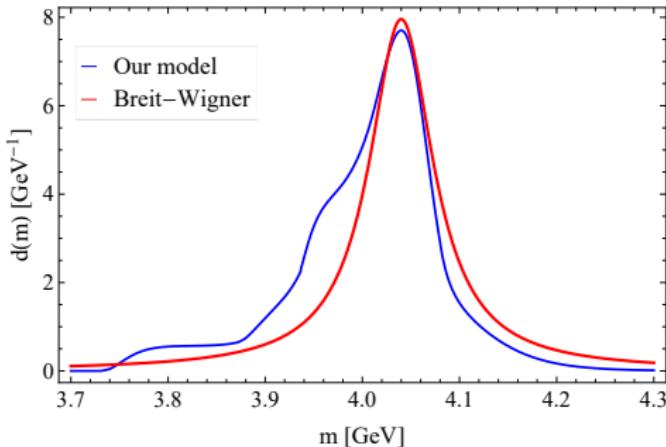


- $3741.2 - i18.5 \text{ MeV}$      $3776.8 - i12.3 \text{ MeV}$
- -  $3773.5 - i5.5 \text{ MeV}$
- ◊  $3741.0 - i9.5 \text{ MeV}$      $3784.9 - i17.2 \text{ MeV}$

## The $\psi(4040)$ and the $Y(4008)$

cf. poster of M. Piotrowska (collab. with F. Giacosa and P. Kovacs)

Total spectral function with channels  $DD$ ,  $DD^*$ , and  $D^*D^*$



Poles around:  $\psi(4040)$  :  $4053 - i39$  MeV  
 $Y(4008)$  :  $3934 - i30$  MeV

## The $\psi(4160)$ and the $Y(4260)\dots$

cf. S. Coito, PoS Hadron2017 (2018) 030.

Coupled-channels (through the loops):

below  $\psi(4160)$  threshold:  $DD \ DD^* \ D^*D^* \ D_sD_s \ D_sD_s^*$

above  $\psi(4160)$  threshold:  $D_s^*D_s^* \ DD_1 \ DD_1'$  (not seen yet)

suppressed channel, but seen in the experiment:  $J/\psi f_0(980)$

## ... and the $\psi(4415)$ and $Y(4390)$

below  $\psi(4415)$  threshold:  $DD \ DD^* \ D^*D^* \ D_sD_s \ D_sD_s^* \ D_s^*D_s^* \ DD_1 \ DD_1'$

above  $\psi(4415)$  threshold:  $D^*D_1 \ D^*D_1' \ D_sD_{s1} \ D_sD_{s1}'$

suppressed channel, but seen in the experiment:  $J/\psi f_0(980)$

**Interactions:**  $V \rightarrow PP, PV, VV, PA, VS$

$$\textcolor{violet}{PP} : \mathcal{L}_I = ig_{VPP} \psi_\mu \left( \partial^\mu D_1 \bar{D}_2 - \partial^\mu \bar{D}_2 D_1 \right) + h.c.$$

$$\textcolor{violet}{PV} : \mathcal{L}_I = ig_{VPV} \tilde{\Psi}_{\mu\nu} D \bar{D}^{*\mu\nu} + h.c. ,$$

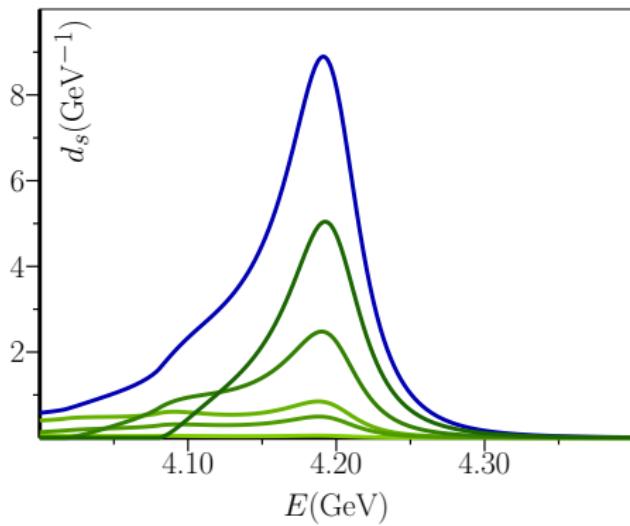
$$\tilde{\Psi}_{\mu\nu} = \frac{1}{2} \epsilon_{\mu\nu\alpha\beta} \Psi^{\alpha\beta} , \quad \Psi^{\alpha\beta} = \partial^\alpha \psi^\beta - \partial^\beta \psi^\alpha , \quad D^{*\mu\nu} = \partial^\mu D^{*\nu} - \partial^\nu D^{*\mu}$$

$$\textcolor{violet}{VV} : \mathcal{L}_I = \frac{i}{2} g_{VVA} \Psi_{\mu\nu} \left( D_1^{*\mu} \bar{D}_2^{*\nu} - D_1^{*\nu} \bar{D}_2^{*\mu} \right) + h.c., \quad \Psi_{\mu\nu} = \partial_\mu \psi_\nu - \partial_\nu \psi_\mu .$$

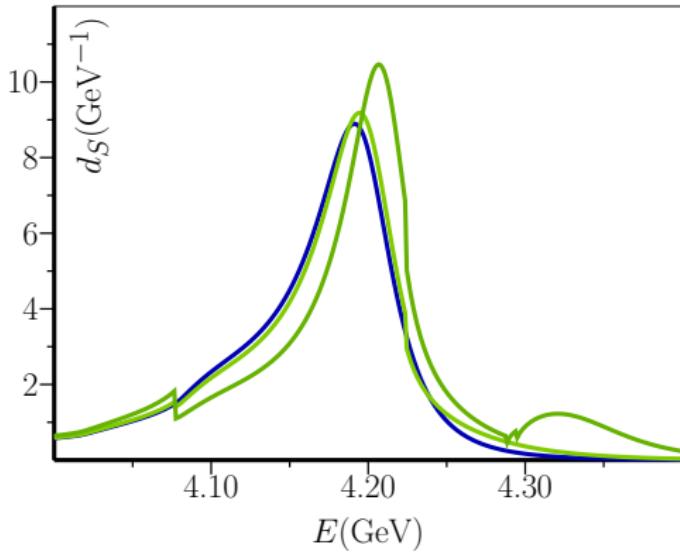
$$\textcolor{violet}{PA} : \mathcal{L}_I = ig_{\psi DD_1} \psi_\mu D \bar{D}_1^\mu + h.c.$$

$$\textcolor{violet}{SV} : \mathcal{L}_I = g \psi_\mu J/\psi^\mu f_0(980)$$

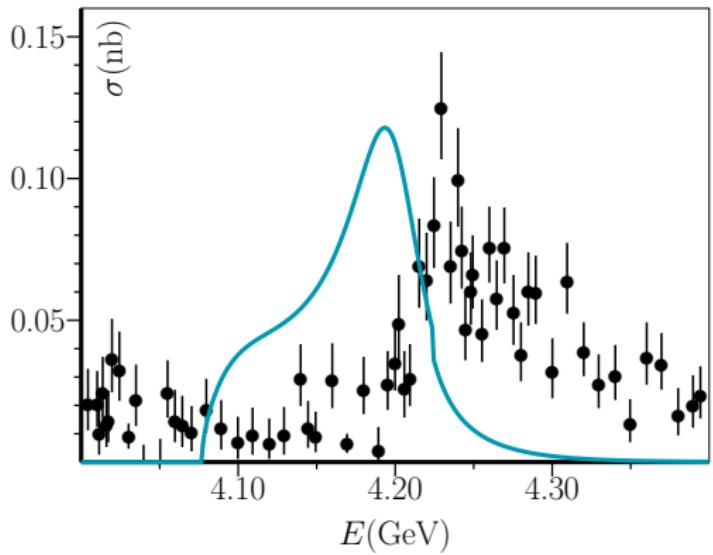
## Line-Shape for the $\psi(4160)$



5 channels:  $DD$   $DD^*$   $D^*D^*$   $D_sD_s$   $D_sD_s^*$



5 channels,  $+D_s^* D_s^*$ , and  $+DD_1 DD'_1$  (with an arbitrary coupling)



Channel  $J/\psi f_0(980)$  compared to  $J/\psi\pi\pi$  data

## Summary and Conclusions

- The  $\psi$  and  $Y$  spectra above  $D\bar{D}$  threshold are very intriguing as there is a big quantum mixing
- Loops  $\Leftrightarrow$  coupled-channels are important and simple Breit-Wigner fits are too naive
- We show results of an effective Lagrangian approach for the  $\psi(3770)$ ,  $\psi(4040)$  and  $\psi(4160)$  interfering with their respective open-decay channels.
- In the presented results the  $Y(4260)$  do not emerge as a companion pole of the  $\psi(4160)$ , but a full study of the interferences including closed-channels and mixing among the different  $\psi$  is still undergoing.

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