

Pion assisted dibaryons: $d^*(2380)$

MESON 2018, Kraków, Poland, June 2018

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- Introduction to non-strange dibaryons, from 1964 to present status report by H. Clement in *Prog. Part. Nucl. Phys.* **93** (2017) 195-242.
- Long-range dynamics of pions, nucleons & Δ 's: 3-body calculations of $N\Delta$ & $\Delta\Delta$ dibaryons by A. Gal, H. Garcilazo, *PRL* **111**, 172301 (2013) and *Nucl. Phys. A* **928** (2014) 73-88.
- Is $\Gamma_{d^*} = 80 \pm 10$ MeV ($\ll 2\Gamma_{\Delta\Delta} \approx 230$ MeV) compatible with a compact $\Delta\Delta$ dibaryon ($B_{d^*} \approx 80$ MeV)? A. Gal, *PLB* **769** (2017) 436.

Introduction

Nonstrange s-wave dibaryon SU(6) predictions
F.J. Dyson, N.-H. Xuong, PRL 13 (1964) 815

dibaryon	I	S	SU(3)	legend	mass	MESON 2018
\mathcal{D}_{01}	0	1	$\overline{10}$	deuteron	A	✓
\mathcal{D}_{10}	1	0	27	virtual	A	✓
\mathcal{D}_{12}	1	2	27	$N\Delta$	A+6B	✓
\mathcal{D}_{21}	2	1	35	$N\Delta$	A+6B	✓
\mathcal{D}_{03}	0	3	$\overline{10}$	$\Delta\Delta$	A+10B	✓
\mathcal{D}_{30}	3	0	28	$\Delta\Delta$	A+10B	?

Assuming ‘lowest’ SU(6) multiplet, 490, within 56×56 .

$M=A+B[I(I+1)+S(S+1)-2]$, $A=1878$ MeV from $M(d)\approx M(v)$.

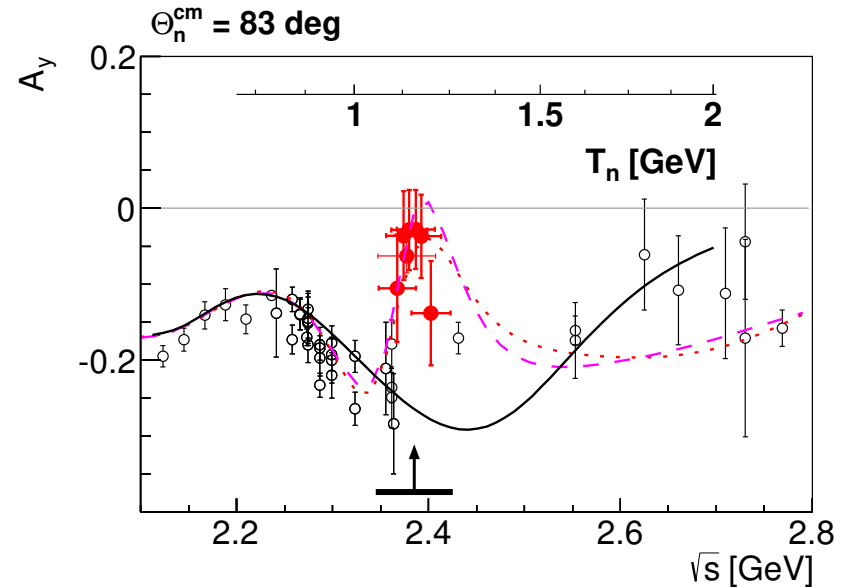
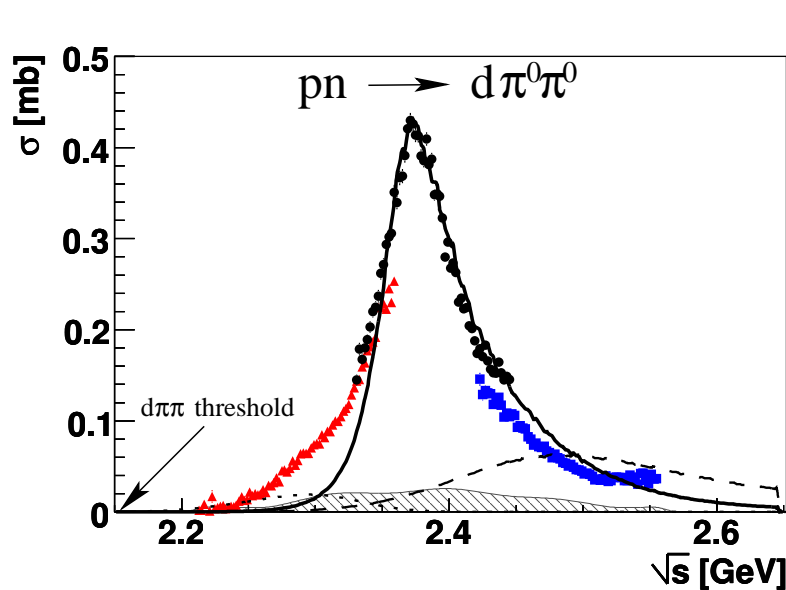
$B=47$ MeV from $M(\mathcal{D}_{12})\approx 2160$ MeV observed in $\pi^+d\rightarrow pp$.

Hence, $M(\mathcal{D}_{03})=M(\mathcal{D}_{30})\approx 2350$ MeV [$2M(\Delta)\approx 2465$ MeV].

Kamae-Fujita, PRL 38 (1977) 468, 471: proton polarization in $\gamma d\rightarrow pn$ supports a dibaryon at $M\approx 2380$ MeV.

Evidence for $\mathcal{D}_{03}(2380 \pm 10)$, $\Gamma = 80 \pm 10$ MeV

Adlarson et al. PRL 106 (2011) 242302 & 112 (2014) 202301



from $pd \rightarrow d\pi^0\pi^0 + p_s$

also in $pd \rightarrow d\pi^+\pi^- + p_s$

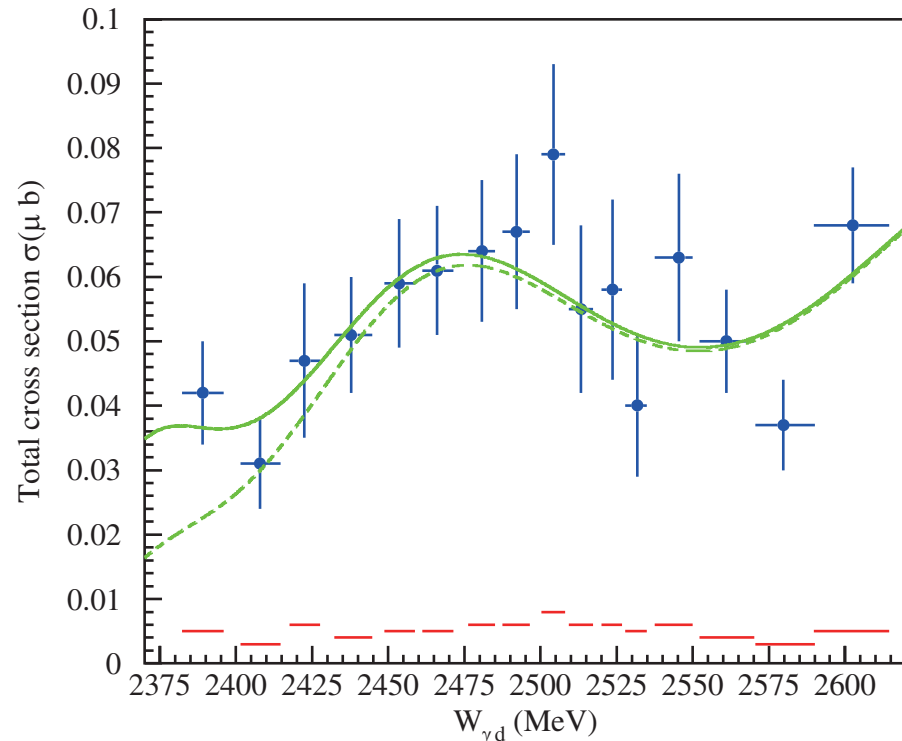
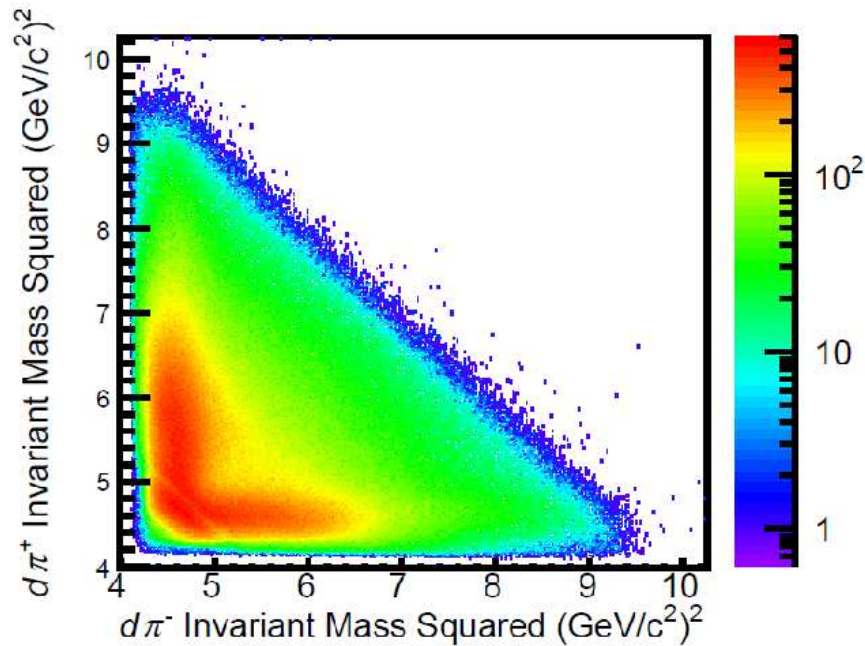
${}^3D_3 - {}^3G_3$ pn resonance

np analyzing power

SAID NN fit requires a resonance pole
WASA@COSY & SAID, PRC 90 (2014) 035204

Given $\Gamma(\Delta) \approx 120$ MeV, what makes \mathcal{D}_{03} that narrow?

Dibaryon searches in $\gamma d \rightarrow d\pi\pi$



$d\pi^+$ vs. $d\pi^-$ in $\gamma d \rightarrow d\pi^+\pi^-$
CLAS prelim. (APS 04/2015)

\mathcal{D}_{12} signal? with BW fit
(M, Γ) = (2.12, 0.125) GeV

\mathcal{D}_{12} enters in \mathcal{D}_{03} hadronic model reported below

$\sigma_{\text{tot}}(W_{\gamma d})$ in $\gamma d \rightarrow d\pi^0\pi^0$
ELPH, PLB 772 (2017) 398
& arXiv:1805.08928

\mathcal{D}_{03} signal? (2.37, 0.068)

\mathcal{D}_{12} signal? (2.15, 0.110)

Quark-based model calculations of \mathcal{D}_{03} & \mathcal{D}_{12}

M(GeV)	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	exp/phen
\mathcal{D}_{03} ($\Delta\Delta$)	2.35	2.36	2.44	2.38	≤ 2.26	2.40	2.46	2.36**	2.38
\mathcal{D}_{12} ($N\Delta$)	2.16*	2.36	–	2.36	–	–	2.17	–	≈ 2.15

1. Dyson-Xuong, PRL 13 (1964) 815; *input **postdiction.
2. Mulders-Aerts-de Swart, PRD 21 (1980) 2653.
3. 1980: Oka-Yazaki, PLB 90, 41 (2.46) Cvetič et al. 93, 489 (2.42)
4. Mulders-Thomas, JPG 9 (1983) 1159.
5. Goldman-Maltman-Stephenson-Schmidt-Wang, PRC 39 (1989) 1889.
6. ...Zhang-Shen..., PRC 60 (1999) 045203 → PRD 96 (2017) 014036.
7. Mota-Valcarce-Fernandez-Entem-Garcilazo, PRC 65 (2002) 034006.
8. Ping-Huang-Pang-Wang, PRC 79 (2009) 024001, 89 (2014) 034001.

BOTH \mathcal{D}_{12} & \mathcal{D}_{03} related correctly only by [1].

Long-range dynamics of dibaryons

A. Gal, H. Garcilazo, PRL 111, 172301 (2013)

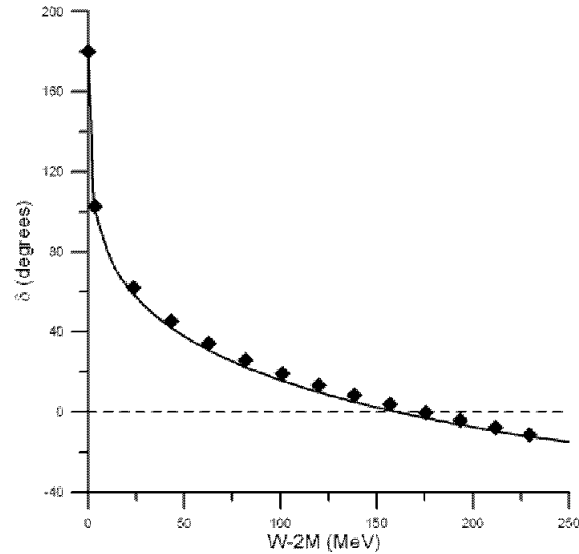
Nucl. Phys. A 928 (2014) 73-88

A. Gal, Phys. Lett. B 769 (2017) 436

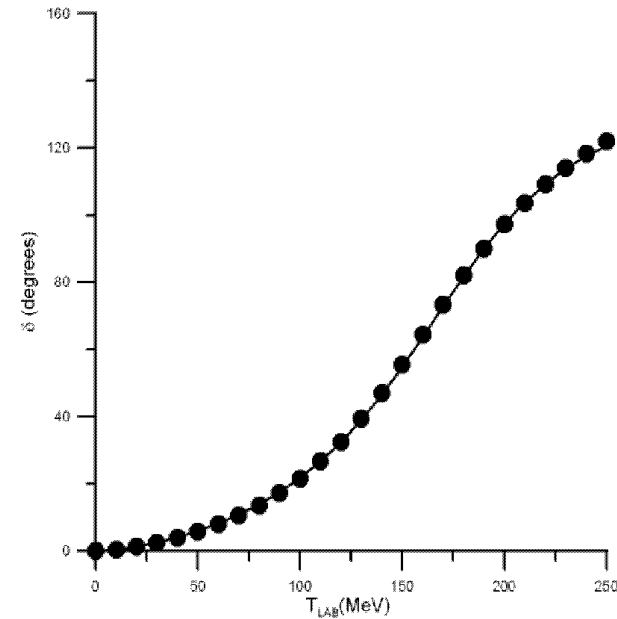
$\mathcal{D}_{12}(2150)$ $N\Delta$ dibaryon near threshold (2.17 GeV)

- Long ago established in coupled-channel $pp(^1D_2) \leftrightarrow \pi^+d(^3P_2)$ scattering & reactions. Arndt et al (1987) & Hoshizaki's (1993): $M \approx 2.15$ GeV, $\Gamma \approx 110 - 130$ MeV.
- Nonrelativistic πNN Faddeev calculation, Ueda (1982): $M = 2.12$ GeV, $\Gamma = 120$ MeV.
- CLAS $\gamma d \rightarrow d\pi^+\pi^-$ data [APS 04/2015] suggest $M_{BW} \approx 2.12$ GeV, $\Gamma_{BW} \approx 125$ MeV.
- Our relativistic-kinematics Faddeev calculation gives robust values $M \approx 2.15$ GeV, $\Gamma \approx 120$ MeV against variations of NN & πN input.

Separable potential fits to NN & πN data



fit to NN $\delta(^3S_1)$



fit to πN $\delta(P33)$

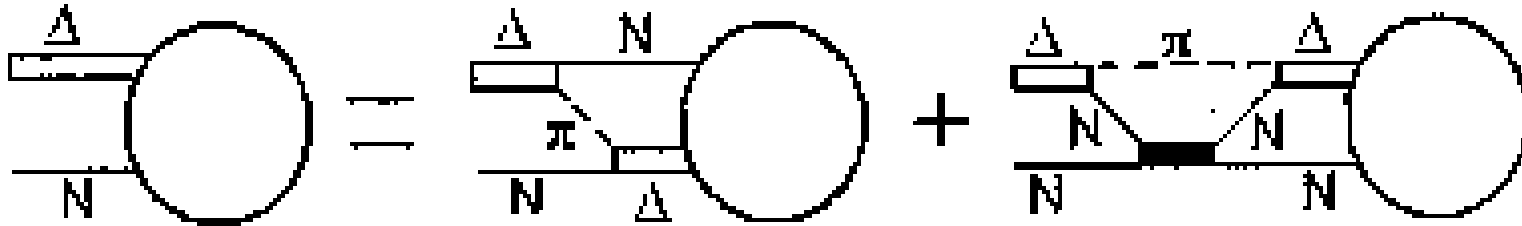
Separable s-wave potentials $v_j \Rightarrow$ separable t matrices t_j

entering πNN Faddeev equations: $T_i = t_i + t_i G_0 \sum_{j \neq i} T_j$

Solve for $I(J^P) = 1(1^+), 1(2^+), 2(1^+), 2(2^+)$

corresponding to $N\Delta$ -acceptable $I(J^P)$ values.

πNN Faddeev Equations



- For separable interactions, Faddeev equations reduce to one effective 2-body equation.

Resonance poles: $IJ = 12, 21$ (yes), $11, 22$ (no).

$W(\mathcal{D}_{12}) \approx 2153 - i65$, $W(\mathcal{D}_{21}) \approx 2167 - i67$ (MeV)

- Construct a $\mathcal{D}_{12}(2150)$ -isobar $(N\Delta)_{\ell=0}$ interaction that, coupled with $(NN)_{\ell=2}$, fits $NN \delta(^1D_2)$ & $\eta(^1D_2)$.

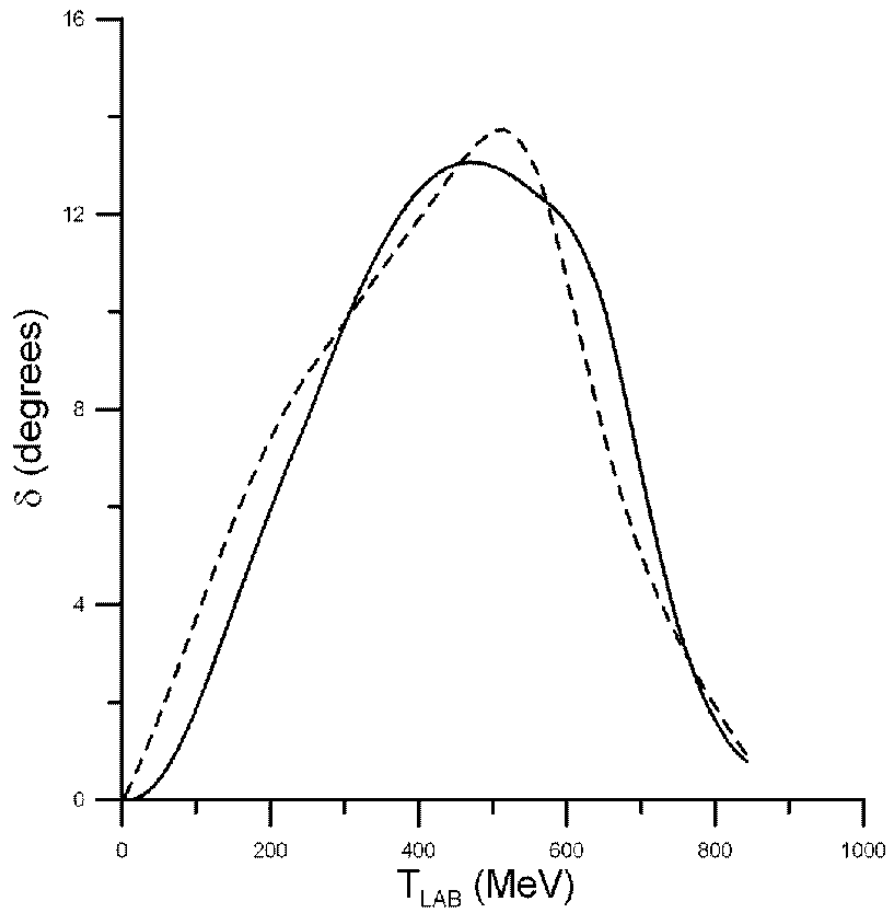
Limit cutoff momenta $\leq 3 \text{ fm}^{-1}$ to stay within

long-range physics e.g. no $\pi N \rightarrow \rho N$.

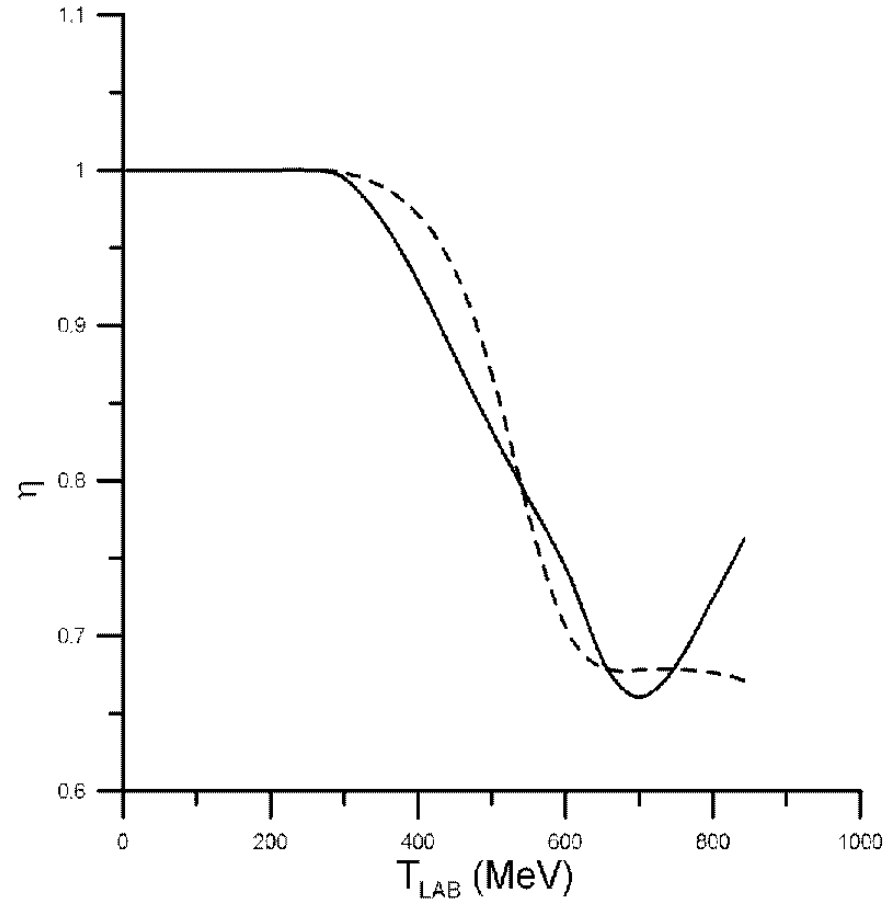
Construction of $N\Delta$ form factor

- Construct $(NN)_{\ell=2} - (NN')_{\ell=0} - (N\Delta')_{\ell=0}$ separable potential. N' -fictitious P_{13} baryon with $m_{N'} = m_{\pi} + m_N$ to generate πNN inelastic cut. Δ' -stable Δ with $m_{\Delta'} = 1232$ MeV.
- No ad-hoc pole is introduced into $(N\Delta')_{\ell=0}$.
- Require form-factor cutoff momenta ≤ 3 fm⁻¹ to be consistent with **long-range physics** e.g. no $\pi N \rightarrow \rho N$.
- Fitting NN $\delta(^1D_2)$ & $\eta(^1D_2)$ determines the $\mathcal{D}_{12}(2150)$ -isobar $(N\Delta')_{\ell=0}$ form factor.

Fitting $NN \delta(^1D_2)$ & $\eta(^1D_2)$



$NN \ ^1D_2$ phase shift fit

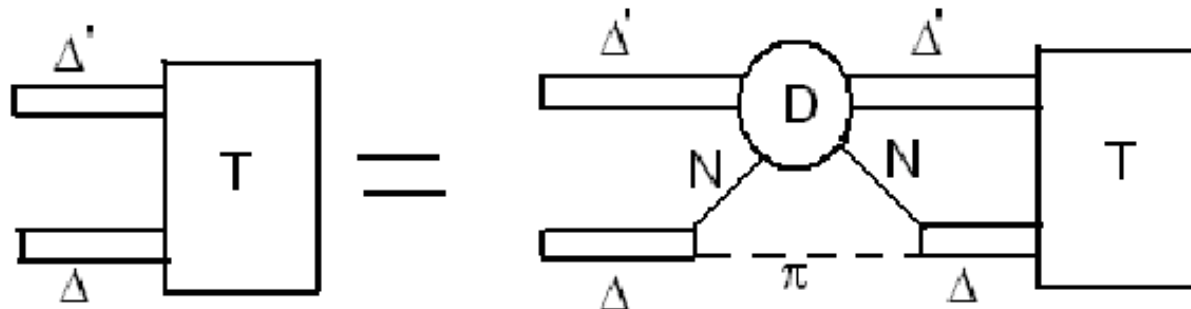


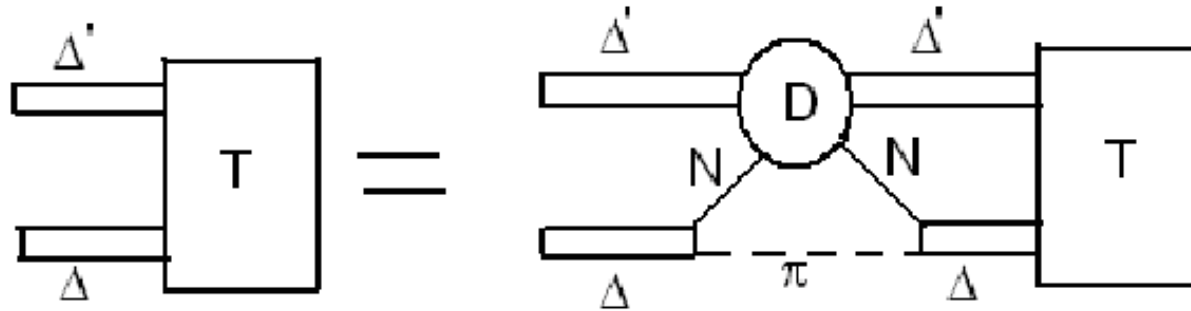
$NN \ ^1D_2$ inelasticity fit

Dashed: gwdac.phys.gwu.edu [SAID], Solid: best fit

Calculation of $\mathcal{D}_{03}(2380)$ $\Delta\Delta$ dibaryon in terms of π 's, N 's & Δ 's

- Approximate $\pi\pi NN$ problem by $\pi N\Delta'$ problem.
- Separable pair interactions: πN Δ -isobar form factor by fitting $\delta(P_{33})$; $N\Delta'$ $\mathcal{D}_{12}(2150)$ -isobar form factor by fitting $NN(^1D_2)$ scattering.
- 3-body S -matrix pole equation reduces to effective $\Delta\Delta'$ diagram:





- Searching numerically for S -matrix resonance poles by going complex, $q_j \rightarrow q_j \exp(-i\phi)$, thus opening sections of the unphysical Riemann sheet to accommodate poles of the form $W = M - i\Gamma/2$.
- In the πN propagator, where Δ' is a spectator, replace real mass $m_{\Delta'}=1232$ MeV by Δ -pole complex mass $m_{\Delta}=1211-i49.5 \times (2/3)$ MeV, **x=2/3** accounting for quantum-statistics correlations for decay products of two $I(JP)=0(3+)$ Δ 's, assuming s -wave decay nucleons.

Results & Discussion

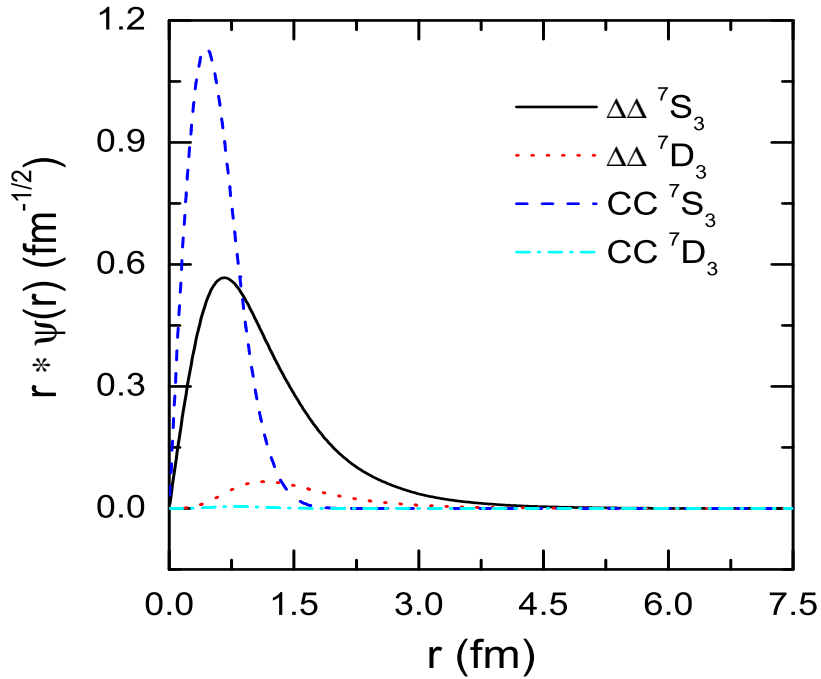
- Using a 1.36 fm sized P_{33} form factor:
 $M=2383$, $\Gamma=82$ MeV ($x=1$: 94 MeV)
in good agreement with WASA@COSY.
- Although bound w.r.t. $\Delta\Delta$, $\mathcal{D}_{03}(2380)$ is resonating w.r.t. the $\pi - \mathcal{D}_{12}(2150)$ threshold. The subsequent decay $\mathcal{D}_{12}(2150) \rightarrow \pi d$ is seen in the πd Dalitz plot projection.
- NN -decoupled dibaryon resonances \mathcal{D}_{21} & \mathcal{D}_{30} predicted 10–30 MeV higher, respectively; Bashkanov-Brodsky-Clement, PLB 727 (2013) 438, discuss effects of Hidden-Color (CC) BB components: $\sqrt{1/5}\Delta\Delta + \sqrt{4/5}\text{CC}$.
Effect of CC on width calculation?

Recent Quark Model $d^*(2380)$ Calculations

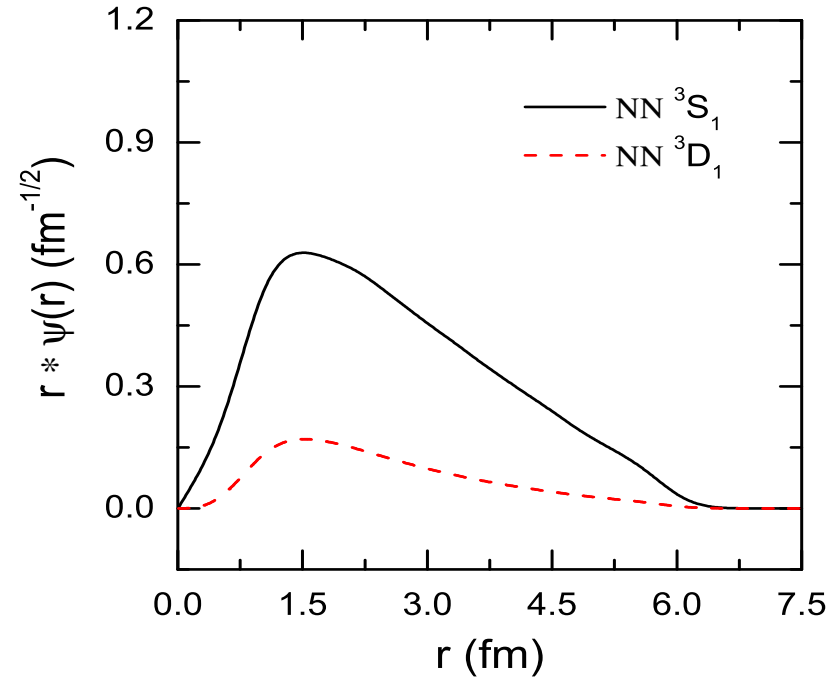
- Park-Park-Lee, PRD 92 (2015) 014037, find the orbitally symmetric $[6] I(JP)=0(3+)$ hexaquark **unbound** by hundreds of MeV.
- H. Huang et al., PRC 89 (2014) 034001, use the Salamanca chiral quark model (**CQM**) to go from $1 \rightarrow 4$ $\Delta\Delta$ channels, then to full 10:
 $M = 2425 \rightarrow 2413 \rightarrow 2393$ MeV
 $\Gamma = 177 \rightarrow 175 \rightarrow 150$ MeV, so Γ is too big.
- Beijing **CQM** [Y. Dong et al. PRC 94 (2016) 014003] finds $M \approx 2400 \pm 20$ MeV & 67% non-decaying CC components, leading to **$\Gamma \approx 70$ MeV.**
A dubious calculation, as discussed below.

Quark-based $\Delta\Delta$ w.f. & deuteron w.f.

arXiv 1408.0458, Chin. Phys. C 39 (2015) 071001



$\Delta\Delta$ wavefunction



deuteron wavefunction

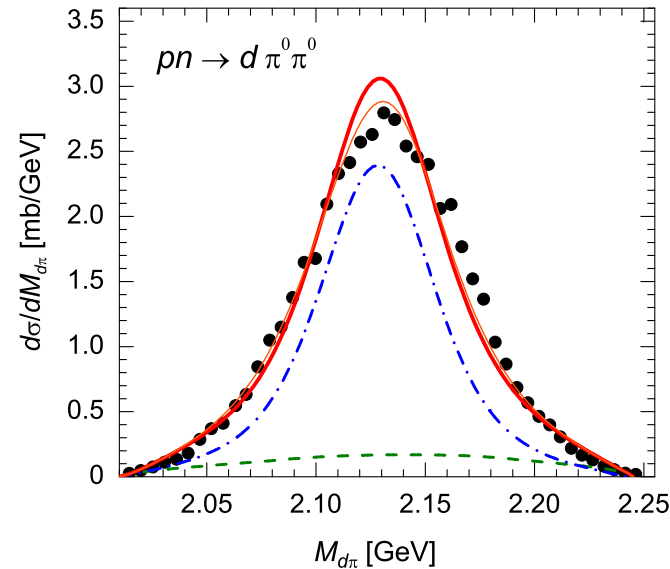
- r.m.s. radius $R(\Delta\Delta)=0.76$ fm \ll $R(\text{deuteron})\approx 2$ fm.
- Small $R(\Delta\Delta)$ implies high Δ -momentum components.

Width Considerations

- $d^*(2380)$ is bound w.r.t. $\Delta\Delta$ by 84 MeV, by 42 MeV on average for each Δ , thereby reducing $\Gamma_{\Delta}^{\text{free}}=115$ MeV to $\Gamma_{\Delta}^{\text{bound}}=81$ MeV.
- However, since none of the Δ s is at rest, $s_{\Delta\Delta}^{\text{bound}}$ decreases further to $(1232-42)^2 - P_{\Delta\Delta}^2$, where $P_{\Delta\Delta} \times R_{\Delta\Delta} \geq 3/2$.
- For $R_{\Delta\Delta} \leq 0.8$ fm, $\Gamma_{\Delta}^{\text{bound}} \leq 34$ MeV, so for the $\pi\pi$ decay modes $\Gamma_{\Delta\Delta}^{\text{bound}} = 5/3 \Gamma_{\Delta}^{\text{bound}} \leq 56$ MeV.
- With $R_{\Delta\Delta}=0.76$ fm, as in the Beijing CQM, $\Gamma_{\Delta\Delta}^{\text{bound}} \leq 47$ MeV, hence quark-based $\Delta\Delta$ models can't reproduce the **LARGE** $d^*(2380)$ width.
- See also J.A. Niskanen, PRC 95 (2017) 054002.

Introducing a $\pi\mathcal{D}_{12}$ component (I)

A. Gal, PLB 769 (2017) 436

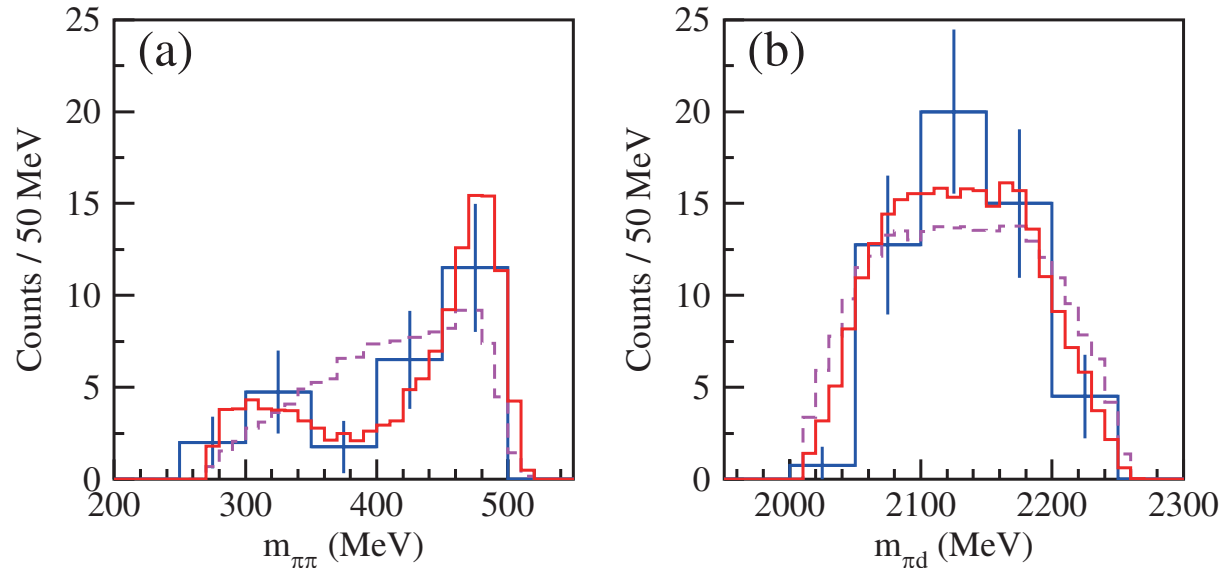


$M_{d\pi}$ decay distribution of $d^*(2380)$ for 2 input choices of \mathcal{D}_{12}

M.N. Platonova & V.I. Kukulin, NPA 946 (2016) 117

- The $\mathcal{D}_{12}(2150)$ $N\Delta$ dibaryon is seen in $d^*(2380)$ decay. With size ~ 2 fm, its ~ 100 MeV pionic decay width is not quenched within the $d^*(2380)$.

Introducing a $\pi\mathcal{D}_{12}$ component (II)



Invariant mass distributions at $W=2.39$ GeV
ELPH, PLB 772 (2017) 398

Lower bump in (a), known as **ABC effect**,
is due to $\Delta\Delta$ decay, with reduced $\Delta \rightarrow N\pi$ phase space.
Upper bump in (a) is due to $d^*(2380) \rightarrow \mathcal{D}_{12}(2150)\pi$ decay,
where the $N\Delta$ dibaryon pionic decay width ~ 100 MeV
in (b) is not quenched owing to its large size ~ 2 fm.

This compensates for the $\Delta\Delta$ quenched width.

d*(2380) decay widths (MeV) & branching ratios (BR,%)

final state	$\Delta\Delta$ ($\alpha = 1$)		$\pi\mathcal{D}_{12}$ ($\alpha = 0$)		mixed ($\alpha = \frac{5}{7}$)		exp.
	$\Gamma_f^{d^*}$	BR	$\Gamma_f^{d^*}$	BR	$\Gamma_f^{d^*}$	BR	BR
$d\pi^0\pi^0$	9.3	12.4	7.6	10.1	8.4	11.2	14(1)
$d\pi^+\pi^-$	17.0	22.7	14.0	18.6	15.3	20.4	23(2)
$pn\pi^0\pi^0$	9.7	12.9	7.9	10.5	8.7	11.6	12(2)
$pn\pi^+\pi^-$	21.7	28.9	17.2	22.9	19.3	25.8	30(5)
$pp\pi^-\pi^0$	4.15	5.55	2.9	3.9	3.55	4.7	6(1)
$nn\pi^+\pi^0$	4.15	5.55	2.9	3.9	3.55	4.7	6(1)
$NN\pi$	—	—	11.5	15.4	6.2	8.3	(≤ 9)
NN	9	12	11	14.7	10	13.3	12(3)
total	75	100	75	100	75	100	103

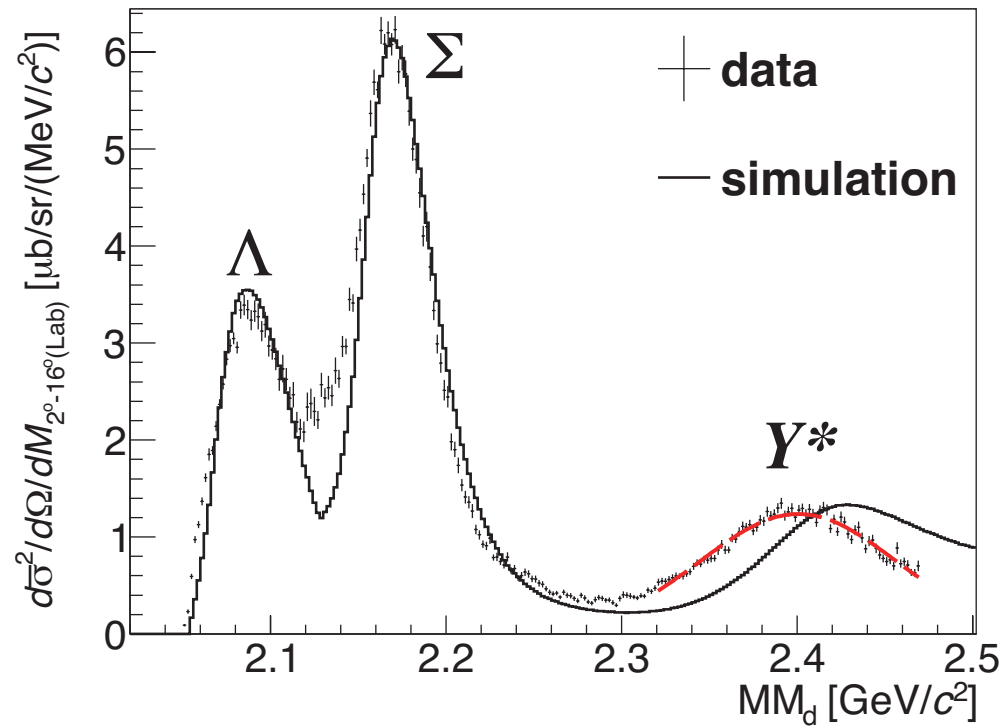
$$\alpha\Gamma_{NN\pi\pi}^{\Delta\Delta} + (1 - \alpha)\Gamma_{NN\pi\pi}^{\pi\mathcal{D}_{12}} = \Gamma_{NN\pi\pi}^{d^*}$$

$$\Gamma_{NN\pi\pi}^{\Delta\Delta} = 44 \text{ \& } \Gamma_{NN\pi\pi}^{\pi\mathcal{D}_{12}} = 100 \text{ for } \Gamma_{NN\pi\pi}^{d^*} = 60 \text{ MeV } \Rightarrow \alpha = \frac{5}{7}$$

Summary

- The two experimentally established nonstrange dibaryons $\mathcal{D}_{12}(2150)$ & $\mathcal{D}_{03}(2380)$ are derived quantitatively with **long-range hadronic physics** guidelines using pions, nucleons & Δ s input.
- Search for NN -decoupled \mathcal{D}_{21} & \mathcal{D}_{30} dibaryons.
- The $d^*(2380)$ is a $\Delta\Delta$ bound state embedded in the $\pi\mathcal{D}_{12}(2150)$ continuum. This is crucial for understanding its **LARGE** width.
- $\Delta(1232) \rightarrow \Sigma(1385)$ for strange dibaryons?
 $\Sigma(1385)N$ ($I = \frac{3}{2}, 2^+$) vs. $\Lambda(1405)N$ ($I = \frac{1}{2}, 0^-$).
- $\pi\Lambda_c N$ ($I = \frac{3}{2}, 2^+$) Gal..., PRD 90 (2014) vs.
 DNN ($I = \frac{1}{2}, 0^-$) ...Oset, PRC 86 (2012)].

Addendum: J-PARC E27 $d(\pi^+, K^+)$ missing-mass spectrum



Y^* quasi-free peak shifted by ≈ -22 MeV,
indicating Y^*N attraction [$Y^* = \Sigma(1385)$ & $\Lambda(1405)$].

Two dibaryons below K^-pp threshold?

(i) deep Σ^*N , E27 (ii) shallow Λ^*N , E15.

$\Lambda(1405)N$ & $\Sigma(1385)N$ dibaryons?

- $\Lambda(1405)N$ is a doorway to an $I=1/2, J^P=0^-$ $\bar{K}NN$, found quasibound in all calculations. Its lower components are $\pi\Lambda N$ and $\pi\Sigma N$, but $\pi\Lambda N$ cannot support any strongly attractive meson-baryon s-wave interaction.
- The $\pi\Lambda N$ system can benefit from strong meson-baryon p -wave interactions fitted to $\Delta(1232) \rightarrow \pi N$ and $\Sigma(1385) \rightarrow \pi\Lambda$ form factors. Maximize isospin and angular momentum couplings by full alignment: $I=3/2, J^P=2^+$, Good example of a **Pion Assisted Dibaryon**, not Oka's $I=1/2, J^P=2^+$ CM-based candidate. Gal-Garcilazo, NPA 897 (2013) 167 & Refs. therein.

- A $\pi\Lambda N - \pi\Sigma N$ resonance about 10–20 MeV below the $\pi\Sigma N$ threshold is found by solving coupled-channel Faddeev equations. The resonance energy is **sensitive** to the pion-baryon p -wave form factors.
- Expect doorway states $\Sigma(1385)N$ and $\Delta(1232)Y$, the lower of which is $\Sigma(1385)N$ with $I=3/2$, $J^P=2^+$. These are different from $I=1/2$, $J^P=0^-$ assigned to $\Lambda(1405)N$, viewed as a doorway to $\bar{K}NN$.
- Adding a $\bar{K}NN$ channel does not help, because the leading 3S_1 NN configuration is Pauli forbidden.
- Search for this \mathcal{Y} dibaryon **at GSI & J-PARC** in:
 $p + p \rightarrow \mathcal{Y}^{++} + K^0$, $\mathcal{Y}^{++} \rightarrow \Sigma^+ + p$,
or $\pi^+ + d \rightarrow \mathcal{Y}^{++} + K^0$, $\mathcal{Y}^{++} \rightarrow \Sigma^+ + p$.
- A (π^+, K^+) reaction as in E27 would lead to YN decay states similar to those expected in searches of K^-pp .
Another possibility at J-PARC or GSI is:
 $\pi^- + d \rightarrow \mathcal{Y}^- + K^+$, $\mathcal{Y}^- \rightarrow \Sigma^- + n$.