

Triangle Singularity Enhancing Isospin Violation in

$D_s^+ \rightarrow \pi^+ \pi^0 f_0(980)$ and $\bar{B}_s^0 \rightarrow J/\psi \pi^0 f_0(980)$ Decays

Wei-Hong Liang

Guangxi Normal University, Guilin, China

Meson 2018

7-12 June 2018, Krakow, Poland

Based on: WHL, S. Sakai, J.J. Xie, E. Oset, CPC 42(2018)044101;
S. Sakai, E. Oset, WHL, PRD96 (2017) 074025.

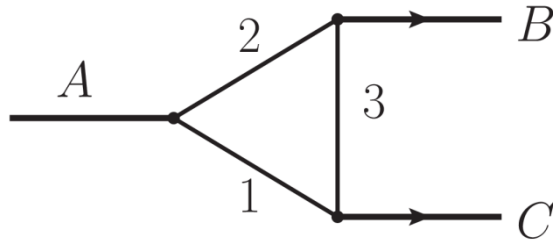
Outline

- Introduction and motivation
- Formalism
- Results and discussions
- Summary

◆ Introduction and motivation

- Triangle singularity (TS) in a reaction

$$A \rightarrow B + C$$



[Landau, Nucl. Phys. 13(1959)181]

[Coleman, Norton, Nuovo Cim. 38 (1965)438]

[Bayar, Aceti, Guo, Oset, PRD 94 (2016)074039]

When all the intermediate particles are placed on-shell and collinear in the rest frame of A , a singularity in the decay amplitude T develops.

If the internal particles have zero width, $|T| \rightarrow \infty$;

If the internal particles have non-zero width, $|T|$ turns into a finite peak.

TS \Rightarrow $\left\{ \begin{array}{l} \text{simulating a resonance;} \\ \text{providing a mechanism for the production} \\ \text{of particular modes in reactions;} \\ \dots \end{array} \right.$

Examples:

- ✓ The $a_1(1420)$ resonance, claimed by COMPASS, would not be a real state but the effect of TS in $a_1(1260) \rightarrow \pi f_0(980)$; COMPASS, PRL115(2015)082001; X.H. Liu, M. Oka, Q. Zhao, PLB753(2016)297;
- ✓ $f_1(1420)$ corresponds to TS in $f_1(1285) \rightarrow \pi f_0(980)$; Debastiani, Aceti, WHL, Oset, PRD95(2017)034015;
- ✓ $f_2(1810)$ peak comes from TS involving $K^* \bar{K}^*$ production; Xie, Geng, Oset, PRD95(2017)034004;

...

◆ Introduction and motivation

• $f_0(980)$ - $a_0(980)$ mixing and isospin violation

A recurrent topic shedding further light into the internal structure of $f_0(980)$ and $a_0(980)$.

Examples:

- ✓ The large isospin violation in $\eta(1405) \rightarrow \pi^0 f_0(980)$ is due to a TS;

BESIII, PRL108(2012)182001;

J.J. Wu, X.H. Liu, Q. Zhao, B.S. Zou, PRL108(2012)081803;

F. Aceti, WHL, E. Oset, B.S. Zou, PRD86(2012)114007;

- ✓ The isospin violation in $f_1(1285) \rightarrow \pi^0 f_0(980)$, $\pi^0 a_0(980)$ was studied theoretically, and was confirmed later in a BESIII experiment.

Aceti, Dias, Oset, EPJA51(2015)48;

BESIII, PRD92(2015)012007;

◆ Introduction and motivation

- **The purpose of our work:**

To search for TS enhanced isospin-violating reactions producing the $f_0(980)$ and $a_0(980)$ resonances, to show the isospin violation as a function of the initial energy.

The selected reactions:

$$D_s^+ \rightarrow \pi^+ \pi^0 a_0(980) (f_0(980)),$$
$$\bar{B}_s^0 \rightarrow J/\psi \pi^0 a_0(980) (f_0(980))$$

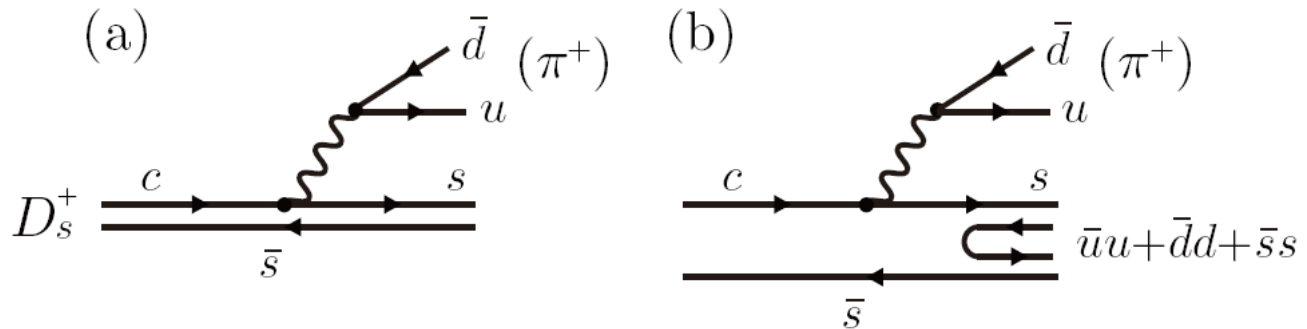
The $a_0(980)$ production mode is isospin-allowed, while the $f_0(980)$ production mode is isospin-forbidden.

Based on the notion that the $a_0(980)$ and $f_0(980)$ are generated from the interaction of pseudoscalar mesons, the results obtained will be tied to the molecular picture of the low lying scalar mesons.

◆ Formalism (for $D_s^+ \rightarrow \pi^+ \pi^0 a_0(980)(f_0(980))$)

A. The $D_s^+ \rightarrow \pi^+ K^0 \bar{K}^{*0}$ reaction

Basic diagram at the quark level:



The hadronization produces a K and an anti-K*:

$$s\bar{s}(\bar{u}u + \bar{d}d + \bar{s}s) = K^+ K^{*-} + K^0 \bar{K}^{*0} + \dots,$$

where “...” indicate terms in η, η' which play no role in the reaction that we study.

$$\frac{d\Gamma_{D_s^+ \rightarrow \pi^+ K^+ K^{*-}}}{dM_{\text{inv}}(K^+ K^{*-})} = \frac{1}{(2\pi)^3} \frac{p_{\pi^+} \tilde{p}_{K^{*-}}}{4m_{D_s^+}^2} C^2 p_{\pi^+}'^2,$$

C is a common factor containing contributions from weak vertex, determined by fitting the experimental data for $\text{BR}(D_s^+ \rightarrow \pi^+ K^{*-} K^+)$

B. The $D_s^+ \rightarrow \pi^+ \pi^0 a_0(980)(f_0(980))$ reaction

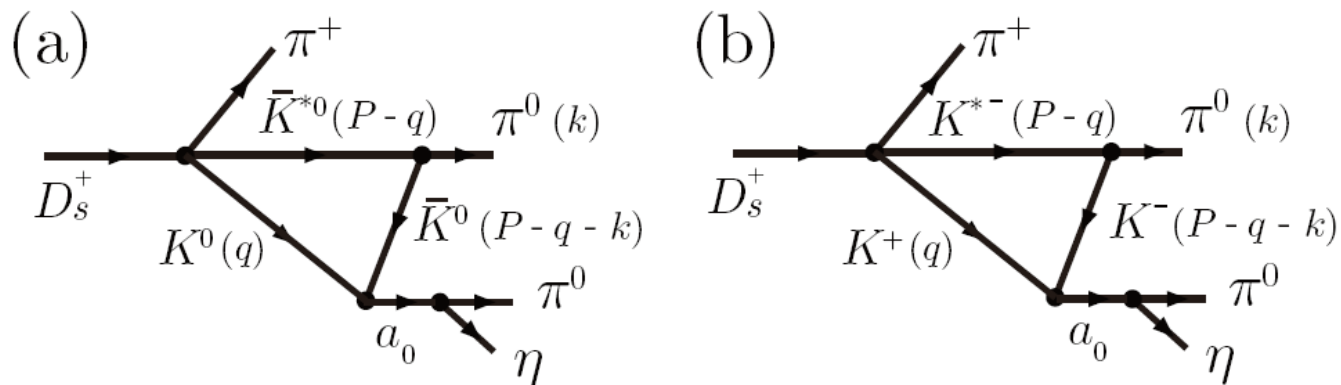


FIG. 2: Triangle mechanism which produces $\pi^+ \pi^0 a_0(980)$. The $\pi^+ \pi^0 f_0(980)$ channel could be seen replacing $\pi^0 \eta$ by $\pi^+ \pi^-$ at the end. The momenta of the particles are given in the brackets.

The double differential mass distribution for $D_s^+ \rightarrow \pi^+ \pi^0 a_0(980)$ decay

$$\frac{d^2\Gamma}{dM_{\text{inv}}(\pi^0 a_0)dM_{\text{inv}}(\pi^0 \eta)} = \frac{1}{(2\pi)^5} \frac{p_{\pi^+} k \tilde{p}_\eta}{4m_{D_s^+}^2} |t'_{\text{eff}}|^2,$$

$$|t'_{\text{eff}}|^2 = \frac{1}{6} C^2 g^2 p_{\pi^+}^2 k^2 \left| t_T(K^0 \bar{K}^0 \bar{K}^{*0}) t_{K^0 \bar{K}^0, \pi^0 \eta} - t_T(K^+ K^- K^{*-}) t_{K^+ K^-, \pi^0 \eta} \right|^2.$$

$$t_T = i \int \frac{d^4q}{(2\pi)^4} \frac{1}{q^2 - m_{K^0}^2 + i\epsilon} \frac{1}{(P - q)^2 - m_{\bar{K}^{*0}}^2 + i\epsilon} \cdot \frac{1}{(P - q - k)^2 - m_{\bar{K}^0}^2 + i\epsilon} \left(2 + \frac{\vec{q} \cdot \vec{k}}{k^2} \right) \quad (14)$$

For the case of $f_0(980)$ production, we use the same formula, substituting $\pi^0 \eta$ in T matrices by $\pi^+ \pi^-$.

◆ Formalism (for $\bar{B}_s^0 \rightarrow J/\psi \pi^0 a_0(980)(f_0(980))$)

A. The $\bar{B}_s^0 \rightarrow \pi^+ K^{*0} \bar{K}^0$ decay

Basic diagram at the quark level:

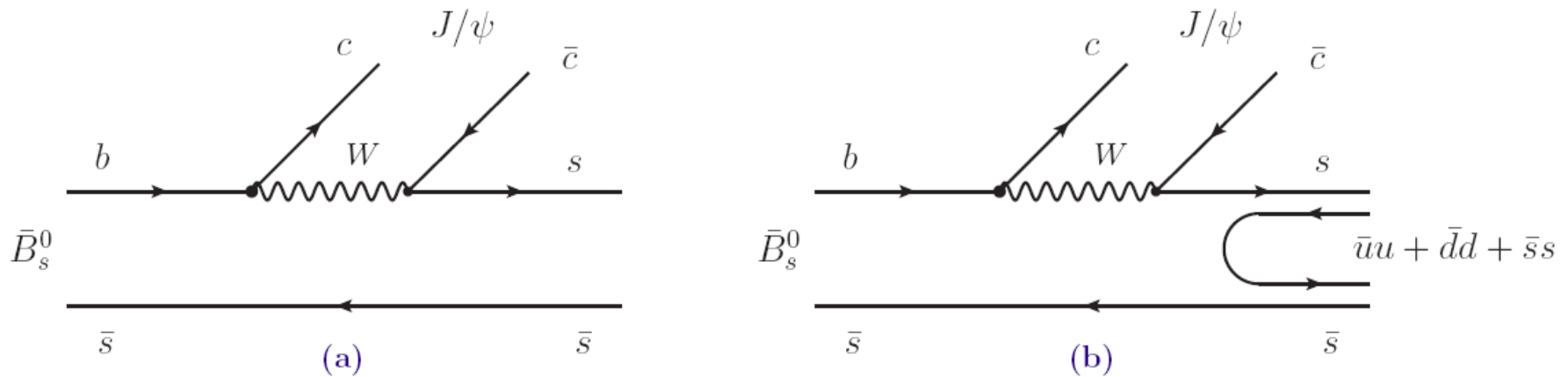
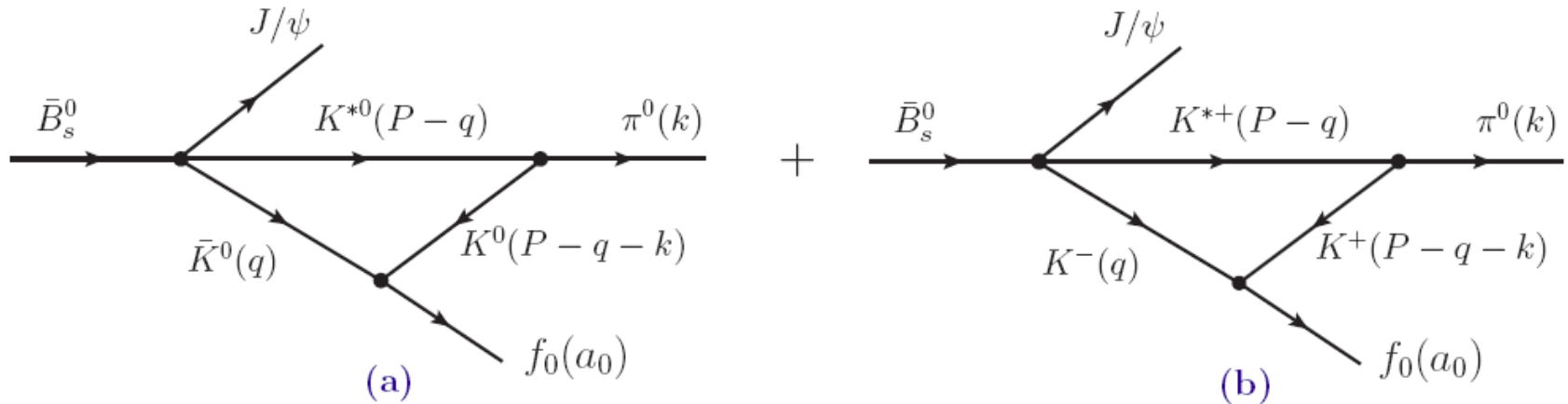


FIG. 1. Diagrammatic representation of $\bar{B}_s^0 \rightarrow J/\psi(c\bar{c})s\bar{s}$ at the quark level.

◆ Formalism (for $\bar{B}_s^0 \rightarrow J/\psi\pi^0 a_0(f_0(980))$)

B. The triangle diagram mechanism for $\bar{B}_s^0 \rightarrow J/\psi\pi^0 f_0(a_0)$



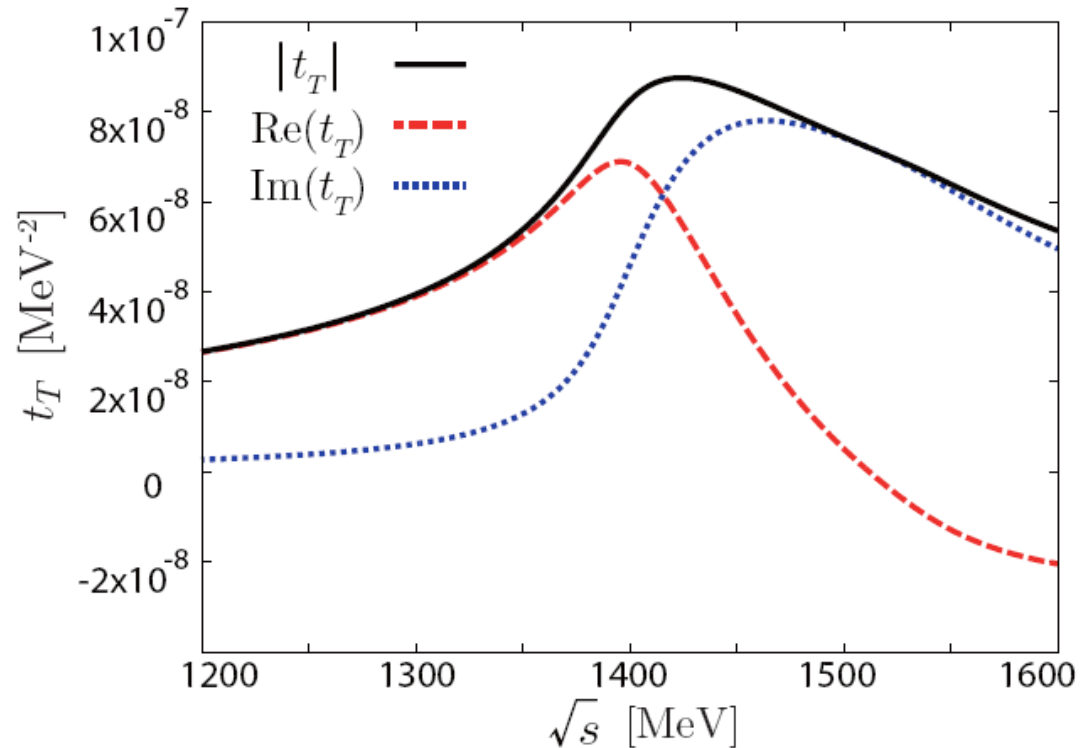
The formulas for $\bar{B}_s^0 \rightarrow J/\psi\pi^0 a_0(f_0(980))$ can be obtained in a similar way.

◆ Results (for $D_s^+ \rightarrow \pi^+ \pi^0 a_0(980)(f_0(980))$)

The results of t_T as a function of $\sqrt{s} \equiv m_{\text{inv}}(\pi^0 a_0)$ taking for $m_{\text{inv}}(\pi^0 \eta)$ ($m_{\text{inv}}(\pi^+ \pi^-)$) the value of 980 MeV.

$|t_T|$ has a broad bump around 1420 MeV.

Its origin is the TS developed by the amplitude.

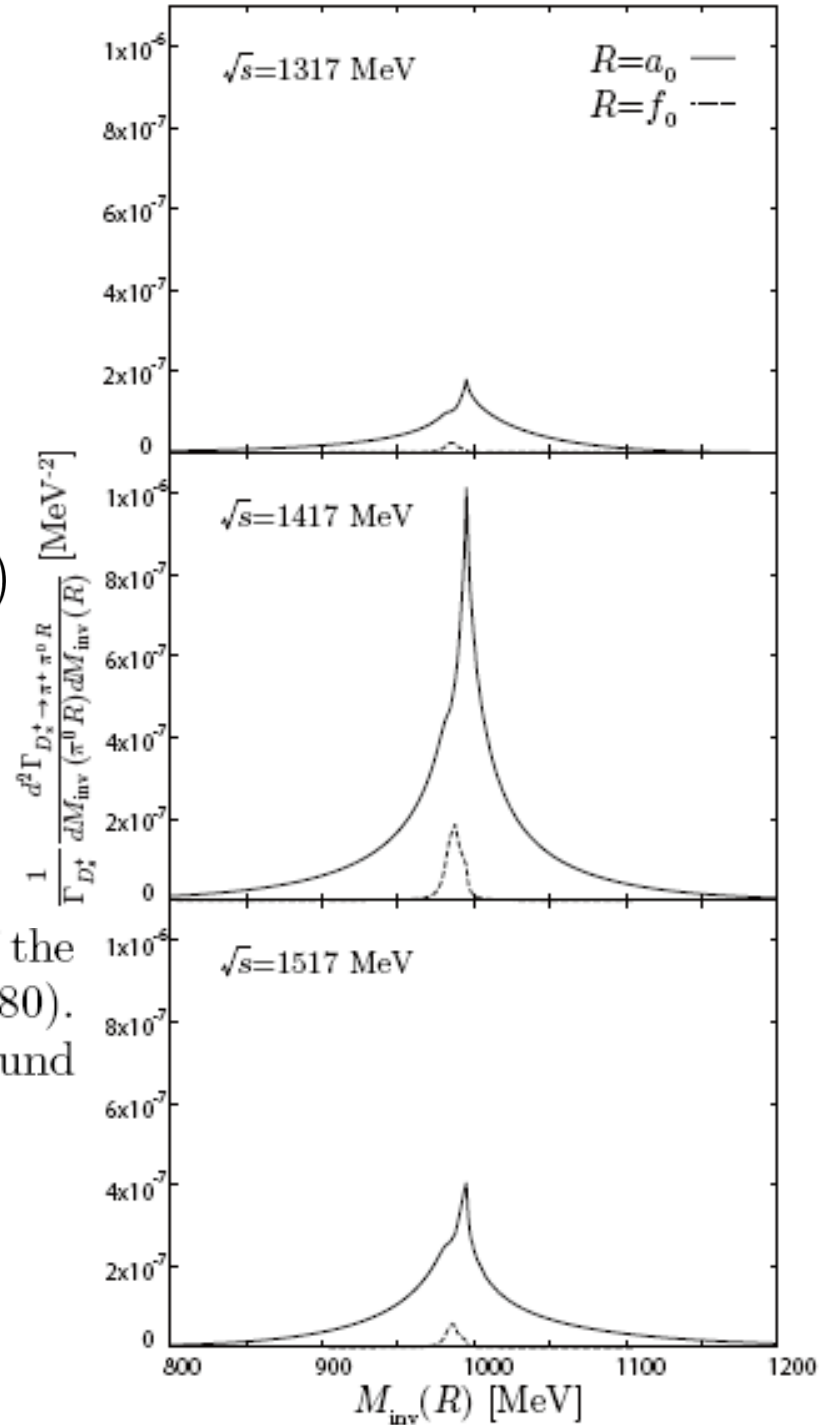


$$\frac{d^2\Gamma_{D_s^+ \rightarrow \pi^+ \pi^0 \pi^0 \eta}}{dM_{\text{inv}}(\pi^0 a_0) dM_{\text{inv}}(\pi^0 \eta)} \frac{1}{\Gamma_{D_s^+}} \quad \text{and}$$

$$\frac{d^2\Gamma_{D_s^+ \rightarrow \pi^+ \pi^0 \pi^+ \pi^-}}{dM_{\text{inv}}(\pi^0 f_0) dM_{\text{inv}}(\pi^+ \pi^-)} \frac{1}{\Gamma_{D_s^+}} \quad \text{as}$$

functions of $M_{\text{inv}}(\pi^0 \eta)$ or $M_{\text{inv}}(\pi^+ \pi^-)$

as 1317, 1417 and 1517 MeV.



The ratio of f_0 to a_0 production is strongly dependent on the $\pi^0 R$ invariant mass.

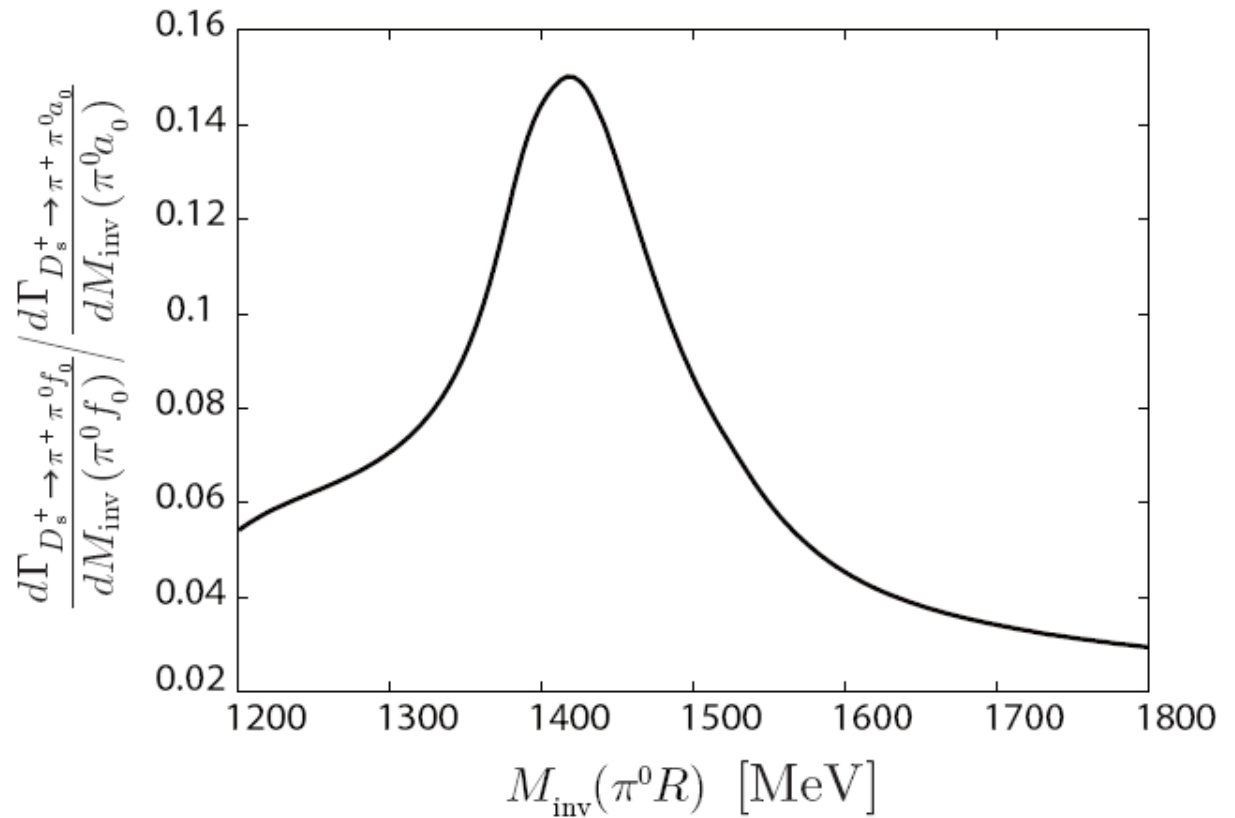


FIG. 6: Ratio of $d\Gamma/dM_{\text{inv}}(\pi^0 a_0)$ and $d\Gamma/dM_{\text{inv}}(\pi^0 f_0)$ as a function of $M_{\text{inv}}(\pi^0 R)$ ($R = f_0, a_0$).

TS acts as a magnifier for the isospin-violating $\pi^0 f_0$ production process.

Finally, we would like to give numbers for the integrated rates of $\pi^+\pi^0 f_0$ and $\pi^+\pi^0 a_0$ production by integrating $d\Gamma/dM_{\text{inv}}(\pi^0 R)$ in the range of invariant masses

We find the numbers

$$\begin{aligned} \text{BR}(D_s^+ \rightarrow \pi^+\pi^0 f_0) &= (4.91 \pm 0.46) \times 10^{-4}, \\ \text{BR}(D_s^+ \rightarrow \pi^+\pi^0 a_0) &= (3.85 \pm 0.36) \times 10^{-3}. \end{aligned} \quad (20)$$

- The rates obtained are within present measurable range;
- Experimental measurement for this reaction will bring further light into the issue of $f_0(980)$ - $a_0(980)$ mixing and the nature of the low lying scalar mesons.

◆ Results (for $\bar{B}_s^0 \rightarrow J/\psi \pi^0 a_0(980)(f_0(980))$)

The TS is expected to appear at

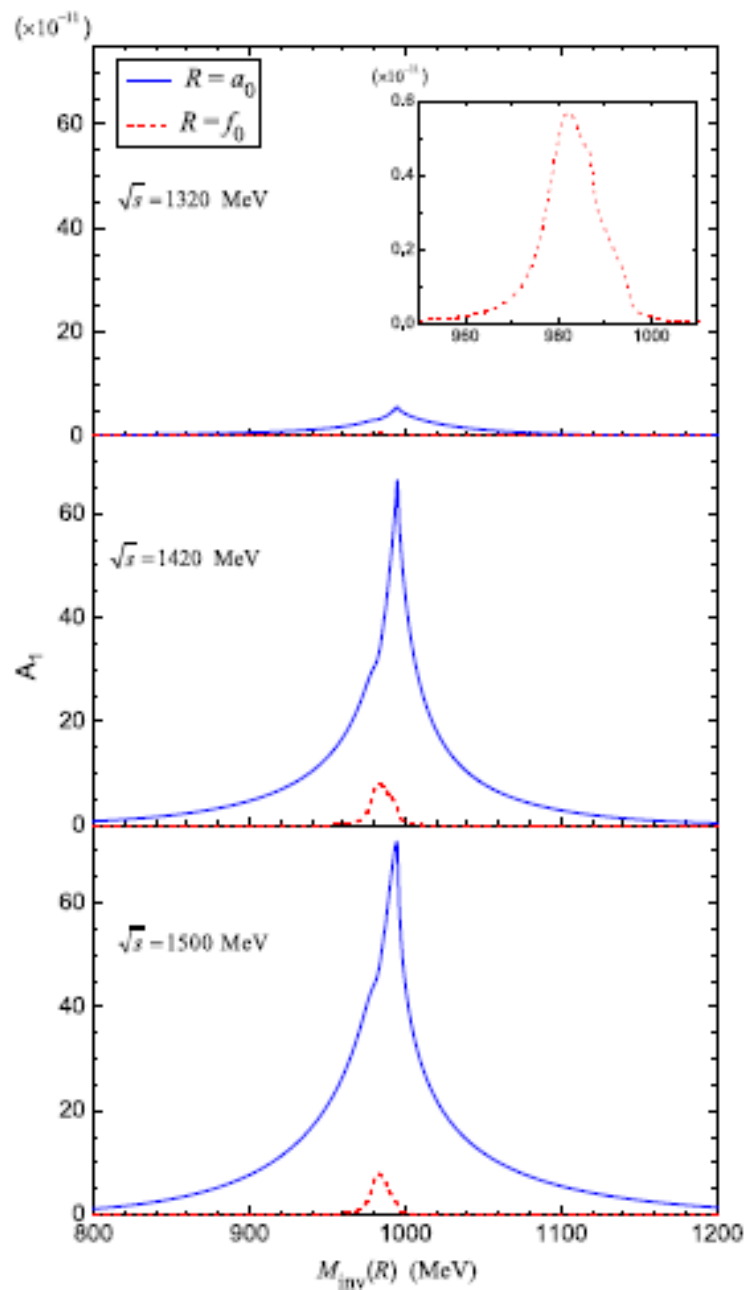
$$M_{\text{inv}}(\pi^0 a_0) \text{ or } M_{\text{inv}}(\pi^0 f_0) \simeq 1424 \text{ MeV}.$$

The double mass distribution as a

function of M_R (i.e. $M_{\text{inv}}(\pi^0 \eta)$

or $M_{\text{inv}}(\pi^+ \pi^-)$) for fixed values of

$M_{\text{inv}}(\pi^0 a_0)$ or $M_{\text{inv}}(\pi^0 f_0)$.



The ratio also peaks around the mass of the TS.

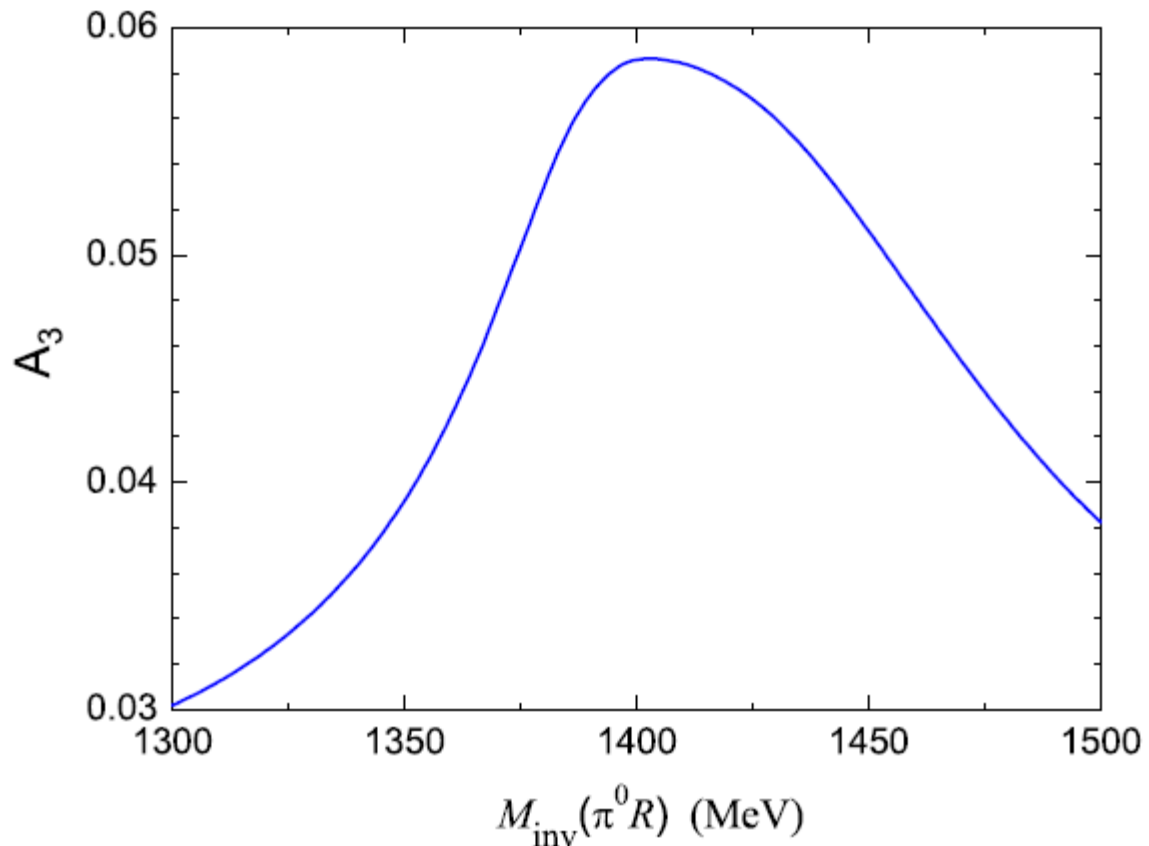


Fig. 6. (color online) Ratio of $d\Gamma/dM_{\text{inv}}(\pi^0 a_0)$ and $d\Gamma/dM_{\text{inv}}(\pi^0 f_0)$ as a function of $M_{\text{inv}}(\pi^0 R)$ ($R = f_0, a_0$). Note: in this figure, the label of the longitudinal axis is $A_3 = \frac{d\Gamma_{B_s^0 \rightarrow J/\psi \pi^0 f_0}}{dM_{\text{inv}}(\pi^0 f_0)} / \frac{d\Gamma_{B_s^0 \rightarrow J/\psi \pi^0 a_0}}{dM_{\text{inv}}(\pi^0 a_0)}$.

We estimate the total rate for $\bar{B}_s^0 \rightarrow J/\psi\pi^0 f_0$ and $\bar{B}_s^0 \rightarrow J/\psi\pi^0 a_0$,

$$\text{Br}(\bar{B}_s^0 \rightarrow J/\psi\pi^0 a_0) = 4.9 \times 10^{-6}.$$

$$\text{Br}(\bar{B}_s^0 \rightarrow J/\psi\pi^0 f_0) = 3.3 \times 10^{-7}.$$

These rates are within present observation capacity at LHCb.

◆ Summary

- We perform calculations for the $D_s^+ \rightarrow \pi^+ \pi^0 f_0(980)(a_0(980))$ and $\bar{B}_s^0 \rightarrow J/\psi \pi^0 f_0(980)(a_0(980))$ reactions, showing that the $a_0(980)$ mode is isospin-allowed while the $f_0(980)$ mode is isospin-suppressed.
- The triangle mechanism develops a TS around the $\pi^0 f_0(980)$ or $\pi^0 a_0(980)$ invariant mass of 1420 MeV, which enhance the isospin violation.
- We calculate absolute rates for the reactions and show that they are within present measurable range. The experimental measurement is encouraged, which will bring further light into the issue of $f_0(980)$ - $a_0(980)$ mixing and the nature of the light scalar mesons.

Thank you for your attention!