

Triangle singularity in the reaction $\gamma p \rightarrow p \pi^0 \eta ??$

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II. Physikalisches Institut

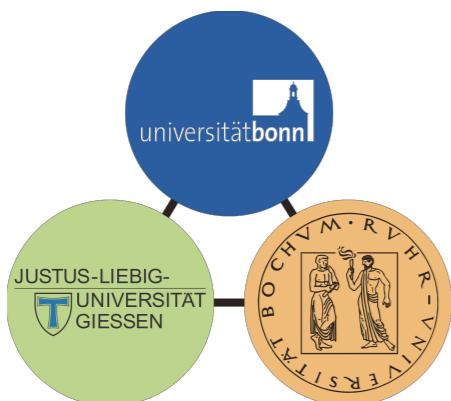


for the CBELSA/TAPS collaboration

in contact with V. Debastiani, E. Oset and S. Sakai // V. Nikonov, A. Sarantsev // B. Kubis

- ◆ de-excitation of higher lying nucleon resonances via multiple meson emission
- ◆ unexplained structures in Dalitz plots
- ◆ experimental evidence for a triangle singularity
- ◆ in the $\gamma p \rightarrow p \pi^0 \eta$ reaction ??
- ◆ summary and outlook

*funded by the DFG within SFB/TR16

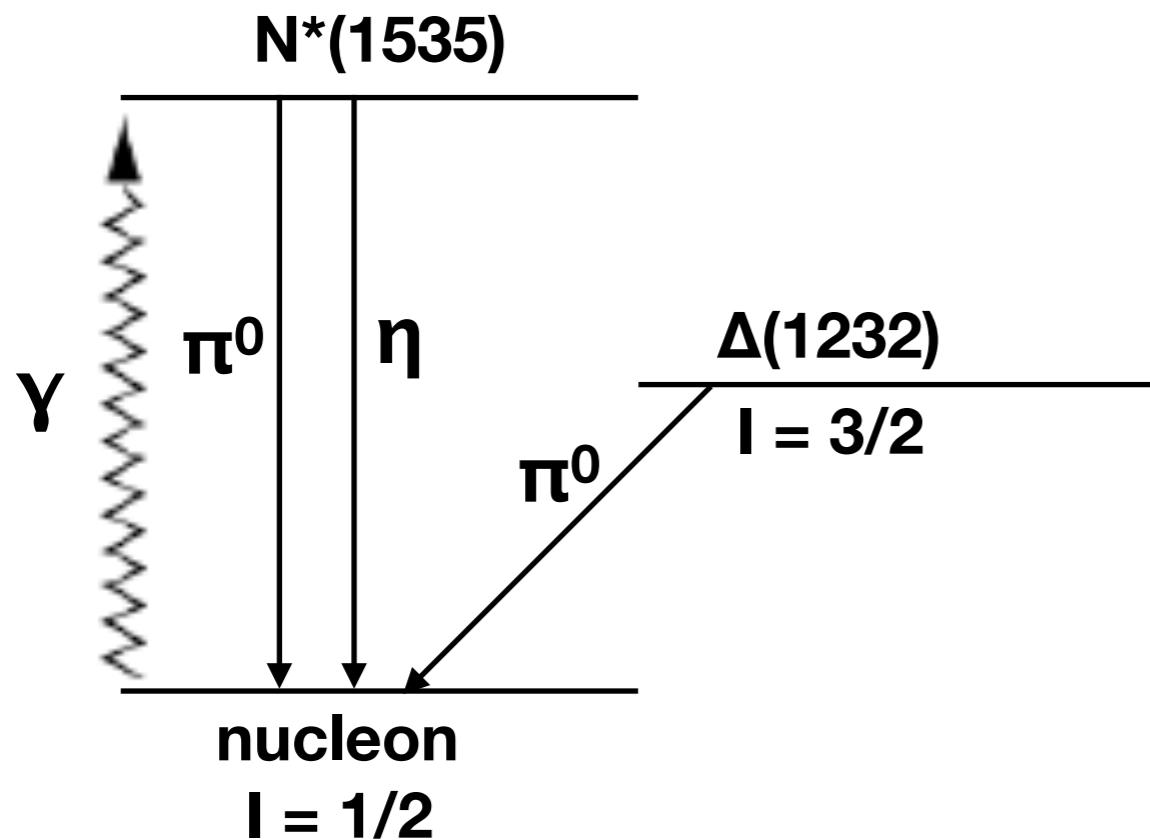


Meson 2018
June 7-12, Cracow, Poland

HIC | FAIR
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decay of higher nucleon resonances

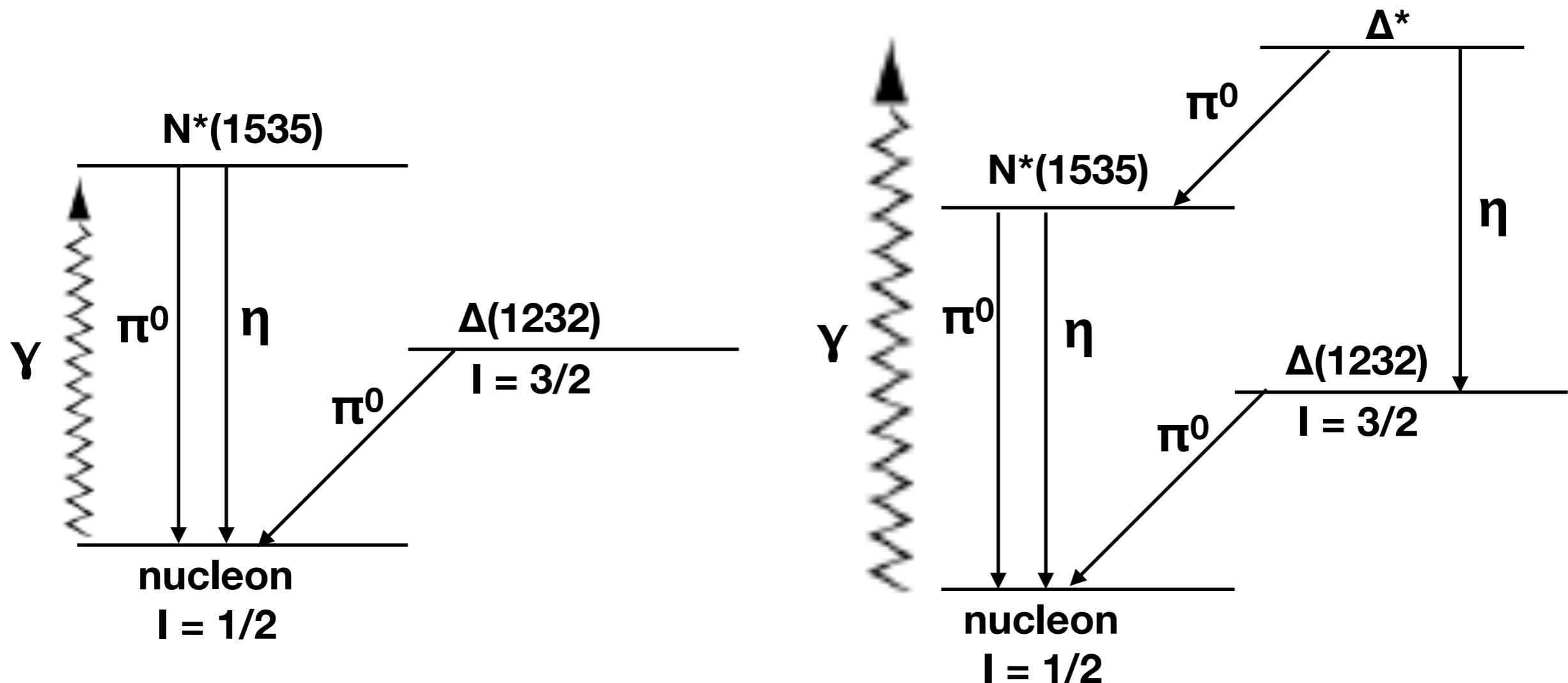
- low lying resonances like $\Delta(1232)$ and $S_{11}(1535)$ well studied



de-excitation by
single meson emission
final states: $p\pi^0, p\eta \rightarrow p 2\gamma$

decay of higher nucleon resonances

- low lying resonances like $\Delta(1232)$ and $S_{11}(1535)$ well studied
- knowledge of higher lying resonances still to be improved

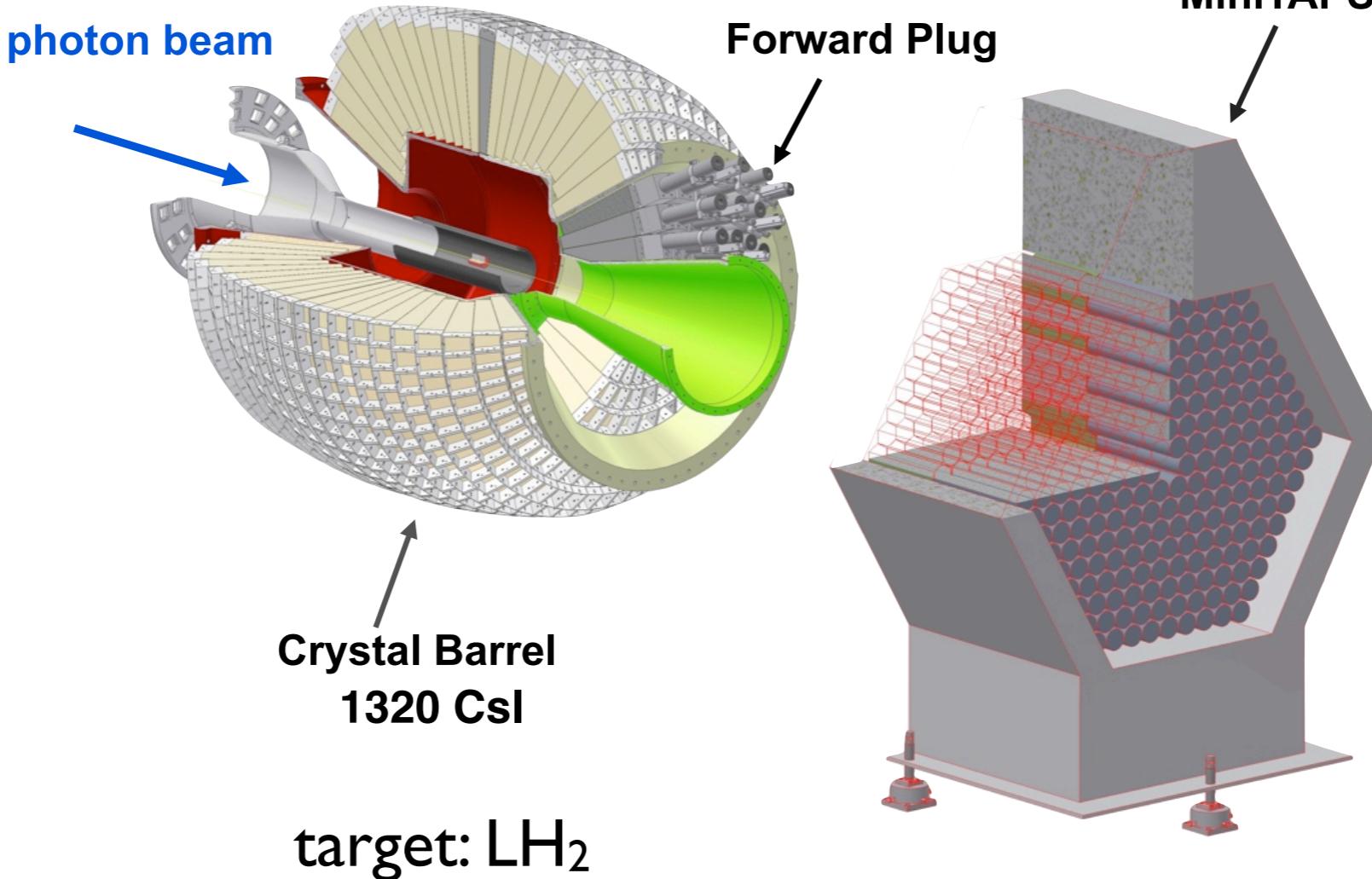


**de-excitation by
single meson emission**
final states: $p\pi^0, p\eta \rightarrow p 2\gamma$

**de-excitation by
meson decay chains**
final states: $p\pi^0\pi^0, p\pi^0\eta \rightarrow p 4\gamma$

CBELSA/TAPS Experiment (Bonn)

$E_\gamma = 1.2 - 2.9 \text{ GeV}$



4π photon detector: ideally suited for identification of multi-photon final states

$\gamma p \rightarrow p \eta \pi^0 \rightarrow p 4\gamma \text{ BR } 38.9\%$

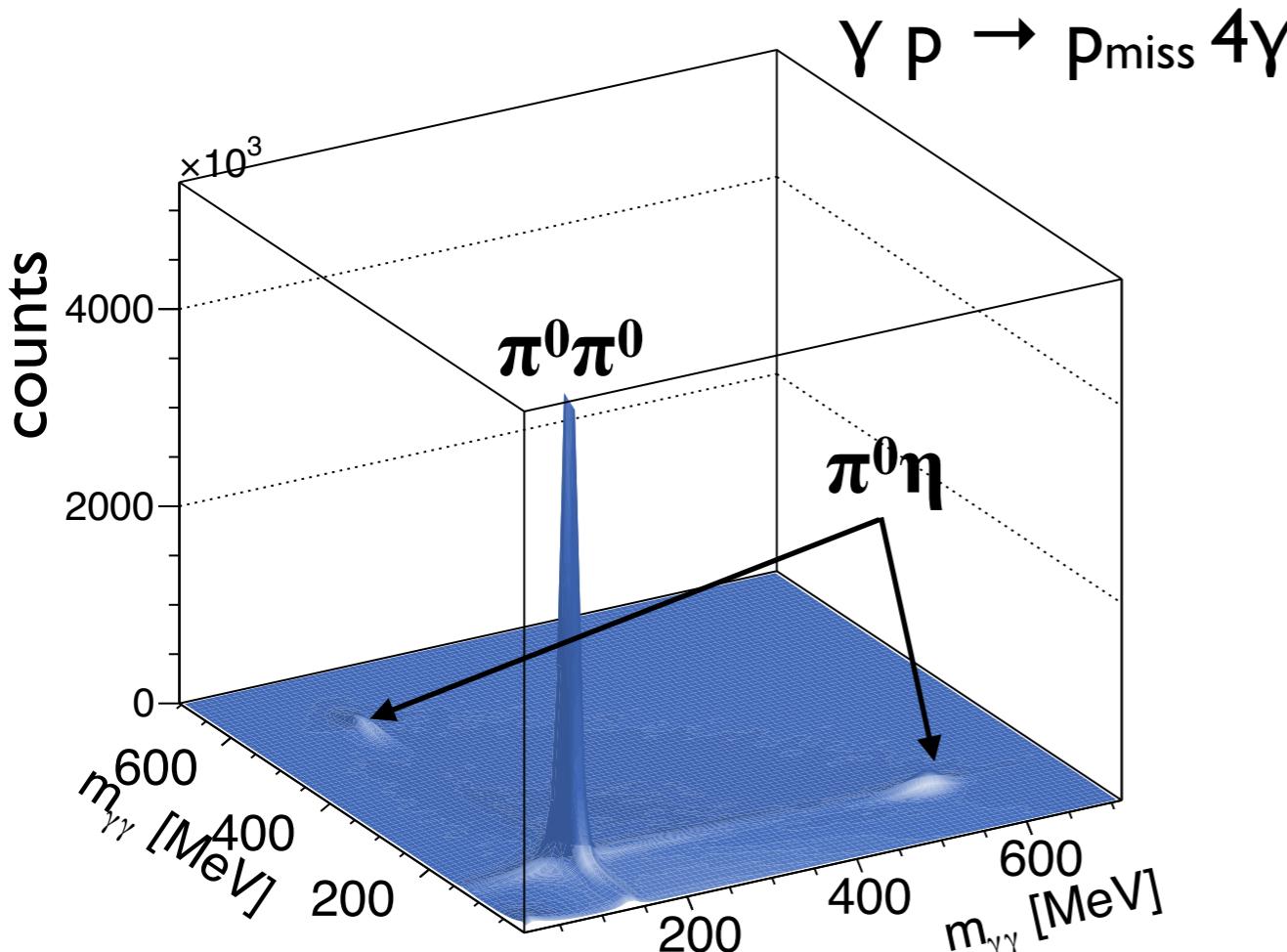
$\gamma p \rightarrow p \pi^0 \pi^0 \rightarrow p 4\gamma \text{ BR } 97.6\% \text{ dominant !!}$

Data analysis: identification of $\gamma p \rightarrow p \pi^0 \eta$

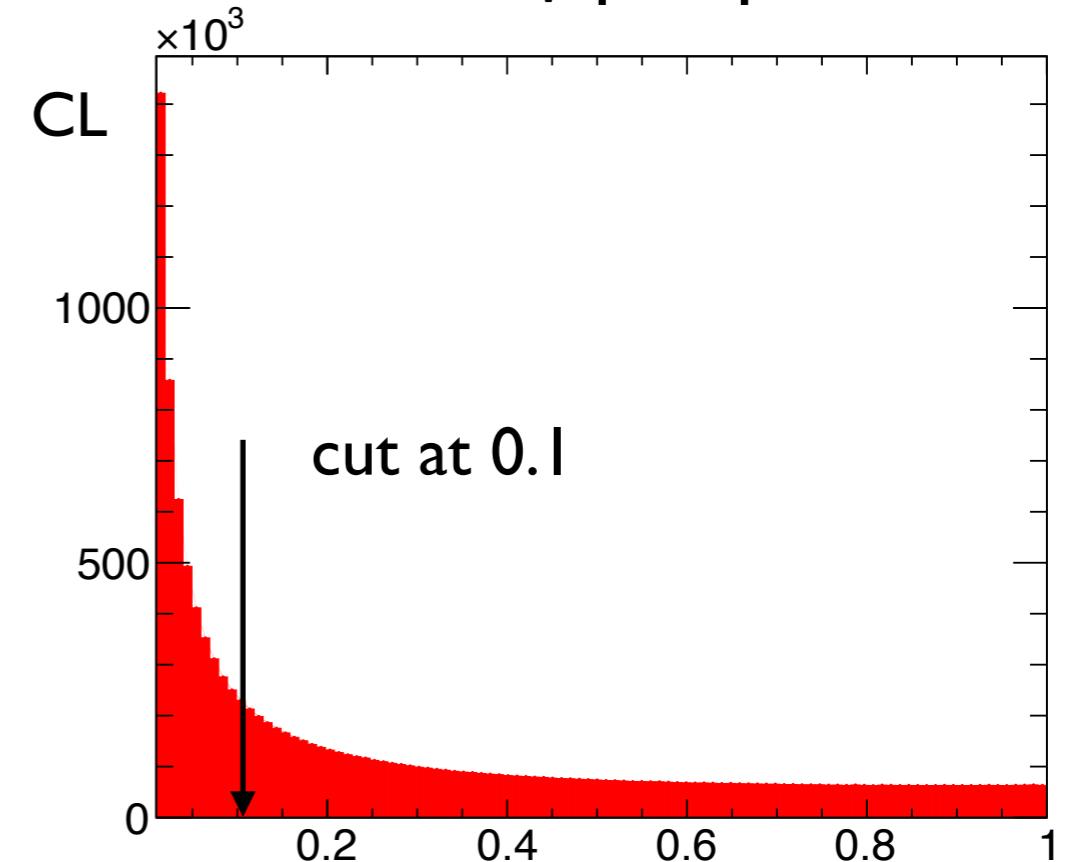
- meson reconstruction in the decay channel: $\pi^0 \rightarrow \gamma\gamma$ and $\eta \rightarrow \gamma\gamma$

4 photons in the final states

$4 \cdot 10^8 \pi^0\pi^0; 2 \cdot 10^7 \pi^0\eta$



- kinematic fit with hypothesis:
 $\gamma p \rightarrow p_{\text{miss}} 4\gamma; \gamma p \rightarrow p_{\text{miss}} \pi^0\eta$
anticut: $\gamma p \rightarrow p_{\text{miss}} \pi^0\pi^0$



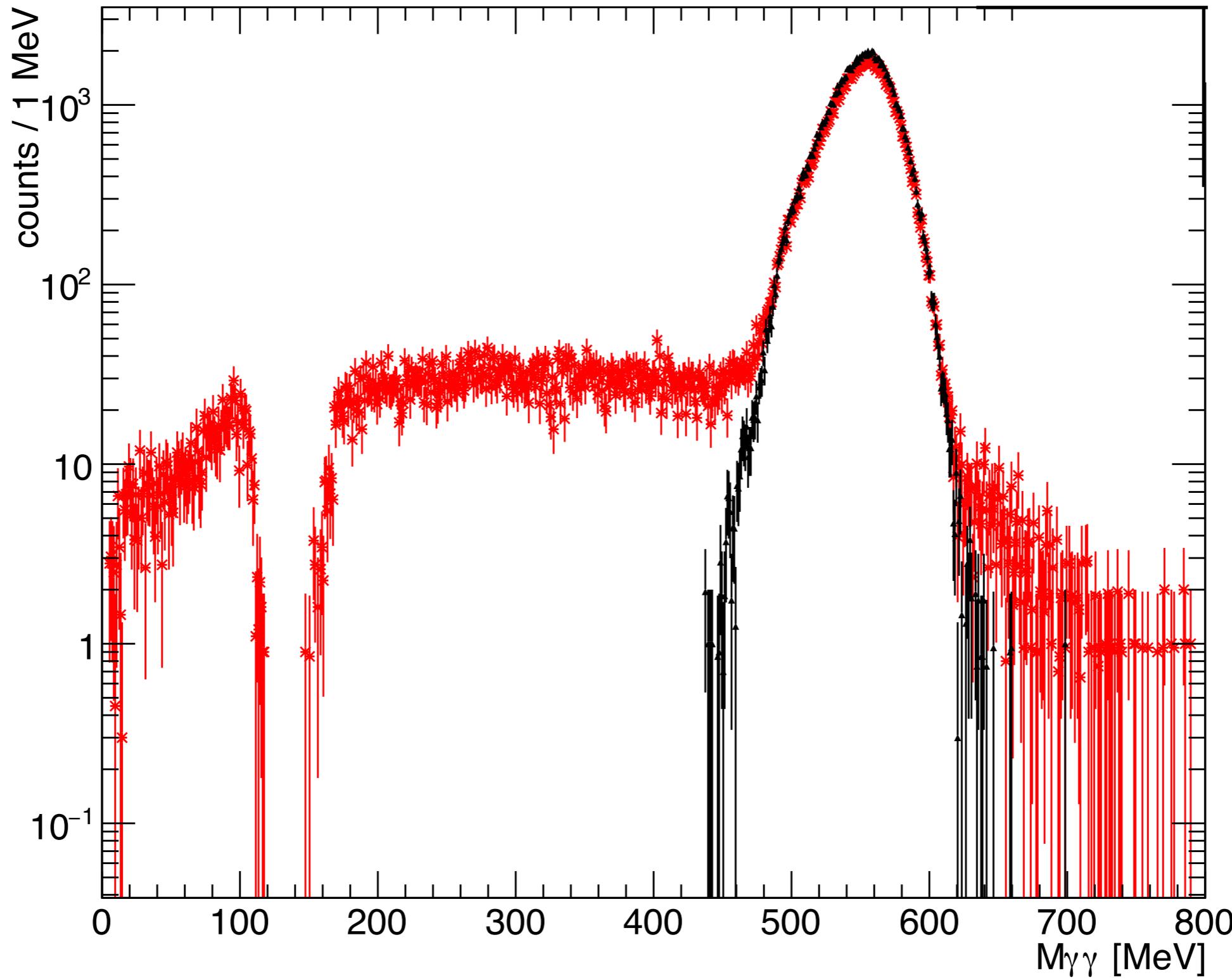
proton treated as missing particle

- coplanarity cut: $\Delta\Phi = \Phi_{4\gamma} - \Phi_p = 180^\circ \pm 9$
- polar angle difference: $\Delta\theta = \theta_p^{\text{meas}} - \theta_p^{\text{miss}} = \pm 8$

selection of $\gamma p \rightarrow p \pi^0 \eta$ events

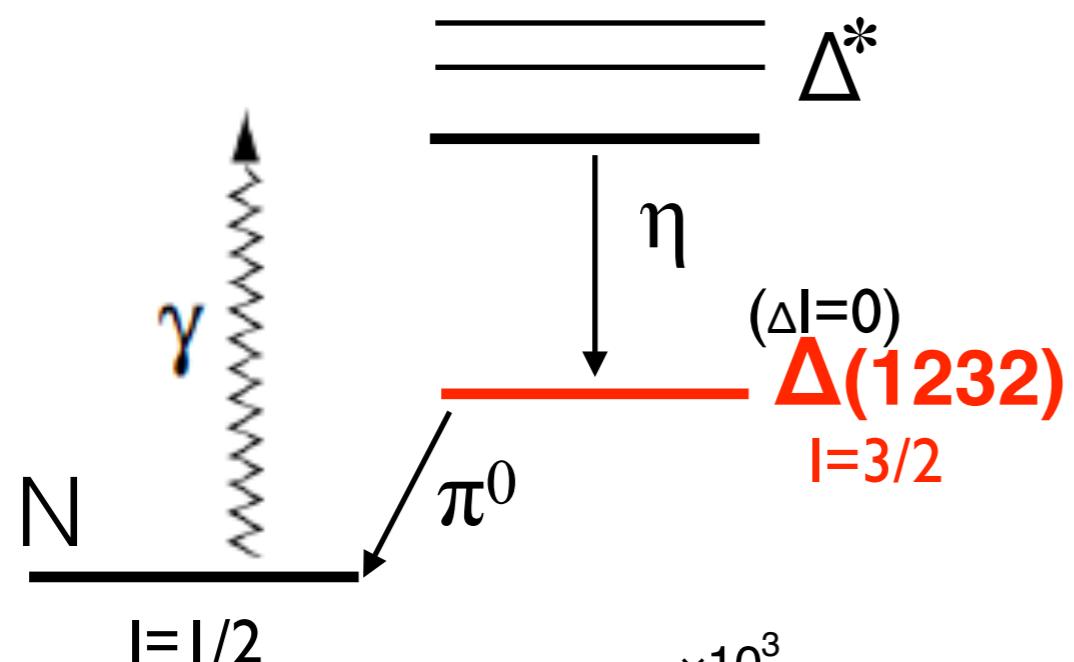
all $\gamma p \rightarrow p \pi^0 \pi^0$ events with $CL > 0.01$ removed

events meeting the $\gamma p \rightarrow p \pi^0 \gamma\gamma$ hypothesis with $CL > 0.1$

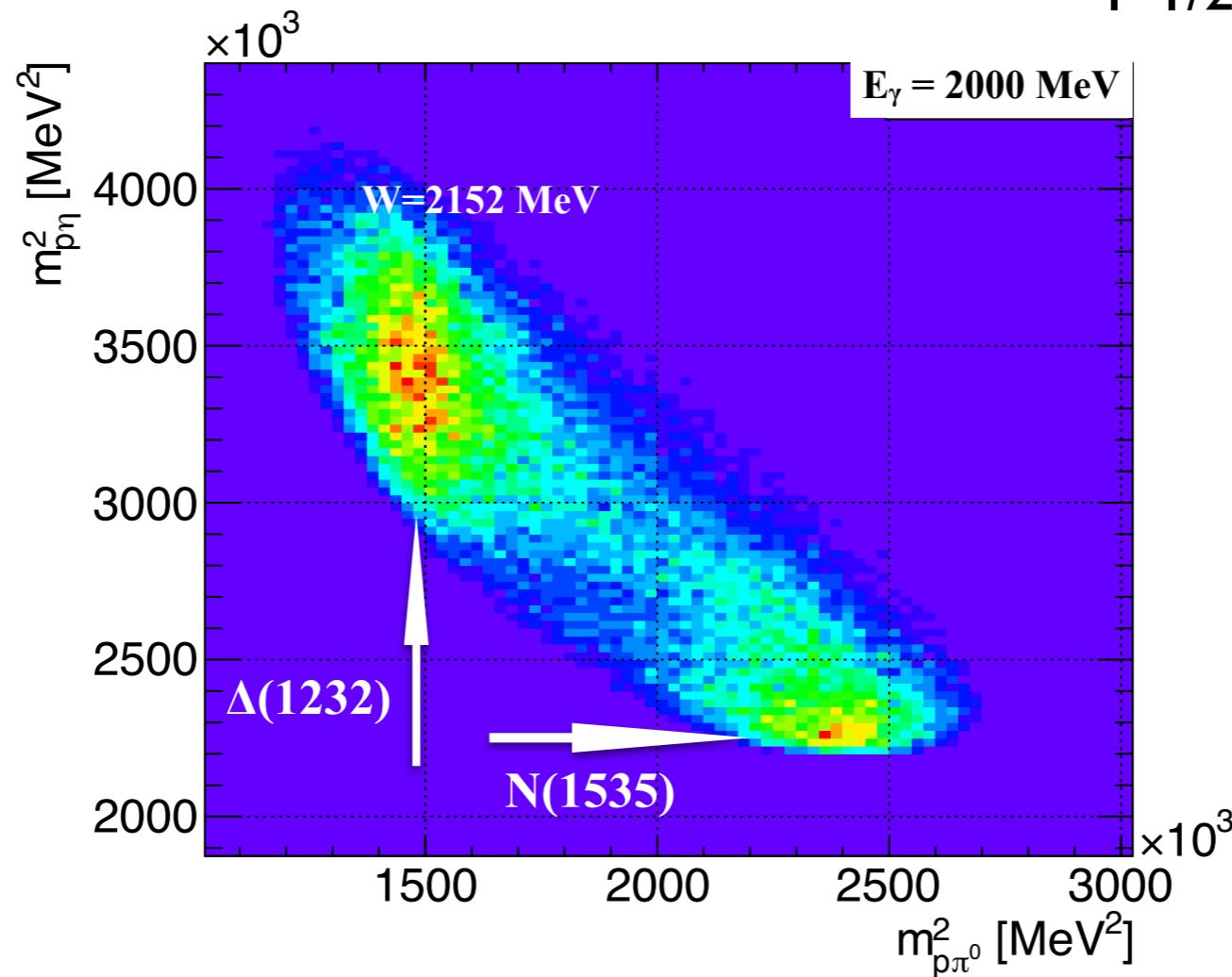
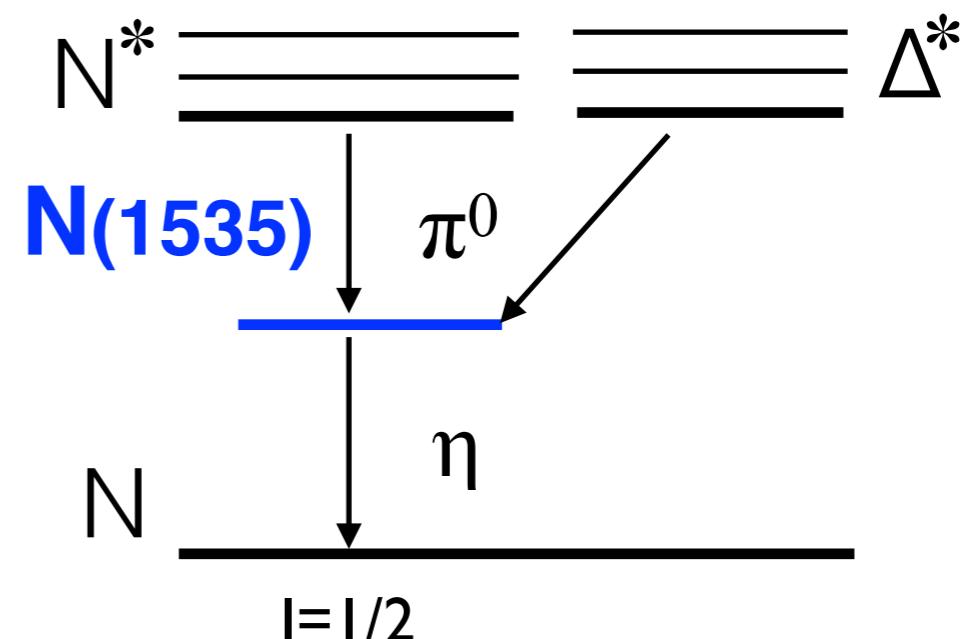


$\gamma p \rightarrow p \pi^0 \eta$: cascade decays

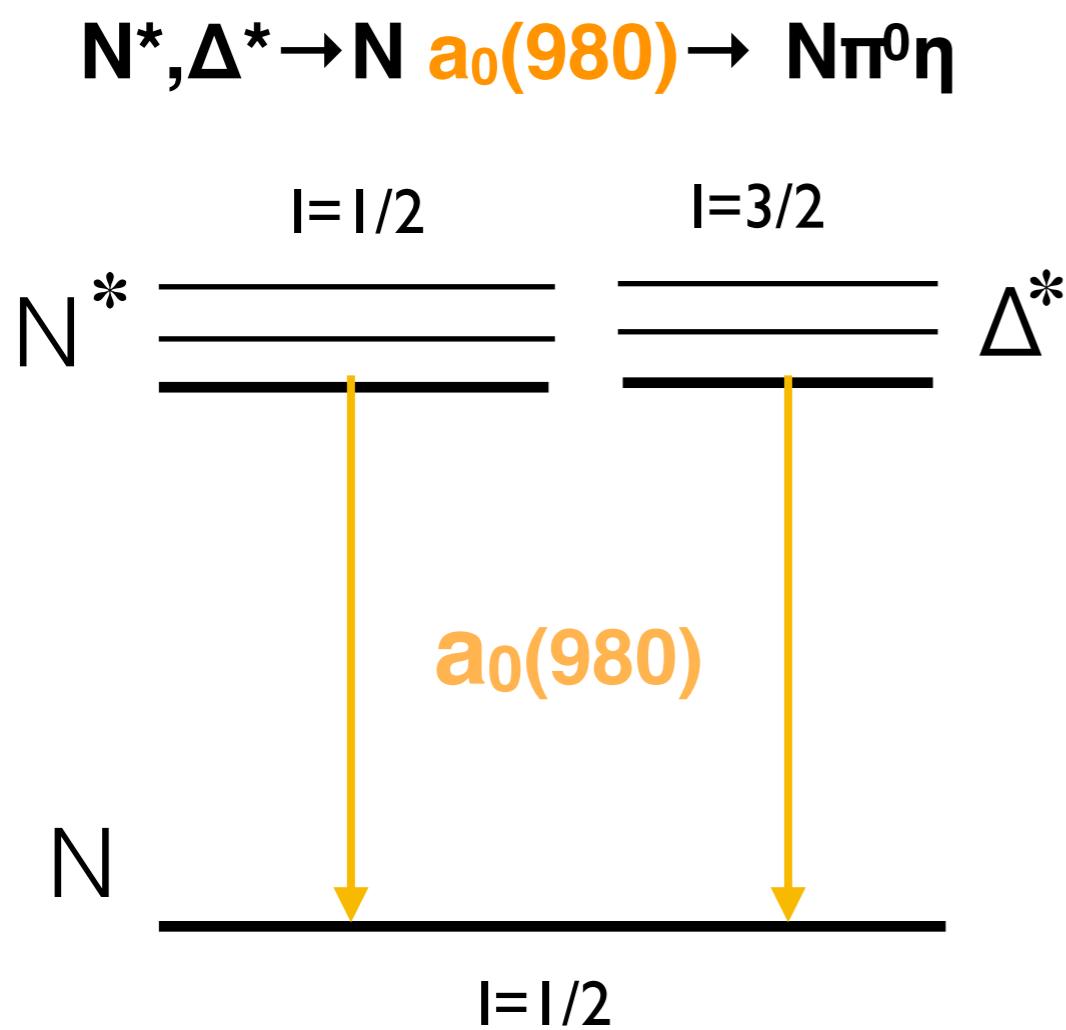
$\Delta^* \rightarrow \Delta(1232) \eta \rightarrow N \pi^0 \eta$;



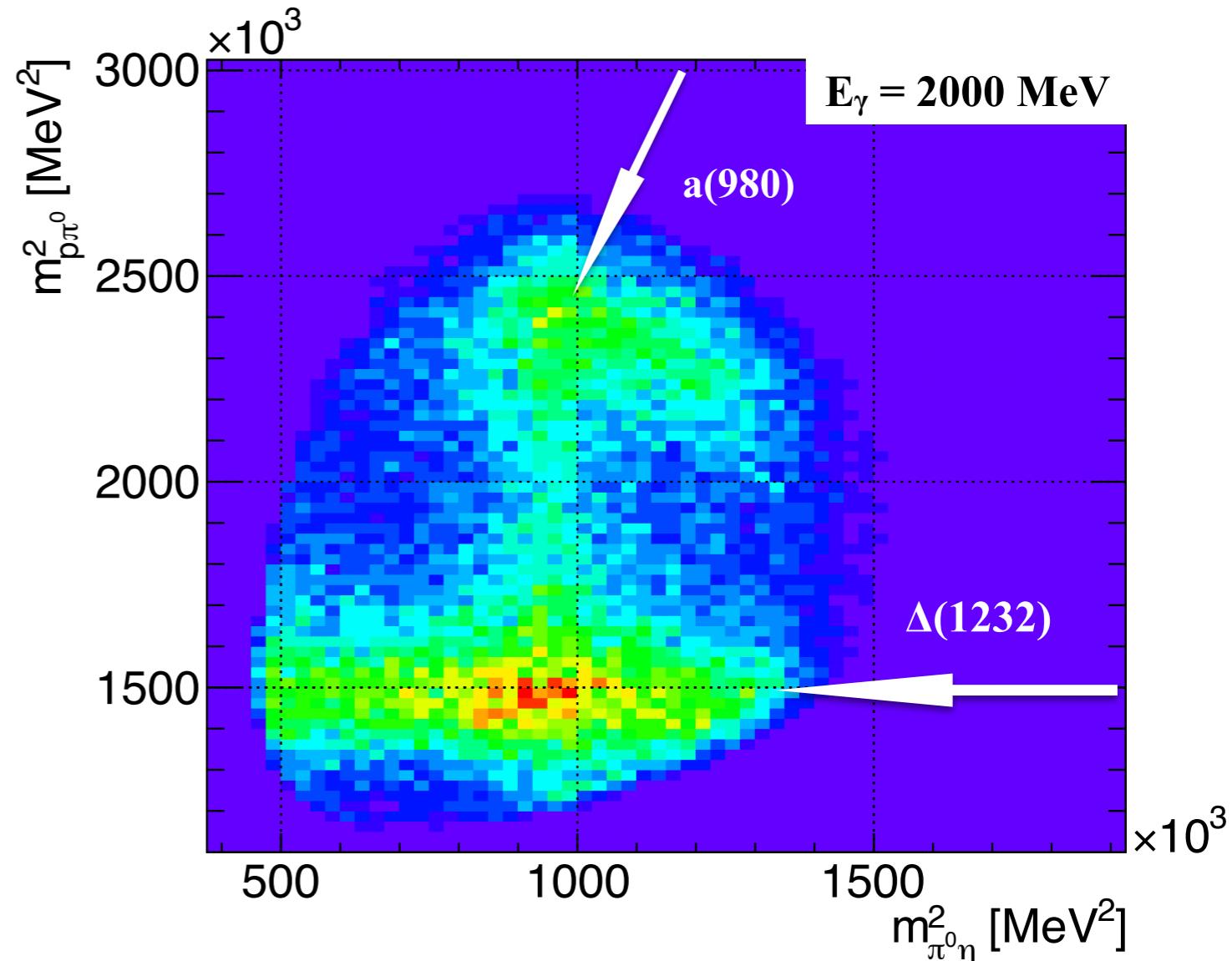
$N^*, \Delta^* \rightarrow N(1535) \pi^0 \rightarrow N \pi^0 \eta$;



$\gamma p \rightarrow p \pi^0 \eta$: direct decay via $a_0(980)$

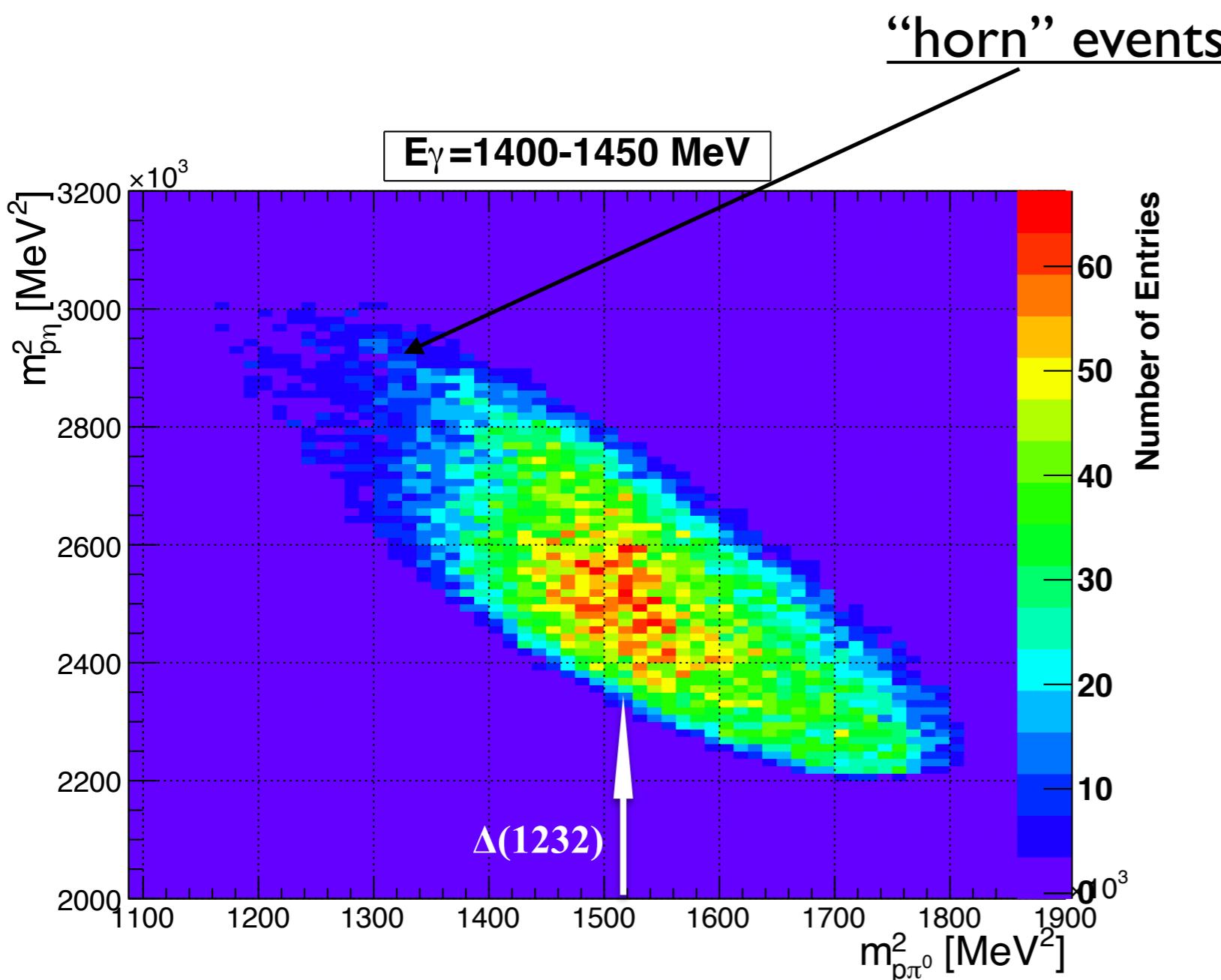


$$a_0(980) \rightarrow \pi^0 \eta \rightarrow 4\gamma$$

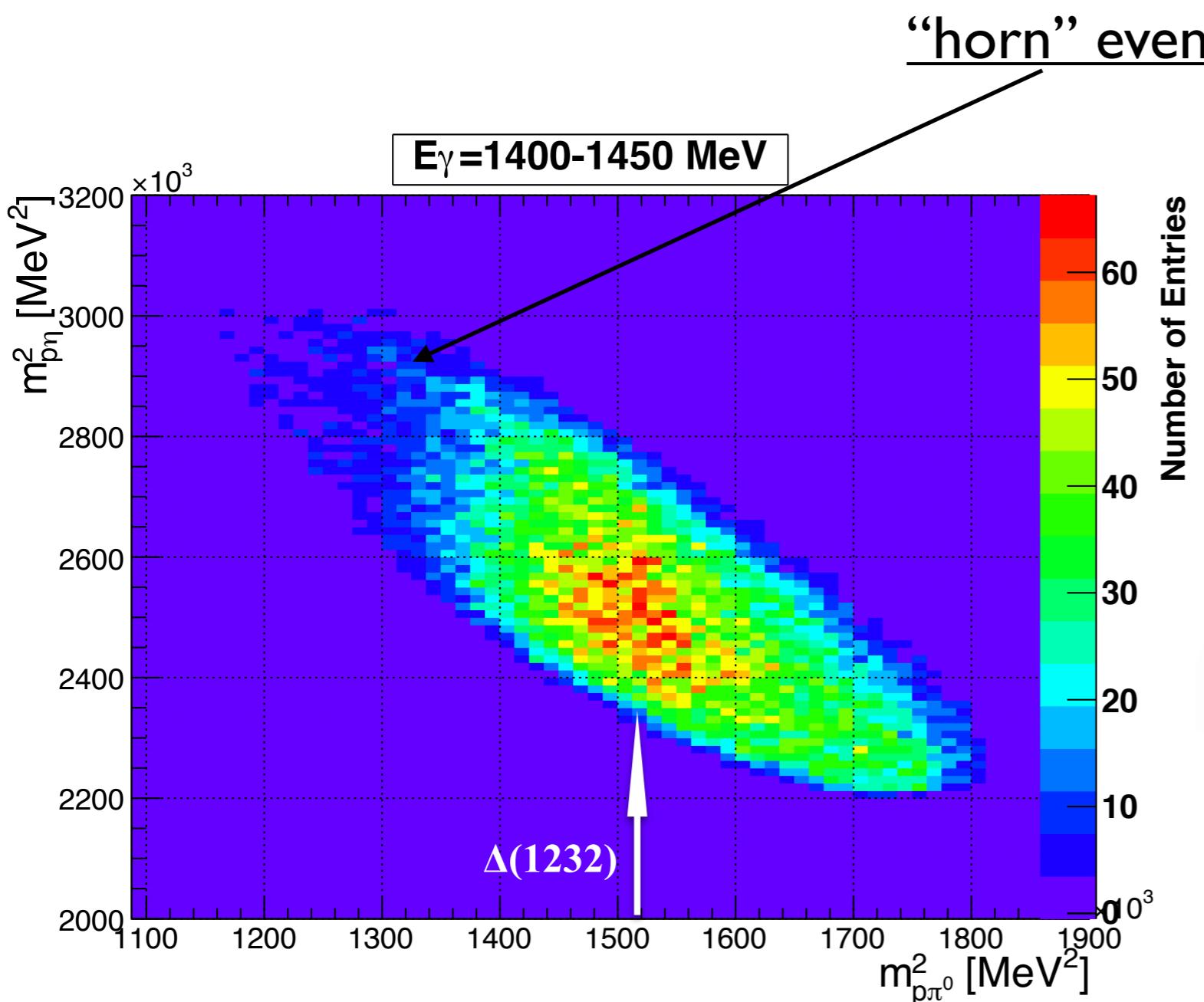


non-resonant t-channel production also possible

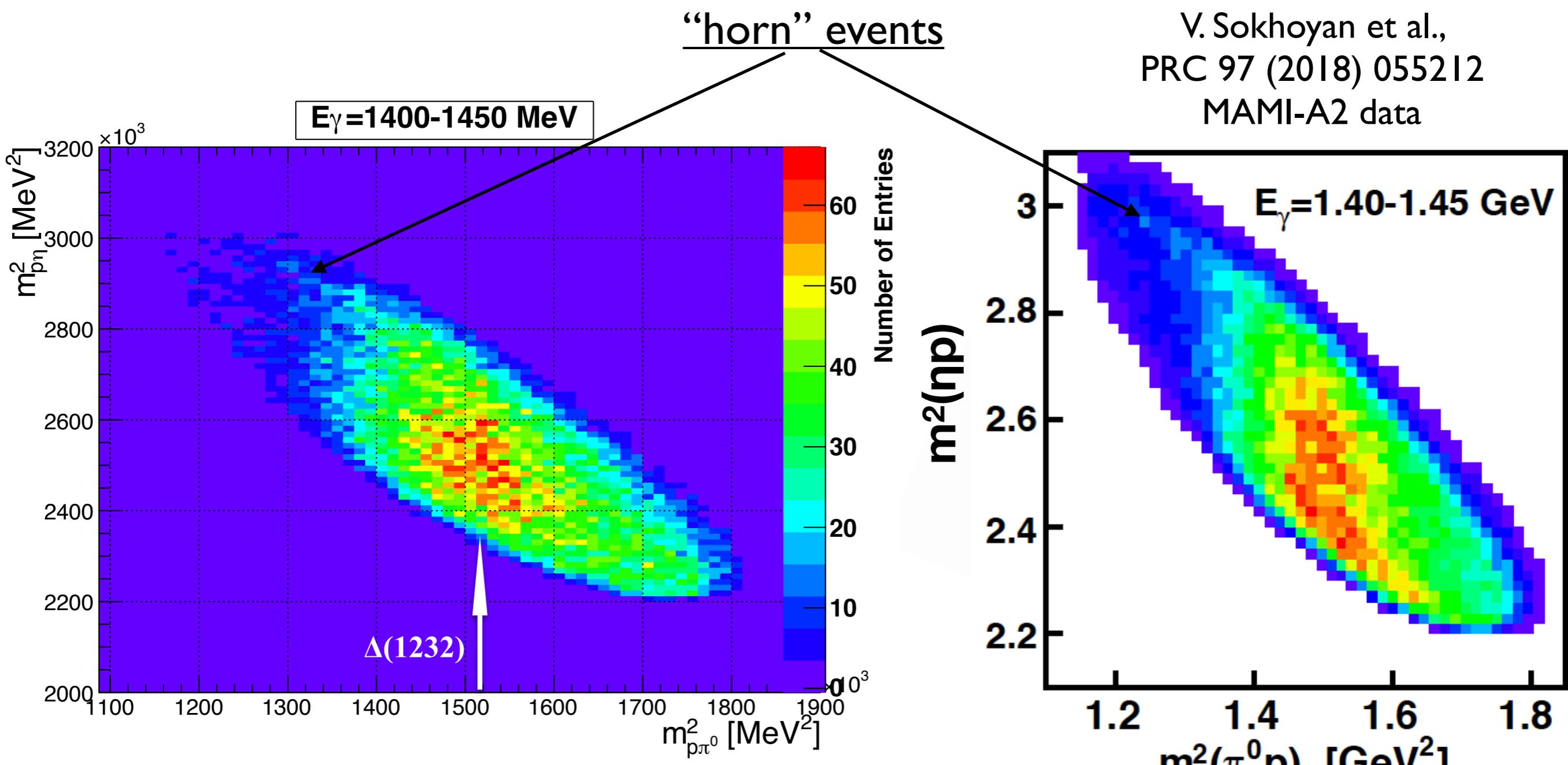
Dalitz plots: $\gamma p \rightarrow p \pi^0 \eta$



Dalitz plots: $\gamma p \rightarrow p \pi^0 \eta$



Dalitz plots: $\gamma p \rightarrow p \pi^0 \eta$



"horn" events:

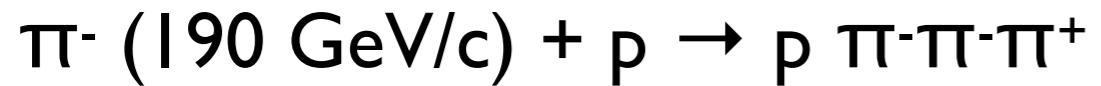
diagonal structure in Dalitz plot indicating a $\pi^0\eta$ correlation near $m_{\pi^0\eta} \approx 720$ MeV

preliminary PWA analysis by V. Nikonov, A. Sarantsev:
indication for a triangle singularity contribution ??

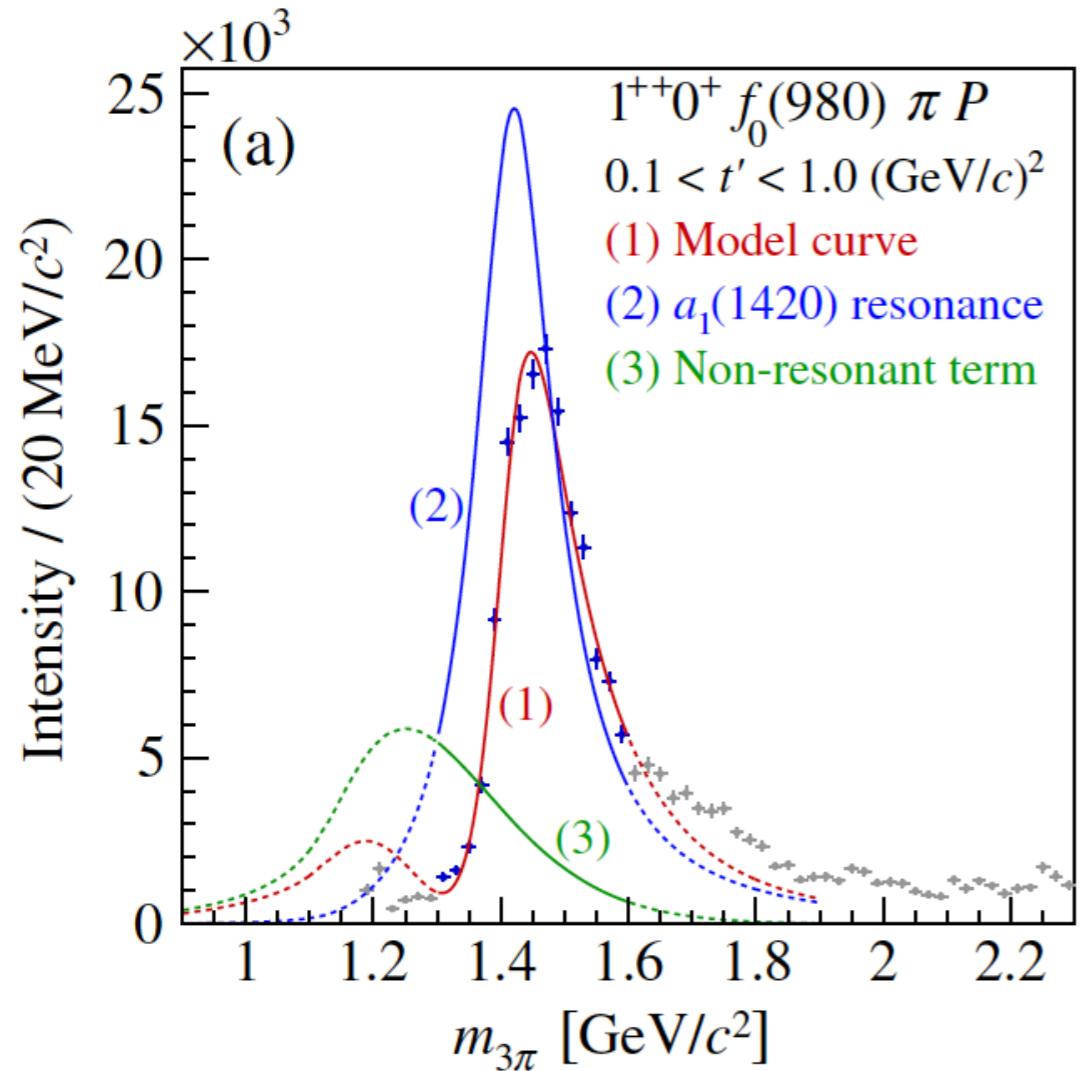
V. Sokhoyan et al.,
PRC 97 (2018) 055212
MAMI-A2 data

$a_1(1420)$: new axial-vector meson or kinematic effect ??

Compass collaboration:



C. Adolph et al., PRL 115 (2015) 082001



exotic meson: $J^{PC} = 1^{++}$

$m = 1414 \pm 15 \text{ MeV}$; $\Gamma = 153^{+8-23} \text{ MeV}$,
decaying into $f_0(980) \pi^-$

$a_1(1420)$: new axial-vector meson or kinematic effect ??

Compass collaboration:

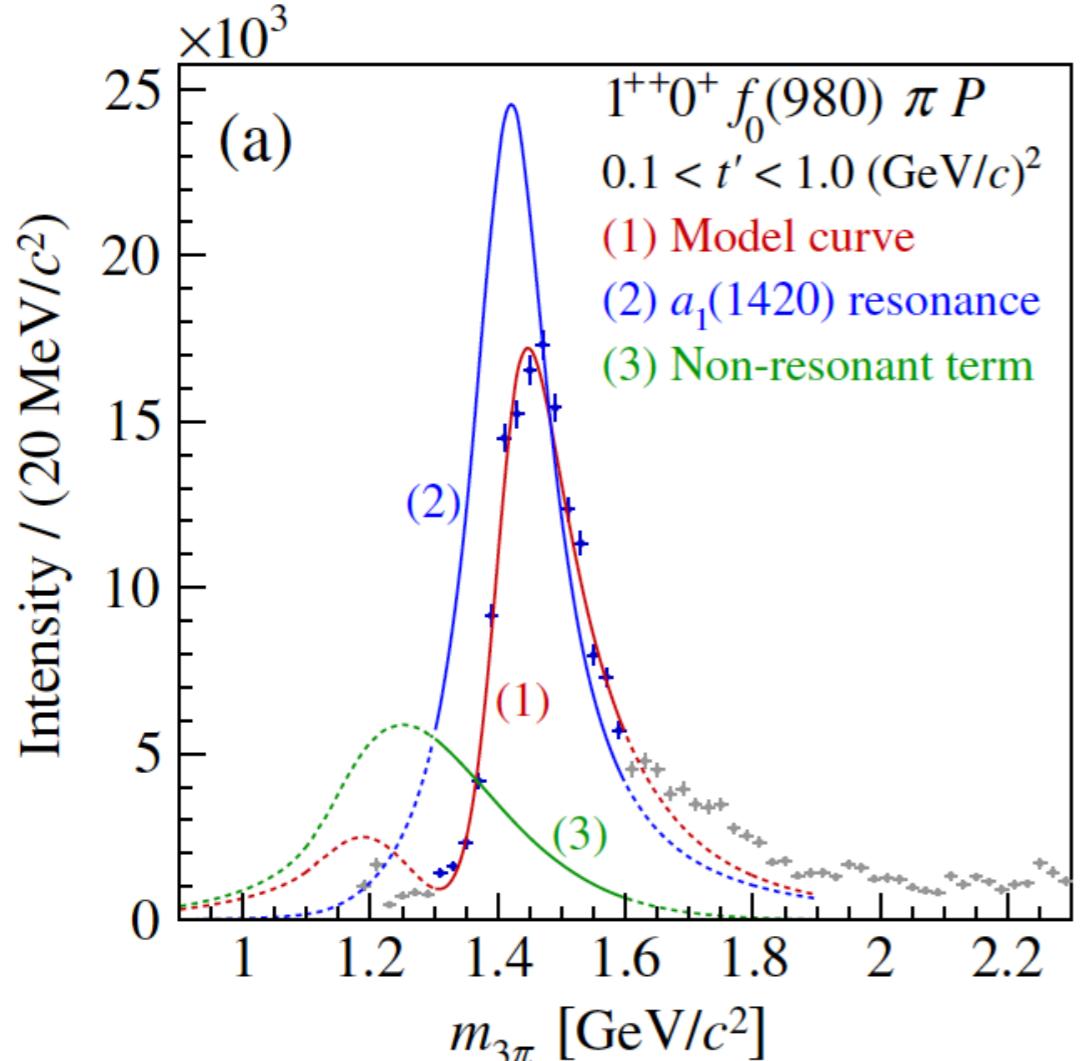
π^- (190 GeV/c) + p \rightarrow p $\pi^-\pi^-\pi^+$

C. Adolph et al., PRL 115 (2015) 082001

M. Mikhasenko, B. Ketzer, A. Sarantsev,

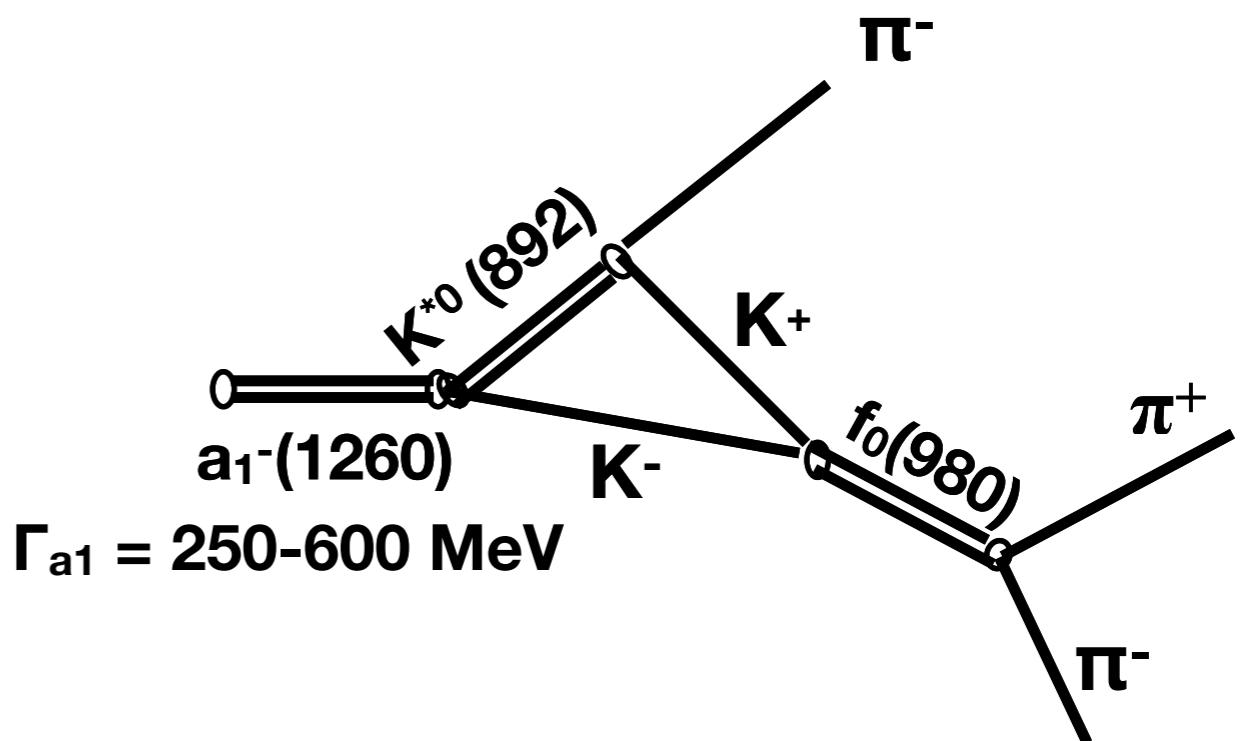
PRD 91 (2015) 094015

F. Aceti, L.R. Dai, E. Oset, PRD 94 (2016) 096015



exotic meson: $J^{PC} = 1^{++}$

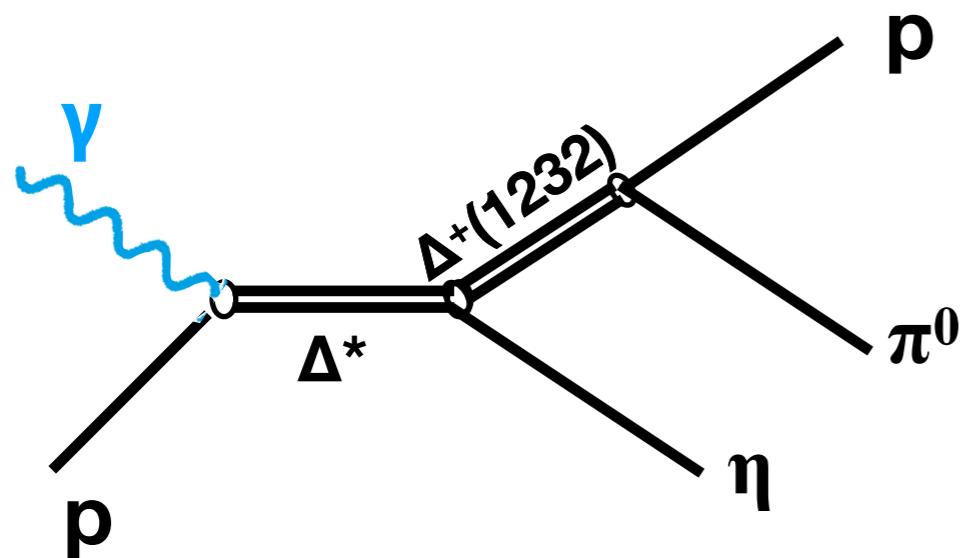
$m = 1414 \pm 15$ MeV; $\Gamma = 153+8-23$ MeV,
decaying into $f_0(980) \pi^-$



triangular loop develops singularity
at $W \approx 1420$ MeV
 \rightarrow observed peak = kinematic effect

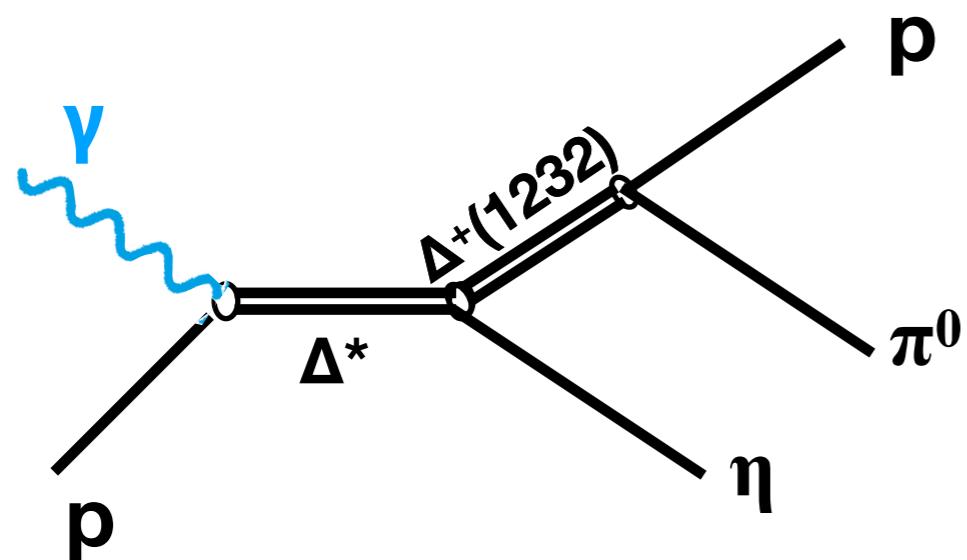
Different reaction amplitudes: $\gamma p \rightarrow p \pi^0 \eta$

resonance production via $\Delta^+(1232)$

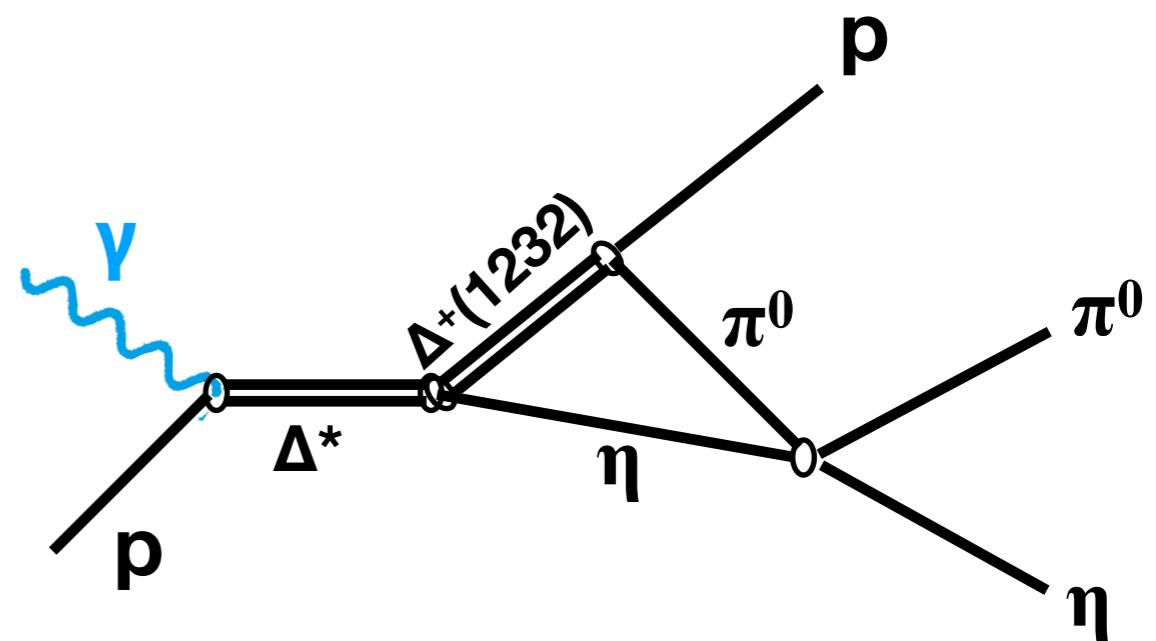


Different reaction amplitudes: $\gamma p \rightarrow p \pi^0 \eta$

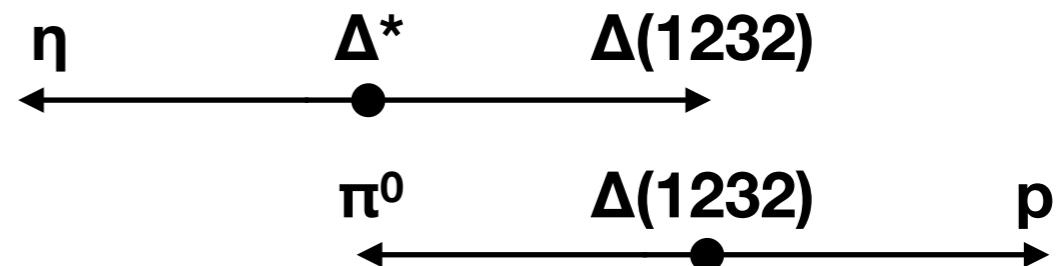
resonance production via $\Delta^+(1232)$



triangular singularity
final state (π^0, η) elastic scattering



singularities in reaction amplitude occur when all particle in triangle are on-shell and their momenta are collinear with $\beta_\pi > \beta_\eta$ so that π^0 and η rescatter:



for $E_\gamma = 1425$ MeV: triangle singularity: Δ^* cms: $\beta_\pi = 0.786 > \beta_\eta = 0.468$

Kinematic conditions for singularities

C. Schmid, Phys. Rev. 154 (1967) 1363

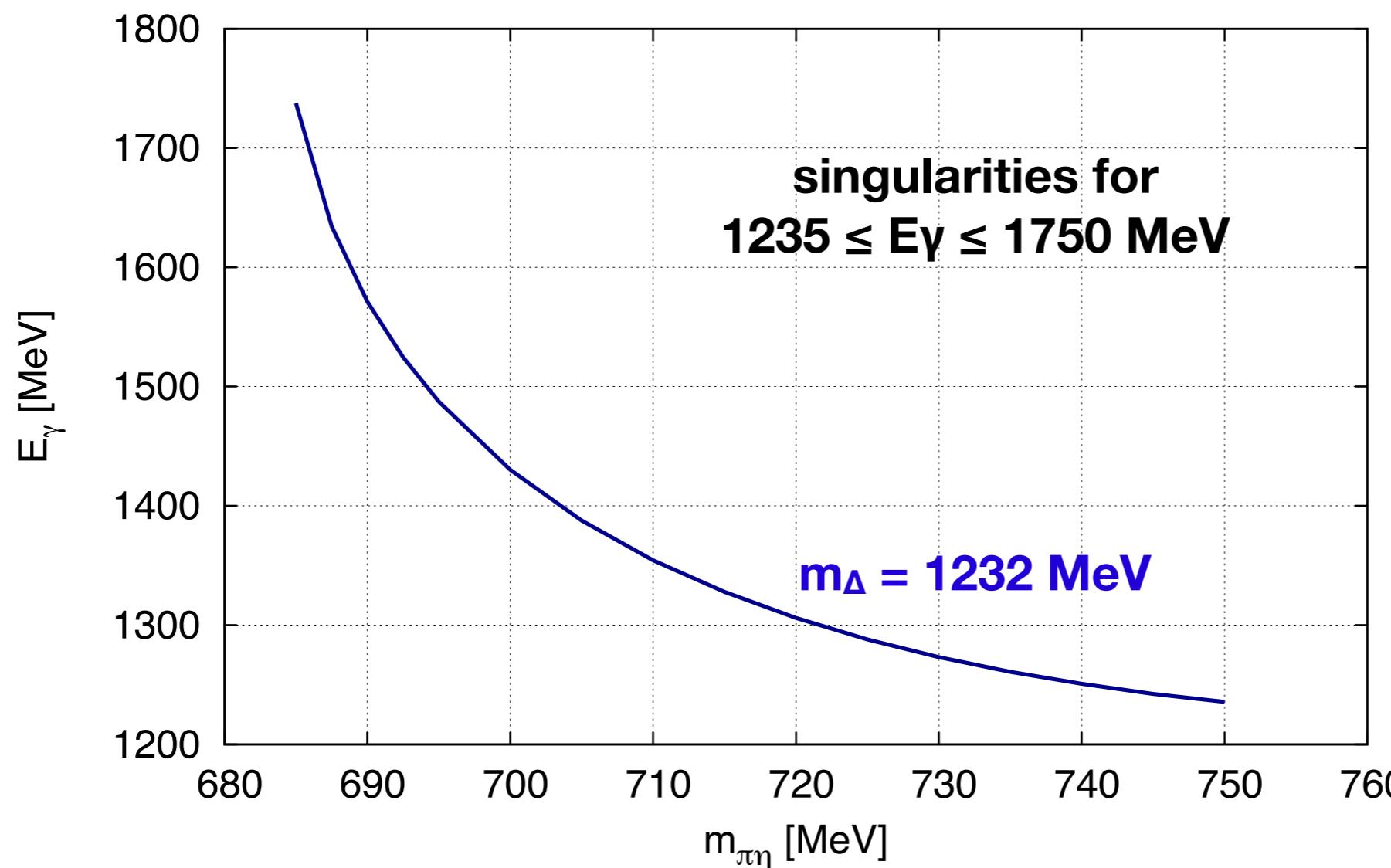
energy and momentum balance of external particles and particles within triangle

$$E_\Delta = (m_\Delta^2 - m_p^2 - m_\pi^2)/2m_\pi; \quad E_\eta = (m_{\pi\eta}^2 - m_\eta^2 - m_\pi^2)/2m_\pi$$

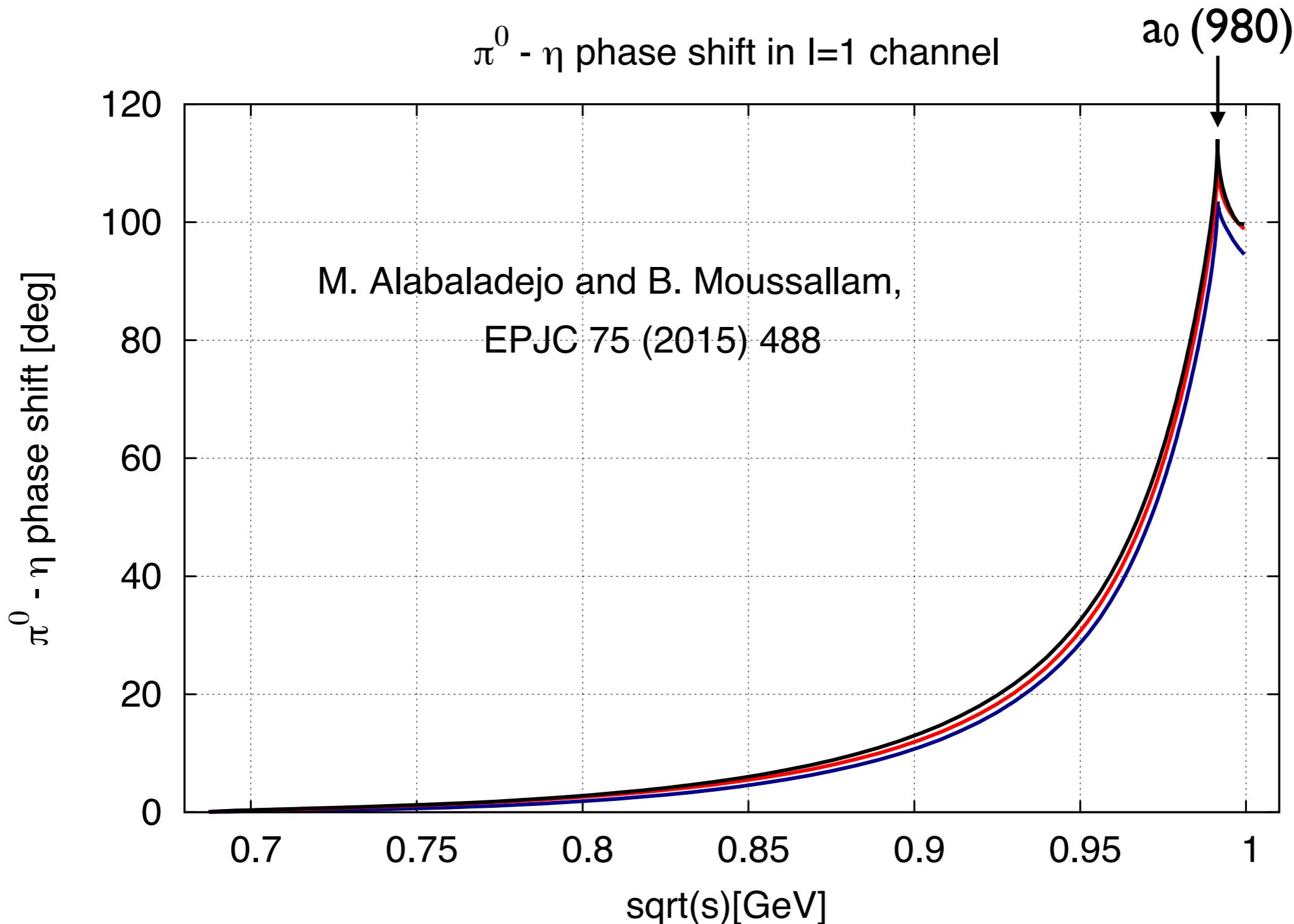
$$p_\Delta = 1/2m_\pi \cdot \sqrt{(m_\Delta^2 - (m_p + m_\pi)^2) (m_\Delta^2 - (m_p - m_\pi)^2)}$$

$$p_\eta = 1/2m_\pi \cdot \sqrt{(m_{\pi\eta}^2 - (m_\eta + m_\pi)^2) (m_{\pi\eta}^2 - (m_\eta - m_\pi)^2)}$$

$$W^2 = m_\Delta^2 + m_\eta^2 + 2 E_\Delta \cdot E_\eta - 2 p_\Delta \cdot p_\eta$$



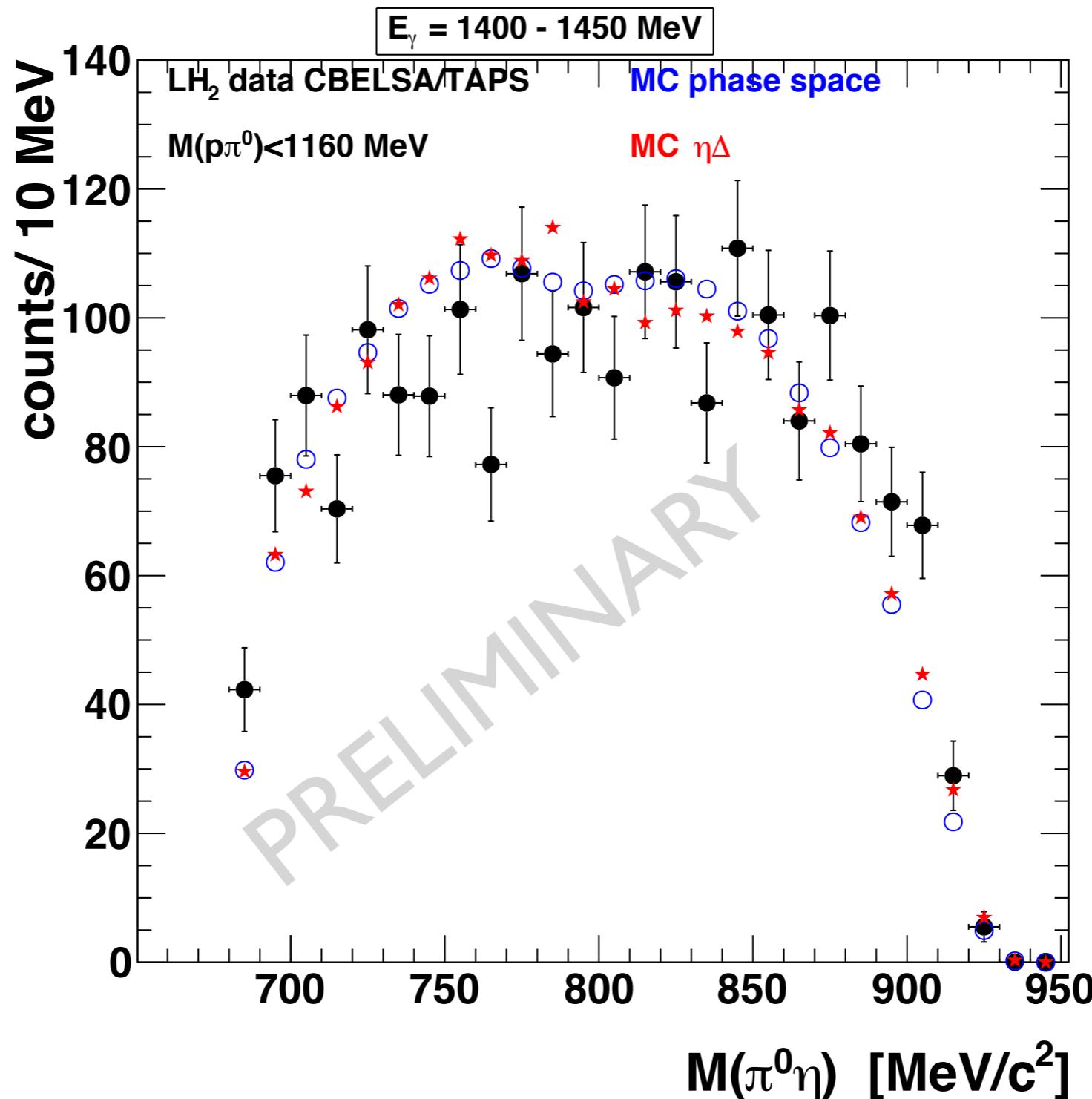
strength of the π^0 - η interaction



π^0 - η interaction quite weak at low \sqrt{s} (B. Kubis)

triangle singularity amplitude quite small (V. Debastiani, E. Oset, S. Sakai)

π^0 - η invariant mass spectrum



no significant deviation of measured $\pi^0\eta$ invariant mass spectrum from spectrum simulated for $\gamma p \rightarrow \Delta^* \rightarrow \eta\Delta(1232) \rightarrow \eta\pi^0 p$
no evidence for a triangle singularity contribution !!

summary

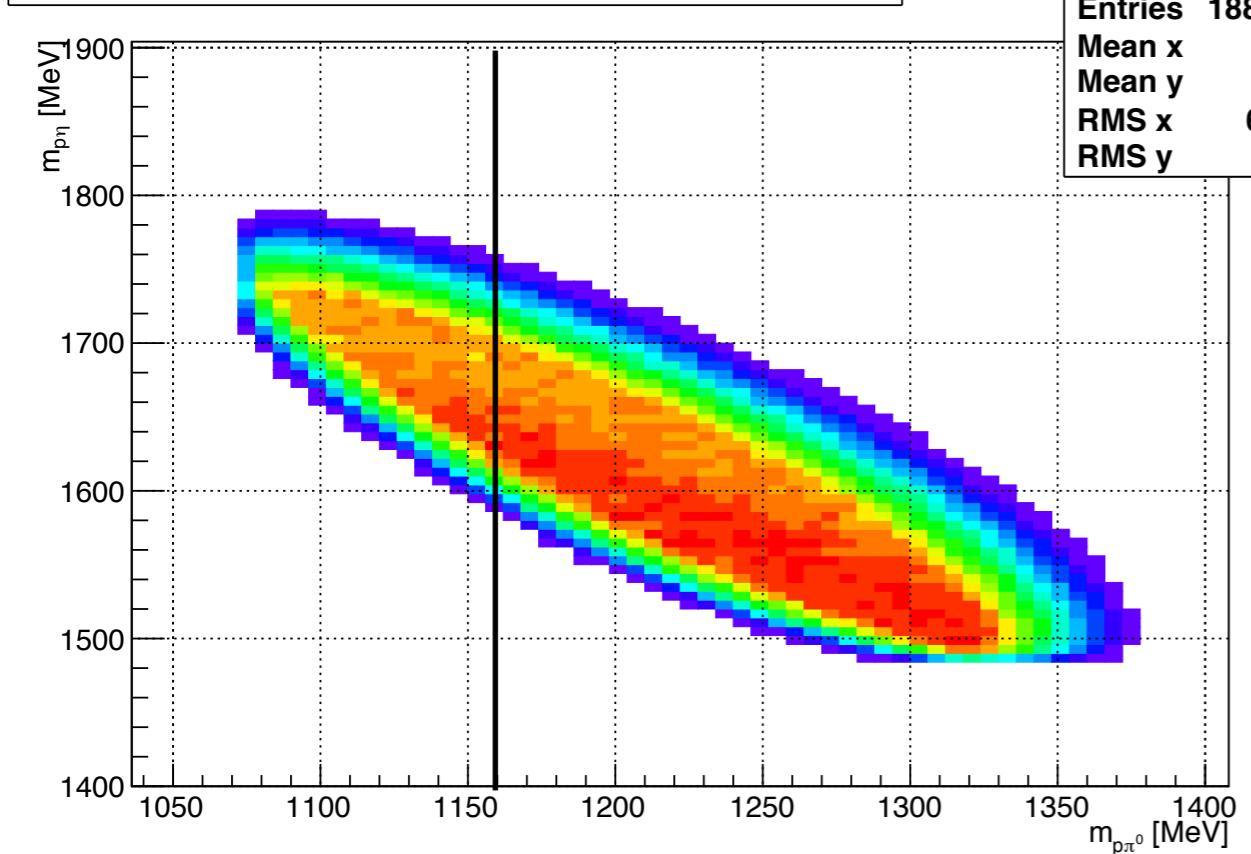
- meson cascade decays dominate de-excitation of higher nucleon resonances
→ multi photon final states → 4 π detectors
- clear evidence for $\eta \Delta(1232)$ and $\pi^0 S_{11}(1535)$ cascade events:
 $\gamma p \rightarrow \Delta^* \rightarrow \eta \Delta(1232) \rightarrow \eta \pi^0 p$; $\gamma p \rightarrow \Delta^*, N^* \rightarrow \pi^0 S_{11}(1535) \rightarrow \pi^0 \eta p$
- kinematic fit essential for identifying the $\gamma p \rightarrow p \pi^0 \eta$ reaction and for removing residual $\pi^0 \pi^0$ events;
final checks of the data analysis in progress
- triangle singularity kinematically possible in $\gamma p \rightarrow p \pi^0 \eta$ for $E_\gamma = 1300-1500$ MeV
- triangle singularity contribution insignificant due to weak $\pi^0\eta$ interaction near threshold

back up

Monte-Carlo simulations: $E_\gamma = 1.40 - 1.45 \text{ GeV}$

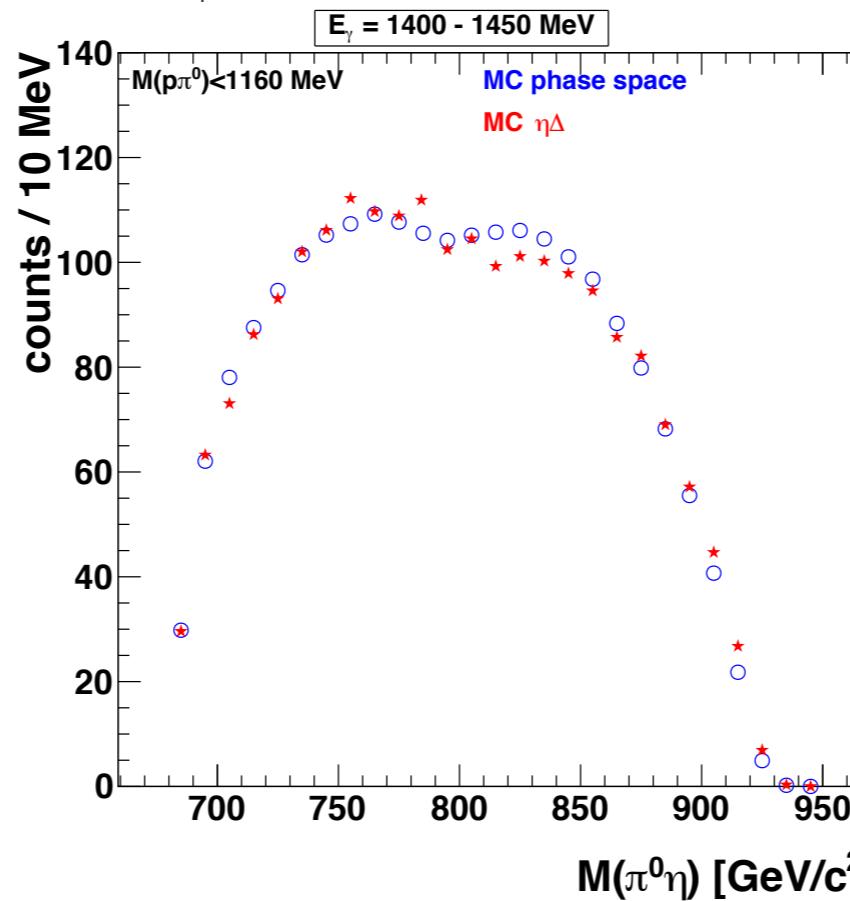
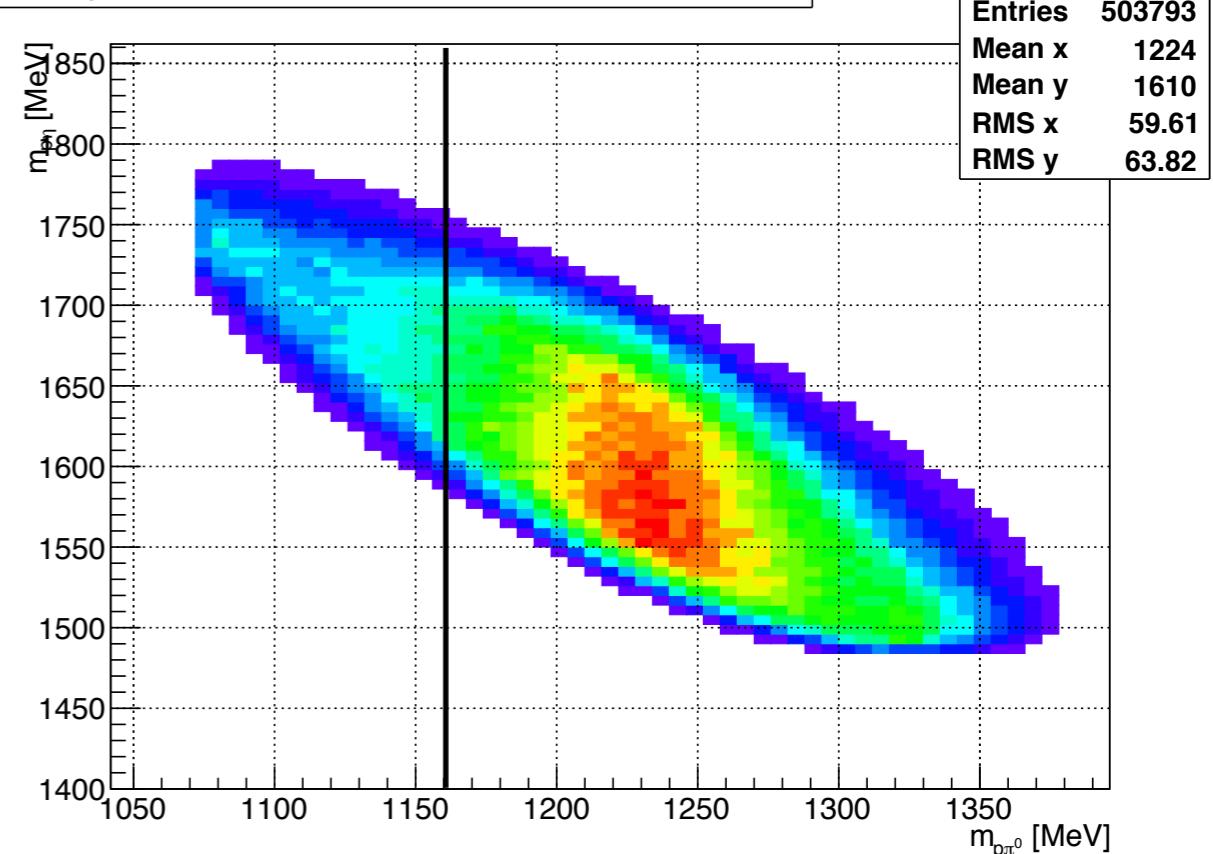
$\gamma p \rightarrow \Delta^* \rightarrow \eta \pi^0 p$; phase space

ProjectionXY, binz=[5,8] [z=1400.0..1500.0]



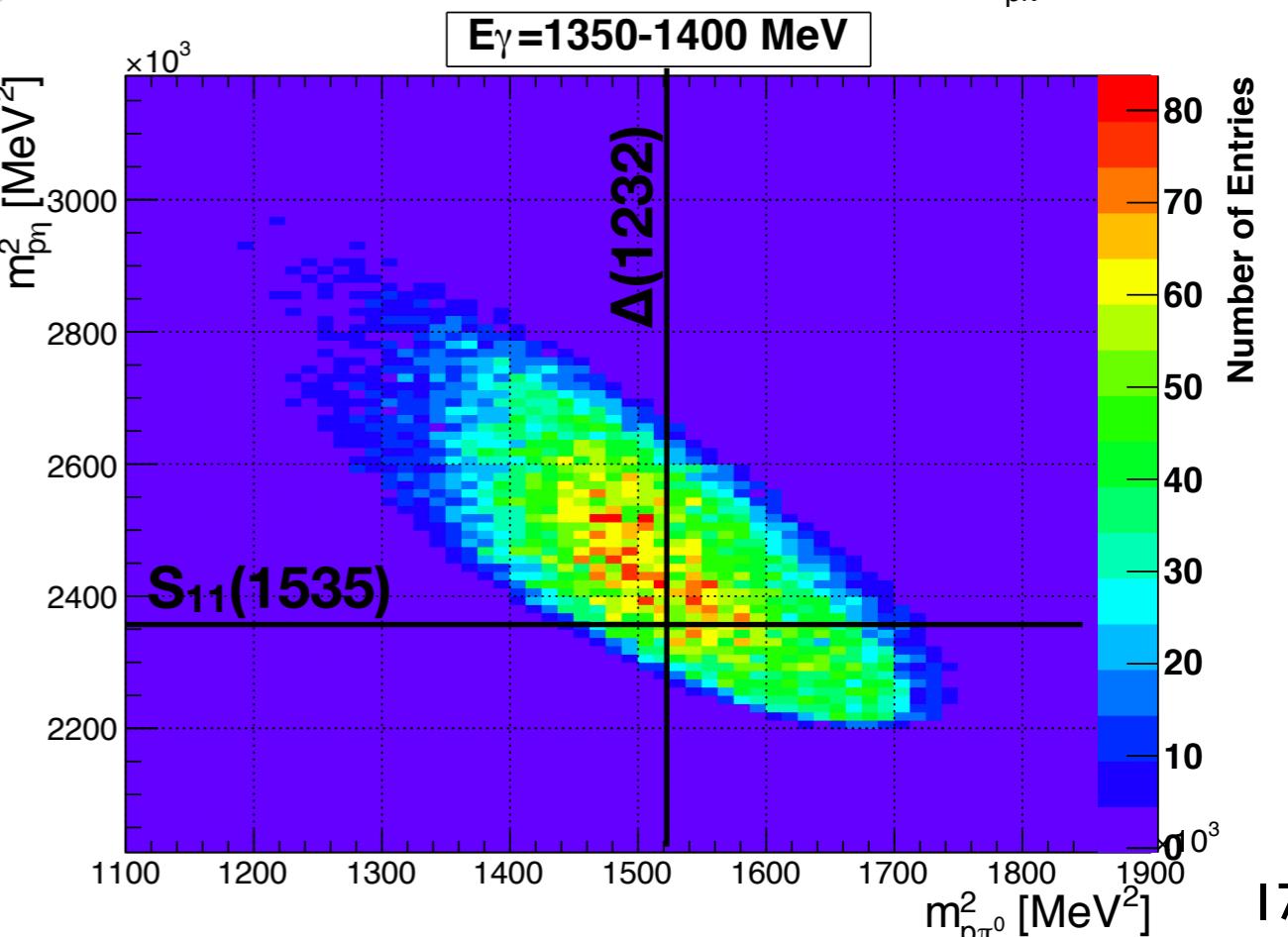
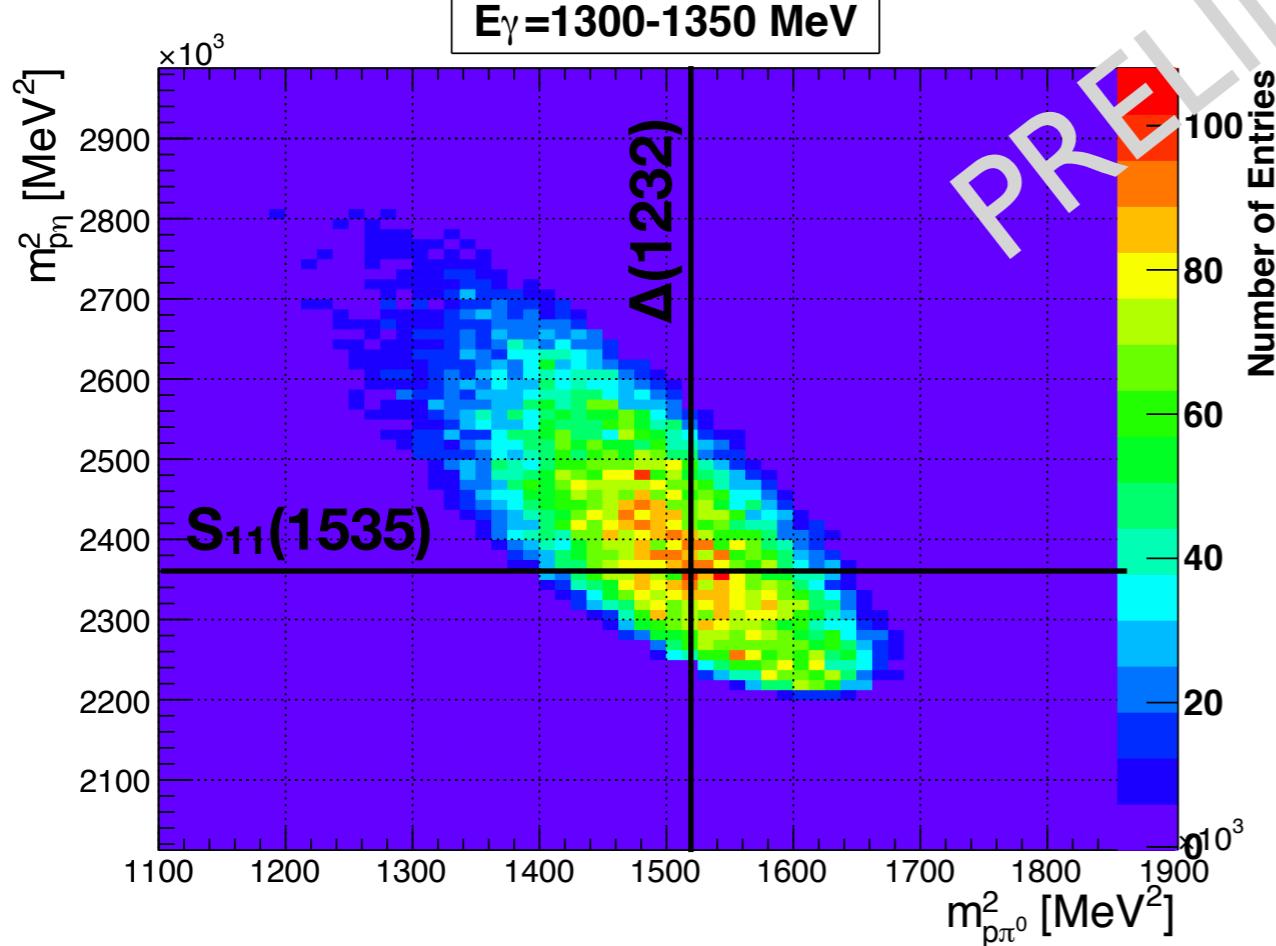
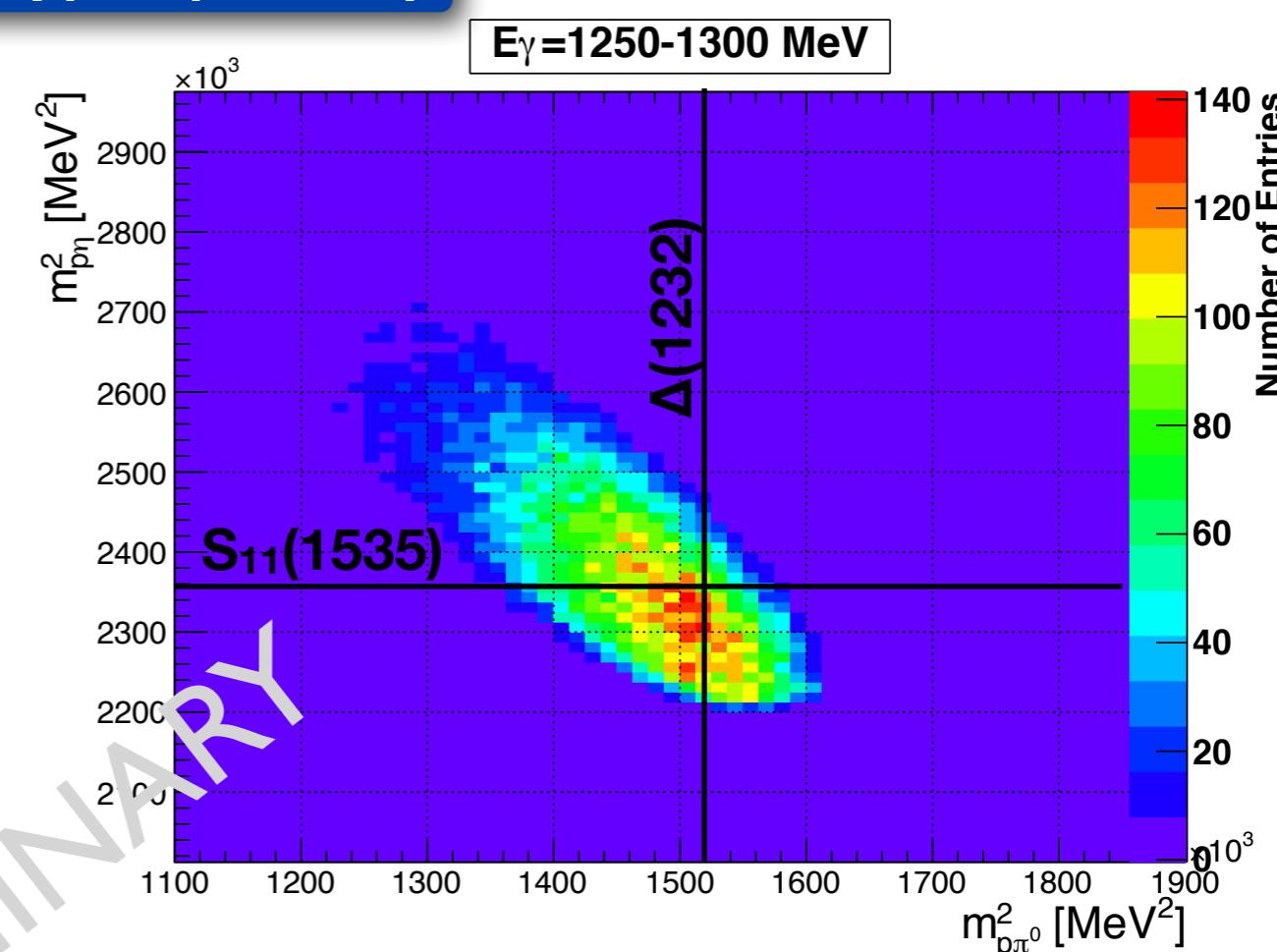
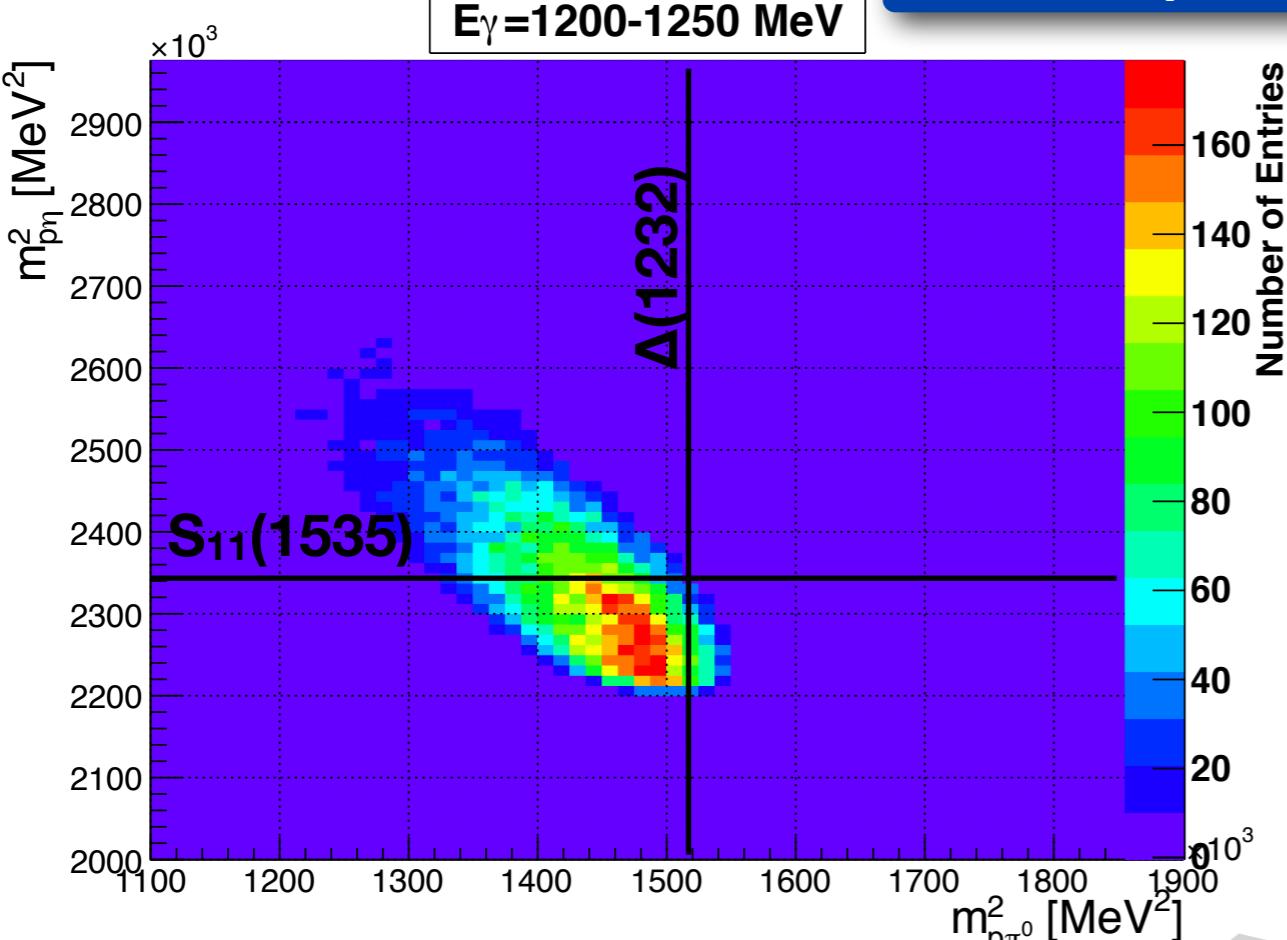
$\gamma p \rightarrow \Delta^* \rightarrow \eta \Delta(1232) \rightarrow \eta \pi^0 p$

ProjectionXY, binz=[5,8] [z=1400.0..1500.0]

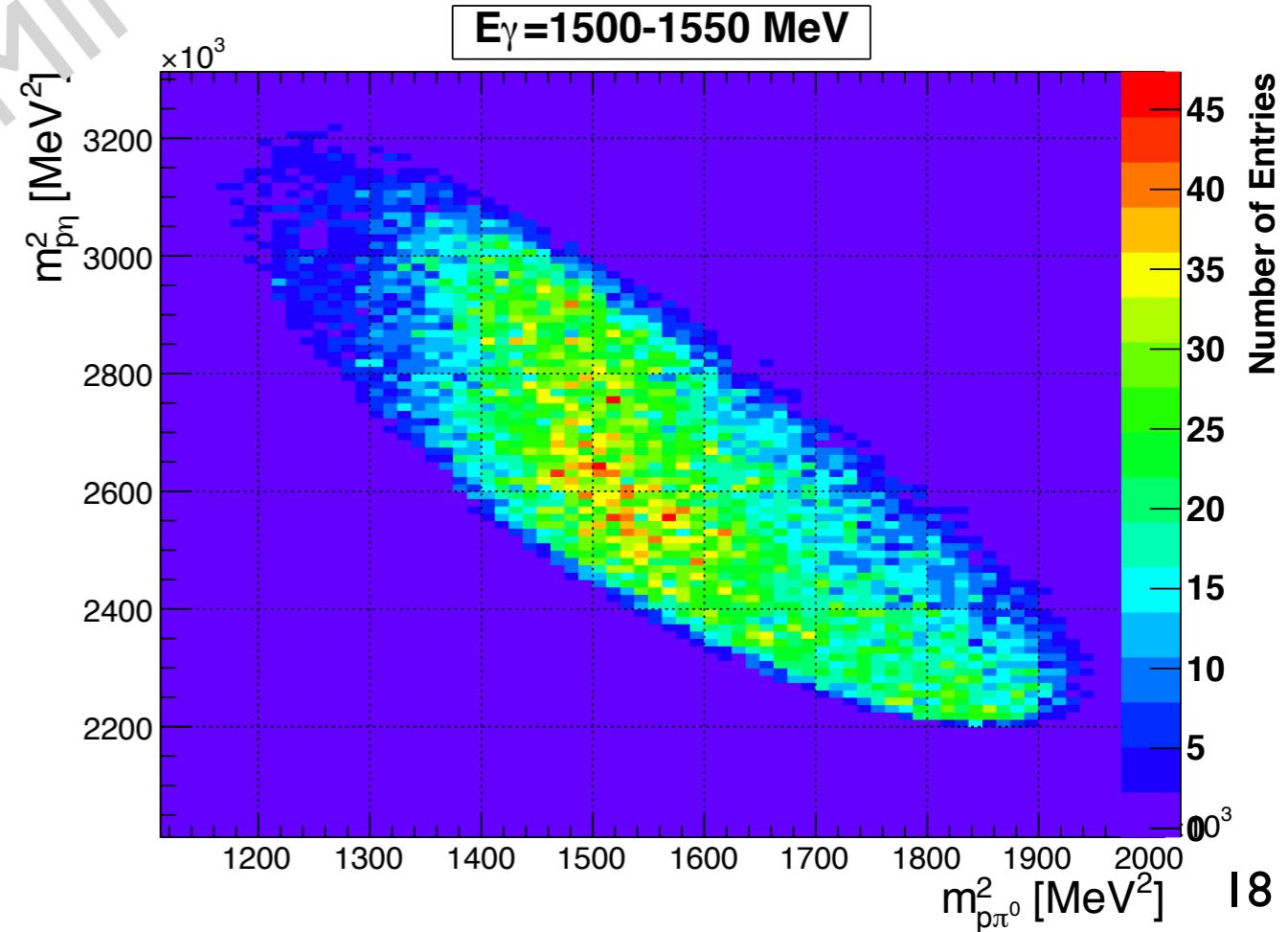
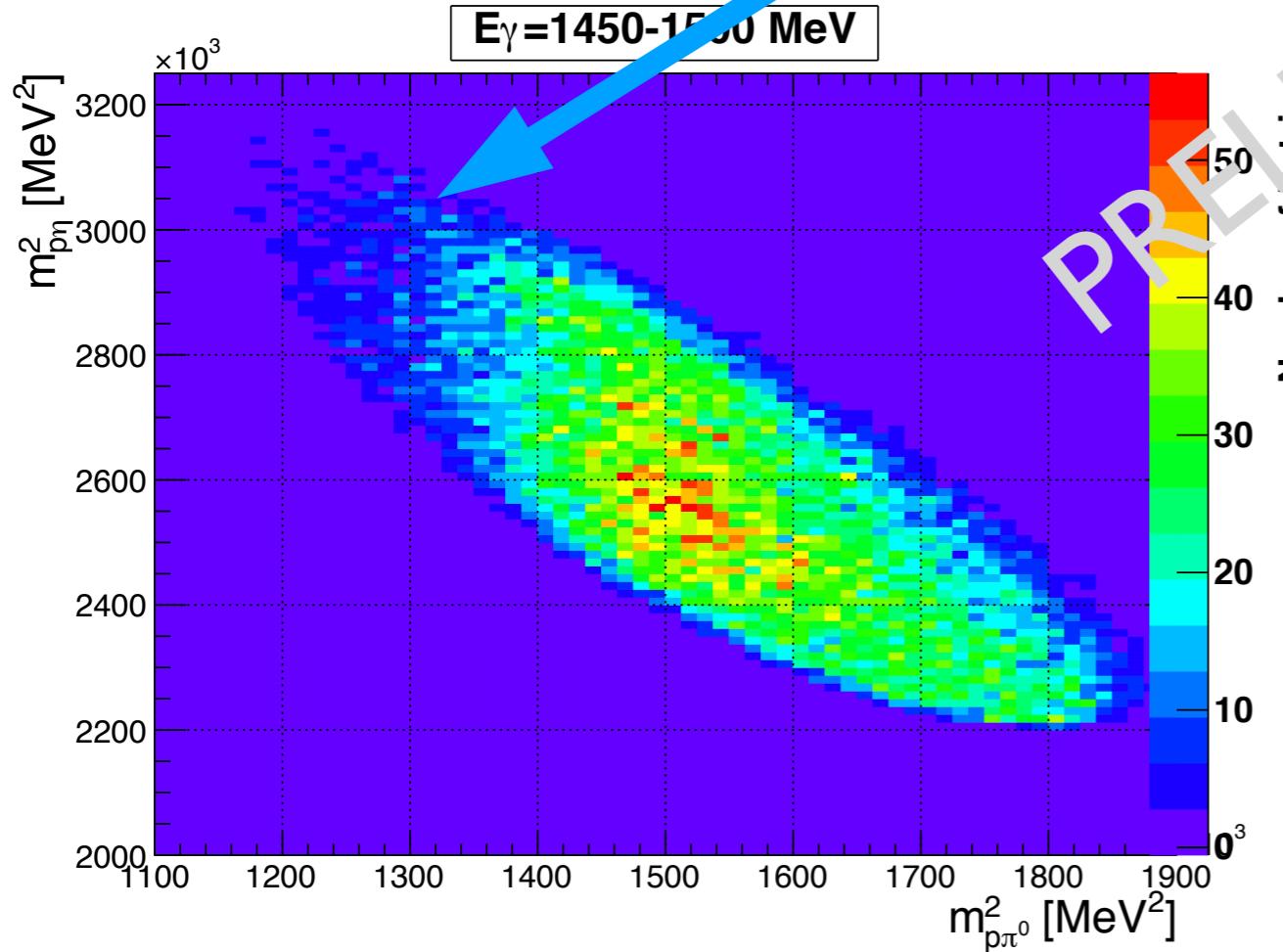
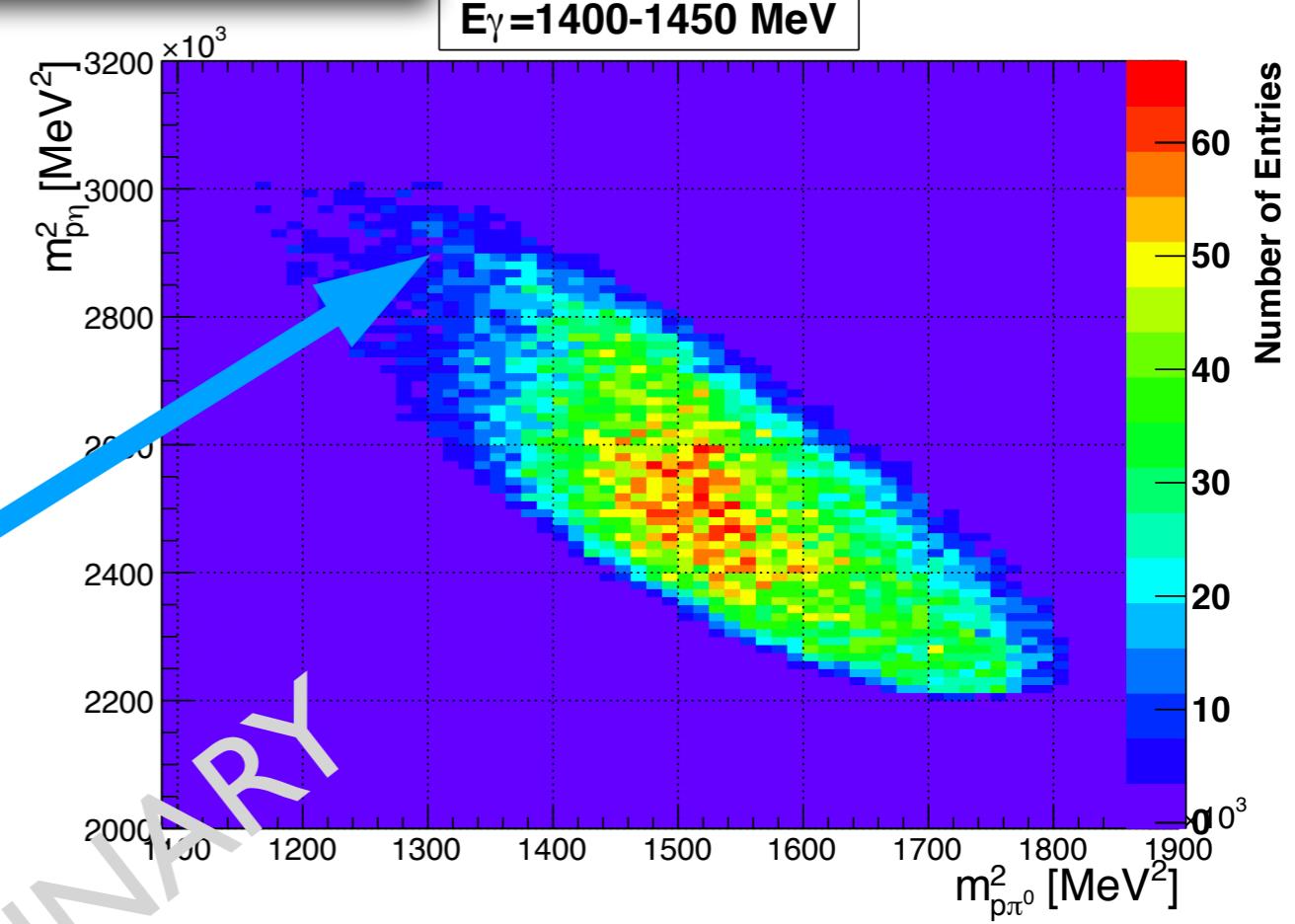
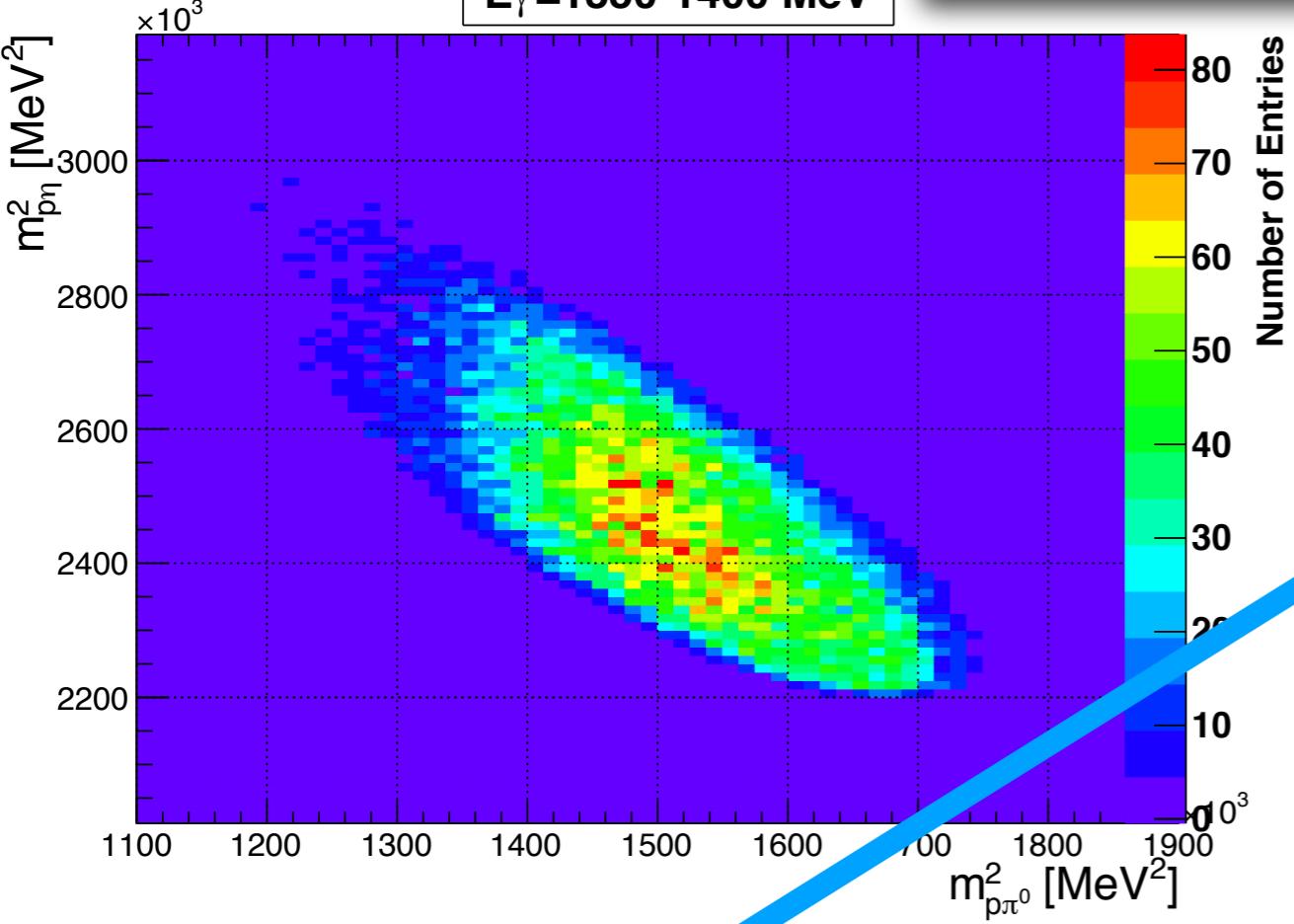


$\pi^0 \eta$ invariant mass spectrum
for $m_{p\pi^0} < 1160 \text{ MeV}$

Dalitz plots: $\gamma p \rightarrow p \pi^0 \eta$



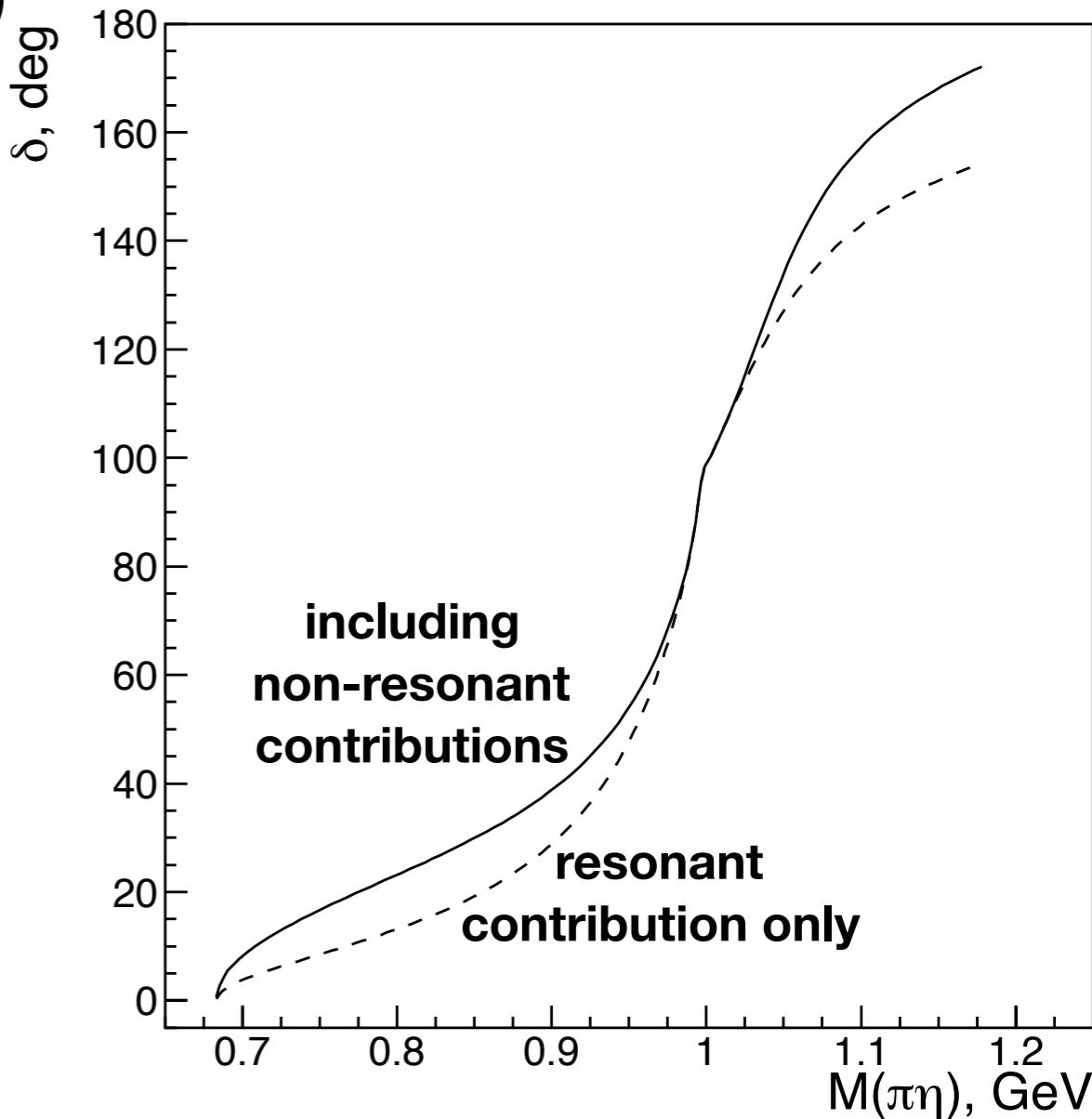
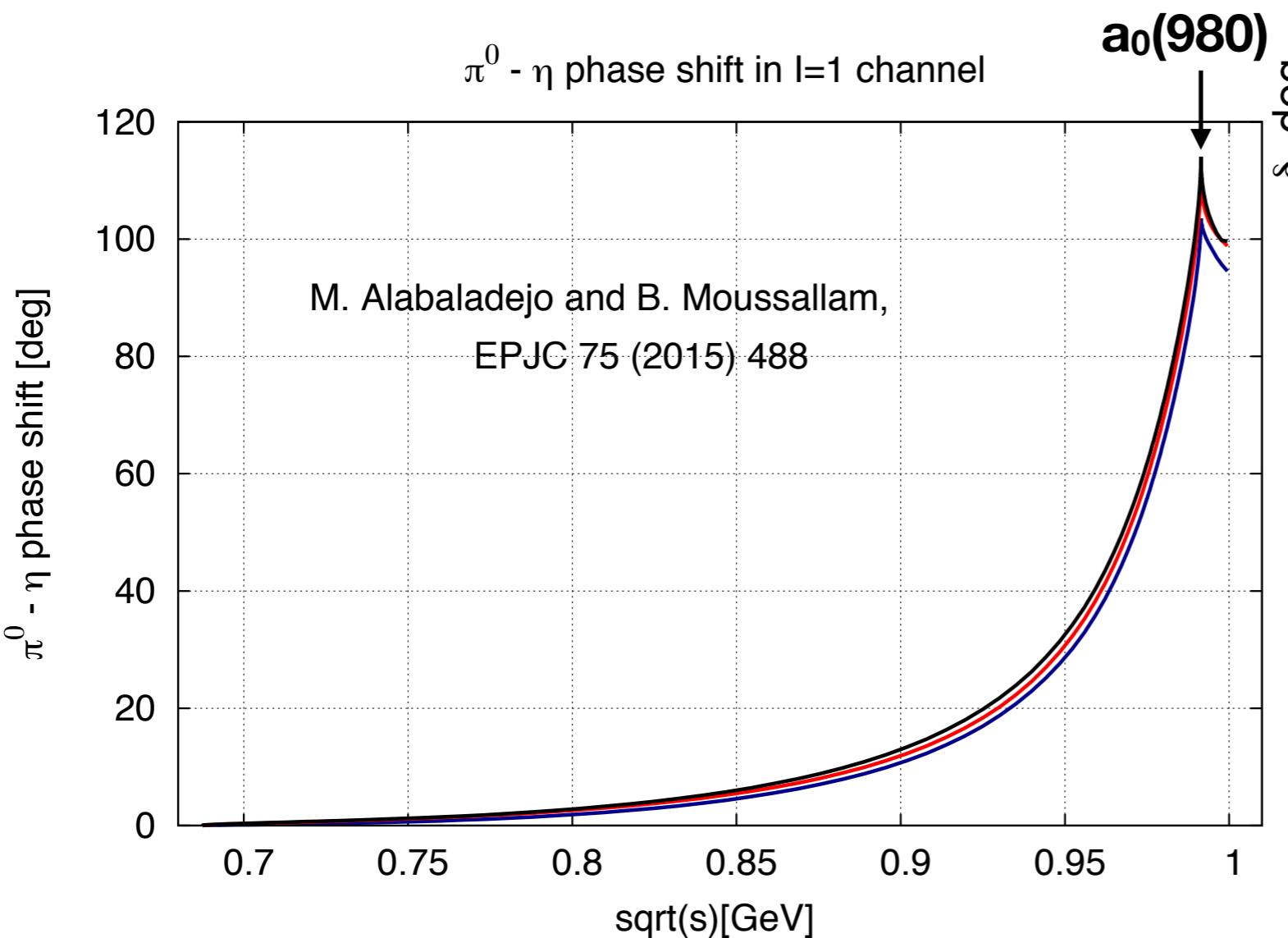
Dalitz plots: $\gamma p \rightarrow p \pi^0 \eta$



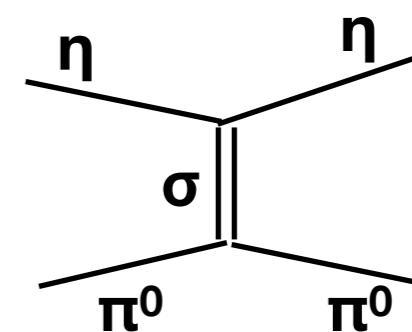
PREUMINARY

phase shift in the $|l=l$ system

V. Nikonov, A. Sarantsev
(priv. com)

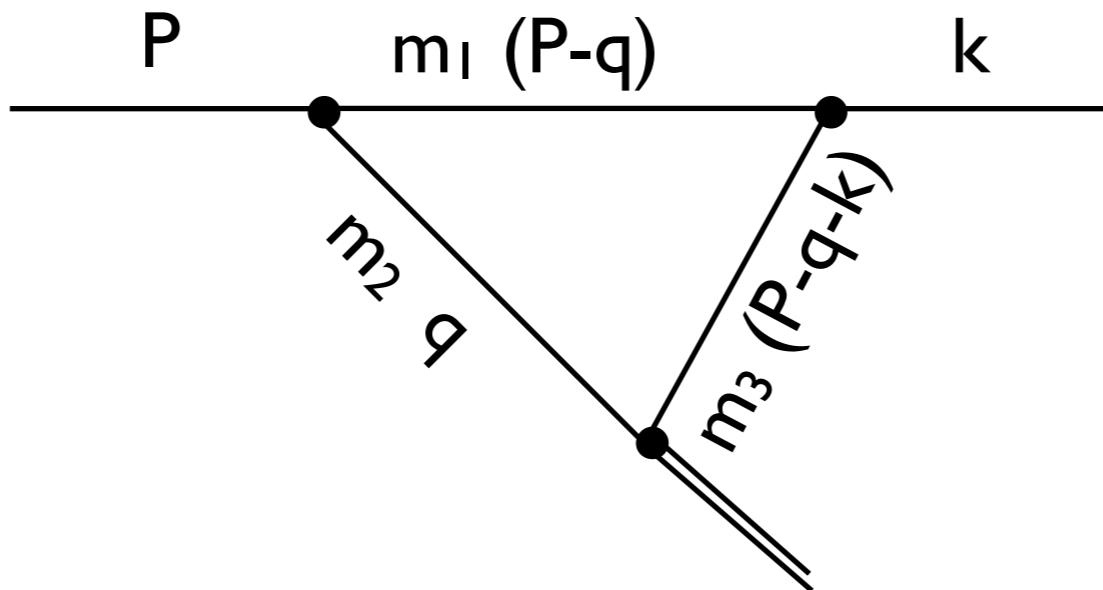


non-resonant
contribution



singularities in reaction amplitude

M. Bayar et al., PRD 94 (2016) 074039

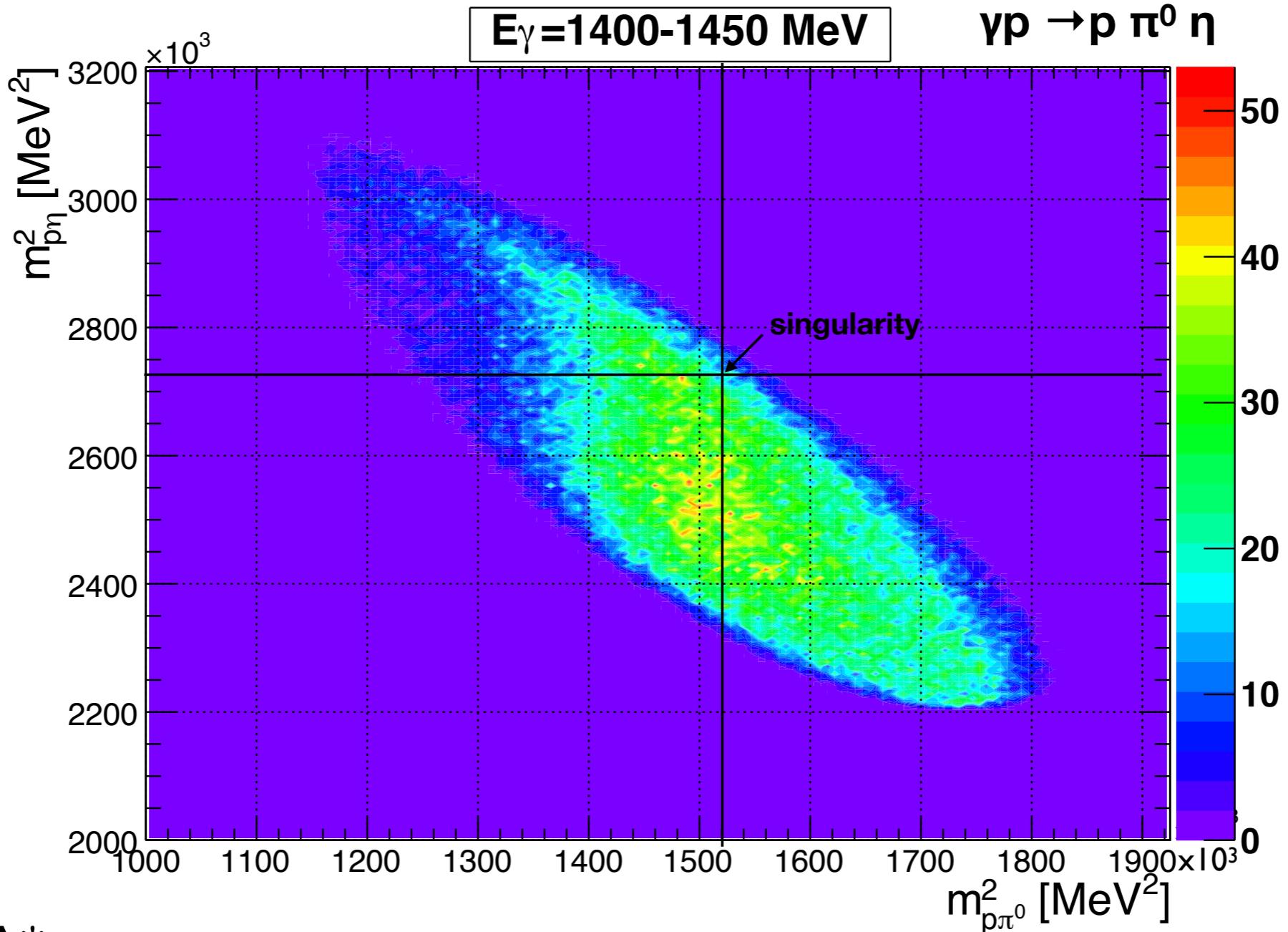


scalar three-point loop integral:

$$A = i \int \frac{d^4 q}{(2\pi)^4 [q^2 - m_2^2 + i\epsilon][(P-q)^2 - m_1^2 + i\epsilon][(P-q-k)^2 - m_3^2 + i\epsilon]}$$

singularities occur when particles in triangle become on-shell

experimental evidence for singularity: “horn” events?



singularity: Δ^* cms

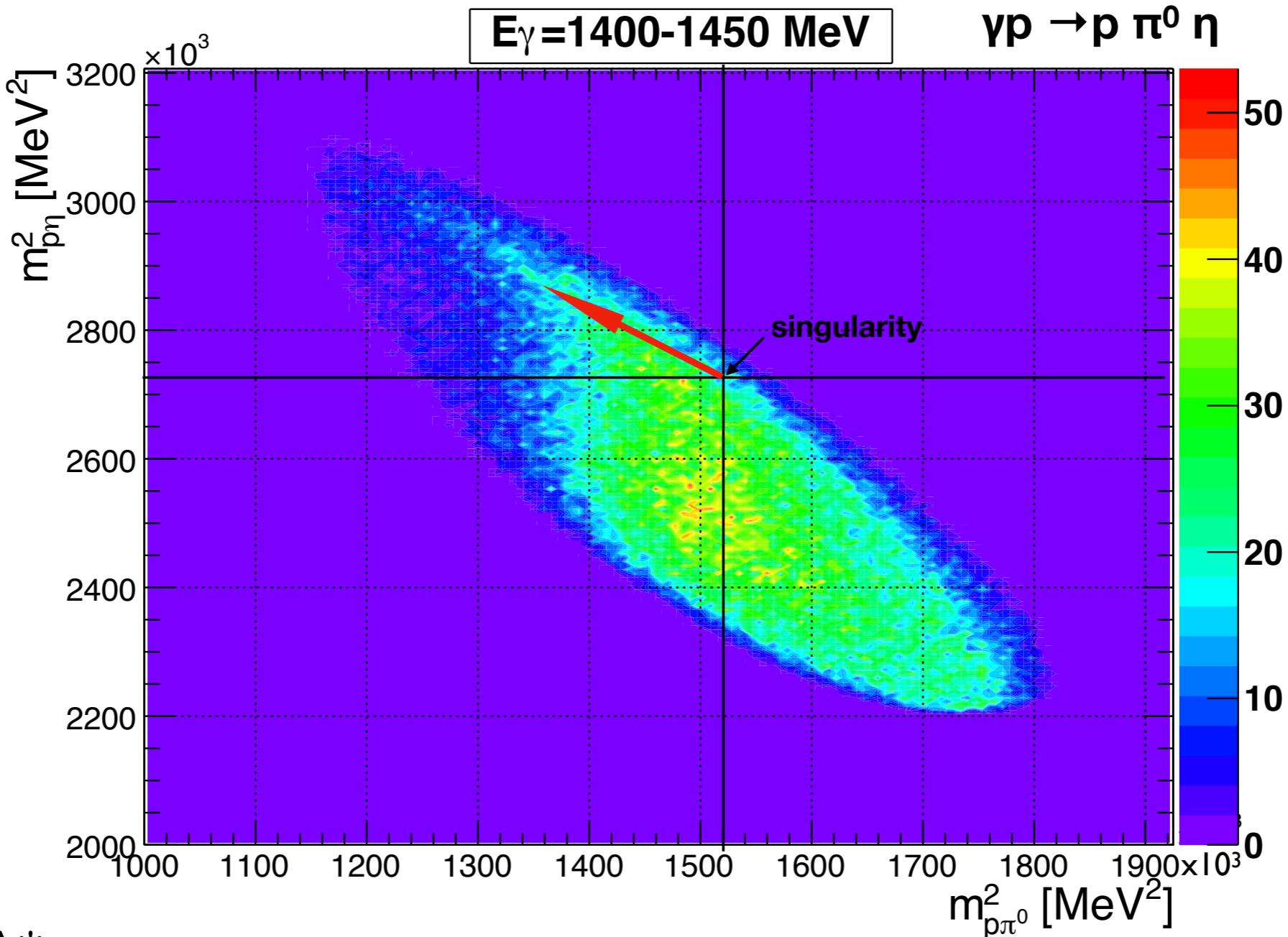
$$\beta_\eta = 0.468$$

$$p_\eta = 619.7 \quad p_p = 462.3$$

$$p_\pi = 172.5$$

$$\beta_\pi = 0.786$$

experimental evidence for singularity: “horn” events?



singularity: Δ^* cms

$$\beta_\eta = 0.468$$

$$p_\eta = 619.7$$



$$p_p = 462.3$$

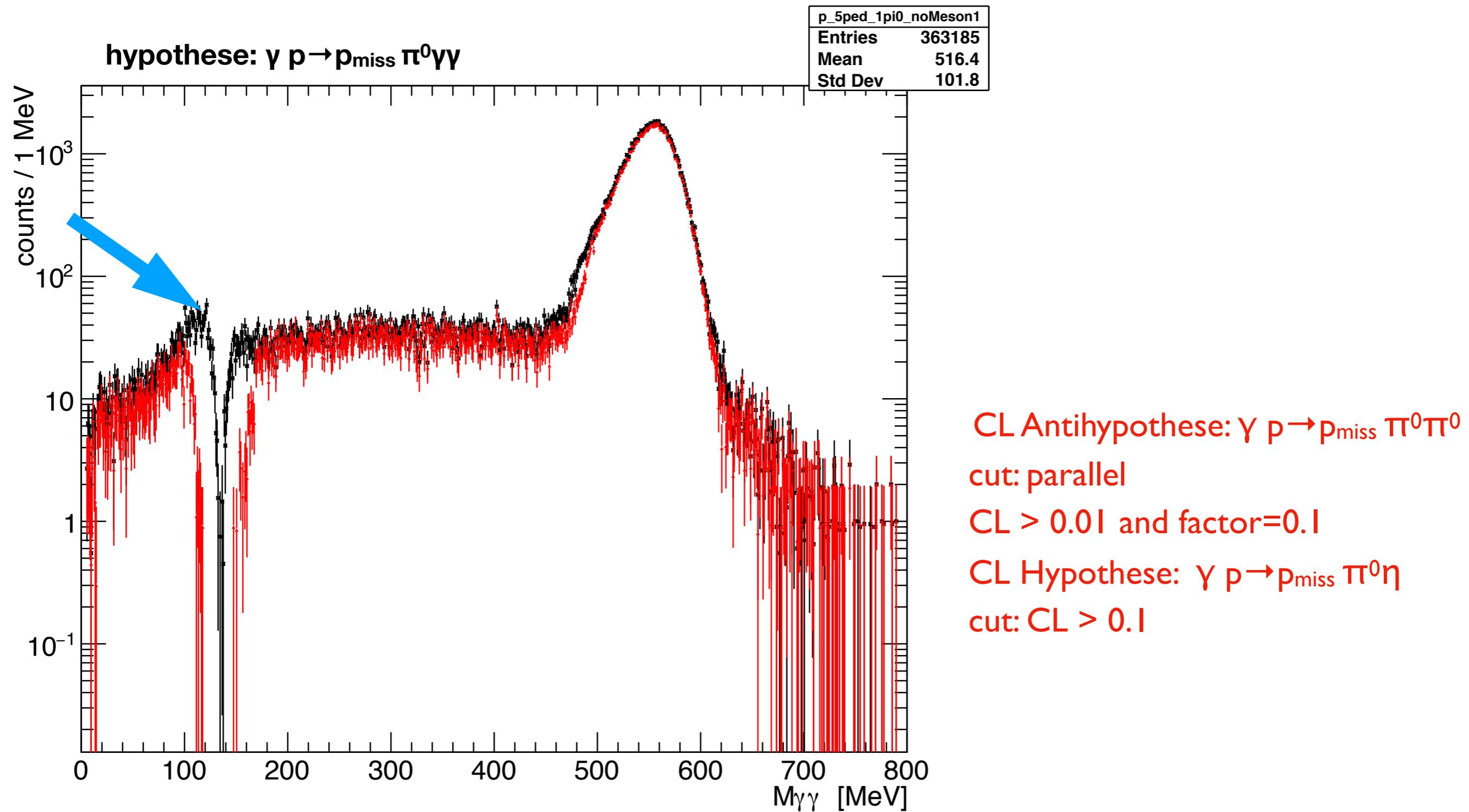
$$\beta_\pi = 0.786$$

in rescattering $m_{\pi\eta} = \text{const}$;
 π^0 slowed down and η speeds up: $m_{p\pi} \downarrow$ and $m_{p\eta} \uparrow$
 one moves along the line

$$m_{p\eta}^2 = W^2 + m_\pi^2 + m_\eta^2 + m_p^2 - m_{\pi\eta}^2 - m_{p\pi}^2$$

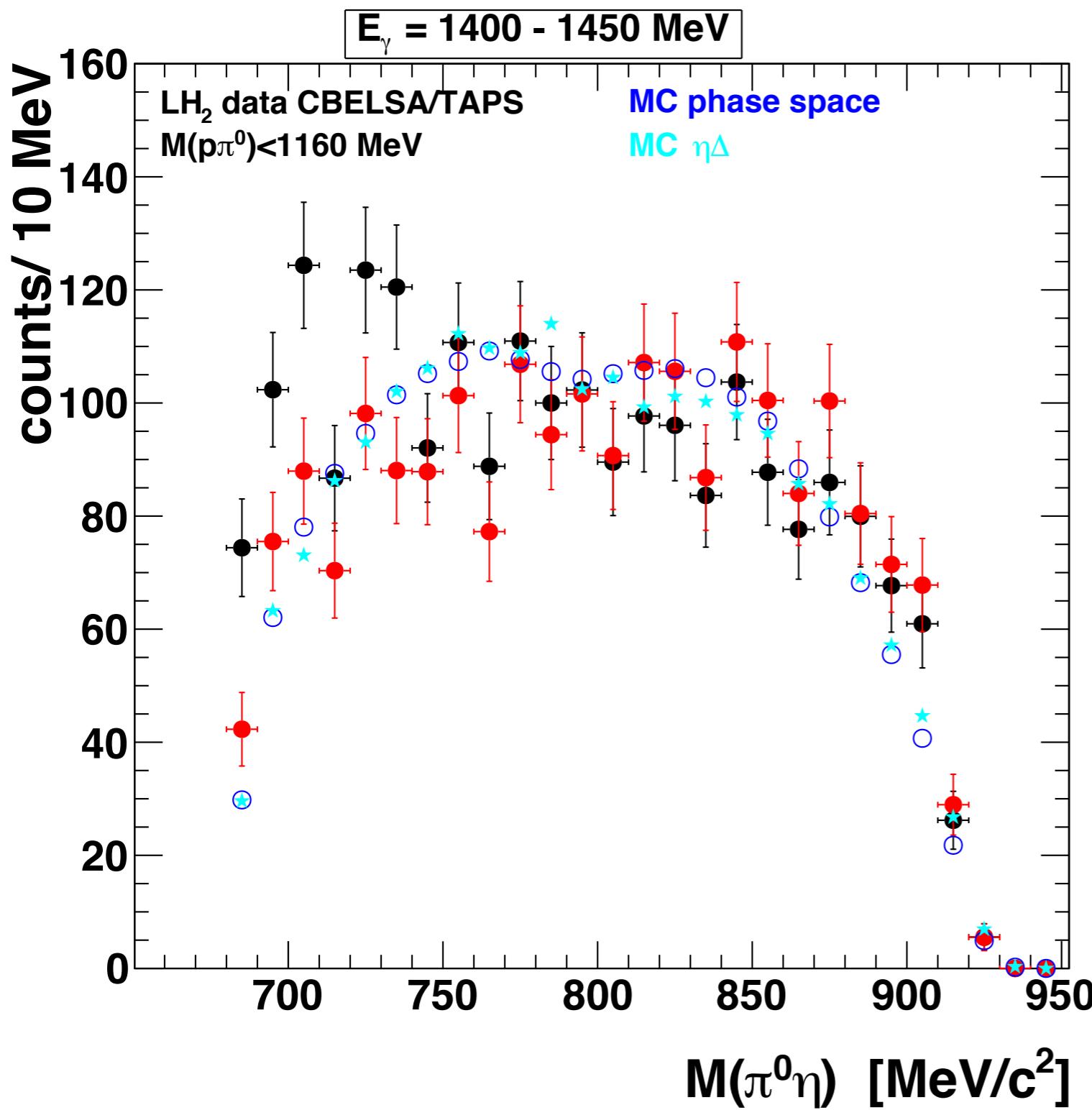
and reaches points in “horn” region

kinematic fit



kinematic fit

$\pi^0\eta$ invariant mass distributions for different rejections of $\gamma p \rightarrow p\pi^0\pi^0$ events



LH₂ data 2013

hypothesis: $\gamma p \rightarrow p_{\text{miss}} \pi^0\pi^0$
CL($\pi^0\pi^0$) anti-cut: diagonal;
hypothesis: $\gamma p \rightarrow p_{\text{miss}} \pi^0\eta$
cut: CL > 0.1

hypothesis: $\gamma p \rightarrow p_{\text{miss}} \pi^0\pi^0$
anti-cut: parallel
CL < 0.01 and factor=0.1
hypothesis: $\gamma p \rightarrow p_{\text{miss}} \pi^0\eta$
cut: CL > 0.1

kinematic fit: $\pi^0\pi^0$ rejection

Dalitz plots: $m_{p\eta}^2$ vs. $m_{p\pi^0}^2$ for different rejections of $\gamma p \rightarrow p\pi^0\pi^0$ events

LH₂ data 2013

hypothesis: $\gamma p \rightarrow p_{\text{miss}} \pi^0\pi^0$

anti-cut: parallel

CL < 0.01 and **factor=0.1**

hypothesis: $\gamma p \rightarrow p_{\text{miss}} \pi^0\eta$

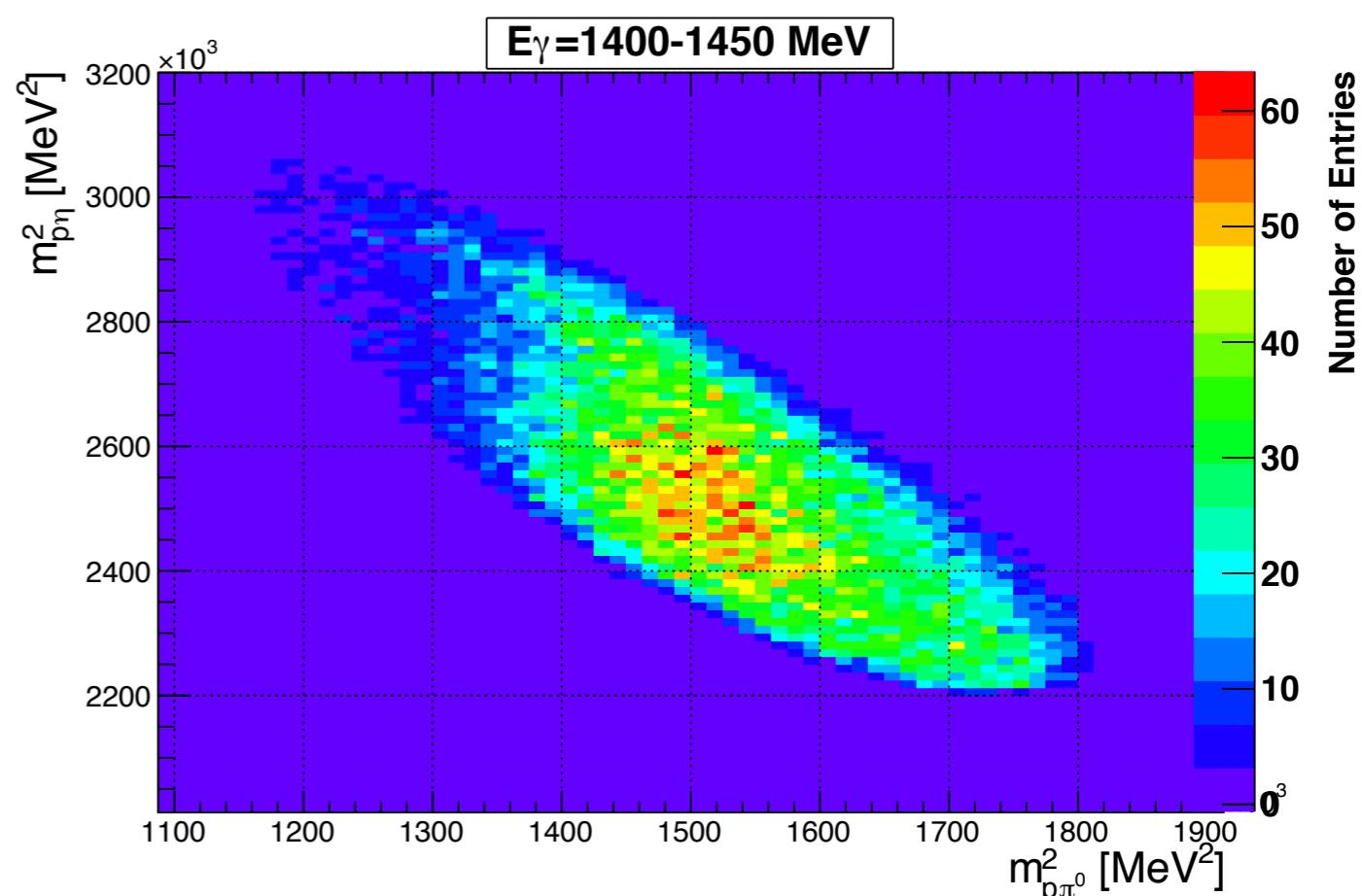
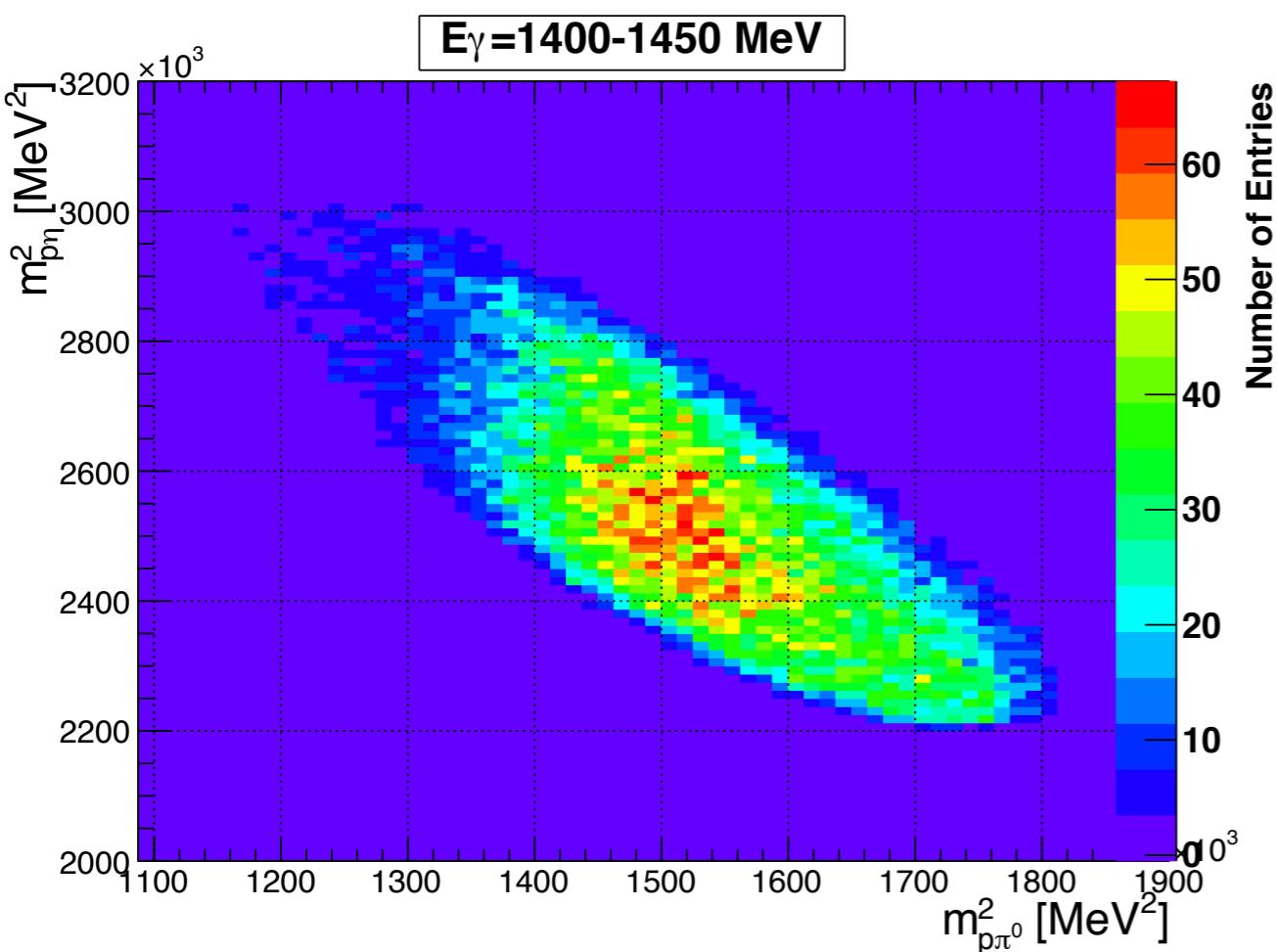
cut: CL > 0.1

hypothesis: $\gamma p \rightarrow p_{\text{miss}} \pi^0\pi^0$

CL($\pi^0\pi^0$) anti-cut: diagonal;

hypothesis: $\gamma p \rightarrow p_{\text{miss}} \pi^0\eta$

cut: CL > 0.1



“horn” events more pronounced